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Experimental and Computer Simulation Study of the Variation with Depth of the X-ray Section Topograph Images of a Dislocation*

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Abstract

A systematic study of the variations of the contrast of a dislocation in silicon on section topographs with the depth of the line was performed both experimentally and with computer simulations. Mo $K\alpha_1$ radiation and $33\bar{3}$ and $\bar{3}33$ symmetric reflections were used. The crystal thickness was 440 μm so that the value of μt was 0.64. The influence of the orientation of the dislocation was studied for values of the angle between the line and its Burgers vector ranging between 60 and 90° in the glide plane. It was observed that when the dislocation lies close to the entrance surface, whatever its orientation, its image is centred around the trace of the plane of incidence passing through the intersection of the dislocation with the direct beam while when the dislocation lies close to the exit surface its image is centred around the projection of the dislocation on the section pattern. The variation of the orientation of the image for intermediate depths of the dislocation is interpreted by means of the geometrical construction of the dynamical image. The values of the orientation of the image calculated according to this simple model are in good agreement with those measured on both experimental and simulated topographs. The same geometrical model enables the difference in the relative positions of the direct and dynamic images of stereo pairs to be explained. A new feature was observed in the simulated images and several of the experimental ones, namely a concentration of intensity along the projection of the dislocation in the reflected direction. Slit width was taken into account in the simulations for a better fit with experimental topographs but not polarization, which was taken to be normal to the plane of incidence. Because of the small value of the crystal

thickness and of μt , the variation of the contrast with the Burgers vector is very small, making its determination very difficult.

1. Introduction

Many papers have been devoted to the study of the main features of dislocation images on X-ray section topographs and to their computer simulations (Authier, 1961, 1967, 1977; Balibar & Authier, 1967; Authier, Balibar & Epelboin, 1970; Epelboin, 1974, 1975, 1979; Suvorov, Polovinkina, Nikitenko & Indenbom, 1974; Suvorov, Gorelik & Ponomareva, 1976; Lefeld-Sosnowska, 1978; Lefeld-Sosnowska & Zawadzka, 1978; Kowalski & Gronkowski, 1982; Epelboin & Patel, 1982; Kowalski, 1984) and the good agreement between experimental and simulated topographs has been established satisfactorily. The influence of the Burgers vectors in certain cases (Epelboin, 1974, 1979; Epelboin & Patel, 1982) and the influence of the position of the dislocation line with respect to the Borrmann fan has been shown (Authier, 1967, 1977; Epelboin, 1975; Lefeld-Sosnowska, 1978; Kowalski & Gronkowski, 1982) but no systematic study has been undertaken as yet of the variations of the contrast and of their physical interpretation in terms of the many parameters on which it depends, namely respective orientations of the crystal surface, diffraction vector, dislocation line and Burgers vector, depth of the dislocation, crystal thickness, absorption coefficient, order of the reflection, structure factor *etc.*

For the experimenter what is important is to be able to derive the properties of a dislocation from the interpretation of the various features of its image. This requires an understanding of the behaviour of wavefields propagating in a deformed region in terms of the distribution of strains and of their gradient and the possibility of predicting how the contrast of the image is modified when the geometrical and diffraction parameters are varied. The latter is obviously a consequence of the former; however it is extremely

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complicated to unravel the intricate mechanisms of dislocation-image formation in section patterns, that is for an incident distribution of spherical waves, and it has actually never been done satisfactorily. It is therefore worth while to pursue concurrent approaches simultaneously, namely studies of wavefield propagation and generation (interbranch scattering) from diffraction theory on one hand and from an analysis of the variations of the contrast with the various parameters on experimental and simulated topographs on the other.

The present paper is the first of a series that will endeavour to show the influence of the geometrical parameters. It is concerned with the variations of the contrast of a series of dislocations with their depth within the crystal for values of their orientations with their common Burgers vector ranging from 60 to more than 90°. The study was performed both experimentally (Lefeld-Sosnowska & Zawadzka, 1978) and with computer simulations performed using the varying-step algorithm (Epelboin, 1983).

