Introduction to the papers of TWG14: University mathematics education

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Research on university level mathematics education is a fast developing field as evident in the growth of the CERME University Mathematics Education (hereafter UME) Thematic Working Group. TWG14 was launched in CERME7 (Nardi, González-Martín, Gueudet, Iannone & Winsløw, 2011). After CERME8 (Nardi, Biza, González-Martín, Gueudet, & Winsløw, 2013), its leader team – in collaboration with TWG14 participants and others – worked towards a Research in Mathematics Education Special Issue on Institutional, sociocultural and discursive approaches to research in university mathematics education (Nardi, Biza, González-Martín, Gueudet & Winsløw, 2014) which focused on research that is conducted in the spirit of the following theoretical frameworks: Anthropological Theory of the Didactic, Theory of Didactic Situations, Instrumental and Documentational Approaches, Communities of Practice and Inquiry and Theory of Commognition.

The work of the group at CERME9 cemented and furthered this work but welcomed contributions from across the board of research approaches: the teaching and learning of advanced topics; mathematical reasoning and proof; transition issues “at the entrance” to university mathematics, or beyond; challenges for, and novel approaches to, teaching (including the teaching of students in non-mathematics degrees); the role of ICT tools (e.g. CAS) and other resources (e.g. textbooks, books and other materials); assessment; the preparation and education of university mathematics teachers; collaborative research between university mathematics teachers and researchers in mathematics education; and, theoretical approaches to UME research.

The critical – and growing – mass and quality of the work presented at TWG14 has led to the launch of an ERME Topic Conference, INDRUM2016, a conference of the newly launched International Network for Didactic Research in University Mathematics (France, Montpellier; March 31 – April 2). Its two broad themes are teaching and learning of specific topics in university mathematics and teachers’ and students’ practices at university level. In anticipation of INDRUM2016, in this report, we outline briefly the main focal points of the 45 papers (31 long and 14 short contributions) that comprise the set of CERME9 TWG14 papers published in these proceedings in accordance with these two broad themes. We note that several papers fit both themes and that we have opted to classify the papers according to what we see as their main research focus and contribution.

TEACHING AND LEARNING OF SPECIFIC TOPICS IN UNIVERSITY MATHEMATICS

The 16 papers classified under this theme (8 long and 8 short papers) address a range of mathematical topics, elaborate discussions of mathematical reasoning, logic and proof and introduce research into the teaching of mathematics to students in other fields (here: engineering and economics).

With regard to mathematical topics, contributions regarded topics in calculus and Complex Analysis. Breen, Larson, O’Shea and Pettersson analyse student data from Ireland and Sweden to discuss concept images of inverse functions, particularly in relation to the predominance of the models of “swapping x and y”, reflection and reversal. Ghedamsi offers a Theory of
Didactic Situations (TDS)-based analysis of a teaching session on sequence convergence in order to examine the ways in which a university calculus teacher attends to students’ prior knowledge in calculus and facilitates the transition from school to university mathematics. Grønbæk and Winsløw deploy an Anthropological Theory of the Didactic (ATD) lens to discuss the teaching of complex numbers using Maple sheets and demonstrate the institutional constraints – Maple sheets cannot create an appropriate media/milieu dialectic – which lead to the development of disconnected practices. The short papers also covered a range of topic-specific research: the transition from informal to formal understanding of the concept of order in abstract mathematics (Akdemir, Narlı and Kaşıkçı); improper integrals (Cortés and Velasco); differential geometry (Dana-Picard and Zehavi); differential equations (Fardinpour); linear independence of functions (Wawro and Plaxco); and, abstract algebra (Mili and Ascah-Coallier).

