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Carrier Frequency Offset Estimation Based on Circular Harmonic Expansion for Optical Coherent M -QAM Communication Systems

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Abstract—Circular harmonic expansion-based carrier frequency offset estimation is investigated for optical M -QAM communication systems. The proposed method, combined with a gradient-descent algorithm, shows better performance compared to already proposed VVMFOE and 4th power methods.

Keywords— M -QAM; optical communication; coherent communication; carrier frequency offset.

I. INTRODUCTION

Coherent detection and M -ary quadrature amplitude modulation (M -QAM) signals are very attractive for optical transmission systems beyond 100 Gbit/s [1]. Coherent detection is usually based on the intradyne detection scheme with unlocked transmitter (Tx) and local oscillator (LO) lasers. In such a scheme, the carrier frequency offset (CFO) between the Tx and LO can reach values as high as a few GHz [2], which does not allow proper recovery of the signal if not compensated. Frequency offset estimation (FOE) is hence required in the digital signal processing (DSP) at the receiver (Rx). Substantial efforts have been dedicated to the design of FOE solutions that do not require training symbols in either feedback [1] or feedforward [3] manners and using time domain [4] or frequency domain [5] approaches. Among those, feedforward FOE provides a better laser phase noise tolerance and is more hardware-efficient than feedback FOE [6]. Moreover, the use of periodograms in frequency domain analysis can quickly estimate the CFO with a smaller number of required symbols compared to the time domain approach [5].

The well-known Viterbi-Viterbi fourth power estimator (VV4PE) used for the FOE of M -ary phase shift keying (M -PSK) signals [3] is no longer valid for M -QAM, especially for cross M -QAM signals (e.g. 32-QAM). Several feedforward FOE methods based on the maximization of symbols periodograms using the fast-Fourier transform (FFT) have been proposed so far [5], including a solution for widening the FOE range [7]. However, the applicability of these methods to cross M -QAM was not discussed in detail. Recently, the Viterbi-Viterbi monomial FOE (VVMFOE)

method has been reported in [8], with an extension for cross M -QAM constellations. The idea behind this method is to assign weight coefficients to symbols with different amplitude levels, usually with negative power for cross M -QAM signals. However, the choice of this negative power value is empirical and the negative power may make the implementation in field programmable gate arrays (FPGAs) more complex and require more computational efforts.

In this paper, we investigate an FOE technique based on the circular harmonic expansion (CHE) of the log-likelihood function (LLF) for both square and cross M -QAM signals, called CHEFOE. Based on this expansion, only the first significant term of the resultant series is chosen as an optimum weighting function for FOE. In this way, a look-up table (LUT) can be easily implemented in FPGAs for weighting the symbol amplitudes. This implementation reduces the complexity since it does not make use of negative power. Although FOE based on the CHE method has been presented in [9], it has, to the best of our knowledge, never been exploited in optical coherent communication systems, in which the typical linewidths of commercial distributed feedback (DFB) and external cavity lasers (ECL) range from several kHz to the order of 10 MHz, potentially leading to significant phase noise in the received M -QAM constellation. Moreover, the combination of CHEFOE and gradient-descent algorithm [5] is also proposed and studied. This proposal provides more accurate estimation of CFO with small mean square error (MSE) and smaller required number of symbols, showing the effectiveness of the proposed method.

II. CIRCULAR HARMONIC EXPANSIONS OF THE MAXIMUM LOGLIKELIHOOD FUNCTION FOR CFO ESTIMATION

In previous work [5, 7] (4th power method), the maximization of the following periodogram of the received QAM signal, $x(k) = r(k) \cdot \exp(j \cdot \phi(k))$, is used to estimate the CFO value, $\phi_f = 2\pi \cdot \Delta f \cdot T_B$

$$\hat{\phi}_f = \frac{1}{4} \arg \max_{\phi \in [-1/2, 1/2]} \sum_{p=1}^2 \left| \frac{1}{N} \sum_{k=0}^{N-1} x^4(k) e^{-j2\pi k \phi} \right|^2 \quad (1)$$

where T_B is the symbol period, N denotes the number of symbols and p index the polarization. For simplicity, the following study considers a unique periodogram associated with a single polarization.

Assuming the received symbols at the baud rate are corrupted by complex additive white Gaussian noise (AWGN) with equal variance σ^2 for both real and imaginary parts, the LLF function for an unknown phase shift due to CFO and the laser phase noise, ϕ_0 , is represented as follows [9]

$$LLF(\phi(k) | x(k)) = \log \left[\frac{1}{2\pi\sigma^2 M} \sum_{m=1}^M \exp \left(-\frac{|x(k)e^{-j\phi(k)} - C_m|^2}{2\sigma^2} \right) \right] \quad (2)$$

where the C_m denote the ideal values of the constellation symbols, $m = 1, \dots, M$, and $\phi(k) = \phi_0 + k \cdot \phi_f$.

