Fatigue life of a shot-peened nickel-based single crystal superalloy: from measurements to modelling.
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Abstract

In this work, X-ray diffraction measurements and finite elements calculations are combined to investigate the effect of the shot-peening process on the fatigue lifetime of the AM1 nickel-based single crystal superalloy. The Ortner method is used to determine residual elastic stress depth profiles in plane-parallel samples. They exhibit a 130-160\(\mu\)m thick hardened layer where compressive stresses up to 1000-1400 MPa take place. The tensile stresses which ensure the mechanical equilibrium of the samples are not localized in a specific layer but rather distributed in a few millimeters thick layer. The eigenstrain theory is then used to incorporate measured stresses in the elastoviscoplastic modelling of shot-peened fatigue test specimens. A numerical method is proposed to initialize hardening variables in the shot-peened layer independently of the complexity of the constitutive law or measurements in calibration samples. Finally, a fatigue analysis at 650\(^\circ\)C is performed in samples with a stress-concentration. The effect of shot-peening on the fatigue lifetime is studied using both modelling and measurements. Results are in good agreement in the investigated range of applied stresses. However, measurements show that the shot-peening operation is not always beneficial.

Introduction

The fatigue analysis of blades in the hot stage of aeronautical gas turbines is extensively investigated to improve the engine reliability. Life prediction of these components under complex thermomechanical loading and environmental conditions is nowadays associated with the design process by the industry. Finite element calculations at the level of the component are able to identify fatigue critical zones and crack initiation time depending on its thermal and mechanical history [1]. The development of a consistent approach connecting the physical variables required to describe the mechanical behavior of the material to those required to describe the fatigue process is still a challenging task because damage is closely connected to the microstructure of the material. For blades made of AM1 nickel-based single crystal superalloy, a lifetime analysis has been developed since the 80’s in the framework of continuum damage mechanics. The elastoviscoplastic model which enables to reproduce the anisotropic behavior of the single crystal at different temperatures is coupled to a creep-fatigue damage model [2, 3, 4].

To delay crack initiation and propagation and thus improve fatigue lifetime, turbine blade roots are shot-peened. The compressive residual stress layer and the plastic deformation created at the surface of the component contribute to relax stress concentration caused by the fir-tree geometry. Due to the complex thermomechanical loading endured by blades during service, one may wonder in which circumstances the shot-peening treatment is really beneficial.

The aim of this study is to take into account stress fields and work hardening generated by shot-peening in the finite element code Zset/Zebulon used by SNÉCMA (SAFRAN group) and ONERA for modeling cyclic fatigue in the AM1 single-crystal superalloy. The ultimate goal of this work is to get efficient estimations of the benefit of the shot-peening treatment regarding the fatigue lifetime.

The paper is organized as follows. The first section is devoted to the determination of elastic stresses using the Ortner method [6]. After a description of the formalism and technical details, stress measurements on a specimen with shot-peened flat surfaces oriented along the \(<100>\) and \(<110>\) crystallographic directions are presented. In the second section, the procedure used to incorporate stresses in the finite element calculations is described and applied to generate the initial mechanical state of a shot-peened single crystal fatigue test specimen. In the last section, the low cycle fatigue lifetime of
specimens exhibiting a stress concentration is calculated and compared to measurements.

Residual stress determination in single crystals using X-ray diffraction

Formalism and methodology

The strain of the crystal lattice is determined by X-ray diffraction measurements. The elastic stress tensor $\mathbf{T}$ is then deduced with the generalized Hooke law:

$$\mathbf{T} = \mathbf{C} : \mathbf{E}$$

(1)

where $\mathbf{C}$ and $\mathbf{E}$ are the elastic stiffness and strain tensors of the crystal lattice. In the case of single crystals, the determination of strains with the $\sin^2\psi$ method is not possible. When a monochromatic wavelength is used, the Ortner method can be employed [6]. The Green-Lagrange strain tensor components $E_{ij}$ are related to the metric tensor components $g_{ij}$ and $g^{ij}$ of the deformed and undeformed crystal lattices by:

$$E_{ij} = \frac{1}{2}(g_{ij} - g_{ij}^0)$$

(2)

where $g_{ij} = \mathbf{a}_i \cdot \mathbf{a}_j$ with $\mathbf{a}_i$ ($i=1,2,3$) the crystal lattice basis vectors.

