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Evaluation of hierarchical watersheds.

Benjamin Perret, Jean Cousty, Silvio Jamil F. Guimarães, and Deise S. Maia

Abstract—This article aims to understand the practical features of hierarchies of morphological segmentations, namely the quasi-flat zones hierarchy and watershed hierarchies, and to evaluate their potential in the context of natural image analysis. We propose a novel evaluation framework for hierarchies of partitions designed to capture various aspects of those representations: precision of their regions and contours, possibility to extract high quality horizontal cuts and optimal non-horizontal cuts for image segmentation, and ease of finding a set of regions representing a semantic object. This framework is used to assess and to optimize hierarchies with respect to the possible pre- and post-processing steps. We show that, used in conjunction with a state-of-the-art contour detector, watershed hierarchies are competitive with complex state-of-the-art methods for hierarchy construction. In particular, the proposed framework allows us to identify a watershed hierarchy based on a novel extinction value, the number of parent nodes, that outperforms the other hierarchies of morphological segmentations. This coupled with the fact that watershed hierarchies satisfy clear global optimality properties and can be efficiently computed on large data, make them valuable candidates for various computer vision tasks.

Index Terms—mathematical morphology, hierarchy of partitions, watershed segmentation, image analysis.

1 INTRODUCTION

Hierarchies of partitions are multi-scale image representations that were first proposed in [1], [2]. They have since appeared under various names: pyramids, hierarchy of segmentations, partition trees, scale-sets. In a hierarchy (of partitions), an image is represented as a sequence of coarse to fine partitions satisfying the strong causality principle [3], [4], i.e., any partition is a refinement of the previous one in the sequence. They have various applications in image processing and analysis: image segmentation [5], [6], [7], [8], [9], [10], [11], occlusion boundary detection [13], image simplification [6], [9], object detection [5], object proposal [10], visual saliency estimation [15]. In particular, they have gained a large popularity in [7] whose hierarchical approach to the general problem of natural image segmentation outperformed state-of-the-art approaches.

It has long been noted [18], [19], [20] that the classical morphological approach to image segmentation, i.e., the watershed, is compliant with the strong causality principle. This enables to define hierarchies of watersheds (see Figure 1) as a sequence of watershed segmentations of an image whose minima are iteratively removed according to an importance measure, e.g., related to their sizes. This definition has been formalized in the context of minimum spanning forests that already enabled to define watershed cuts as an optimal solution to a combinatorial problem related to minimum spanning tree [21]. It has also been shown that hierarchies of watersheds are linked to the quasi-flat zones hierarchies [22], to the single-linkage clustering problem [23], and to connective segmentation [14], [24].

Hierarchies of watersheds are thus multi-scale representations which satisfy a global optimality property. Moreover, there exist efficient algorithms, with the same time complexity as minimum spanning tree algorithms, to construct them enabling to process large images in real time [25], [26]. In recent years, they have been used for the computation of morphological operators [27], in the context of stochastic watershed segmentation [28], [29], [30]. However, their practical performances have not yet been studied in the general case of natural image analysis and the aim of this work is...
to understand their practical features and to evaluate their potential in this context.

To this end, we propose a novel evaluation framework for hierarchies of partitions specifically designed to capture the various aspects of those representations: 1) quality of regions and contours, 2) quality of produced segmentations with horizontal cuts and optimal cuts, and 3) easiness of finding a set of regions representing a semantic object. These measures are evaluated on two types of natural image datasets: 1) Pascal Context segmentation dataset [31], and 2) MS-COCO [32] and Pascal VOC’12 [33] object segmentation datasets. Compared to the classical approach for hierarchy evaluation that focuses only on the horizontal cuts and the image segmentation problem, we believe that the proposed framework offers a richer assessment that better accounts for the hierarchical nature of the representations and it is not limited to a single use case.

This framework can be used to evaluate and understand the strengths and weaknesses of the considered hierarchies of morphological segmentations. In particular, it allows us to identify a watershed hierarchy based on a novel extinction value, the number of parent nodes, that outperforms the other hierarchies of morphological segmentations. Then, we study the importance of the gradient measure for all other hierarchies of morphological segmentations. Finally, the properties of the best found solutions are discussed and compared to a state-of-the-art approach.

The definition of quasi-flat zones and watershed hierarchies are given in Section 2. Existing evaluation methods for hierarchies are discussed in Section 3. Section 4 presents the evaluation framework and the new measures. The experiments and their outcomes are discussed in Section 5. The work is finally concluded in Section 6.