2. Experimental conditions

The dislocations studied in the present paper were contained in a 440 μm thick slab cut perpendicular to the $[112]$ direction and parallel to the $[11\bar{1}]$ pulling axis of an as-grown Cz silicon crystal. Fig. 1 shows a selected area from a $\bar{3}\bar{3}3$ traverse topograph of this

Fig. 1. (a) X-ray traverse topograph of a (112) silicon crystal, $\bar{3}\bar{3}3$ reflection, $\text{Mo } K\alpha_1$. (b) Schematic diagram showing the dislocations, labelled 1 to 6, studied in this paper, and the crystallographic orientations on the crystal surface. The dislocations lie in a (111) glide plane, which intersects the crystal surface along $[110]$.

slab. The dislocations observed in Fig. 1 and labelled 1 to 6 were shown in a previous study (Lefeld-Sosnowska & Zawadzka, 1978) to lie in a (111) slip plane and to have $\frac{1}{2}[01\bar{1}]$ as Burgers vector. Presumably they were generated by a source that was activated by stresses present during the cooling of the crystal but this point is not really relevant for the present study. Fig. 2 is a diagram showing the position of the two extreme dislocations, 1 and 6, within the crystal and the orientation of the Borrmann prism. Close to their outcrop at the entrance surface the dislocations are parallel to $[10\bar{1}]$ and are of 60° type. Their orientation changes progressively as they get deeper inside the crystal, more rapidly so from dislocation 1 to dislocation 6 so that the orientation of dislocation 6 close to the exit surface is approximately $[2\bar{1}\bar{1}]$ and it is of edge type.

Fig. 3 shows the intersection of one of these dislocation lines with the Borrmann prism for a given position of the entrance slit. The orientations of the axes that have been used for the calculations are indicated. Let D_1 be the intersection of the dislocation with the direct beam. For a straight dislocation the depth z_1 of D_1 below the surface is related to the distance $O'A'$ of the edge of the Borrmann prism from

Fig. 2. Diagram showing the position of the dislocations in the crystal with respect to that of the Borrmann prism.

Fig. 3. Intersection D_1D_2 of a dislocation with the Borrmann prism.

the outcrop O' of the dislocation at the entrance surface by the relation

$$\overline{O'A'} = z_1 (\tan \alpha - \tan \theta), \quad (2.1)$$

where θ is the Bragg angle and α is the angle between the normal to the crystal surface and the projection of the dislocation line on the plane of incidence. The latter angle is related to the direction cosines of the dislocation line u, v, w by

$$\tan \alpha = u/w. \quad (2.2)$$

The value of $|\alpha|$ is equal to 70.5° for all the orientations of the dislocations studied in this paper since they lie in a (111) plane, the intersection of which with the plane of incidence is $[11\bar{2}]$.

The whole present study was performed using $\text{Mo } K\alpha_1$ radiation and the $\bar{3}33$ and $33\bar{3}$ reflections, which are here symmetric. The values of the main diffraction parameters are the following:

Bragg angle	$\theta = 10.83^\circ$
Fourier coefficient of the real part of susceptibility (after Aldred & Hart, 1973)	$\chi_{rh} = -0.947 \times 10^{-6}$
Fourier coefficient of the imaginary part of susceptibility (after Aldred & Hart, 1973)	$\chi_{ih} = -0.95 \times 10^{-8}$
<i>Pendellösung</i> distance	$A = 70.4 \mu\text{m}$
Width of the rocking curve	$\delta = 0.297 \times 10^{-5} \text{ rad}$
Product of absorption coefficient and crystal thickness	$\mu t = 0.64$

3. Computer simulations

The simulations were performed by solving the Takagi-Taupin equations by means of the half-step derivative method used by Authier, Malgrange & Tournarie (1968) and the variable-step algorithm introduced by Epelboin (1983). Petrashen (1976) suggested decreasing the steps of integration near the edges of the Borrmann fan and Epelboin (1981, 1983) wrote an algorithm where the steps are automatically adjusted to the local oscillation of the wavefields. They are small near the edges and become large in the middle of the Borrmann fan where the amplitudes vary slowly. This ensures both a much higher accuracy and a smaller computing time than with a constant-step algorithm.

The simulated image is photographed from a Numelec-Pericolor 2000 raster picture system. With a minicomputer Mini 6/53 CII-HB linked to an FPS 100 array processor, the total computing time including input and output of the data is of the order of a few

minutes only for a section topograph calculated for a single point source. It is therefore easy to perform many simulations and to study by means of computer experiments how the contrast is modified when the geometrical and diffraction parameters are varied.