With regard to mathematical reasoning, logic and proof, Hausberger introduces the innovation of the banquet, a pocket-size algebraic structure aimed at helping students reflect on mathematical structures and the axiomatic method. Bridoux and Durand-Guerrier, through an a-priori and a-posteriori analysis of two tasks in an exam paper taken by students of a Computing Sciences module that aimed at improving students’ proof production, find that the course did improve students’ proof fluency, although they also observe that many difficulties remain. In their short paper concerning students’ conceptions of logic, Kazima, Eneya and Sawerengera also highlight some of these difficulties, mainly focusing on issues of language.

With regard to research into the teaching of mathematics to students in other fields, a relatively novel strand, Biehler and Kortemeier analyse students’ work with a typical electrical engineering task in relation to an expert solution and conclude that it is counterproductive to try to separate the mathematical and “real world” (engineering) parts of the problem. Kürten and Greerfrath report aspects of a “bridging” course aiming to reduce engineering students’ difficulties with mobilizing school mathematical skills. Mkhatshwa and Doerr investigate economics students’ reasoning about marginal change (instantaneous rate of change) and in her short paper Selinski explores student noticing of exponential and power functions in university financial mathematics.

TEACHERS’ AND STUDENTS’ PRACTICES AT UNIVERSITY LEVEL

The 29 papers classified under this theme (23 long and 6 short papers) also address a range of teaching and learning issues: curriculum and assessment; innovative course design in UME; student approaches to study; relating research mathematicians’ practices to student practices; views and practices of mathematics lecturers; and, methodological and theoretical contributions to UME research.

In the cluster of papers on curriculum and assessment, González-Martín deploys a combination of theoretical frameworks (ATD and the documentational approach) to investigate the use of textbooks by pre-university teachers (particular focus: the topic concept of series of real numbers) and to observe that the textbook is a central tool for the teachers, who align with its presentation and organisation. Dibbs describes the outcomes of the use of formative assessment in a calculus class and concludes that regular participation in formative assessment is the best predictor of achievement. Raen compares the assessment of student competencies through closed book examination and talk aloud interviews. She concludes that different methods reveal different competencies and that therefore a mixture of assessment methods is desirable. Thoma and Iannone use two different frameworks, the MATH framework based on Bloom’s taxonomy, and a framework based on functional linguistics and Sfard’s commognitive approach, to analyse tasks from an examination in abstract algebra. They find both frameworks useful in highlighting different, and often complementary, aspects of the tasks. In their short paper Derouet, Henríquez, Menares and Panero also deploy a priori analyses of examination tasks in order to compare final secondary assessments in different countries.

With regard to innovative course design in UME, Biza and Vande Hey deploy the Communities of Practice approach to study the process of – and the pedagogical benefits deriving from – involvement of two undergraduate students in a project of resource development for statistics. Mesa and Cawley report the 3-year implementation of Inquiry-Based Learning (IBL) in a range of courses. Drawing on data from teacher logs and a Mathematical Knowledge for Teaching (MKT)
framework, they discuss challenges of the IBL approach. Nardi and Barton present a commognitive analysis of a “low lecture” episode (student-led inquiry oriented discussion on open-ended problems) to illustrate crucial steps of student enculturation into mathematical ways of acting and communicating, including a shift away from the lecturer’s ‘ultimate substantiator’ role. Rämö, Oinonen and Vikberg take a similar approach to report the shifting of an introductory course on linear algebra from a “lecture based” format to a new “extreme apprenticeship” format.

In the growing area of student approaches to study, Farah investigates the role of students’ personal work in mathematics and highlights the influence of institutional differences on student approach. Gómez-Chacón, Griese, Roesken-Winter and González-Guillén report similarities in the learning strategies employed across two cohorts of engineering students, in Spain and Germany. Liebendörfer and Hochmuth identify different factors which support or hinder the autonomy of first year students and observe that student teachers are not convinced about the need of university mathematics for teaching at school. Lehmann, Roesken-Winter and Schueler reveal that mathematical competencies and beliefs about physics are substantial for engineering students’ success in technical mechanics. In their short papers in this area, Griese, Lehmann and Roesken-Winter focus on what obstructs or facilitates examination success in first year engineering and Švecová, Kohanová and Drábeková explore issues concerning the mathematical literacy of first year students.

