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Competition Between Regulation-Providing and Fixed-Power Charging Stations for Electric Vehicles

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Abstract—This paper models a non-cooperative game between two EV charging stations. One is a fixed-power charging station purchasing electricity from the grid at wholesale price and reselling the energy to EV owners at a higher retail price; the other is regulation-providing and varies the recharging power level of its clients to provide regulation services to the grid, so its profit comes from both EV owners (who buy energy) and the grid (which pays for regulation services). Users are reluctant to charging power variations and prefer shorter overall charging times, hence regulation-providing charging has to be cheaper than fixed-power charging.

We analyze the competition among those charging providers, and examine the performance at the equilibrium in terms of user welfare, station revenue and electricity prices. As expected, competing stations provide users with lower charging prices than when both charging solutions are offered by a monopolistic provider. Moreover, while competition benefits users, it also benefits the grid in that the amount of regulation services increases significantly with respect to the monopolistic case.

I. INTRODUCTION

Among the main difficulties of the penetration of Electric Vehicles (EVs) in the smart city is the associated energy equation: how can the power grid accommodate the corresponding demand? [1]. And together with the technical limitations, the question of economic incentives to elicit the most efficient use of resources needs also to be considered (see [2] and references therein). But EVs do not *use* the energy in real time, they just *store* it in their batteries until leaving the charging station. This particularity of EV charging demand can be leveraged, in particular for *regulation* purposes. In practice, when there is extra (resp. a lack of) energy production with respect to demand, the grid can send a “down” (resp., “up”) regulation signal so that the production side—or here, the consumption side—reacts accordingly. In this paper, we consider the economic aspects of such an option, from the point of view of EV owners and charging stations.

Previous work focuses on fairness issues among users in terms of final state-of-charge [3]; on incentivizing EV owners to contribute to regulation [4], [5]; or on the resulting user welfare [6], [7]. The closest works to ours are [8], [9], where the focus is on the pricing strategies of the charging stations: in [8], Gao *et al.* consider a regulator designing contracts to incentivize EVs to participate so that the station profit

is maximized. On the other hand, in [9] we considered a charging station offering two simple options, namely a fixed-power charging (no regulation) and a varying-power charging (following regulation signals). Another difference is that [8] allows vehicle-to-grid energy exchanges while in [9] the regulation services are just provided by varying the current charging power. But both of those works, as well as [10], assume a monopolistic revenue-maximizing charging station.

In this paper, we focus on the effect of *competition*, by considering two competing charging stations, one implementing only regulation-based charging and the other only fixed-power charging. When compared to monopolistic situations, we expect competition to benefit to users, through lower recharging prices. But also, we investigate the viability of each competitor: indeed, regulation is rewarded through financial incentives, and providing regulation during charging may not yield sufficient revenues if those incentives are not large enough. Hence some regions of reward values where EV-charging-based regulation can occur; this was investigated in the monopolistic case in [9], here we study the effect of competition on that aspect as well.

Our results indicate that, as expected, competition is beneficial to users, through lower recharging prices. Also, competition appears to be better from the grid perspective, since both the region of rewards for which regulation is viable and the amount of regulation offered are larger in the competition setting. The remainder of the paper is organized as follows. Section II presents our model; Section III analyzes the price competition and the resulting Nash equilibrium; In Section IV we compare the performance of the competition with the monopolistic case and Section V concludes the paper.

II. MODEL DESCRIPTION

According to a national household travel survey of the United States [11], [12], a passenger vehicle spends on average 75 minutes a day on journey, hence is parked most of the time. We assume this to remain true for EVs. So this is interesting, at least for some EV drivers, to accept longer charging durations for cheaper energy. This opens an opportunity for charging stations to increase revenue through the rewards offered to regulation-contributing entities, as well as for EV owners to save on their energy bill.

Conventional recharging services are provided by what we will call an *S-charging* station, purchasing electricity at the low wholesale unit price $t\text{€/kWh}$ and reselling it to EV owners at a higher price; whereas in a *R-charging*, charging power

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is not guaranteed but subject to variations over time, as a response to regulation requests issued by grid operators. We model the interactions among both stations (or sets of stations, each set controlled by a separate entity) as a noncooperative game since they compete over prices to attract EV owners. User preferences between price and charging power variations are assumed heterogeneous, so each station seeks the best tradeoff between market shares and per-client profit in order to maximize its expected revenue.