2 Preliminary on graphs and hierarchies

In this section, we first review the definitions of graphs and hierarchies of partitions. Then, we recall the definition of the hierarchies of morphological segmentations used in this article, namely the quasi-flat zones hierarchies and the watershed hierarchies.

2.1 Graphs and hierarchies

In the sequel of this paper, the graph $G$ is defined as a pair $(V, E)$ where $V$ is a finite set and $E$ is composed of unordered pairs of distinct elements in $V$, i.e., $E$ is a subset of $\{ \{x, y\} \subseteq V \mid x \neq y\}$. Each element of $V$ is called a vertex or a pixel, and each element of $E$ is called an edge. The graph $G$ will model the image spatial domain, e.g., $V$ is the regular 2D grid of pixels, and $E$ is the 4- or 8-adjacency relation.

We denote by $W$ a function from $E$ to $\mathbb{R}$ that weights the edges of $G$. Therefore, the pair $(G, W)$ is an edge-weighted graph, and, for any $u \in E$, the value $W(u)$ is the weight of $u$.

A partition, also called a segmentation, $P$ of $V$ is a family of subsets of $V$ such that: 1) the intersection of any two distinct elements of $P$ is empty, and 2) the union of the elements of $P$ is equal to $V$. Each element of a partition $P$ is called a region of the partition $P$. Given two partitions $P_1$ and $P_2$, we say that $P_2$ is a refinement of $P_1$ if every region of $P_2$ is included in a region of $P_1$.

A hierarchy (of partitions) is a sequence $H = (P_0, \ldots, P_n)$ of partitions of $V$ such that $P_0$ contains every singleton of $V$, i.e., $P_0 = \{ \{x\} \mid x \in V \}$, the partition $P_n$ is the single region partition $P_n = \{V\}$, and $P_{i+1}$ is a refinement of $P_i$ for any $i$ in $\{1, \ldots, n\}$ (see Figure 2).

Given a hierarchy $H = (P_0, \ldots, P_n)$, the set of regions of $H$, denoted by $R_H$ is the union of all partitions of $H$. The inclusion relation on $R_H$ induces a tree structure (or a dendrogram) where: $V$ is the root, the singletons $\{x\}$ with $x \in V$ are the leaves, and the parent of a region $R \neq V$ of $R_H$, denoted by Parent($R$), if the smallest region $R'$ of $R_H$ that is strictly larger than $R$ (see Figure 2).

Given a hierarchy $H = (P_0, \ldots, P_n)$, a partition $P$ of $V$ made of regions of $H$ (i.e., $P \subseteq R_H$) is called a cut of $H$ (see Figure 2). The set of all cuts of a hierarchy $H$ is denoted by $\Pi(H)$. A cut $P$ of a hierarchy $H = (P_0, \ldots, P_n)$ is said horizontal if $P = P_i$ for some $i$ in $\{0, \ldots, n\}$.

2.2 Quasi-flat zones hierarchy

The quasi-flat zones have been studied since the 70’s (see e.g., [14], [34], [35]). They are deeply linked to single-linkage clustering and to the notion of a minimum spanning tree [23]. A quasi-flat zone of the weighted graph $(G, W)$ at level $\lambda$ is a maximal set of vertices such that there exists a
path of maximal weight $\lambda$ between any two of its vertices. The set of quasi-flat zones of the weighted graph at a given level $\lambda$ is a partition of its vertices (see Figure 3.a). The sequence of partitions obtained for all possible values of $\lambda$ is a hierarchy called the quasi-flat zones hierarchy of the weighted graph (see Figure 1), and denoted by QFZ (see Figure 3b).

![Weighted graph (G, W) and its quasi-flat zones](image)

![Quasi-flat zones hierarchy of (G, W)](image)

Figure 3. a) A weighted graph $(G, W)$ and its sets of quasi-flat zones at levels $\lambda$ equals to 0 (red), 1 (green), 2 (blue), and 3 (orange). The bold edges are in the paths of minimal weight inside the quasi-flat zones. b) The quasi-flat zones hierarchy QFZ of $(G, W)$: the gray nodes corresponds to the nodes of $G$. The number inside each node indicates the level $\lambda$ where the node appears in the hierarchy.