Diffraction techniques involve measurements in the dual (reciprocal) space of the crystal lattice. By definition of the reciprocal space basis $\{\mathbf{g}_i^*\}$ ($i=1,2,3$), the components of its metric tensor $g_{ij}^* = \mathbf{a}_i^* \cdot \mathbf{a}_j^*$ are obtained by inverting the $g_{ij}$ matrix:

$$[g_{ij}^*] = [g_{ij}]^{-1}$$

(3)

and are related to diffraction angles by:

$$\sum_{i,j=1}^{3} h_i h_j g_{ij}^* = d_{h}^{-2} = \frac{4\sin^2\theta_h}{m^2\lambda^2}$$

(4)

where the coefficients $\{h_i\}$ correspond to the Miller indices of the lattice plane associated with the node of the reciprocal lattice designated by the vector $\mathbf{h}$, $\theta_h$ is the angle between the incident beam and the scattering planes, $m$ is an integer corresponding to the order of the reflection and $\lambda$ is the wavelength of the incident wave. In principle, six Bragg angles corresponding to non colinear $\mathbf{h}$ vectors have to be measured in order to fully determine the metric tensor. However, in order to reduce the effect of uncertainties on the accuracy of the solution, the number of lattice planes $N$ is usually taken larger [7, 8]. Therefore, the system which must be solved is made of $N$ linear equations with six unknown components $(g_{11}^*, g_{22}^*, g_{33}^*, g_{23}^*, g_{13}^*, g_{12}^*)$ since metric tensors are symmetric. The best solution in the sense of least-square minimization is obtained by solving the normal equations. Thus, the six independent coefficients of the reciprocal space metric tensor $g_{ij}^*$ are given by :

$$[g^*] = ([h]^T [h])^{-1} [h]^T [d^{-2}]$$

(5)

with

$$[h] = \begin{bmatrix} h_1^2 & k_1^2 & l_1^2 & 2k_1l_1 & 2h_1l_1 & 2h_1k_1 \\ h_2^2 & k_2^2 & l_2^2 & 2k_2l_2 & 2h_2l_2 & 2h_2k_2 \\ \vdots & \vdots & \vdots & \vdots & \vdots & \vdots \\ h_N^2 & k_N^2 & l_N^2 & 2k_Nl_N & 2h_Nl_N & 2h_Nk_N \end{bmatrix}$$

(6)

$$[d^{-2}] = \begin{bmatrix} 4\sin^2\theta_1 \\ \vdots \\ 4\sin^2\theta_N \end{bmatrix}$$

(7)

$$[h]^T [d^{-2}]$$

(8)

where $h_i$, $k_i$ and $l_i$ are the Miller indices of the $i$th lattice plane used for the measurement. To minimize numerical errors, the number of lattice planes and their orientation relationship must be chosen such that the condition number associated with the linear equation 5 is small [7, 8, 9].

The methodology applied in the following to determine residual stress depth profiles can be summarized as follows:

- measurement of $N > 6$ Bragg angles
- calculation of $g_{ij}^*$ using Eq. 5
- calculation of $[g_{ij}] = [g_{ij}]^{-1}$
- calculation of the crystal lattice strain tensor $E_{ij}$ using Eq. ??
- calculation of the crystal lattice stress tensor $T_{ij}$ using Eq. 1
- calculation of the stress tensor in the reference system of the specimen
- material removal by electropolishing and iteration of the procedure.

Material and technical details

Samples Electro Discharge Machining (EDM) is used to obtain 15 mm x 6 mm x 6mm plane-parallel samples from a bar of the AM1 nickel-based single crystal produced by directional solidification at SNECMA. For all samples, the 6 mm x 6mm surfaces are oriented along the [010] crystallographic direction which corresponds to the solidification axis and the primary arms axis of dendrites. Other surfaces have <100> (Fig. 1a) or
Figure 1: Schematics of the relationship between sample geometry, dendrites and crystallographic orientations of investigated samples. \( \mathbf{e}_1, \mathbf{e}_2, \mathbf{e}_3 \) designates the Cartesian coordinate system used to express tensor components. Shot-peening and X-ray diffraction measurements are realized on the dotted surface which is oriented along (a) the [001] crystallographic direction or (b) the [101] crystallographic direction. (c) and (d) are optical micrographs of sample sides where ”PDAS” denotes the Primary Dendrite Arm Spacing. Black and white spots represent porosity and eutectic phases respectively. (e) is a Scanning Electron Microscopy micrograph of the cuboidal \( \gamma' \) precipitates (dark grey) surrounded by the \( \gamma \) matrix (light grey).

