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A Framework for Optimal Decentralized Power Control with Partial CSI

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Abstract—In this paper, we use a recent information theoretical result to develop a general framework for finding optimal power control policies in the case of interference channels. The aforementioned result characterizes the achievable payoffs for an N -Agent (transmitters in our application) coordination problem with a certain information structure. We then provide an algorithm which exploits the characterization of achievable payoffs by conditional probability distributions to find optimal decision functions for the transmitters. Due to its general nature, the developed framework is conducive for applications to diverse scenarios in wireless communications. In this article, we restrict our attention to the case of decentralized power control in interference channels for different utility functions namely sum-rate, sum-energy and sum-goodput. Our approach has the following salient features: 1) The method proposes optimal power control functions for any given utility function as opposed to ad-hoc solutions for different utilities proposed in the literature, and 2) Noise in the channel estimation is taken into account, thus providing robust optimal solutions.

I. INTRODUCTION

One of the key contributions of this paper is to exploit the recent theorem derived in [1] to find power control functions which may exploit the available knowledge optimally (in the long run). As an example, we treat the well studied problem of optimal power control in interference channels ([2], [3], [4]) and show that not only does our framework attain various payoffs identical to the state of the art, it also provides the optimal power control functions in diverse scenarios. The scenarios considered resemble those of [5], [6]. These works propose ad hoc solutions for specific utilities but not a generic framework which directly provides a power control function that aims at exploiting the available and arbitrary information as well as possible. Indeed our approach is very general and can be used to treat more complex and interesting scenarios by considering different kinds of channel state informations available at transmitters, different common objectives, robust power control taking the noisy communications into account, vectorial optimization etc.

The generality of the approach is by virtue of exploitation of some recent information theoretical results [1]. A similar approach, albeit with a different information structure and for only 2 transmitter-recipient pairs was proposed in [7]. The information structure considered in this paper is more adapted for the application proposed under realistic assumptions, the important assumptions being 1) No knowledge of future realizations of the nature state w.r.t. which the agents are coordinating, 2) Any number of agents with only

a partial and noisy information about the current nature state, and 3) Decision functions must be found in a decentralized manner for having more robustness leading to simpler design architectures.

Indeed, for the case of power control in wireless interference channels, these assumptions have been paid some attention. The necessity of minimizing the information required at the transmitters for coordination led to approaches proposed in [8], [9], [10]. They consider only local channel state information at the transmitters (CSIT). This is also important for reducing the complexity of the optimizations to be performed. For sum-rate maximization, the scenario considered by us is comparable to a single-carrier version of the iterative water filling algorithm (IWFA) [11]. In the case of sum-energy utility, channel inversion strategy was proposed by [12], whereas the multi-carrier version of the problem was considered by [13]. Decentralization of the power control, or for that matter for any wireless network design, is the reason why game theory has been extensively applied to such problems [14]. We thus compare our results to game theoretic equilibria analysis as most of the decentralized optimization literature only guarantees convergence to Nash equilibria.

The article follows the structure from more general results to specific application of the framework proposed. To this effect, Sec. II describes the performance limits of a general coordination problem characterizing the optimal achievable payoffs. The characterization lays the foundation for an algorithm proposed in Sec. III for finding the optimal decision policies of the coordinating transmitters. While we continuously illustrate what the developed framework corresponds to for wireless applications, in Sec. IV-A we describe the specific problem of power control in interference channels. A numerical analysis is conducted for diverse scenarios and the results are compared to existing literature in Sec. IV-B. Concluding remarks are provided in V

II. PERFORMANCE LIMITS OF AN N -TRANSMITTERS INTERFERENCE COORDINATION PROBLEM

Consider a coordination problem where N transmitter-recipient pairs are trying to coordinate the power emitted by them $X_i \in \mathcal{X}_i$, $i \in \{1, \dots, N\}$ with respect to a nature state represented by $X_0 \in \mathcal{X}_0$ to optimize a common payoff function $w(x_0, x_1, x_2)$ over a long time period T . The nature state X_0 for applications to wireless communications is the channel gain matrix $g_{ij} = |h_{ij}|^2$, with g_{ij} being the

channel gain of the link between transmitter i and receiver j . $X_0 = (g_{11}, \dots, g_{NN})$ is a random state which affects the common payoff function for the system and is not controlled by the coordinating transmitters. The realizations of the nature state $X_{0,t}$ at each time instant t are i.i.d. and follow a distribution ρ . In wireless communications ρ is typically an exponential distribution for each channel gain g_{ij} . Our aim is to characterize all the achievable expected payoffs under a certain information structure over the large time period T , $T \rightarrow \infty$.