Simulations are calculated, using as an incident wave a spherical wave emitted by a single point source on the crystal surface. This is a very different situation from the experimental one where the incident beam is a superposition of spherical waves emitted by the anode of the X-ray tube. Each wave is limited by the angular admittance of the crystal, that is the width of the rocking curve and the beam is limited by an entrance slit. The best way to simulate this situation is to superpose a series of simulations performed for a series of point sources distributed over the width of the slit (Aristov, Kohn, Polovinkina & Snigirev, 1982; Epelboin & Authier, 1983). The results show a slight blurring of the spherical-wave Kato *Pendellösung* fringes and a much better overall agreement between experimental and simulated topographs (Epelboin & Authier, 1983) to the point that the width of the slit can be fitted for best agreement. The simulated topographs of Figs. 4 and 15 of the present paper were calculated using a $12 \mu\text{m}$ wide entrance slit corresponding to the superposition of five topographs calculated with an incident point source, at $2.4 \mu\text{m}$ intervals. The other simulations were calculated for an incident point source. They show details of the image that cannot be expected to be resolved on an experimental topograph.

Polarization has been assumed to be normal to the plane of incidence. For best correspondence with experiment, the average between the images calculated for polarization normal and parallel to the plane of incidence should be taken. This has not been done here because this would have implied computing twice the number of images simulated. The numerical precision of the varying-step algorithm is sufficient for polarization to be taken into account and this will be discussed in a separate paper.

4. Comparison of experimental and simulated section topographs

A series of more than ten section topographs of the silicon slab was taken for successive positions of the crystal with respect to the slit for both $\bar{3}33$ and $33\bar{3}$ reflections. For this purpose, the crystal was translated by steps of about $50 \mu\text{m}$ in front of a 10 to $15 \mu\text{m}$ wide slit. Figs. 4(a) and (c) show examples of the section topographs thus obtained, which are most characteristic of the observed variations of the contrast as the dislocation dips into the crystal. Images of dislocation 1 only are represented here. The estimated depths at which the dislocation line cuts the direct beam for each position of the crystal are given in Table 1 as well

Table 1. *Depths and orientations of dislocation 1 corresponding to the experimental topographs of Fig. 4*

z_1 : depth of the intersection of the dislocation with the direct beam.
 φ : angle between the dislocation and its Burgers vector.

 $\bar{3}\bar{3}\bar{3}$ (Fig. 4a)

No. of section		1	2	3	4	5
Experimental	z_1 (μm)	44 (7)	108 (7)	223 (7)	299 (7)	352 (7)
	φ ($^\circ$)	60	60	60	71 (2)	83 (2)

 $\bar{3}\bar{3}\bar{3}$ (Fig. 4c)

No. of section		1	2	3	4	5
Experimental	z_1 (μm)	82 (7)	127 (7)	196 (7)	370 (7)	440
	φ ($^\circ$)	60	60	60	77 (2)	80 (2)

Fig. 4. Experimental (a and c) and simulated (b and d) section topographs for the $\bar{3}\bar{3}\bar{3}$ (a and b) and $\bar{3}\bar{3}\bar{3}$ (c and d) reflections of dislocation 1. The experimental topographs were taken for successive positions of the crystal. The corresponding depths and orientations of the dislocation are given in Table 1. The simulated topographs were calculated for the same values of the depth and the orientation of the dislocation, Burgers vector $\mathbf{b} = \frac{1}{2}[01\bar{1}]$ and an entrance-slit width of 12 μm . The topographs are viewed looking towards the X-ray source.

as the estimated orientation of the line at that point. These values are necessarily approximate, not only because of the width of the entrance slit but also because of the manner by which they are estimated. This can be done in four different ways. First of all they can be deduced by means of (2.1) from the positions of the crystal read on the driving screw; however only relative translations of the crystal can be measured and absolute values are not known; furthermore, the movement of the screw is not perfectly accurate. The depth of the dislocation can also be deduced from the position of its direct image in the section topograph but this image is very large and it is therefore difficult to find where the centre of the strain field exactly lies, all the more so since an accurate model of the formation of the image is lacking.

The depth of the dislocation can also be confirmed independently by two indirect ways. One is to find among the simulations that have been performed for various depths the one that fits best with experiment. The other one is to measure the angle of the dynamical image with the axis of the section pattern, which is directly related to the depth and orientation of the dislocation through (6.3). The orientation of the dislocation can be deduced from a traverse topograph. The values of depth and orientation given in Table 1 are the result of the best fitting of all the available data.