### 2.3 Watershed hierarchies

Watershed hierarchies were first proposed in [13], [19], [20] and have since been formalized in the context of minimum spanning forests [21], [25]. Given a weighted graph and a family of markers (i.e., subsets of the graph vertices identifying the objects of interest), the problem of minimum spanning forest is to find a spanning forest of minimum total weight, defined as the sum of the weights of its edges, such that each connected component of the forest contains (is rooted in) exactly one marker. The connected components of the minimum spanning forest then form a segmentation with a global optimality property similar to the one of the minimum spanning tree. When the markers are the regional minima of the weight map, the corresponding minimum spanning forest segmentations are indeed the watershed segmentations defined by the drop of water principle [21].

If the markers are ranked, e.g., according to an importance measure, it is possible to obtain a sequence of nested minimum spanning forests such that the $k$-th minimum spanning forest is rooted in the $k$-most important markers. Thus, one can obtain a sequence of nested partitions, hence a hierarchy of partitions as defined in this article, where every partition is optimal. A usual choice to define a sequence of markers is to rank the minima of the weight map according to extinction values [36]. Such hierarchies are called hierarchical watersheds; their theoretical properties and some algorithms to construct them are in particular studied in [22], [25], [26].

Extinction values are defined through regional attributes defined on the connected components of the level sets of the weight map [36]. Intuitively, the extinction value of a minimum $m$ for a given regional attribute is the smallest value $\lambda_m$ such that the minimum $m$ “disappears” when all components with an attribute smaller than $\lambda_m$ are removed. Common regional attributes are related to the size and to the contrast of the components [36], [37]; e.g., dynamics, area, or volume. Other authors have proposed regional measures related to topological properties of the function inside the components: topological height [39], or number of descendants [38]. We propose to use a novel attribute counting the number of parent nodes in the min-tree of the weighted graph, i.e., the number of non leaf nodes among the descendents of a node (see next section 2.4). All these regional attributes and their associated extinction values can be computed from the quasi-flat zones hierarchy of the weighted graph [26]. Among all the possibilities we have chosen to present the results of (see Figure 1):

- area, volume, and dynamics which are the most widely presented measures in the literature;
- number of parent nodes, which is up to our knowledge a new proposal, that provides the best performances in the following assessments.

Those regional attributes lead to the hierarchies denoted respectively by WS-Area, WS-Volume, WS-Dynamics, and WS-Parents in the following of this manuscript.

### 2.4 Attribute number of parent nodes

In this section, we present the proposed attribute Number of Parents.

Given an edge weighted graph $(G = (V, E), W)$ and its quasi-flat zones hierarchy QFZ, the min-tree MT of the weighted graph is the set of regions of the QFZ hierarchy minus the singletons, i.e., $MT = QFZ \setminus \{\{x\} \mid x \in V\}$. The min-tree MT is not a hierarchy of partitions, however equipped with the inclusion relation on its elements, it is a tree isomorphic to QFZ in the sense of [22] (see Figure 1). The leaves of MT correspond to the regional minima of the weighting function $W$ and are thus associated to the catchment basins of the watersheds of $W$.

For any element $n$ of MT, the number of parent nodes of $n$, denoted $NumPar(n)$ is then defined as the number of elements of MT included in $n$ and having at least one child, i.e., $NumPar(n) = |\{x \in MT \mid x \subseteq n, \exists y \in MT, y \subset x\}|$ (see Figure 4). $NumPar$ measures the number of times the minima of the gradient are modified, either by the addition of new pixels (growth of the associated catchment basin), or by the merging with another minima (fusion of catchment
their evaluation along the sequence of partitions produces the so-called precision-recall curves. To evaluate a hierarchy on a whole dataset, two aggregated measures are then defined: 1) the optimal image scale OIS measuring the best achievable score when taking the optimal horizontal cut in each hierarchy, and 2) the optimal data-set scale ODS measuring the best achievable score when taking horizontal cuts at the same level (the optimal scale) in every hierarchy. The difference between the ODS and the OIS assesses the consistency of the hierarchy in terms of scale: close OIS and ODS values suggest that regions of equivalent perceptual importance in different images are represented at the same level of their respective hierarchies.

This framework has been applied with three different measures: 1) F-Measure for regions (FR) \[40\] where image segmentation is viewed as a multi-class clustering problem on the image pixels, 2) F-Measure for boundaries (FB) \[40, 41, 42\] where image segmentation is viewed as a binary clustering problem on the pixels’ boundaries, and 3) F-Measure for objects and parts (FOP) \[43\] which defines empirical (pseudo) precision, recall based on the heuristic classification of each region of the partitions as an object, a part of an object, or noise. The work of \[45\] on the evaluation of segmentation assessment measures has shown that FB and FOP are highly discriminant between ground truths of different images on the BSDS 500 image dataset \[7\]. On the contrary, FR has shown a low discriminant power.