\(<110> \) (Fig. 1b) crystallographic orientations depending on the batch of samples. Optical microscopy observations reveal dendrites with a primary arms separation in order of 500 \( \mu m \) (Fig. 1c and Fig. 1d). Porosity due to the solidification process and coarse \( \gamma' \) particles which have not been entirely removed by the solution heat treatment are also present (black and white spots in (Fig. 1c-d)). Shot-peening and diffraction measurements are realized on one of the 15 x 6 mm\(^2\) surfaces. To remove the oxidation layer and the residual stresses which may have been introduced by the EDM, this surface is subjected to a soft mechanical polishing. Solution and ageing heat treatments are then realized to obtain an austenitic nickel rich \( \gamma \) matrix strengthened by about 70% volume fraction of \( \gamma'\text{-Ni}_{3}\text{Al} \) ordered precipitates with a cubic L1\(_2\) structure. \( \gamma' \) precipitates have cuboidal shapes with sizes lower than 1 \( \mu m \) and are homogeneously distributed in the \( \gamma \) matrix ((Fig. 1e). The lattice mismatch between the two phases is smaller than 0.05%. The last step of samples preparation is the shot-peening which is realized with 1 mm diameter 100Cr6 steel shots at 100% coverage by an ultrasonic technique.

Measurements conditions and data analysis  

The diffraction measurements are realized using a diffractometer composed of a Rigaku microfocus X-ray generator equipped with parabolic optics (Cu wavelengths), a general purpose Huber 6-circles goniometer and a NaI(Tl) scintillation detector located at 700 mm from the sample position. The opening of the divergence and detector crossed slits is set to 1 mm \( \times 1 \) mm in order to have a good signal to noise ratio when high angles diffraction peaks are investigated in shot-peened samples. Once the diffraction condition has been found for a given (hkl) reflection, all the goniometer motor positions are recorded and a \( \theta-2\theta \) scan is realized to obtain the diffraction peak. Data are then corrected by the Lorentz-polarisation factor and scans are analyzed with a least-square fitting procedure using a Rachinger doublet [10]. As explained above, the knowledge of the Miller indices and the Bragg angle of at least six reflections enables to determine the metric tensor of the crystal unit cell, thus the six parameters of the Bravais lattice.

Due to the small lattice mismatch between the \( \gamma \) and \( \gamma' \) phases, the contribution of the two phases in (hkl) diffraction peaks with \( h,k,l \) having the same parity are not differentiated using our experimental setup. In principle, additional monochromators would probably help but with higher X-ray beam fluxes. Also, the large peak broadening caused by shot-peening would not guaranty a quantitative deconvolution of the two contributions. Therefore, our analysis of fundamental reflections provide the average strain between the \( \gamma \) and \( \gamma' \) phases. Best strain sensitivity and a small conditions numbers

Figure 2: \((\omega, \eta)\) intensity maps (counts per second) around the \((T33)\) reflexion in the reference sample at at depth of 202 \( \mu m \).
are obtained with reflections diffracting at high Bragg angles. In this work, \{420\}, \{331\}, \{004\} and \{222\} reflections are considered. This corresponds to diffraction angles close to 147°, 138°, 118° and 96° respectively. 21 Bragg angles are used in the calculations when the sample surface is oriented along the [100] crystallographic direction, 20 when the surface is oriented along the [110] direction. To determine the residual stress tensor components, a macroscopic stiffness tensor determined from mechanical testing measurements at room temperature is used: \(C_{1111}=296 \text{ GPa}, C_{1122}=204 \text{ GPa}\) and \(C_{2323}=125 \text{ GPa}\) [12]. Superstructure reflections are related to the \(\gamma\)' phase only and have intensities more than 1000 times smaller than fundamental reflections [13]. For the shot-peened specimen, crystal misorientations near sample surface reduce significantly the maximum intensity of Bragg peaks resulting in intensities comparable to the noise intensity. Thus, our setup is not able to provide a complete residual strain depth profile related to the \(\gamma\)' phase.

The evaluation of uncertainties is performed through a Monte-Carlo approach, assuming random fluctuation around the measured diffraction angle. Uncertainties include lattice parameter variations due to composition fluctuations, mosaic spread introduced by the dendrites and errors arising from the least-squares fitting procedure of the Bragg peaks. Details are provided in [13].