A. Regulation mechanism

Frequency regulation, depending on the response time, is mainly divided into: primary, secondary, and tertiary control, with the response time increasing from seconds, to minutes and finally to half an hour respectively [13]. In our proposal, the *R-charging* station modulates the EV charging power to provide the secondary control: one regulation time slot lasts for Δ hours, with Δ typically between 0.1 (6 minutes) and 0.25 (15 minutes). Periodically, the grid operator, buyer of the regulation service, sends a regulation request to the *R-charging* station specifying its demand, which can be regulation-up, -down or -null. Receiving the signal, the *R-charging* station sets the EV recharging power to be 0 kW¹, P_d kW, or P_n kW respectively: P_d is the maximum acceptable power level allowed by the EV supply equipment in the station, and P_n is the default recharging power ($0 \leq P_n \leq P_d$) defined by the *R-charging* station itself, when no regulation is needed, namely regulation null. Note that this mechanism increases (decreases) the EV consumption responding to regulation-down (-up). This counter-intuitive naming stems from conventional regulation services, where providers are *generation units* whereas the task is given to *consumers* here. For later convenience we will use the notation $x := \frac{P_n}{P_d}$, so that $x \in [0, 1]$.

At the *S-charging* station, EVs are always charged at full speed P_d kW. Figure 1 illustrates the charging power profiles for the two stations as well as the energy accumulated in an EV battery being charged for a given scenario of regulation requests. We denote by C_B the energy demand of an EV, and by ρ_u (ρ_d) the probability of occurrence of regulation-up (-down) at each time slot, those signals being assumed independent at each regulation period in this paper.

There may be concerns that varying the charging power for all EVs in *R-charging* station(s) simultaneously and drastically following this “ping-pong” policy can lead to an oversupply of regulation, i.e., the aggregated increase or decrease in power is larger than that actually needed by the grid operator. This is hardly possible since in the scale of a grid operator, the disposable regulation capacity scattered in EVs is non-dominant if not negligible given the current penetration levels. For example data from RTE (Réseau de transport d’électricité), the biggest independent system operator in France, show that the regulation-down demand in 30 minutes² can easily go over

¹We do not allow here EVs to deliver energy to the grid (the so-called vehicle-to-grid transfer).

²<http://clients.rte-france.com/lang/fr/visiteurs/vie/mecanisme/jour/volume.jsp>

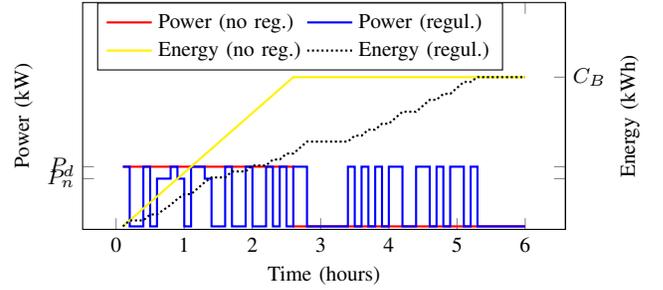


Fig. 1: Power and cumulated energy an EV obtained with and without regulation (simulation with $C_B = 50$ kWh, $P_d = 20$ kW, $P_n = 16$ kW, $\Delta = 0.1$ hour, $\rho_u = \rho_d = 0.45$ [9])

100 MWh, a quantity that could only be absorbed by at least ten thousand EVs doing level 2 recharging (19.2 kW [14]) at the same time. Since the whole country has an EV population of 30 thousand, sharing 8600 public charging facilities, the regulation oversupply problem is not of concern so far. But it can rapidly become one if EV penetration increases; nevertheless we expect that in this case, the incentives to provide regulation will be adjusted (regulation being rewarded less) so that market mechanisms will reduce supply. In addition, demand for regulation is likely to increase in the next future, with the development of renewable energy production which cannot be controlled like fossil-based electricity plants can: the overall supply-demand balance will be more difficult to maintain, hence a probable larger need for ancillary services such as regulation.

B. Regulation incentives

In return for providing regulation, the *R-charging* station receives monetary incentives, with respect to the default wholesale price t .