Firstly, we need to define the information structure under consideration. At every instant t , all the transmitters are assumed to have an image or a partial observation $S_{i,t}$ of the nature state $X_{0,t}$ with respect to which they are coordinating. In the case of our application, this could be knowledge of only local CSIT, i.e. transmitter i observes a noisy version (in general) of only the direct link channel gain g_{ii} . One could imagine other kinds of information available at the transmitters: for example, transmitter i observes all the links $g_{ji} \forall j$. The observations $S_{i,t}$ are assumed to be generated by a memoryless channel whose transition probability is denoted by $\Upsilon_i(S_{i,t}|X_{0,t})$. All transmitters have to choose the power emitted by them $X_{i,t}$ based on this information received. Formally, the sequences of decision functions for each agent i , $\sigma_{i,t}$, is defined as:

$$\sigma_{i,t} : \mathcal{S}_i^t \times \mathcal{U} \rightarrow \mathcal{X}_i \quad (1)$$

$$(s_i(1), s_i(2) \dots s_i(t), u(t)) \mapsto x_i(t) \quad (2)$$

where $\mathcal{S}_i^t = \mathcal{S}_i(1) \times \mathcal{S}_i(2) \dots \times \mathcal{S}_i(t)$ is the discrete observation alphabet till the instant t and \mathcal{X}_i is the power emitted for transmitter i with $|\mathcal{S}_i|, |\mathcal{X}_i| < \infty$. \mathcal{U}_t is the alphabet of the auxiliary variable U which is discussed in more detail later. $s_i(t)$, $u(t)$ and $x_i(t)$ are the realizations of the corresponding variables at instant t .

The problem is said to be decentralized as each transmitter chooses its power independently based on the information received by it. Since the channel gains are generated by a random process, and thus in general also the corresponding chosen power levels, the quantity to be optimized is the expected objective function:

$$\mathbb{E}_Q[w(X)] = \sum_{x \in \mathcal{X}} w(x_0, x_1, \dots, x_N) Q(x_0, x_1, \dots, x_N) \quad (3)$$

where $X = (X_0, X_1, \dots, X_N)$, $x = (x_0, x_1, \dots, x_N)$, and $\mathcal{X} = \mathcal{X}_0 \times \prod_{i=1}^N \mathcal{X}_i$. An important point to note is that since expectation is a linear operator, optimizing the expected payoff is equivalent to finding the optimal distribution $Q(x_0, x_1, \dots, x_N)$. However, the optimization problem is not so trivial as indeed there are certain restrictions on the distributions Q that are implementable given the imposed information structure. For doing that, one first needs to define the notion of an implementable distribution.

Definition 1 (Implementability). *Let the information structure be as defined in (1). The probability distribution*

$\bar{Q}(x_0, x_1, \dots, x_N)$ *is implementable if there exist decision functions $\sigma_{i,t}$ such that as $T \rightarrow +\infty$, we have for all $x \in \mathcal{X}$,*

$$\frac{1}{T} \sum_{t=1}^T Q_{X_0 \dots X_N, t}(x_0, \dots, x_N, \cdot) \rightarrow \bar{Q}(x_0, \dots, x_N) \quad (4)$$

where $Q_{X_0 X_1 \dots X_N, t} = Q_{X_1, \dots, X_N | X_0, t} \times \rho$ is the joint distribution induced by $\sigma_{i,t}$ at stage t .