Results and discussion

Reference sample Figure 3 represents the six unit cell parameters of the undeformed state: measurements of the unit cell parameters in a reference sample which has not been subjected to shot-peening. (a) cell lengths (b) cell angles \(\alpha_i = (a_j, a_c)\)

Two methods are commonly employed to determine the metric tensor \(g^0\) of the undeformed state: measurements of the unit cell parameters in a reference sample or, for low penetrating radiations, the plane stress approximation, where the lattice parameter of the reference state is taken such that the component \(T_{33}\) of the stress tensor related to the deformed state is zero (with \(e_3\) direction along the surface normal of the sample). For the Cu wavelength, the X-ray attenuation length in the superalloy is close to 10 \(\mu\)m. Depending on the orientation of the sample with respect to the incoming and diffracted beams, the characteristic depth probed ranges from 1\(\mu\)m for grazing angles to 10 \(\mu\)m close to normal angles. Both methods are assessed in this work.

Marty et al. and Brückner et al. have shown that in the diffraction condition, several local maxima are visible due to the misorientation between dendrites [14, 15]. This is illustrated in Fig. 2. In such case, \(\theta-2\theta\) scans are recorded for \(n\) local maxima, with \(n \leq 4\) in order to quantify the variations of the lattice plane spacing. The strain is calculated from the middle of the variation range of peak positions, while the error bar is computed from half the range. After an optimization work detailed in Ref. [13], we show that the lattice parameter fluctuations related to the dendritic microstructure and the choice of reflections in the calculations result in 30 MPa uncertainties on the calculated stress tensor components.

Sample with a \{100\} shot-peened surface Stress calculations in samples with a shot-peened surface oriented along the \{001\} crystallographic direction are determined from 21 Bragg angles. Residual elastic stress depth profiles resulting from sets of measurements and layer removals are represented in Fig 4 using the metric tensor of Eq. 9 (Fig. 4a) and the plane stress approximation (Fig. 4b). The evolution of \(T_{11}\) and \(T_{22}\) which differ by less than 30 MPa, shows compressive stresses taking place in the 150\(\mu\)m thick surface layer and almost zero residual stress deeper. The shear components \(T_{ij}\) with \(i \neq j\) are close to zero for all depths. Although
Figure 4: Independent components of the residual stress tensor calculated from measured crystal lattice parameters $a_i$ and $\alpha_i$ ($i=1,2,3$) as function of depth in the shot-peened sample whose surface is oriented along a $\{100\}$ crystallographic direction. The Cartesian basis is oriented such as $\hat{e}_2$ and $\hat{e}_3$ are colinear with the surface normal and the long edge of the sample (schematics). Dashed line corresponds to the ultimate stress of the AM1 superalloy determined from tensile or fatigue tests [16].

Each measurement is realized on a free surface, in the layer affected by the shot-peening process, $T_{33}$ significantly differs from zero when the metric tensor of the reference sample is used (Fig. 4a). This is probably due to the modification of the material properties (solid solution gradients, loss of coherency strains) in this layer because of the strong hardening caused by shot-peening and the lattice parameter of the reference state should not be taken like the measured one in the reference sample. In figure 4, the dashed line represents the ultimate stress limit of the AM1 material [16]. In Fig. 4a stresses close to the sample surface are larger than this value. The maximum difference with this limit is about 300 MPa at the 20 µm depth. This is not incompatible since the material is strongly hardened in this area and if all the tensor components are considered, the Von Mises stress is only 60 MPa above the ultimate stress limit. Fig. 4b represents the residual stress profile determined from the same measurement but with the plane stress approximation ($T_{33} = 0$). The evolution of the lattice parameter of the reference state (cubic symmetry) as a function of depth is represented in the inset. Up to 200 µm, its value differs from the lattice parameter of the reference sample (dashed line). As in figure Fig. 4b, $T_{11}$ ans $T_{22}$ components are almost equal ans shear components close to zero. The highest absolute value is about 1000 MPa close to the surface.

Figure 5: Evolution of residual stresses as a function of depth. Filled symbols correspond to $T_{11} = T_{22} = T_{33}$ and open symbols to $T_{33} = T_{11}$. The profile with square symbols is determined with respect to the lattice parameter of a reference sample and circle with respect to the plane stress hypothesis.