- In *regulation-null* periods, it charges each plugged EV with power P_n kW, and pays $\Delta t P_n$ monetary units (no compensation) over such a duration- Δ ;
- in *regulation-up* periods, the grid operator “re-buys” the energy saved at a unit price $r_u t$, hence the station pays $\Delta t (1 - r_u) P_n$ monetary units over such a period (note that we can expect to have $r_u \geq 1$, although it is not always the case in practice);
- similarly, in a *regulation-down*, the *R-charging* station pays for the extra energy it consumes at a discount price $t(1 - r_d)$ monetary units per kWh, thus a total price paid $\Delta (P_n t + (P_d - P_n) t (1 - r_d))$ monetary units per EV.

Together with the probabilities of regulation-up (ρ_u) and down (ρ_d), the expected net revenue (possibly negative) over one regulation slot is:

$$E_\Delta = t \Delta (\rho_u r_u P_n - \rho_d (1 - r_d) (P_d - P_n) - P_n) \quad (1)$$

C. User preferences

We assume that each EV owner needs C_B kWh of energy, say, per day, the owner can choose to charge at the constant

power P_d in the *S-charging* station, or to charge at a variable power in the *R-charging* station. They can also choose neither solution (a *no_charging* choice) if they consider both too expensive. Naturally, users are assumed to:

- prefer to recharge faster, i.e., at higher power rate;
- be reluctant to *uncertainty* in the recharging power caused by regulations. Additionally, batteries can be sensitive to power variations in the recharging process, another reason for EV owners to be reluctant to contributing to regulation.

Following these criteria, we define the user utility (willingness-to-pay minus price paid) for a recharging option as being of the form

$$V = \theta(\bar{P} - \gamma\delta(P)) - TC_B$$

where \bar{P} is the expected charging power, and $\delta(P)$ its standard deviation. θ is user-specific: we assume it to be exponentially distributed, with mean $\bar{\theta}$, over the EV owner population. The parameter γ is the reluctance toward power fluctuations, and is assumed the same for all users. Finally, T represents the unit energy price set by the charging station chosen by the user. (We take $T = 0$ for users who choose *no_charging*).

Let us define P_A as the value of $\bar{P} - \gamma\delta(P)$ for the *R-charging* option, which can easily be expressed from P_d , P_n , ρ_d and ρ_u . The parameter (γ) we choose always guarantees $P_A \geq 0$ which means that this proposal does not target users with a too high sensitivity to power fluctuation. The probability α_r (resp., α_s) that a user chooses the *R-charging* (resp., *S-charging*) station can then be expressed as

$$\alpha_r = \begin{cases} 1 - \exp\left(-\frac{C_B(T_s - T_r)}{\theta(P_d - P_A)}\right) & \text{if } T_r < 0 \\ \exp\left(-\frac{C_B T_r}{\theta P_A}\right) - \exp\left(-\frac{C_B(T_s - T_r)}{\theta(P_d - P_A)}\right) & \text{if } 0 \leq T_r \leq \frac{P_d}{P_A} T_s \\ 0 & \text{otherwise} \end{cases} \quad (2)$$

$$\alpha_s = \begin{cases} \exp\left(-\frac{C_B T_s}{\theta P_d}\right) & \text{if } T_s \leq \frac{P_d}{P_A} T_r \\ \exp\left(-\frac{C_B(T_s - T_r)}{\theta(P_d - P_A)}\right) & \text{otherwise.} \end{cases} \quad (3)$$

Note that we allow negative charging prices with the *R-charging* station: indeed, since that station can make money from the grid thanks to EV owners, the corresponding rewards could be so large that the station would be willing to attract a large number of EVs, even by paying them. This case is for completeness of the model, we think it is not very likely to occur but we cover it in this paper.

Following the classical backward induction method, we first assume P_n (or equivalently x) fixed and analyze the pricing game (defined bellow). The outcome is dependent on x so the *R-charging* station can maximize its profit through altering its value. We examine the first part analytically while the second numerically due to complexity.

Definition 1. *The pricing game between the S-charging station and the R-charging station as a collection: $\langle \mathcal{N}, \mathcal{T}, (R_i) \rangle$, where the player set \mathcal{N} consists of the two stations, the price profile \mathcal{T} is a vector (T_s, T_r) on the semi-plane $\mathbb{R}_{\geq 0} \times \mathbb{R}$, and the payoff function $R_i : \mathcal{T} \rightarrow \mathbb{R}$ gives each station's expected revenue obtained from one EV.*

Table I summarizes the notations used in our model.