Dislocation 1 remains parallel to $[10\bar{1}]$ down to about three quarters of the crystal thickness and then begins to rotate slightly towards the $[2\bar{1}\bar{1}]$ direction.

About 150 simulations have been calculated for various depths and orientations of the dislocation line, for the two possible orientations of the Burgers vector, $\frac{1}{2}[01\bar{1}]$ and $\frac{1}{2}[0\bar{1}1]$, and for the two reflections, $\bar{3}3\bar{3}$ and $33\bar{3}$. Figs. 4(b) and (d) present the simulations for which depth and orientation of the dislocation have been fitted for best agreement of the images with the experimental ones. They have been calculated for an entrance slit width of $12\text{ }\mu\text{m}$.

The agreement of experimental and simulated topographs is seen to be quite good. The contrast is different for $\bar{3}3\bar{3}$ and $33\bar{3}$, the more so as the dislocation lies deeper inside the crystal. It changes drastically with the depth of the dislocation. This very important point will be discussed after the principles of image formation have been recalled.

5. Image formation in section topographs

Section topographs were the first type of topographs by means of which single dislocations were observed (Lang, 1957). They have the big advantage of containing a lot of information about the strain field inside the crystal but are more complicated to interpret than plane-wave topographs because of the spherical-wave nature of the incident beam and the influence of the slit width.

The main features in a dislocation image, namely the direct image, the dynamic image and the intermediary image have been described by Authier (1967) and have been observed by many authors. They are schematically represented in Fig. 5 as an example.

The relative position and importance of these features depend strongly on the various geometrical and diffraction parameters and the exact mechanism of their origin is not yet really known. Simulations are a good way to progress in their understanding with respect to the time they were first described.

Apart from these features, there are other aspects in many dislocation images on section topographs. One is the deformation of the normal spherical-wave Kato *Pendellösung* fringes. This effect is due to a decrease of the *Pendellösung* distance, itself a consequence of the bending of wave fields in slightly deformed areas far from the dislocation core. It was first observed and explained by Kato (1963) and was further discussed by Suvorov *et al.* (1974) in terms of the phase shift to be associated with the relative translation of lattice planes above and below a dislocation. It is sketched in Fig. 5(a) and is clearly visible on most of the topographs of Fig. 4. This effect can obviously only be seen for values of μt for which *Pendellösung* fringes are visible.

Another very interesting feature that can be observed in some cases is a line of high intensity along the projection of the dislocation line on the photographic plate, that is along what would be the direct image on a traverse pattern. Such an accumulation of

Fig. 5. (a) Schematic diagram showing the various features of the dislocation image according to the simulation of: two black lobes, i_1 : direct image; shaded area: intermediary image; area limited by broken lines: dynamic image; straight black line between i_1 and the left-hand extremity of the section pattern: last fringe of the intermediary image. It lies along the projection of the dislocation on the topograph; thin vertical black lines: Kato fringes deformed around the dislocation image. (b) Simulated topograph, $\bar{3}3\bar{3}$ reflection, Burgers vector $\frac{1}{2}[01\bar{1}]$, depth of the dislocation: $240\text{ }\mu\text{m}$. The contour drawn by the computer surrounds the region corresponding to an intensity higher than a certain arbitrary value. It corresponds roughly to the direct image.

intensity along the reflected direction from the dislocation was first observed on simulations of energy propagation in the plane of incidence (Epelboin, 1975) and it was mentioned in a comparison of simulated and experimental topographs (Gronowski & Kowalski, 1981). It is very clearly seen on practically all simulated topographs of Fig. 4 and quite well on many of the experimental ones. It is represented as a straight line on the diagram of Fig. 5. Its contrast is the strongest when the dislocation lies closest to the direct-beam side of the Borrmann prism. This is confirmed by simulations; if the dislocation lies in the incident beam, the contrast of this image is maximum while it is not to be seen if the dislocation lies in the reflected-direction side of the Borrmann prism (Authier, 1985). The length of the image is proportional to the depth of the dislocation inside the crystal as will be clear from its geometrical construction, which will be described in § 6 in connection with the formation of the dynamical image (Figs. 7 and 9). This is why it is most visible on experimental topographs when the dislocation lies deepest in the crystal (see also Fig. 11).