As seen before, the expected payoff is characterized by the probability distribution Q over all the variables that intervene in the payoff function. Thus, the time averaged expected payoff \bar{w} is said to be achievable, if and only if the corresponding distribution \bar{Q} is implementable. The following theorem characterizes precisely the distributions that are implementable under the information structure (1).

Theorem 1. [1] *Assume the random process $X_{0,t}$ to be i.i.d. following a probability distribution ρ and the available information to the transmitters $S_{i,t}$ to be the output of a discrete memoryless channel obtained by marginalizing the conditional probability $\Upsilon(s_1, \dots, s_N | x_0)$. An expected payoff \bar{w} is achievable in the limit $T \rightarrow \infty$ if and only if it can be written as:*

$$\bar{w} = \sum_{x_0, x_1, \dots, x_N, u, s_1, \dots, s_N} \rho(x_0) P_u(u) \times \Upsilon(s_1, \dots, s_N | x_0) \times \left(\prod_{i=1}^N P_{X_i | S_i, U}(x_i | s_i, u) \right) w(x_0, x_1, \dots, x_N) \quad (5)$$

where U is an auxiliary variable which can be optimized.

The auxiliary variable U is an external lottery known to the transmitters beforehand which can be used to achieve better coordination. An example for how this variable U can help coordinate better in the case of power control is shown in Sec. IV-A.

Theorem 1 helps us find the best achievable payoffs on an average with arbitrary information to the transmitters as long as it follows the structure (in terms of when the information is available to whom) defined in equation (1). However, this theorem does not provide optimal sequences of decision functions $\sigma_{i,t}$ for the time averaged expected payoff. In the following section, we shall give an algorithm which helps find a suboptimal solution for the decision functions. The suboptimality is due to the high complexity of a multilinear optimisation problem. Nonetheless, In Sec. IV-B we see that the solutions obtained using this algorithm match the state of the art solutions proposed for different utilities discussed.

III. ALGORITHM FOR FINDING SUB-OPTIMAL LOW-COMPLEXITY DECISION FUNCTIONS

As seen from Theorem 1, optimal performance for the coordination problem depends only on the vector of conditional probabilities $(P_{X_1 | S_1, U}, \dots, P_{X_N | S_N, U})$. Thus, it suffices to find an optimum vector of lotteries for every action X_i possible to obtain the best achievable payoff. However, one can see that this task is computationally very demanding. Instead, we apply a suboptimal approach by searching for

the conditional probabilities in a distributed manner, thus reducing the complexity of the search. To this effect, we apply sequential best response dynamics [14]. This consists of each transmitter choosing the best corresponding power given that others keep their powers constant, and each transmitter doing so sequentially within an iteration. Note that by doing so, the optimization problem becomes linear, and hence its solution lies at a vertex, i.e. either $(P_{X_i|S_1,U}) = 0$ or $(P_{X_i|S_1,U}) = 1$. Thus the search for conditional probability distributions simplifies to search for decision functions

$$f_i : \mathcal{S}_i \times \mathcal{U} \rightarrow \mathcal{X}_i \\ (s_i(t), u(t)) \mapsto x_i(t)$$

An important point to note is that we search for stationary strategy, i.e. f_i does not depend on the time instant t . This simplification is practical as it leads to simpler design structures and easier to find in terms of complexity. Also, the auxiliary variable U , which serves a coordination key, is exchanged *offline* beforehand and thus does not entail any signalling cost.

The procedure outlined below is performed many times till convergence is achieved, typically in a few iterations. The number of iterations required for convergence of course depends on the number of agents coordinating, but it scales up very slowly as best response dynamics normally converge very fast. Furthermore, since we are considering a common 'team' payoff $w(x_0, x_1, \dots, x_N)$, the convergence of best response dynamics is guaranteed [15].

Proposition 1. *Algorithm 1 converges always for a common performance criteria $w(x_0, x_1, \dots, x_N)$.*

Proof: The result can be proved by induction or more generally by calling for an exact potential game property (the latter argument may hold in the more general case in which the transmitter have different performance criteria).