The horizontal cuts considered in that framework represent a subset of all possible partitions that can be constructed from a hierarchy. In order to better evaluate the potential of hierarchies the authors of \[44, 45\] proposed to look for the optimal cut, generally not horizontal, in a hierarchy according to a given evaluation measure. This leads to combinatorial optimization problems that have been solved in the two following cases: 1) upper bound on FB solved as a linear fractional combinatorial optimization problem \[44\], and 2) upper bound on local additive region measures solved with dynamic programming \[45\] (similar to finding the optimal partition for a given energy function \[6, 46\]). Those methods do not provide any tool to extract this upper bound cut when the ground truth is unknown: they only measure the full potential of a hierarchy.

Up to our knowledge \[47\] is the single attempt to provide a hierarchical ground-truths datasets. They defined a hierarchical ontology of semantic objects with 3 levels and asked human subjects to decompose scene according to it: their dataset is thus strongly focused on the category identified in the ontology and does not corresponds to a general segmentation objective.

## 4 Proposed evaluation methodology

In this section, we present an evaluation framework for hierarchies of partitions. This framework is composed of several supervised assessment measures, each enabling to quantify a different aspect of the hierarchy. First, we motivate the choice of the assessment measures and their contributions. Then, we give a detailed description of each measure.

The popular evaluation strategy for hierarchies of partitions, precision-recall curves for FB and FOP, assesses only the horizontal cuts of hierarchies with similarity measures
between segmentations. Indeed, the framework of precision recall curves can be applied to any sequence of partitions without any hierarchical constraint between them. However, hierarchies of partitions are rich representations with strong structural properties that are used by many applications beyond their simple horizontal cuts: energies and algorithms for optimal cut segmentation [6, [11], [12], [46], image filtering with hierarchy pruning [5], [14], [48], objects detection [10], [49], interactive segmentation with multi-scale region selection [5], [9], [50], therefore, our goal is to complete the standard precision-recall curves with other measures in order to capture more information relevant to those applications fields.

Upper-bound measures [44], [45], which enable to quantify the maximal achievable score among all possible cuts of a hierarchy, can provide valuable information for all the applications based on non-horizontal cuts: they are thus a candidate of choice to extend precision-recall curves assessment. This segmentation ability can be studied with respect to the number of desired regions in the target segmentation, enabling to identify, in the context of hierarchies, some classical properties of image segmentation such as under- and over-segmentation. The comparison of this upper-bound score with the scores obtained on horizontal cuts also enables to evaluate if the indexing of the partitions of the hierarchy is coherent with the ground truths.

Thus, in order to evaluate the cuts of a hierarchy, both horizontal and non-horizontal, we propose to use both precision-recall curves and upper bound measures. Precision-recall curves and upper-bound measures rely on a similarity measure between segmentations. As shown in [43], the complementarity between region based and boundary based similarity measures is important for the evaluation of segmentations. For precision-recall curves, we will use the combination of similarity measures FB and FOP (see Section 3).

For the upper-bound assessment, we will also use the similarity measure FB to evaluate the quality of boundaries. However, we still lack a computationally tractable algorithmic solution to find the upper-bound partition for FOP measure, which implies that we have to use a less discriminant measure [45] in order to evaluate the upper-bound quality of regions. In [45], the authors focused on the upper-bound of the directional Hamming distance [51]. However, this similarity measure is transparent to under-segmentation, i.e., it does not penalize the merging of several regions of the ground truth into a single region in the proposal segmentation (the single region partition always achieves the highest similarity with any other partition).

In this work, we propose instead to use the Bidirectional Consistency Error BCE [40] measure in order to overcome this limitation of the directional Hamming distance. Indeed, BCE is a symmetric measure, i.e., it enables to evaluate both over- and under-segmentation.

Concerning methods focusing on regions of the hierarchy, we propose new evaluation measures that aim to quantify the easiness of finding a set of nodes of a hierarchy representing a semantic object in the scene. This approach considers sets of nodes of the hierarchy which are generally not cuts and the proposed objects generally do not exist in any of the cuts of the hierarchy. Intuitively, an object will be considered easy to find if it can be retrieved with few markers, i.e., if the user of an interactive segmentation procedure can retrieve the object precisely with few annotations.