One of us (Authier, 1985) performed simulations for the same crystal and dislocation geometry but a larger crystal thickness. The intermediary image is then very clearly visible because it contains more fringes and it can be seen that the new image is actually part of the intermediary image. This is confirmed by simulations made with a large value of μt for which the intermediary image has a strong contrast while the direct image is almost absorbed out.

6. Geometrical shape of the dynamical image

Figs. 6 and 7 illustrate the formation of the dynamical image from a geometrical point of view. Fig. 6(a) shows the paths of the wavefields propagating from the apex of the Borrmann triangle to the dislocation for several planes of incidence. Let $A_1B_1C_1$ and $A_2B_2C_2$ be those which pass through the intersections D_1 and D_2 of the dislocation with the direct and reflected beams, respectively, and ABC a particular plane of incidence. Further, let D be the intersection of the dislocation with that plane, P the intersection of the wavefield propagating along AD with the base BC of the Borrmann triangle, I and I_1 , the projections of D and D_1 on BC and on B_1C_1 , the reflected direction, respectively.

The top part of Fig. 7(a) shows the frontal projection of all the planes of incidence and the dislocation on the particular one, ABC , and the bottom part a projection on the photographic plate in the reflected direction. The section topograph is limited by the projection $b_1b_2c_1c_2$ of the base of the Borrmann prism and the dynamical image lies along the projection c_1pb_2 of the curve C_1PB_2 . The line b_2ii_1 is the

projection of the dislocation and is part of the direct image on a *traverse* or *projection* topograph (Lang, 1958). On the *section* topograph, the direct image is a spot centred around the projection i_1 of D_1 , and along b_2ii_1 can be seen this concentration of intensity, which was described at the end of § 5 and looks like the extremity of the intermediary image.

Figs. 6(b) and 8 illustrate situations where the outcrop of the dislocation at the exit surface of the crystal lies within the Borrmann prism. Figs. 6(b) and 8(a) correspond to the case where the dislocation intersects the direct beam. The dynamical image is along opc_1 and the reflected direction along oi_1 (Fig. 8a). This situation is that of the experimental and simulated topographs of Figs. 4(a)5 and 4(b)5. Fig. 8(b) describes a situation where the dislocation does not intersect the direct beam. There is no direct image and the dynamical image b_2po lies very close to the projection of the dislocation line on the section topograph. This situation is that of the experimental and simulated topographs of Figs. 4(c)5 and 4(d)5.

Let us now consider a set of coordinate axes b_2X ,

Fig. 6. Projection of the dislocation on the exit surface of the crystal: (a) The dislocation intersects both sides of the Borrmann prism at D_1 and D_2 . C_1B_2 : shadow of the dislocation cast along the direction of propagation of the wavefields; it corresponds to the dynamic image. I_1B_2 : projection of the dislocation along the reflected direction; I_1 corresponds to the direct image. (b) The dislocation intersects only the direct-beam side of the Borrmann prism. OD_1 is the dislocation, OC_1 its shadow, OI_1 its projection in the reflected direction.

(a)

(b)

Fig. 7. Construction of the direct and dynamical images (a) $\bar{3}33$ reflection; (b) $33\bar{3}$ reflection. The top part of each figure is a projection of the crystal on a particular plane of incidence, ABC . D_1D_2 is the projection of the dislocation on that plane, D its intersection with it. The bottom part is a projection on the photographic plate; bc is the trace of the plane of incidence ABC , b_2i_2 is the projection of the dislocation and i_2 the direct image; b_2c_1 is the projection of the shadow cast on the exit surface by the dislocation, it is its dynamical image.

(a)

(b)

Fig. 8. Same construction as for Fig. 7 but for a situation where the dislocation intersects one side only of the Borrmann prism. (a) $\bar{3}33$. The dislocation intersects the direct beam side of the Borrmann prism. There is a direct image i_1 and a dynamical image oc_1 . (b) $33\bar{3}$. The dislocation intersects the reflected beam side of the Borrmann prism. There is no direct image and only the dynamical image ob_2 .

b_2Y in the plane of the section topograph (Fig. 7a). It can be shown that the equation of the dynamical image b_2pc_1 is given by

$$y = \frac{Z \tan^{-1} \delta (\tan \alpha - \tan \theta) x}{\tan \alpha + \tan \theta - 2x \tan \theta}, \quad (6.1)$$

where x , y and Z are reduced coordinates:

$$x = X/\overline{b_2c_2}; \quad y = Y/\overline{b_2c_2}; \quad Z = z_1/t$$

$$(\overline{b_2c_2} = 2t \sin \theta).$$

X and Y are the coordinates of point p of the dynamical image, $\overline{b_2c_2}$ is the width of the section pattern, z_1 the depth of D_1 , t the crystal thickness; $\tan \alpha$ is given by (2.2).