For further justification of the simplification made by finding functions f_i instead of conditional probability distributions, note that the optimization problem is linear w.r.t. each component of the vector $(P_{X_i|S_1,U})$ that we are searching. The problem is therefore multilinear and Algo 1 will converge to the vertex of the polytop defined by the constraints. Note however that we might lose out on finding the global optimum by doing so. Nonetheless, the power control functions obtained by the simplification are sufficient to compare with the existing literature which typically provide optimal control functions and not mixed randomized strategies.

To apply best response dynamics, we rewrite the expected utility given by Theorem 1 in the following way:

$$\bar{w} = \sum_{x_0, x_1, \dots, x_N, u, s_1, \dots, s_N} \rho(x_0) P_U(u) \times \quad (6)$$

$$\mathbb{1}(s_1, \dots, s_N | x_0) \times \quad (7)$$

$$\left(\prod_{i=1}^N P_{X_i|S_i,U}(x_i | s_i, u) \right) w(x_0, x_1, \dots, x_N) \\ = \sum_{a_i, b_i, u} \theta_{a_i, b_i, u} P_{X_i|S_i,U}(x_{a_i} | s_{b_i}, u) \quad (8)$$

where a_i, b_i, u are the respective indices of x_i, s_i, u and

$$\theta_{a_i, b_i, u} \triangleq \left[\sum_{a_0} \rho(x_{a_0}) \mathbb{1}_i(s_i | x_{a_0}) \sum_{a_{-i}} w(x_{a_0}, x_{a_1}, \dots, x_{a_N}) \times \right. \\ \left. \sum_{b_{-i} \ i' \neq i} \mathbb{1}_{i'}(s_{b_{i'}} | x_{a_0}) \prod_{i' \neq i} P_{X_{i'}|S_{i'},U}(x_{i'} | s_{b_{i'}}, u) \right] P_U(u) \quad (9)$$

where a_{-i}, b_{-i} are the indices which represent a_i, b_i being constant, while all the other indices are summed over. Written in this form, the linearity of the problem w.r.t. any one of the variables $P_{X_i|S_i,U}(x_i | s_i, u)$ is even more explicit. Note that we have also assumed the independence of the observation channels of all the agents, i.e. $\mathbb{1}(\underline{s} | x_0) = \mathbb{1}_1(s_1 | x_0) \times \dots \times \mathbb{1}_N(s_N | x_0)$. For interference channels, this assumption is reasonable as all transmitters receive independent feedback of the channel gains.

An important point to note is that the transmitters can run this algorithm offline as all they need to know are the channel statistics ρ . This helps in using the optimal functions for the entire timeslot where the channel statistics remain constant right from the start as opposed to taking some time initially to find the optimal functions online. The latter is the case for some decentralized solutions proposed such as the algorithms based on water-filling techniques proposed in [5], [6].

IV. APPLICATION TO POWER CONTROL IN INTERFERENCE CHANNELS

In the previous sections, we developed the framework, giving intuition as to what the defined quantities might represent in diverse optimization problems of wireless communications. In this section, we concentrate on the problem of power control in interference channels [14] and provide numerical analysis of some special cases for the above problem.

A. System Model

Consider N single-antenna Transmitter-Receiver pairs Transmitter _{i} , Receiver _{i} , $i \in \{1, 2, \dots, N\}$ with a single band interference channel with the channel gains being g_{ij} , $i, j \in \{1, 2, \dots, N\}$ and $g_{ij} \in \mathcal{G}$. \mathcal{G} is considered to be a discrete set and represents the alphabet of the possible channel gains. A well accepted model of statistics for the channel gains $g_{ij} = |h_{ij}|^2$ is Rayleigh fading. In this model, due to central limit theorem, the real and the imaginary components of h_{ij}

share this drawn sequence. Now consider a trivial function common to all transmitters $\Delta : \mathcal{U} \rightarrow \mathcal{P}$ which maps every realization of U , u_i to one of three possible optimal power control vectors $\{(P_{max}, 0), (0, P_{max}), (P_{max}, P_{max})\}$. Under this setup, one can do monte-carlo simulations for a large number of channel gain realizations, and find the optimal probabilities (α_1^*, α_2^*) by doing an exhaustive search. This is done by searching over a discrete space $\alpha_i \in [0, 1]$, $i \in \{1, 2\}$. For the discretization, the step size is chosen to be 0.01 for obtaining reasonably precise 'optimal' probability values.