Two additional corrections must be done to the stress profile calculated from Bragg peak positions: the first one to account for the stress relaxations resulting from material removals and the second to account for the fact that the X-ray beam probes a stress gradient. In the latter case, it can be shown that the measured value of the $T_{33}$ component close to the surface plane is twice its true value providing that the stress gradient at the surface is zero (see discussion in [13]). The Moore and Evans correction for stress relaxations due to material removals is applied [17]. The resulting stress profiles are represented in Fig. 5. The residual stress depth profile exhibit a 130-160µm thick hardened layer where $T_{11}$ and $T_{22}$ compressive stresses up to 1000-1400 MPa take place depending on the assumption used to describe the initial state. The tensile stresses which ensure the mechanical equilibrium of the sample are not localized in a specific layer with high levels of stresses but rather distributed in a few millimeters thick layer.

Effects of the crystal anisotropy To quantify the effect of the crystalline anisotropy on the stress field caused by the shot-peening process, samples with surfaces oriented along the $<100>$ and $<110>$ crystallographic directions have been shot-peened in the same conditions. The relationship between the sample surface and the crystal unit cell orientations is represented in Fig. 6. For both orientations, shear components of stress tensors are almost zero (within the ± 30 MPa uncertainty) with re-
The eigenstrain framework enables to account for strains caused by phenomena such as thermal expansion mismatch, phase transformation or plastic deformation. The formalism can be easily implemented in finite element calculations and a detailed modeling of the process generating residual stresses is not required when measurements are available. The method is extensively used to investigate stresses in shot-peened components mainly for the following reasons: (1) for a given eigenstrain distribution, an equilibrated residual stress distribution can be calculated for any geometry. (2) the residual stress state evolution during an additional plastic activity in the material is able to be modelled through the modification of the eigenstrain distribution. (3) the eigenstrain distribution related to the shot-peening process can be determined from residual stress measurements on samples with simple geometries and then be incorporated into the modeling of components with more complex geometries.

In the small strain approximation, the mechanical equilibrium of a system with stress free boundary conditions at the surfaces is obtained by solving the following set of equations:

\[
\begin{align*}
\text{Inc} \quad \epsilon &= 0 \\
\nabla \cdot \sigma &= 0 \\
\sigma \cdot n &= 0 \\
\epsilon &= S : \sigma + \epsilon^*
\end{align*}
\]

where \(\sigma\) is the residual stress tensor, \(\epsilon\) is the total strain tensor, \(S = C^{-1}\) is the compliance tensor, \(\epsilon^*\) is the eigenstrain tensor and \(n\) corresponds to the surface normal. The shot peening being operated in normal conditions, we assume that only the stress tensor components in the surface plane are non-zero. The solution of Eqs. 10 for a plate-like sample which has been shot-peened on a face oriented along the \(\hat{e}_3\) direction has the following form:

\[
T_{11} = \begin{pmatrix} T_{11}^1 & T_{12}^1 & T_{13}^1 \\ T_{12}^1 & T_{22}^1 & T_{23}^1 \\ T_{13}^1 & T_{23}^1 & T_{33}^1 \end{pmatrix}
\]

where \(T_{ij}\) are the diagonal components of the stress tensor in the sample coordinate system.

Table 1: Diagonal components of the \(T\) stress tensor at a 20\(\mu\)m depth when the shot-peened sample surface is oriented along the [001] or the [101] crystallographic direction. Values are given in MPa in the \((\hat{e}_1, \hat{e}_2, \hat{e}_3)\) sample basis (see Fig. 6). The reference state corresponds to a cubic lattice with \(a^0 = 3.58985\AA\) or to the plane stress hypothesis.

<table>
<thead>
<tr>
<th>Surface orientation</th>
<th>Reference state</th>
<th>(T_{11})</th>
<th>(T_{22})</th>
<th>(T_{33})</th>
</tr>
</thead>
<tbody>
<tr>
<td>[001]</td>
<td>reference</td>
<td>-1363</td>
<td>-1363</td>
<td>-177</td>
</tr>
<tr>
<td>[101]</td>
<td>sample</td>
<td>-1500</td>
<td>-1180</td>
<td>-112</td>
</tr>
<tr>
<td>[001]</td>
<td>plane stress</td>
<td>-1010</td>
<td>-1010</td>
<td>0</td>
</tr>
<tr>
<td>[101]</td>
<td>hypothesis</td>
<td>-1275</td>
<td>-957</td>
<td>0</td>
</tr>
</tbody>
</table>

Finite element calculations incorporating residual stresses resulting from shot-peening

The initial state introduced in the calculations must be as close as possible to the state generated by the shot-peening process and corresponds to a mechanical equilibrium. To reproduce stress redistributions during cyclic loading conditions, internal variables such as eigenstrain, kinematic hardening and accumulated plastic deformation must be carefully initialized in addition to the choice of their governing equations. In the case of single crystals, data obtained from measurements are not able to provide such values for every Gauss point. Therefore assumptions and interpolation schemes are required. In the following, we present a generic approach to initialize internal variables in the layer affected by the shot-peening in the case of single crystals. The method is then applied to investigate the lifetime of a fatigue test specimen made of the AM1 superalloy.