4.1 Upper-bound measure

We propose an evolution of the upper-bound evaluation on regions proposed by Pont-Tuset et al. [44], [45] that consists in the definition of a new type of curve, the fragmentation-upper bound curve that enables to measure the potential gain of non-horizontal cuts compared to horizontal cuts.

Given a similarity measure s, an image I, one ground-truth segmentation T, and a proposal segmentation S, we denote by s(S, T) the similarity between S and T for s. Given a hierarchy of partitions H on the image I, one ground-truth segmentation T and a number k of regions, the Upper-Bound score for s (UBs) for H is the highest score according to s for all the cuts of H composed of k regions:

\[ UB_s(H, T, k) = \max_{S \subseteq \Pi_{H}(k)} s(S, T). \]

In the context of Upper-Bound measure, when several distinct ground truths are available for a same image, we propose to define the image score as the average score over the set of ground truths. Indeed, a good hierarchy should be able to successfully represent the image at different scales. Therefore, if the experts provide different levels of details in different regions of the image, there should exists a good partition in the set all cuts of the hierarchy for each ground truth.

This leads to the mean-average Upper-Bound FB score on a database, i.e., the mean image score over the database. Finally, we propose to study the Fragmentation–Optimal Cut score curve (FOC), where the mean-average Upper-Bound score is plotted against the fragmentation level of the segmentation defined as k/|T|, the ratio between the number of regions in the segmentation and the number of regions in the ground truth (see Figure 7).

The gain achieved by taking a non-horizontal cut in the hierarchy is evaluated with a second curve called Fragmentation-Horizontal Cut score curve (FHC) where the mean-average FB score of the horizontal cuts of the hierarchies is plotted against the fragmentation level of the cuts. A large difference between the FOC and FHC curves suggests that the optimization algorithm has selected regions from various levels of the hierarchy to find the optimal cut: the regions of the ground-truth segmentations are thus spread at different levels in the hierarchy.

The FOC curve starts at the value corresponding to the single region partitions (independent of the evaluated hierarchy). Then, it generally quickly increases at low fragmentation levels as the optimization first selects the largest regions that summarize the ground truth. Then, the optimal cut starts to include smaller regions that provide only little score gain: this corresponds to the nearly flat part of the curve. At a high level of fragmentation (not visible in the figures), the algorithm cannot add new regions without lowering the score and the curve starts to decrease.

In the ideal case, the maximum of the FOC and FHC curves is achieved for a fragmentation of 1 (i.e., when the proposed partition and the ground truth contain the same
4.2 Object detection measure

The last measure, introduced in our previous work [50], is based on supervised object detection with markers. It quantifies how well a specific object of a scene can be retrieved with different levels of information given on its position.

In this evaluation, we chose to use the procedure described in [5] that constructs a two-classes segmentation from a hierarchy of partitions and two non-empty markers: one for the background and one for the object of interest. Its principle is to identify the object as the union of the regions of the hierarchy that intersect the object marker but does not touch the background marker. Formally, given an image \( I \), a hierarchy \( H \), an object marker \( M_o \), and a background marker \( M_b \), the extracted object is defined by:

\[
O(H, M_o, M_b) = \bigcup \{ R \in R_H \mid R \cap M_o \neq \emptyset, R \cap M_b = \emptyset \}.
\]

(2)

The extracted object is thus a union of regions of the hierarchy: i.e., it is generally not a region in any of the partitions of the hierarchy (it is not present in any cut of the hierarchy).

This result can be computed efficiently with Algorithm 1.

In the first step of the algorithm, the hierarchy is browsed from the leaves to the root. If the current node is labeled Background then its parent node intersects the background marker and is labeled Background. If the current node is labeled Object and its parent is not currently labeled then it can be labeled Object. In the second step, the tree is browsed from the root to the leaves and any non-labeled node takes the label of its parent. Finally, the labels of the leaves (the image pixels) give the segmentation result. In practice this algorithm enables to process the hierarchy of an image from MS-COCO and Pascal VOC'12 datasets in less than a millisecond.