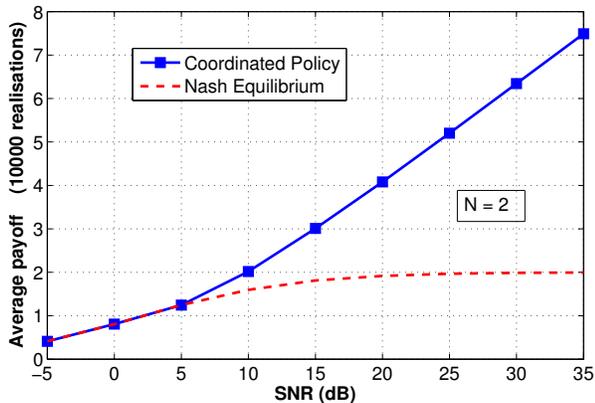


Fig. 1. The figure shows the performance in terms of sum-rate with : the proposed coordination mechanism using a public key shared beforehand; the single-carrier counterpart of the iterative water-filling algorithm. Without additional signalling, a significant gain is obtained.

In Fig. 1, we plot the average payoff for the coordinated policy using the pre-drawn lottery U in terms of SNR (which is equal to P_{max} due to normalization of channel noise variance σ^2). We compare the average payoffs for the coordinated policy as well as for nash equilibrium and see that at higher SNR, it is indeed preferable to coordinate using U . This is not surprising at all, as at higher SNRs, the interference generated is too high, whereas time-sharing helps avoid this.

In the following section, we provide the simulation setup and discuss the power control functions given by our approach. We do not consider the pre-drawn lottery U in our analysis, although in general U will only help improve the coordination performance. This is because the solution where transmitters ignore the coordination key is always possible.

B. Numerical Analysis

1) *Simulation Setup:* We implement Algo. 1 for the case of power control in a single band interference channel [14]. To this effect, we use the correspondence established in Sec. IV-A. We consider the case when $N = 2$. Note that exponential distributions for channel gain statistics g_{ij} are characterized only by their mean \bar{g}_{ij} . We shall consider standard scenarios where $(\bar{g}_{ii}, \bar{g}_{ij}) = (1, 0.3)$, $i \neq j$.

As mentioned before, the noise variance of the channel has been normalized to one. Thus, the SNR is regulated via $P_{max} = 20db$. The possible power levels emitted by

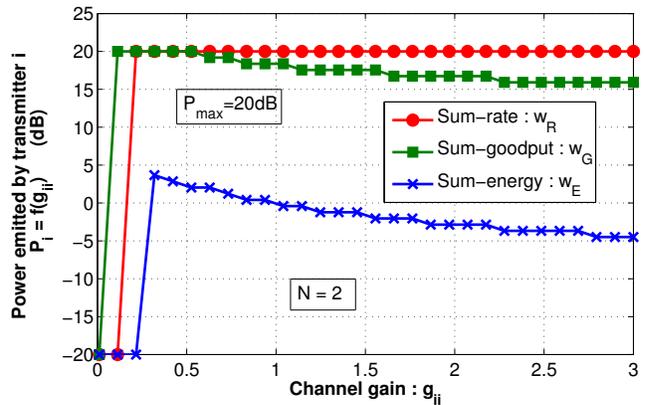


Fig. 2. The figure represents the power control functions provided by Algorithm 1 for the three performance metrics under consideration in this paper. In particular, it is seen that for maximizing sum-energy, the obtained power control function exhibits a threshold under which transmission should not occur for a given transmitter.

transmitters (P_i) are uniformly quantized between $P_i \in [-20, 20]_{db}$, with 50 quantization points.

Since the setup considered is symmetric for all Transmitter-Receiver pairs, we plot the power control functions $f_i(s_i)$, where $\mathcal{S}_i = \mathcal{G}_{ii}$, for the transmitter i . Note that since we do not consider the auxiliary variable u from here on, the function f_i is represented with only one argument s_i .