Internal variables initialization

Eigenstrain. The eigenstrain framework enables to account for strains caused by a wide range of phenomena such as thermal expansion mismatch, phase transformation or plastic deformation. The formalism can be easily implemented in finite element calculations and a detailed modeling of the process generating residual stresses is not required when measurements are available. The method is extensively used to investigate stresses in shot-peened components mainly for the following reasons: (1) for a given eigenstrain distribution, an equilibrated residual stress distribution can be calculated for any geometry. (2) the residual stress state evolution during an additional plastic activity in the material is able to be modelled through the modification of the eigenstrain distribution. (3) the eigenstrain distribution related to the shot-peening process can be determined from residual stress measurements on samples with simple geometries and then be incorporated into the modeling of components with more complex geometries.

In the small strain approximation, the mechanical equilibrium of a system with stress free boundary conditions at the surfaces is obtained by solving the following set of equations:

\[
\begin{align*}
\text{Inc} \quad \epsilon &= 0 \\
\nabla \cdot \sigma &= 0 \\
\sigma \cdot n &= 0 \\
\epsilon &= S : \sigma + \epsilon^*
\end{align*}
\]

where \(\sigma\) is the residual stress tensor, \(\epsilon\) is the total strain tensor, \(S = C^{-1}\) is the compliance tensor, \(\epsilon^*\) is the eigenstrain tensor and \(n\) corresponds to the surface normal. The shot peening being operated in normal conditions, we assume that only the stress tensor components in the surface plane are non-zero. The solution of Eqs. 10 for a plate-like sample which has been shot-peened on a face oriented along the \(\hat{e}_3\) direction has the following form:

\[
T_{11} = \begin{pmatrix} T_{11}^1 & T_{12}^1 & T_{13}^1 \\ T_{12}^1 & T_{22}^1 & T_{23}^1 \\ T_{13}^1 & T_{23}^1 & T_{33}^1 \end{pmatrix}
\]
Figure 7: Evolution of residual elastic stresses (left axis) and eigenstrain (right axis) as a function of depth. Circles corresponds to X-ray diffraction measurements and lines to modeling. $X_\parallel$ and $X_\perp$ denotes in-plane and normal components of $X$ tensor.

expression:

$$
\begin{align*}
\epsilon^{\ast}_{11}(z) &= A_1 z + B_1 - [S_{11} \sigma_{11}(z) + S_{12} \sigma_{22}(z)] \\
\epsilon^{\ast}_{22}(z) &= A_2 z + B_2 - [S_{12} \sigma_{11}(z) + S_{22} \sigma_{22}(z)] \\
\epsilon^{\ast}_{33}(z) &= -[\epsilon^{\ast}_{11}(z) + \epsilon^{\ast}_{22}(z)]
\end{align*}
$$

with

$$
A_i = \frac{12}{h} \int_{-h/2}^{h/2} z \epsilon^{\ast}_{ii}(z) dz
$$

$$
B_i = \frac{1}{h} \int_{-h/2}^{h/2} \epsilon^{\ast}_{ii}(z) dz = <\epsilon^{\ast}_{ii}>_z
$$

where $h$ is the sample thickness. As illustrated in Fig. 7, the residual elastic stress depth profile of Fig. 5 is easily modelled if a Gaussian function is assumed for the $z$ dependence of $\epsilon^{\ast}_{11}(z)$ and $\epsilon^{\ast}_{22}(z)$ (dashed lines in the figure).