In order to perform an objective assessment of the different hierarchies, we propose several automatic strategies to generate object and background markers from the ground truths. Our main idea is to not reproduce the interactive segmentation process experienced by a real user but rather to obtain markers representing different difficulty levels or that resembles to human-generated markers. The generated markers are the following (see Figure 5): 1) Erosion (Er): erosion by a ball of radius 45 pixels. If a connected component is completely deleted by the erosion then a single point located in the ultimate erosion [52] of this connected component is added to the marker, 2) Skeleton (Sk): morphological skeleton given by [53], and 3) Frame (Fr): frame of the image minus the object ground truth if the object touches the frame (background only). Using the frame as the background marker is nearly equivalent to having no

1. Demonstration available online with an interactive segmentation tool at [https://perso.esiee.fr/~perretb/ISeg/](https://perso.esiee.fr/~perretb/ISeg/)
background marker in the sense that it does not depend on the ground truth or of the image.

In the following, the combination of the background marker MB and the object marker MF is denoted MB-MF (for example, Fr-Sk stands for the combination of a Frame marker for the background and a skeleton marker for the object). Among all the possible combinations of markers, we chose to concentrate on the following ones: 1) Sk-Sk resembles to human generated markers, 2) Er-Er leaves a large space between markers and represent a difficult case. Nevertheless, this combination is symmetric in the sense that the boundaries of the correct segmentation are roughly at equal distance from the object and from the background marker, and 3) Fr-Sk where the object marker resembles to a human generated marker and the background marker conveys nearly no information: this case is thus asymmetric.

The performance of each segmentation result is evaluated with the F-Measure. The median score for the 3 marker combinations is called Object Detection Median and is denoted ODM.

5 Experiments

This section presents the results of the experiments and some discussions.

Precision-recall curves on FOP and upper-bound on FB measure are evaluated on the Pascal Context dataset \[31\] which consists of a pixel-wise segmentation of the 10 103 images on the Pascal VOC’10 dataset \[54\]. In our experiments, the test set is composed of the last 2 498 images of the Pascal VOC’10 validation set as proposed in \[55\]. The object detection measure is evaluated on the MS-COCO \[32\] and Pascal VOC’12 segmentation \[33\] datasets. Each object of these two datasets is processed independently using the framework described in Section 4.2. This leads to a total of 291 875 objects from the 40 504 images of the MS-COCO 2014 validation set and 3 427 objects from the 1 449 images of the Pascal VOC’12 segmentation test set. We study the importance of the gradient measure for all methods (Section 5.1) and the necessity to perform a filtering of some hierarchies (Section 5.2). The overall results are discussed and compared to state-of-the-art methods (Section 5.3).

5.1 Influence of gradient

A usual way to weight the edges of a graph in image analysis in general and for morphological segmentation in particular is to use a gradient measure. The aim of this section is to evaluate the influence of the gradient measure on the assessed quality of the hierarchies.

The most simple gradient measures use only colorimetric information from the two pixels of an edge: in this category, we consider an Euclidean distance in the RGB color space and an Euclidean distance in the Lab color space, the latter being more compliant with human color perception \[56\]. However, recent advances on contour detection have lead to non local supervised gradient estimators achieving better performance on contour detection benchmarks: in this category, we consider the structured edge detector (SED) from \[17\]. For SED, we used the default parameters given in \[17\]: single scale with sharpening and 4 decision trees.

Figure 7 shows the result of WS-Dynamics and WS-Area with three considered gradients: 1) RGB, 2) Lab, and 3) SED. The results of QFZ (respectively WS-Volume and WS-Parents), not shown here, are similar to the results of WS-Dynamics (respectively WS-Area). A first observation on WS-Dynamics with RGB and Lab gradients is that its FOC and FHC curves on FB and BCE are nearly flat. This is the result of the hierarchy not being able to provide any meaningful partition with at most twice the number of regions in the ground truth. It can be a consequence of WS-Dynamics and QFZ having their upper levels made only of small salient regions; a solution to this problem is presented in the next section.

We do not observe a clear improvement with Lab gradient compared to RBG gradient. However, there is almost always a large gain by switching from a local RGB or Lab gradient to the supervised non-local gradient SED. The FOC and FHC curves show that WS-Dynamics requires a large number of regions to reach its maximal scores with SED gradients which implies that the hierarchy tends to have small irrelevant regions on its highest levels. This suggests that despite the regularization effect based on the dynamics, which tends to send lowly contrasted regions to the lowest levels of the hierarchy, WS-Dynamics remains sensitive to small regions of high contrast.

In conclusion, we recommend the use of SED gradient to build watershed hierarchies on natural images and the
5.2 Small regions removal

As observed in the previous section, QFZ and WS-Dynamics are sensitive to small regions even with a smooth gradient as SED. In this section we evaluate the impact of an area post-filtering on those hierarchies.