2) *Results:* In Fig. 2, we plot the power control functions f_i obtained using the Algo 1 for the case $N = 2$ against g_{ii} the direct channel gain between the i^{th} Transmitter-Receiver pair. We do not consider noise in the channel estimation for the moment, and thus in this case $s_i = g_{ii}$. Three different utilities are considered, sum-rate, sum-energy, and sum-goodput.

For the case of sum-rate, it is known that binary power control $P_i \in \{P_{min}, P_{max}\}$ is optimal for 2 Transmitter-Receiver pairs [9]. Moreover, as shown in [8], optimal power control functions with only local CSIT (g_{ii}) amounts to $P_i(g_{ii}) = P_{min}$ if $g_{ii} \leq g^*$ and $P_i(g_{ii}) = P_{max}$ otherwise. It is reassuring to find that our results verify this. Thus, in the case of sum-rate with local CSIT, we find exactly the same results as state of the art.

In the case of sum-energy, we see that all the available power P_{max} is not used. Indeed, even in the case of only 1 Transmitter-Receiver pair, the optimal power control function is $\frac{c}{g_{11}}$. We see that there is also a threshold value of g_{ii} below which, $P_i = P_{min}$. Above the threshold value, the function is similar to the optimal solution obtained in the case of only 1 Transmitter-Receiver pair. The threshold function is also seen as solution in the case of Sum packet rate. This is because the utility function is not monotonous w.r.t. SINR. To the best of our knowledge, the power control functions found for sum-energy are new. Solutions in literature do not propose thresholding of power control functions to help reduce interference in case of bad direct channel gains. Admittedly, this requires greater analysis and comparisons with the state of the art.

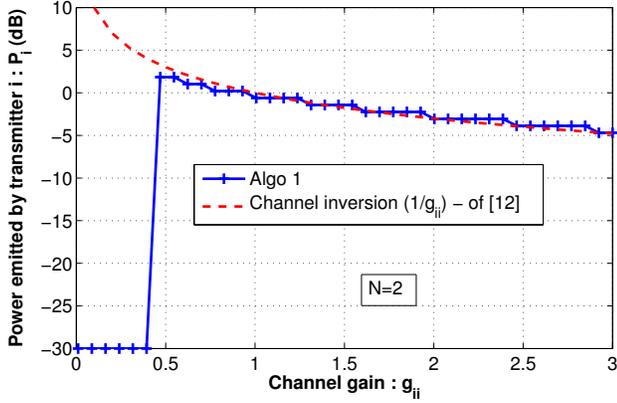


Fig. 3. Our algorithm reveals the shape of good power control functions in the presence of interference. In contrast with related works on energy-efficiency, our work shows that thresholding is required to manage interference efficiently.

To investigate the function for sum-energy further, in 3 we compare the function obtained using our algorithm with that proposed by [12]. We see that unlike [12], we find a threshold below which emitting no power is more optimal. We also see that the presence of noise makes the power control function more uniform. Our approach is shown to be much more robust to noise than one proposed by [12] as the function $1/g_{ii}$ is very sensitive to noise at low values of g_{ii} .

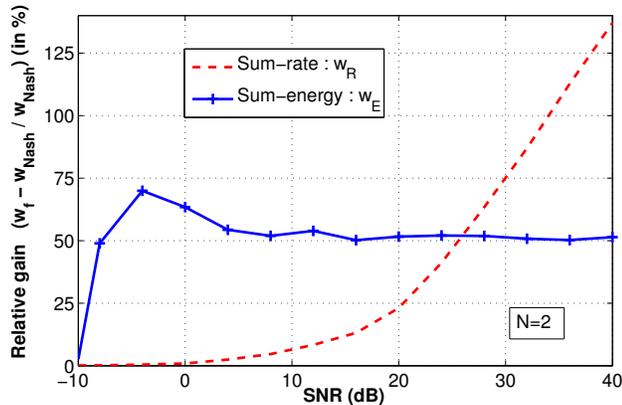


Fig. 4. Relative performance gain ($w_f - w_{Nash}/w_{Nash}$ in %) of our algorithm when compared to average payoffs obtained by Nash equilibrium for sum-rate and sum-energy. The curve for sum-energy saturates as at high SNR, P_{max} is not utilized as power emitted is much lower.