TABLE I: Model notations

t	unit price of energy paid by stations (unit: €/kWh)
r_u	remuneration ratio for regulation-up (no unit)
r_d	discount ratio for regulation-down (no unit)
ρ_u (resp. ρ_d)	probability of an ‘‘up’’ (resp. ‘‘down’’) regulation signal
C_B	average energy recharged per EV per day
θ	user sensitivity to recharging power (including variability)
$\bar{\theta}$	average value of θ among users
γ	user reluctance to power variation
P_n (resp. P_d)	default (resp. ‘‘regulation-down’’) recharging power
x	$\frac{P_n}{P_d}$
\bar{P}	$\rho_d P_d + (1 - \rho_u - \rho_d) P_n$
$\delta(P)$	$\sqrt{\rho_u \bar{P}^2 + \rho_d (P_d - \bar{P})^2 + (1 - \rho_u - \rho_d) (P_n - \bar{P})^2}$
$P_A(x)$, or P_A	$\bar{P} - \gamma\delta(P) (> 0)$

III. ANALYSIS OF THE GAME

In this section, we analyze the non-cooperative strategic game defined in 1. We derive their respective best-response prices, to characterize the Nash equilibria.

A. Best-response prices

1) *S-charging station revenue and best-response price T_s^{br}* : For the *S-charging* station owner, its average income R_s depends on the market share α_s , and the unit price T_s it offers:

$$R_s = C_B(T_s - t)\alpha_s = \begin{cases} C_B(T_s - t) \exp\left(-\frac{C_B T_s}{\theta P_d}\right) & T_s \leq \frac{P_d}{P_A} T_r \\ C_B(T_s - t) \exp\left(-\frac{C_B(T_s - T_r)}{\theta(P_d - P_A)}\right) & T_s > \frac{P_d}{P_A} T_r. \end{cases} \quad (4)$$

Depending on its opponent's strategy T_r , the price T_s that maximizes R_s provides the best-response price.

Proposition 1. *The S-charging station has a unique best-response price as follows:*

$$T_s^{br}(T_r) = \begin{cases} t + (P_d - P_A) \frac{\bar{\theta}}{C_B} & \text{if } T_r < (t + (P_d - P_A) \frac{\bar{\theta}}{C_B}) \frac{P_A}{P_d} \\ t + P_d \frac{\bar{\theta}}{C_B} & \text{if } T_r > (t + P_d \frac{\bar{\theta}}{C_B}) \frac{P_A}{P_d} \\ T_r \frac{P_d}{P_A} & \text{otherwise} \end{cases} \quad (5a) \quad (5b) \quad (5c)$$

Proof: The proof is provided in the Appendix of the full paper version [15]. ■

Figure 2 illustrates the *S-charging* station revenue as a function of T_r , and the best-response $T_s^{br}(T_r)$.

2) *R-charging station revenue and best-response price $T_r^{br}(T_s)$* : Let us now consider the *R-charging* station owner, having to decide its price T_r .

To estimate how much net remuneration the *R-charging* station gets from recharging EVs through regulation, we multiply the regulation revenue per slot, i.e. E_Δ in (1), by the average number of slots a regulating EV remains plugged-in before its battery is fully recharged, i.e. $C_B/(\Delta\bar{P})$. To facilitate the writing we further divide the product, which has a unit of €, by the EV energy demand (C_B kWh), so that its final unit is €/kWh and has a form of