Expanding (2) in Fourier series along the phase ϕ , the LLF approximation retaining only the first nonzero harmonic component over N symbols is given by [9]

$$LLF(\phi_0, \phi_f | x(k)) \approx \text{Re} \left[e^{-j4\phi_0} F_4(4\phi_f) \right] \quad (3)$$

in which $F_4(4\phi_f) = \sum_{k=1}^N A_4(r(k)) e^{-j4\phi(k)} e^{-j4k\phi_f}$, and $A_4(r)$ is the amplitude of the fourth harmonic.

The CFO is compensated based on the following estimator rule

$$\widehat{\phi}_f = \frac{1}{4} \arg \max_{4\phi_f} \left| F_4(4\phi_f) \right| \quad (4)$$

Comparing (4) to (1), it can be observed that CHEFOE is another version of the 4th power estimator with radius weighting function and without the (negative) power requirement for signal amplitudes. It is also shown that the VVMPE estimator based on optimal nonlinear least-square (NLLS) is inferior to the CHE estimator, especially for cross M -QAM constellations, due to the sign-changing nature of the weighting function $A_4(k)$ [9].

Fig. 1 presents the configuration for M -QAM FOE based on the CHE method. The proposed estimator is cascaded with a fine step implementation of the gradient-descent algorithm to fast converge and to minimize the MSE of the estimated CFO. The fine estimated CFO is given by [5]

$$\widehat{\phi}_f(k+1) = \widehat{\phi}_f(k) + \mu \left[\frac{\partial F_4(4\phi_f)}{\partial \phi_f} \Big|_{\widehat{\phi}_f(k)} \Big/ \frac{\partial^2 F_4(4\phi_f)}{\partial \phi_f^2} \Big|_{\widehat{\phi}_f(k)} \right] \quad (5)$$

in which μ is the step size depending on the symbol block length. This optimization technique reduces the MSE to $1/N^3$ [5].

III. NUMERICAL RESULTS AND DISCUSSION

In order to evaluate the performance of the proposed FOE method, numerical simulations are carried out with 10 GBaud

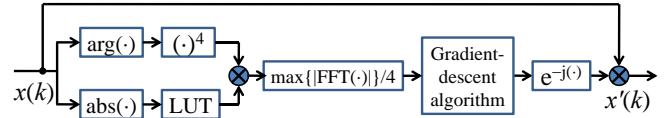


Fig. 1. Block diagram of CHEFOE.

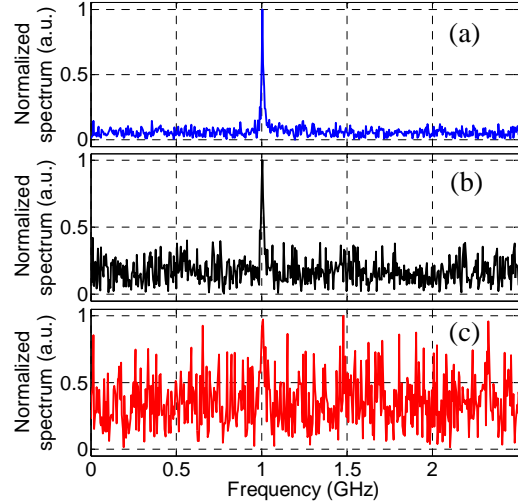


Fig. 2. Examples of normalized spectra of 32-QAM signals with CFO of 0.25 GHz using (a) CHEFOE; (b) VVMFOE; (c) 4th power methods.

16-QAM and 32-QAM signals under the impact of phase noise originating from the laser sources. In the transmitter, the M -QAM signals are generated by differential encoding of a pseudo-random binary sequence (PRBS) with length of $2^{13}-1$ onto the constellation. The phase noise caused by the combined laser linewidth, $\Delta\nu$, is modeled as a discrete time random walk $\phi_n = \phi_{n-1} + \Delta_n$, in which Δ_n is a Gaussian random variable with zero mean and variance $2\pi\Delta\nu T_B$. Moreover, $\sim 130\,000$ symbols are transmitted and corrupted by AWGN noise. The noise is specified by the signal-to-noise ratio (SNR) in the electrical domain. To focus on the FOE function, other sources of impairments such as chromatic dispersion, polarization mode dispersion and timing clock recovery errors are assumed to be completely compensated. Finally, the received symbols are decimated to the baud rate before being sent to the FOE stage. In the following study, 16-QAM and 32-QAM signals at the respective SNRs of 18.4 dB and 20.8 dB, corresponding to 1 dB penalty at the hard forward-error correction (FEC) BER limit of 10^{-3} are used. The mean and standard deviation (STD) of the CFO estimator are calculated based on 500 runs of simulation and compared to the 4th power [5] and VVMFOE [8] methods.