In Fig. 4, we compare the performance of the power control function with that of Nash equilibrium for different SNRs in the case of sum-energy and sum-rate. Thus, on the y -axis we see the relative performance gain ($w_f - w_{Nash}/w_{Nash}$ in %) of our algorithm when compared to average payoffs obtained by Nash equilibrium. Current state of the art propose solutions which converge to the Nash equilibrium. Thus, the solutions are generally not optimal while maximizing common utilities that are sum of the individual utilities. The evaluations for obtaining average

expected payoffs was done for 10^6 channel realizations. They were drawn according to the distribution $\prod_{i=1}^N \prod_{j=1}^N e^{-\bar{g}_{ij}}$. The channel gain statistics \bar{g}_{ij} were the same as the ones used for running the algorithm.

We see that for sum-energy, there is no performance gain at higher SNRs. This is because as seen from Fig. 2, the optimal power used is very low for all g_{ii} . However, we see that when compared to nash equilibrium, we obtain a significant gain of around 55%. In the case of sum-rate, performance obtained matches with [8] since the power control functions obtained are identical. Not surprisingly, at higher SNRs, Algo 1 does much better as Nash equilibrium, which is all transmitters transmitting at P_{max} generates too much interference.

One of the advantages of our framework is that it provides optimal power control functions even for noisy channel estimates. We illustrate this in Fig. 5 where power control functions for different levels of noise in channel estimation are plotted. This noise simulates the error in estimation due to noise in feedback transmission, or just simply statistical estimation error. The noise for the simulations is modeled to be gaussian, i.e. $s_i = g_{ii} + z$ where $Z \sim \mathcal{N}(0, \sigma_z^2)$. As expected, the power control functions become more uniform at higher noise levels, as the information received is less reliable, and thus transmitters emit at a power level which maximizes the utility for an average case.

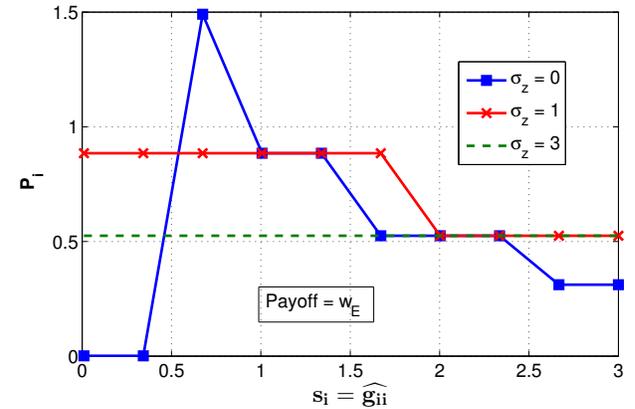


Fig. 5. Influence of channel estimation noise on the power control functions. We see that as noise increases, the optimal power emitted becomes more uniform. This is intuitive as higher the noise, higher the uncertainty in the observation leading to same power emitted for all channel gains observed in the asymptotic case.

V. CONCLUSIONS

The proposed framework was shown to be relevant in diverse scenarios of single band interference channel for finding optimal power control functions. Moreover, the power control functions depended only on local CSIT, thus having the merit of being implementable in a completely decentralized manner. Also, the solutions obtained take noise in the estimation of the channel gain into account. All the above features illustrate the generality of our approach in

tackling problems of power control for maximizing sum-utility functions.

However, the framework can be exploited further for tackling other problems in wireless communications as well. For example, one could consider the problem of power allocation in a multi-band interference channel. Also, the auxiliary variable U was not exploited, which in general will only make the solution more optimal. One could also consider different information available at transmitter i : $g_{ij} \forall j$. In future, we hope to analyze more complex problems and show the merit of the proposed framework in finding decentralized strategies for transmitters to cooperate for optimizing common utilities.

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