$$E_r := t(\rho_u r_u x - \rho_d(1 - r_d)(1 - x) - x) \frac{P_d}{\bar{P}}.$$

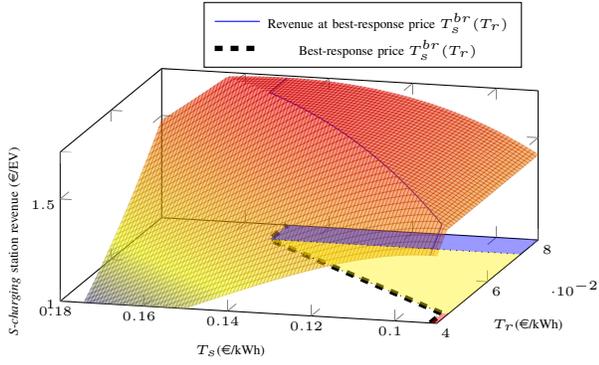


Fig. 2: *S*-charging station revenue as a function of T_r and T_s ($t = 0.03$, $\bar{\theta} = 0.3$, $C_B = 50kWh$, $x = 0.8$). The red, yellow and blue areas are separated by $T_r = (t + (P_d - P_A) \frac{\bar{\theta}}{C_B}) \frac{P_A}{P_d}$ and $T_r = (t + P_d \frac{\bar{\theta}}{C_B}) \frac{P_A}{P_d}$, referring to (5).

The average *R*-charging station revenue consists of remuneration from providing regulation and income from charging EVs:

$$R_r = \begin{cases} C_B(T_r + E_r)[1 - \exp(-\frac{C_B(T_s - T_r)}{\theta(P_d - P_A)})] & T_r < 0 \\ C_B(T_r + E_r)[\exp(-\frac{C_B T_r}{\theta P_A}) - \exp(-\frac{C_B(T_s - T_r)}{\theta(P_d - P_A)})] & 0 \leq T_r \leq \frac{P_A}{P_d} T_s \\ 0 & \text{otherwise} \end{cases} \quad (6)$$

The following result summarizes the optimal *R*-charging station reaction to its competitor.

Proposition 2. *The R-charging station has a unique best-response price as follows:*

$$T_r^{br}(T_s) = \begin{cases} T_s \frac{P_A}{P_d} & \text{if } T_s \leq -E_r \frac{P_d}{P_A} \\ 0 & \text{if } T_s \in \{T_s : E_{r,1}(T_s) \leq E_r \leq E_{r,2}(T_s)\} \\ \{T_r \in \mathbb{R} : \frac{\partial R_r}{\partial T_r} = 0\} & \\ C(\min\{0, -E_r\}, \max\{0, \min\{\frac{\bar{\theta} P_A}{C_B} - E_r, \frac{P_A}{P_d} T_s\}\}) & \text{otherwise} \end{cases} \quad (7)$$

where

$$E_{r,1}(T_s) = \frac{\bar{\theta}(P_d - P_A)(1 - \exp(-\frac{C_B T_s}{\theta(P_d - P_A)}))}{C_B(\frac{P_d}{P_A} - 1 + \exp(\frac{C_B T_s}{\theta(P_d - P_A)}))}$$

$$E_{r,2}(T_s) = E_{r,1}(T_s)(1 + (\frac{P_d}{P_A} - 1) \exp(\frac{C_B T_s}{\theta(P_d - P_A)})).$$

Proof: The proof is provided in the Appendix of the full paper version [15]. ■

Figure 3 shows the *R*-charging station revenue as well as the best-response price $T_r^{br}(T_s)$, as a function of T_s .

B. Nash equilibrium

Proposition 3. *The pricing game defined in 1 has either a unique Nash equilibrium or a unique Pareto-dominant one*

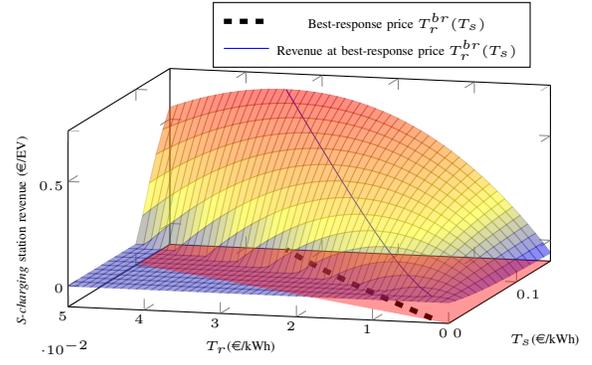


Fig. 3: *R*-charging Station revenue as a function of T_r and T_s ($t = 0.03$, $r_d = 0.7$, $r_u = 2.1$, $C_B = 50kWh$, $\rho_d = 0.48$, $\rho_u = 0.48$, $\gamma = 0.05$, $\bar{\theta} = 0.3$, $x = 0.8$). Red region corresponds to non-negative revenue, i.e. $\frac{T_r}{P_A} < \frac{T_s}{P_d}$