The area filter described in [57] removes contours iteratively in the hierarchy: starting from the leaves and moving toward the root, the children of a node are merged if at least one of them contains less than \( k \) pixels. In the following, we express the strength of the filter as the ratio \( r_k = k/N \), with \( N \) the number of pixels in the considered image.

Figure 7 shows the results of the filtering on QFZ (the results on WS-Dynamics are similar) with four different values of \( r_k \): 0 (no filter), 0.4‰ (roughly 50 pixels in a BSDS 500 image [7]), 0.8‰, and 1.6‰. We observe that that the introduction of the filtering immediately produces a large performance boost. Between \( r_k = 0.4\% \) and \( r_k = 0.8\% \), the situation is mixed with an improvement in image segmentation measures (precision-recall curves and fragmentation curves) and a small decrease on objection detection measures. This tendency continues when \( r_k \) increases to 1.6‰. This situation can be the results of two factors: 1) the tradeoff between the number of regions necessary to describe the scene and the precision of boundaries, and 2) the difference between Pascal Context dataset, where most image segments are large, and MS-COCO and Pascal VOC’12 datasets which contain a large number of small objects that may be affected by strong filters. The effect of the filtering on over-segmentation can be observed on

<table>
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<th>Marker combination</th>
<th>Score</th>
<th>VOC’12</th>
<th>Mean score</th>
</tr>
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<tbody>
<tr>
<td>WS Dynamics - RGB</td>
<td>0.309</td>
<td>0.146</td>
<td>0.521</td>
</tr>
<tr>
<td>WS Dynamics - Lab</td>
<td>0.309</td>
<td>0.146</td>
<td>0.521</td>
</tr>
<tr>
<td>WS Dynamics - SED</td>
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<td>0.281</td>
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<td>WS Area - RGB</td>
<td>0.403</td>
<td>0.217</td>
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<td>0.496</td>
</tr>
<tr>
<td>WS Area - SED</td>
<td>0.512</td>
<td>0.290</td>
<td>0.552</td>
</tr>
</tbody>
</table>

Table: Supervised object detection on MS-COCO and Pascal VOC’12 datasets (supervised object detection). The last column of the table gives the mean score of each method.
fragmentation curves, where the positions of the maxima of the curves tend to move from large fragmentation values toward 1 when the size of the filter \( r_k \) increases.

In conclusion, for QFZ and WS-Dynamics we recommend to perform a post-filtering of the hierarchy by removing regions smaller than 0.4\% or 0.8\% of the image size. One can notice that the object detection measure is less sensitive to the area filtering than other evaluation measures. This suggests that, for some applications, the processing of the hierarchy is naturally robust to small nodes and this filtering may not be necessary or even be detrimental.

### 5.3 Discussions

This section compares and discuss the best results obtained for each morphological hierarchy (see Figure 9) and compare them to state-of-the-art methods in terms of evaluation measures (see Figure 10) and computation times (see Table 1).

We can observe that the scores of QFZ are lower than the results of the other methods on all the measures.

WS-Dynamics shows good performances on horizontal cuts (precision-recall curves) and medium performance on supervised object detection. However, it is behind in terms of upper-bound measures. It has a tendency for oversegmentation (maximum of FOC and FHC curves occur at large values of fragmentation). We can also notice that WS-Dynamics (and QFZ) performances for object detections in the Er-Er and Sk-Sk cases are significantly lower than other methods; this suggests that those hierarchies fail to correctly order regions near the boundaries which is coherent with its tendency to over-segment (more regions are needed to obtain the true contours).

WS-Area shows very good performances on quality of regions both on horizontal and non-horizontal cuts. It also has the highest upper-bound FB measure but, a low FB measure on horizontal cuts, suggesting a strong problem in the indexing of its regions. Its scores on supervised object segmentation are quite low compared to other methods: the scores of WS-Area on the Fr-Sk markers are particularly low. This can be explained by the asymmetric nature of the markers in this case (the true contours are located much closer to the object marker than the background frame), WS-Area is then penalized by its tendency to produce a regular (in size) tiling of the image.

WS-Volume behavior is close to WS-Area, its performances are however more balanced with higher scores of FB on horizontal cuts and lower ones on non-horizontal cuts. Its scores on supervised object segmentation are also very good.

WS-Parents offers the best overall performances. While
not being first on every measure, it is the most balanced method. As WS-Area and WS-Volume, it shows a small tendency for under-segmentation.