In the first step, the CFO is set to 0.5 GHz and 0.25 GHz for 16-QAM and 32-QAM signals, respectively. The gradient-descent algorithm is not activated for a fair comparison. Fig. 2 presents examples of normalized spectra of 32-QAM signals obtained using 1024 symbols. It can be seen that the CHEFOE and VVMFOE methods provide a better periodogram than the 4th power method. However, the periodogram obtained by CHEFOE is less noisy than that of VVMFOE, indicating a better estimator. In the next step, the CFO estimation error (the difference between the predefined CFO and the estimated one) is evaluated as a function of

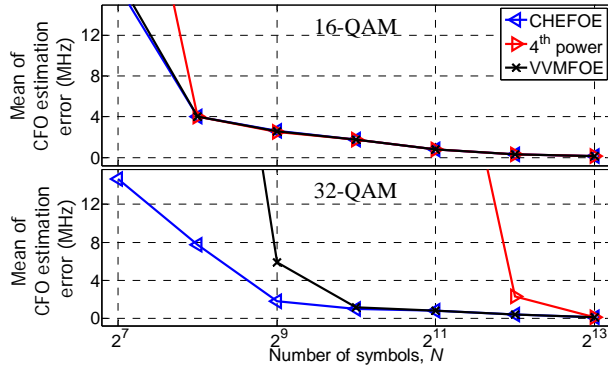


Fig. 3. Average value of the CFO estimation error as a function of the number of symbols, N .

number of utilized symbols, N . The mean (Fig. 3) and the STD (not plotted due to space limitations) of the CFO estimation error are investigated for 16-QAM (upper row) and 32-QAM (lower row) signals. For 16-QAM signals, the three methods give similar performance as the number of symbols exceeds 2^8 , resulting in mean and STD of estimation error smaller than 4 MHz and 2 MHz, respectively. For 32-QAM signals, the required number of symbols for CHEFOE, VVMFOE and 4th power methods required to achieve similar mean and STD values as for 16-QAM signals are 2^9 , 2^{10} and 2^{13} , respectively. It means that the proposed method requires less than half the number of symbols for FOE compared to VVMFOE and 8 times less than the 4th power method, indicating the robustness of the CHEFOE method. The laser linewidth tolerance of the three methods is further studied (Fig. 4) with symbol lengths of 2^9 and 2^{10} for 16-QAM and 32-QAM signals, respectively. For 16-QAM signals, the normalized linewidths that can be tolerated can take values as high as 2.5×10^{-3} , 10^{-3} and 5×10^{-4} using the CHEFOE, VVMFOE and 4th power methods, respectively, in order to obtain a mean of the estimation errors inferior to 5 MHz. For 32-QAM signals, the 4th power method does not work, whereas the normalized linewidth tolerance of the VVMFOE method reduces to 10^{-4} . The CHEFOE method still allows a normalized linewidth tolerance up to 2.5×10^{-3} for a mean of the estimation error below 5 MHz, confirming the effectiveness of the proposed method.

Finally, the gradient-descent algorithm combined with CHEFOE is activated and considered only for 16-QAM signals in comparison to the VVMFOE method with $N = 256$. The extrema of periodogram are chosen such that $4\phi_f T_B$ lies in two adjacent FFT points. Fig. 5 presents the mean and STD of the estimation error using the CHEFOE and VVMFOE methods before and after applying the gradient-descent algorithm. It can be observed that the combination of FOE with gradient descent algorithm reduces by up to a factor two the CFO estimation error compared to FOE alone, indicating the accuracy of the proposed combination estimator.

IV. CONCLUSIONS

A carrier frequency offset estimation based on circular harmonic expansion in combination with the gradient-descent algorithm is proposed and numerically studied for optical

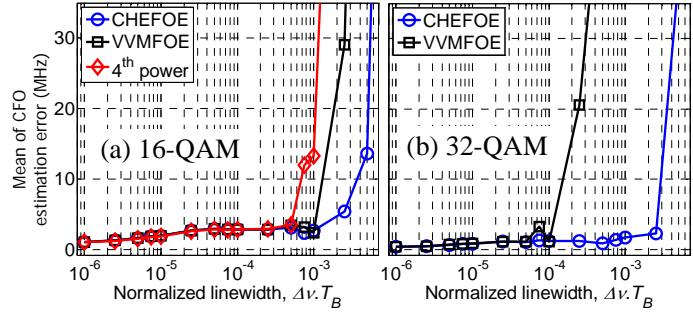


Fig. 4. CFO estimation error versus normalized linewidth.

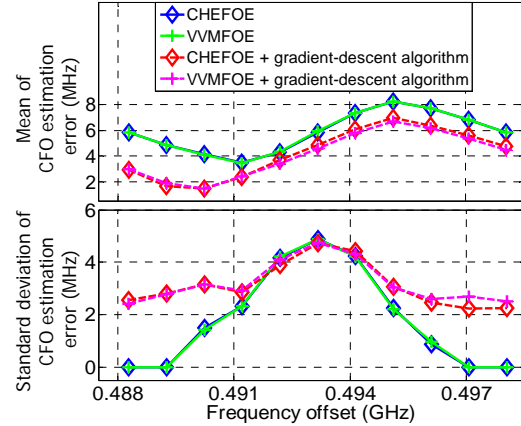


Fig. 5. Mean and STD of the estimation errors for 16-QAM in a FFT interval.

M -QAM communication systems. The proposed method outperforms the VVMFOE and 4th power methods in terms of number of required symbols and laser linewidth tolerance, especially for cross M -QAM signals.

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