when there exist infinite number of Nash equilibria. The equilibria prices N^E in different circumstances are:

$$\begin{cases} T_r = -E_r; T_s = -\frac{P_d}{P_A} E_r \\ \text{if } E_r \leq -\frac{P_A}{P_d} [t + (P_d - P_A) \frac{\bar{\theta}}{C_B}] \end{cases} \quad (8a)$$

$$\begin{cases} T_r \in (0, \min\{\frac{\theta P_A}{C_B} - E_r, \frac{P_A}{P_d} T_s\}); T_s = t + (P_d - P_A) \frac{\bar{\theta}}{C_B} \\ \text{if } -\frac{P_A}{P_d} [t + (P_d - P_A) \frac{\bar{\theta}}{C_B}] < E_r < E_{r,1}(t + (P_d - P_A) \frac{\bar{\theta}}{C_B}) \end{cases} \quad (8b)$$

$$\begin{cases} T_r = 0; T_s = t + (P_d - P_A) \frac{\bar{\theta}}{C_B} \\ \text{if } E_{r,1}(t + (P_d - P_A) \frac{\bar{\theta}}{C_B}) \leq E_r \leq E_{r,2}(t + (P_d - P_A) \frac{\bar{\theta}}{C_B}) \end{cases} \quad (8c)$$

$$\begin{cases} T_r \in (-E_r, 0); T_s = t + (P_d - P_A) \frac{\bar{\theta}}{C_B} \\ \text{if } E_{r,2}(t + (P_d - P_A) \frac{\bar{\theta}}{C_B}) < E_r \end{cases} \quad (8d)$$

Proof: The proof is provided in the Appendix of the full paper version [15]. ■

Note that $N^E(8a)$ which occurs when $E_r \leq -\frac{P_A}{P_d} [t + (P_d - P_A) \frac{\bar{\theta}}{C_B}]$ is not profitable for the *R*-charging stations since zero revenue is obtained, and that the condition for a positive *R*-charging station revenue is $-\frac{P_A}{P_d} [t + (P_d - P_A) \frac{\bar{\theta}}{C_B}] < E_r$. We will refer to this condition in Section IV-B.

Figure 4 illustrates best-response prices and resulting Nash equilibria in four different circumstances. Figure on the left hand side shows that when regulation remuneration is not significant (eg. $r_u = 1$ and $r_d = 0$ in the figure), it is likely to encounter equilibrium $N^E(8a)$ or $N^E(8b)$, due to small regulation profit E_r . On the right hand side, equilibrium $N^E(8c)$ or $N^E(8d)$ happens when regulation revenue is very attractive. Note that we choose very high regulation prices just to depict the case where free recharging or even negative price recharging is offered. To our knowledge, such high prices rarely exist on the market.

1) *Optimization of P_n :* The pricing game defined in 1 is played given a fixed P_n , set by the *R*-charging station, who

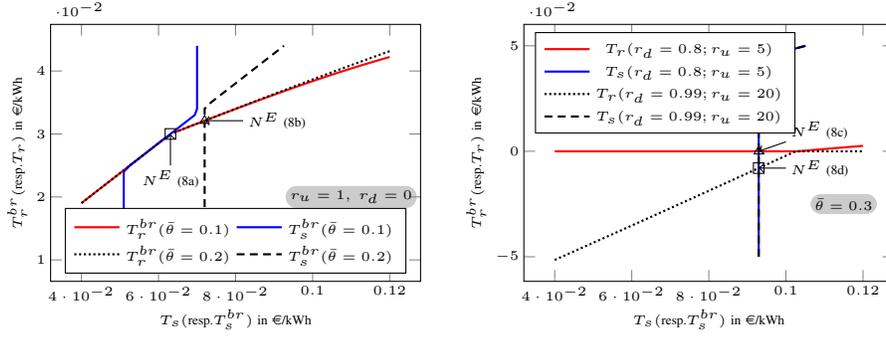


Fig. 4: Four Nash equilibria in different cases

can afterwards modify its value to pursue a higher equilibrium revenue. Due to the complexity of the equilibrium price profile we resort to numerical search for the optimal P_n .