Kinematic hardening and accumulated plasticity. The method is inspired by the work of Grasty and Andrew [18] where the upper layers of the system are subjected to a squeeze pressure such that a small plastic deformation is generated. This process was iterated by the authors until a known curvature caused by the indentation process is retrieved. Here, we use a similar strategy in the sense that a pressure is applied at different depths in such a way that after release eigenstrain values determined previously are found. The pressure is applied using a serrated function of time until the mechanical state has reached the equilibrium and the accumulated plastic deformation a target value, which is material history dependent. Here, as a rough approximation, diffraction peak widths recorded in shot-peened sample are compared to peak widths evolution determined in calibration samples with a known amount of macroscopic plastic deformation. To reduce calculation costs, this procedure is applied only to a finite set of representative volume elements (RVE) chosen at different locations in the system of interest. The values of variables resulting from independent calculations are then associated with the considered Gauss point and values related to other points are determined by interpolation. In practice, due to the symmetry of the eigenstrain tensor determined previously, the pressure is applied only to the element surface which is parallel to the shot-peened surface, all other boundaries being fixed.

Crystal anisotropy. To take into account the effect of the crystal anisotropy, the procedure developed above can be applied to residual elastic stress measurements in samples with different surface orientations. However, if data are not available, the pressure caused by multiple shots during the peening operation can be supposed...
independent of the crystallographic orientation of the sample surface. This implies that the pressure value and the number of cycles determined for the [100] crystallographic direction can be used to determine eigenstrain, kinematic hardening, accumulated plastic deformation and residual elastic stress values for all crystal orientations. This methodology is applied to a fatigue test specimen with a cylindrical geometry (3.11mm radius). Calculations are realized at room temperature with the anisotropic elastoviscoplastic model developed for the AM1 superalloy [19]. Fig. 8 represents the hoop ($\sigma_{\theta\theta}$) and axial ($\sigma_{zz}$) stresses in a quarter of cross-section. The hoop stress is significantly affected by the crystal anisotropy since in Fig. 8a, stresses differ by about 500 MPa between the [100] and [110] crystal directions in the shot-peened layer. In the case of the [100] direction, the depth profile exhibit compressive stresses up to 1000 MPa in a 150$\mu$m thick layer and tensile stresses are smoothly distributed with depth (solid line in Fig. 8b). In the case of the [110] direction, compressive stresses up to 1500 MPa take place in a 100$\mu$m thick layer and a tensile stress layer is clearly visible. The axial stress behavior is less affected by the crystal anisotropy as shown in Fig. 8c and Fig. 8d (dashed line). Calculations only show that the layer where compressive stresses take place is thinner in the [110] direction than in the [100] direction. At a 20 $\mu$m depth, the calculated hoop component is 34% lower in the [110] direction than in the [100] direction. This value has to be compared with 28% in the case of measurements in flat samples (see Tab. 1). The axial stress is 10% lower in the calculations whereas it is 5% higher in experiments. X-ray measurements in a shot-peened fatigue specimen are in progress to assess the relevance of trends observed in calculations.

Towards fatigue lifetime assessment

The ultimate goal of this work is to get efficient estimations of the benefit of the shot-peening treatment regarding the fatigue lifetime. The generated residual stresses that influence the mechanical state at the surface of the part may evolve with the development of the plasticity in the component during cyclic loading conditions and work hardening will also play a significant role on this stress relaxation. Residual stresses and work hardening need then both to be taken into account in the fatigue analysis. The method proposed in the previous section to introduce those quantities in a finite element mechanical analysis in fatigue allows for an assessment of their combined and separated contribution. In the following, the method is used to estimate the low cycle fatigue lifetime to crack initiation at 650°C on notched specimens made of the AM1 single crystal superalloy. The accuracy of the proposed approach to account for the influence of residual stresses and work hardening on lifetime prediction is assessed through comparisons with experimental results.

The fatigue life analysis of structures more often is based on the use of a damage model to describe the initiation and coalescence of micro-cracks leading to an observable macroscopic crack. The damage evolution usually expressed in terms of damage increment per cycle is then introduced into a lifetime workflow. As admitted generally for metallic materials, this workflow can be build assuming an uncoupled formalism between the descriptions of the viscoplasticity and hardening mechanisms occurring in the materials and the damage evolution [20]. However, interaction between damage mechanisms induced by fatigue and creep is often considered eventually coupled with oxidation effects [3]. The lifetime assessment of the fatigue samples considered in this study is then performed following several steps briefly presented hereafter.

Figure 9: Left - local damage maps calculated model in notched cylindrical fatigue test samples with a stress-concentration factor $K_t=1.6$ subjected to an applied stress of 800 MPa at 650°C (f=15Hz, $R_\sigma=0$). Zoom in the crack initiation area in (a) a smooth sample (c) a shot-peened sample. Views are mirrored for sake of comparison. Right - fracture SEM micrographs in corresponding fatigue test specimens.