As reference state-of-the-art results, we include Multiscale Combinatorial Grouping (MCG) hierarchies from [10], Convolutional Object Boundaries (COB) hierarchies from [59, 58], and Least Effort Segmentation (LEP) from [59] in our assessment. MCG also uses SED as the main cue for contour detection, but then merges several hierarchies (referred to as OWT-UCM in the literature [7]) computed at different scales. COB relies on hierarchy construction algorithm similar to MCG but uses a CNN based gradient detector. LEP also relies on a modified version of SED for contour detection and utilizes a region merging criterion that combines a classical data fidelity term with a new regularization term that measures the effort needed for a human segmenter to draw the contour of a region. Finally, we also include the results obtained with a Random Hierarchy to provide a baseline. The Random Hierarchy of an image is defined as the QFZ hierarchy of a random gradient. This random gradient does not contain any information about the image content: the edges of the graph are weighted by random uniformly distributed values.

Comparing to state-of-the-art methods, COB, which is the only method to rely on a convolutional neural network trained on Pascal Context train set, clearly dominates. WS-Parents does not perform as well as other methods on precision-recall curves but is competitive in terms of upper-bound measures: this indicates that the indexing of the regions in the WS-Parents is not optimal.

Execution times are reported in Table 1. Watershed hierarchies are at least an order of magnitude faster than other methods on BSDS 500 images [7]. The execution time of the different watershed hierarchies are all similar as the computation of the attribute values represent a negligible part of the total computation. We also performed tests on high resolution RGB images (4160 × 2340 pixels) giving a mean processing time of 5.5 s (4 s to compute SED gradient and 1.5 s to construct the watershed hierarchy).

<table>
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<tbody>
<tr>
<td>gradient</td>
<td>70 ms</td>
<td>1 s</td>
<td>4 s</td>
<td>300 ms</td>
</tr>
<tr>
<td>hierarchy</td>
<td>20 ms</td>
<td>1 s</td>
<td>4 s</td>
<td>300 ms</td>
</tr>
<tr>
<td>total</td>
<td>90 ms</td>
<td>2 s</td>
<td>24 s</td>
<td>800 ms</td>
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Figure 9. Best achieved results for watershed hierarchy. (See Figure 7 for explanation).
the complementarity of the new metrics – FHC curve, FOC curve, and object detection – with the standard precision-recall curve. The FOC and FHC curves enable to see a difference between the behavior of LEP and MCG that is not noticeable in the precision-recall curves, showing that LEP has a tendency for over-segmentation. They also enable to characterize the indexing problem in the WS-Parents hierarchy which exhibits a large gap between the FHC and FOC curves. The discrepancy between the results of WS-Parents on precision-recall curves and supervised object detection also supports the need for assessment measures that go beyond the use of horizontal cuts. Finally, we can observe that the three metrics are clearly able to discriminate the baseline method (Random Hierarchy).

6 Conclusion

We have proposed a novel evaluation framework for the assessment of hierarchies of partitions that enables to capture the quality of different aspects of the hierarchies: regions, contours, horizontal cuts, optimal cuts, nodes grouping, under or over-segmentation. Compared to the classical approach for hierarchy evaluation that concentrates only on the horizontal cuts and the image segmentation problem, we believe that the proposed framework offers a richer assessment that better accounts for the hierarchical nature of the representation and is not limited to a single use case.

This framework was used to assess various hierarchies of morphological segmentations. In particular, we studied the importance of the gradient measure for all methods and the necessity to perform a filtering of some hierarchies. The framework also allowed us to identify a watershed hierarchy which exhibits a large gap between the FHC and FOC curves. The framework also enabled us to characterize morphological hierarchies as hierarchical representations, which are well defined structure, satisfying global optimality properties, and can be efficiently computed on large data: they are thus valuable candidates for various computer vision tasks.

All the programs used to compute the hierarchies and the evaluation measures (and their source code) are available online at http://www.esiee.fr/~perretb/supeval.html. In future work, we plan to study the integration of more complex and relevant visual cue to define watershed hierarchies, such as the ongoing works from [30], [60] on

![Figure 10. Comparison with state-of-the-art methods. (See Figure 7 for explanation).](image-url)
iterative stochastic watershed hierarchy generation or on watershed hierarchies combinations. Another challenge will be to take account for richer multi-scale and oriented gradient information provided by deep learning methods that enabled a large performance boost in COB [56].

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