IV. COMPARISON BETWEEN THE NASH EQUILIBRIUM AND THE MONOPOLISTIC CASE

In this section we compare the competition model with the monopolistic case where a single manager sets both the *S-charging* price as well as the *R-charging* price to maximize its overall revenue. We do not repeat the results in [9] for the monopolistic case due to space limit, but simply compare their performances under the same parameters.

A. User welfare

User welfare is the average user utility over the distribution of user preference parameter, i.e. θ . The following formula works for both the monopolistic case and the Nash equilibrium.

$$\begin{aligned}
 U &= \int_{\frac{T_r C_B}{P_A}}^{\frac{(T_s - T_r) C_B}{P_d - P_A}} (\theta P_A - T_r C_B) \frac{1}{\theta} \exp\left(-\frac{\theta}{\bar{\theta}}\right) d\theta \\
 &+ \int_{\frac{(T_s - T_r) C_B}{P_d - P_A}}^{+\infty} (\theta P_d - T_s C_B) \frac{1}{\theta} \exp\left(-\frac{\theta}{\bar{\theta}}\right) d\theta \\
 &= \alpha_r \bar{\theta} P_A + \alpha_s \bar{\theta} P_d
 \end{aligned}$$

The first column in Figure 5 shows a significant increase of user welfare (U^M for monopoly and U^E for equilibrium) after breaking a monopolistic station into two competing ones. Although the total station revenue decreases, the social welfare which is the user utility plus station revenue has a net increase of over 20%. The second column illustrates an increase of EVs being served, thanks to a decrease of energy prices depicted in the third column.

B. Application in a real world market

Figure 6 compares the regions for rewards $\{r_d, r_u\}$ where offering *R-charging* is profitable. At equilibria (second row), the black zones where *R-charging* is not preferred is remarkably smaller than those in the monopolistic case. This is because that in a monopoly, feasible region for rewards $\{r_d, r_u\}$ is composed of those that make the following equation of x solvable in the interval of $[0, 1]$ [9]:

$$\rho_u r_u x - \rho_d (1 - r_d) (1 - x) - x - \bar{P}(x) P_A(x) P_d^{-2} > 0$$

Whereas in competition, (8a) and (8b) give the condition of:

$$\begin{aligned}
 &t(\rho_u r_u x - \rho_d (1 - r_d) (1 - x) - x - \bar{P} P_A P_d^{-2}) \\
 &+ \frac{1}{t} \bar{P} P_A P_d^{-2} [P_d - P_A] \frac{\bar{\theta}}{C_B} > 0
 \end{aligned}$$

Comparing these two we find that the competition enlarges the viable region of $\{r_d, r_u\}$. The blue and red areas in Figure 6 are referring to the optimal default recharging power P_n in these regions, i.e. the optimal x after exhaustive search. In most combinations of $\{r_d, r_u\}$, this optimal x is either 0 or 1, except for a few $\{r_d, r_u\}$ observed in the gap between the blue region and the red, in the figures on the third column where average user preference on power is smaller: $\bar{\theta} = 0.1$ and user sensitivity to variation is greater: $\gamma = 0.5$. We also plot the actual $\{r_d, r_u\}$ offered by a French operator RTE on these figures. The blue circles correspond to the 48 $\{r_d, r_u\}$ pairs on the day of 20/07/2015 and the red rectangles are showing the daily averages during the week from 20/07/2015 to 26/07/2015.

V. CONCLUSION AND PERSPECTIVES

This paper considers a competition between two self-interested charging stations. At the Nash equilibrium of this non-cooperative game, both stations tends to offered lower prices to EV owners than a monopolistic controller would do, thus more clients are attracted and greater regulation services is provided to the grid operator. This work can be extended in several ways including: bring in more actors such as charging stations with private renewable energy sources; considering the actor of a ‘‘Grid’’ who can play with the wholesale electricity price imposed on both *R-charging* and *S-charging* station; or differentiate two charging stations by their locations, which effect users’ preferences among them.