Three papers documented the interplay between research mathematicians’ pedagogical and mathematical practices and the influence of these on learner practices. Cooper proposes a commognitive configuration of MKT (MDT, Mathematical Discourse for Teaching) as a tool to identify – and make optimal pedagogical use of – differences in the student teachers’ and a mathematician’s discourses. Ouvrier-Buffet presents a model of how research mathematicians practise the construction of formal mathematical definitions and highlights the pedagogical potency of epistemological analyses of mathematicians’ practices. Kondratieva also favours epistemological analyses and discusses the pedagogical potential of exposing students to mathematical problems with different, more or less advanced, solutions to problems as opportunities for building mathematical connections.

In the populated area of studies on the views and practices of mathematics lecturers (6 long and 3 short papers), Bergsten and Jablonka investigate the views of mathematics lecturers on the transition problem for engineering students and observe that, despite the engineering context, lecturers see this transition as apprenticeship into becoming a mathematician, namely able to produce mathematics. Hernandes Gomes and González-Martín highlight differences in how teachers in engineering and in mathematics address rigor, approximation and modelling differently and how these views influence their teaching. Gueudet deploys the documentational approach to study teacher preparation and communication practices. She traces the interaction of teachers with resources in a goal-oriented activity that produces documentation systems (structured set of all the documents they develop) and identifies features of these systems. Mali studies how teachers with different disciplinary backgrounds use examples and representations in their teaching. Petropoulou, Jaworski, Potari and Zachariades deploy the Teaching Triad construct to investigate lecturer practices and rationales. They illustrate a case of a lecturer who shows sensitivity to students’ needs and draws students into mathematical culture through mathematical challenge. Viirman offers commognitive analyses of how lecturers’ epistemological and ontological positions on mathematics are articulated in their teaching discourse. The three short papers in this area touch on ways to enable student meaning making (Didis and Jaworski), UME conceptualisations of pedagogical content knowledge (Khakbaz) and tackling the difficulties of the transition from school to university mathematics (Kouvela, Biza and Zachariades).

Finally, Kaspersen, Pepin and Sikko propose a methodological advance in the study of the transition from higher education to the world of work through proposing an approach to purposeful sample selection for measuring student teachers’ beliefs and practices. An advance of a methodological as well as theoretical character is put forward by Tabach, Rasmussen, Hershkowitz and Dreyfus who use a transcript of an excerpt of four undergraduate students’ interaction while working on a specific initial value problem, to demonstrate a local integration of two theoretical and methodological perspectives on knowledge construction, namely Abstraction in Context (focusing on individuals) and Documenting Collective Activity.
IN CLOSING

While our presentation of CERME7 and CERME8 papers was in accordance with slightly different themes – for example in CERME8: transitions, affect, teacher practices and mathematical topics – some comparative observations across the three sets of papers are apt. As we noted in the Editorial of the RME Special Issue (Nardi et al., 2014), there is a clear surge of sociocultural and discursive approaches – and the number of papers using ATD and TDS is also remarkable. An emerging focus seems to be also on systematic investigations of innovative course design and implementation and there is certainly a rise in the number of studies that examine the teaching and learning of mathematics in the context of disciplines other than mathematics, such as engineering and economics. Furthermore, this time we welcomed more colleagues from outside Europe and also noted the rise in the number of papers on assessment and examination. We also observed the further strengthening, maturity and increasingly more robust theorizing of studies into teaching practices. Finally, we noticed in several papers the establishing of promising liaisons across different theoretical perspectives. We now look forward to cementing these developments further in future CERME conferences, in the rich presence of UME at the upcoming ICME13 and EMF2015 conferences – and of course INDRUM2016!

REFERENCES