Firstly, the procedure described before is used to introduce in the finite element model the initial profiles of the residual stresses and all the hardening variables considered in the constitutive model, chosen to simulate the mechanical behavior of the material. Then, the fatigue loading sustained by the specimens presenting a stress concentration ($K_t=1.6$ in the gauge length) is simulated to account for the stress redistributions due to cyclic plasticity namely in the affected layer by the
shot-peening process. At this stage it is particularly important that the constitutive model chosen to describe the behavior of the material allows for an accurate simulation of both the residual stress relaxation and the work hardening evolution. Determination of their profile after interrupted fatigue tests may be necessary and a specific formulation of the kinematic hardening variables describing Bauschinger effects can be used [4]. Finally, the damage model is applied as a post-processing on mechanical quantities obtained at the stabilized cycle such as for instance the octahedral shear stress amplitude, the mean value of the hydrostatic stress and the maximum stress eigen to compute the fatigue life and to get the crack localization in the structure. For the analysis performed in this study, a multiaxial creep-fatigue damage model, recently improved, has been used to compare the estimated lifetime between smooth and shot-peened specimens. A zoom of the local damage map is represented in Fig. 9 for both type of samples. Calculations correspond to a cyclic fatigue test at 650°C and a 800 MPa applied stress. In the case of the smooth specimen, the maximum of damage is localized at the sample surface and corresponds to 3000 cycles before crack initiation (Fig. 9a). The effect of shot-peening is clearly visible in Figs. 9c since the maximum of damage is localized about 200 µm beneath the surface and corresponds to a number of cycles one order of magnitude higher. These trends are corroborated by the scanning electron micrographs which show that cracks initiate at the sample surface for the smooth specimen and at a 200 µm depth for the shot-peened specimen (arrows in Fig. 9b and Fig. 9d). Numerical and experimental results obtained for different levels of nominal applied stress are represented in Fig. 10. Calculated and experimental lifetimes are in good agreement when the shot-peening process has beneficial effects. The lifetime is 10(12) times higher at 800 MPa and 4(4) times higher at 635 MPa in the modelling (measurements) respectively. However, in measurements a crossover is observed between 585 MPa and 635 MPa since the lifetime is lower for shot-peened samples. This tends to show that the sample surface roughness is the limiting factor for the fatigue lifetime in the small applied stress regime.

Conclusion

In this paper, X-ray diffraction measurements and finite element calculations are performed to study the effect of shot-peening on the low cycle fatigue of a nickel-based single crystal superalloy (AM1). In the modelling, the mechanical state associated with the shot-peened operation is incorporated using the results of the residual elastic stress measurements, the eigenstrain framework and a generic procedure which enables to initialize the kinematic hardening and accumulated plastic deformation variables independently of the constitutive equation complexity. A specific approach is also implemented to take into account crystal anisotropy effects when residual stress depth profiles are not available for all surface orientations. These developments are applied to the lifetime prediction of notched fatigue test samples with a stress-concentration factor $K_t = 1.6$.

The residual stress depth profile is determined using the Ortner method in a plane-parallel sample with a shot-peened surface oriented along the [100] crystallographic direction. The profile exhibits a 160 µm-thick hardened layer, where compressive in-plane stresses up to 1000-1400 MPa take place. The tensile stresses which ensure the mechanical equilibrium are smoothly distributed in the sample thickness. Measurements realized in a shot-peened sample with a surface oriented along the [110] crystallographic direction reveal a 30% increase of compressive stresses for the component which is not crystallographically equivalent with respect to the [100] surface orientation. The other in-plane component of the stress tensor is weakly affected by the crystal anisotropy. The eigenstrain distribution associated with the residual (elastic) stress profile is then calculated and elastoplastic calculations are performed to initialize the internal variables of the model in the surface layer affected by the shot-peening process. With this approach, a physically justified equilibrated mechanical initial state is generated and the study of stress redistributions during cyclic thermal and mechanical load-
ings is possible in samples with specific geometries. Finally, the ability of the proposed approach to account for the influence of residual stresses and work hardening on lifetime prediction is assessed in the case of fatigue tests at 650°C on samples having a stress-concentration (Kt=1.6). The results of modelling are in good agreement with measurements in the 635-800 MPa range of applied stress. The increase of the fatigue lifetime due to shot-peening is between a factor 4 and 10. For smaller applied stress, a deleterious effect of shot-peening is measured probably due to a higher sensibility of the damage to the surface roughness of samples.

References