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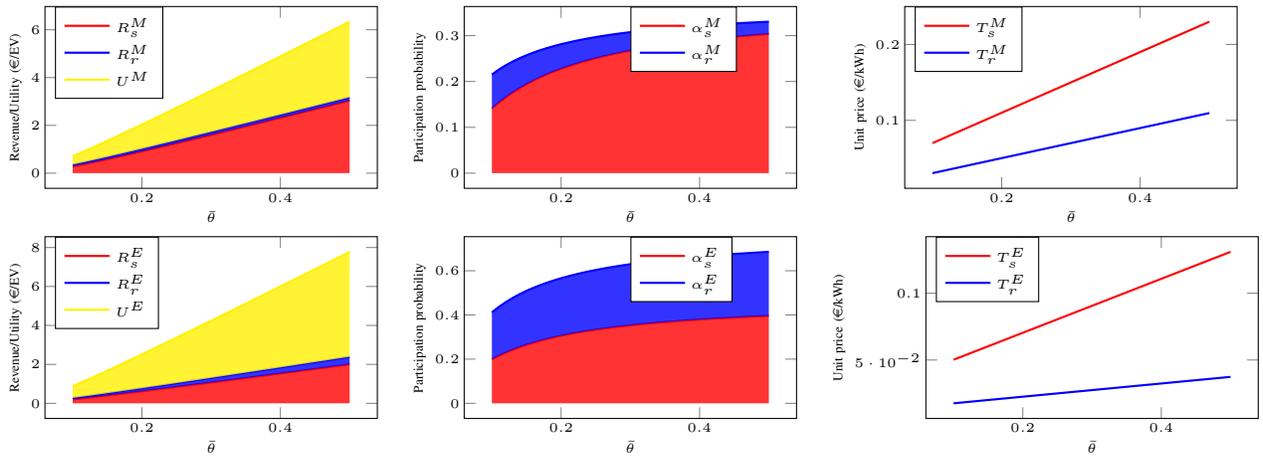


Fig. 5: Comparison between Monopoly (first row) and Nash equilibrium (second row), with $t = 0.03$, $\bar{\theta} = 0.3$, $C_B = 50$, $\rho_d = \rho_u = 0.48$, $\gamma = 0.05$, $r_d = 0.4$, $r_u = 1.6$ (r_d and r_u are the daily average of 20/07/2015).

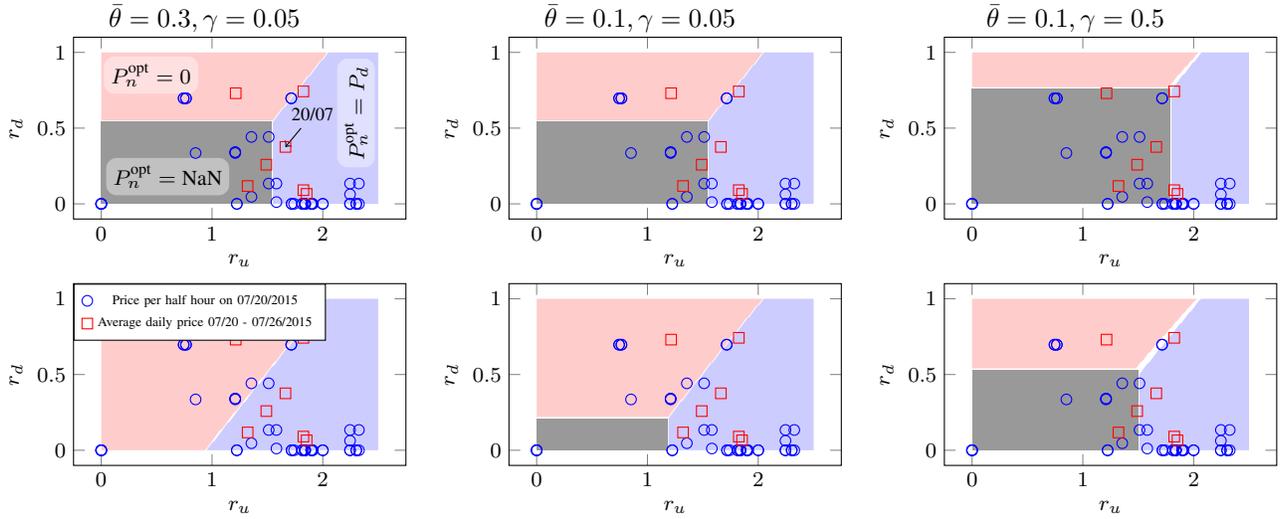


Fig. 6: Comparison of variable regions on $r_d \times r_u$ plane and the x chosen, $t = 0.03$, $C_B = 50$, $\rho_d = \rho_u = 0.48$

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