Equation (6.1) shows that the shape of the dynamical image is a hyperbola. The angle α between the projection of the dislocation on the section topograph and the axis of that section are given in terms of the direction cosines of the dislocation by

$$\tan \delta = (u \cos \theta + w \sin \theta)/v. \quad (6.2)$$

The slope of the line $\overline{b_2c_1}$ (Fig. 7a) that connects the two ends of the dynamical image is given by:

$$\tan \delta' = \tan \delta / Z \quad (6.3)$$

when the dislocation line intersects both sides of the Borrmann triangle;

$$\tan \delta' = (u \cos \theta - w \sin \theta)/v \quad (6.4)$$

when the dislocation intersects the direct beam side only (Fig. 8a);

$$\delta' = \delta \quad (6.5)$$

when the dislocation intersects the reflected-beam side only (Fig. 8b).

It can be noticed on the topographs of Fig. 4 that the dynamical image lies below the direct image for the $3\bar{3}3$ reflection and above it for $33\bar{3}$. This can be readily understood from a comparison of Figs. 7(a)

and 8(a) on one hand and Fig. 7(b) and 8(b) on the other, which illustrate the construction of the dynamical image for the two situations, respectively. It can further be noticed in these figures that for $3\bar{3}3$ the dynamical image lies between the projection b_2i_1 of the dislocation and b_2c_1 and outside the angle formed by these two lines for $33\bar{3}$. These remarks would be reversed if the slope of the projection of the dislocation on the plane of incidence had the opposite sign. Coupled with (6.3) to (6.5) they confirm that the orientation of the dislocation can be deduced from these if its direct and dynamical images on a traverse and a section topograph, respectively, are taken with a single reflection only (Authier, 1961).

As an illustration of the agreement between the observed and calculated shape of the dynamical image, Figs. 9(a) and (b) represent the calculated shape of the dynamical image and the predicted line of concentrated intensity for each of the section topographs of Figs. 4(a) and (b) and 4(c) and (d), respectively.

7. Variation of the contrast with depth of the dislocation for several orientations

7.1. Observations

Fig. 10 compares computer simulations of the image of the dislocation for the $3\bar{3}3$ reflection and a depth of 20 μm and two orientations of the dislocation line with respect to their Burgers vector $\frac{1}{2}[01\bar{1}]$ in the slip plane, 60 and 98°. It can be observed that the dynamical image is in both cases practically normal to the axis of the section but that the perturbation of the Kato *Pendellösung* fringes extend over a much greater distance for the dislocation which is practically along the edge than for the 60° one.

Figs. 11(a) and (b) compare simulated and experimental images for similar conditions as before but for depths of 240 and 350 μm respectively and for four orientations of the dislocation with respect to its Burgers vector in the slip plane: 60, 72, 90 and 98°.

Fig. 9. Calculated dynamical images for the topographs of Fig. 4. The black dot represents the direct image and the dashed line the projection of the dislocation line.

Fig. 10. Variation of the contrast with orientation for a given depth of the dislocation. Simulated topographs, $3\bar{3}3$ reflection, depth 20 μm . Burgers vector $\frac{1}{2}[01\bar{1}]$. (a) Angle φ of the dislocation to its Burgers vector: 60°, angle δ of the projection of the dislocation on the section topograph to the trace of the beam (see Fig. 7): 120°. (b) $\varphi = 98^\circ$, $\delta = 158^\circ$.

Fig. 11. Variation of the contrast of the dislocation with orientation for two values of the depth. Comparison between simulations (*a* and *c*) and experimental topographs (*b* and *d*). 333 reflection, Burgers vector $\frac{1}{2}[01\bar{1}]$. (*a*) and (*b*) depth: 240 μm. Orientations (from left to right): $\alpha = 60, 72, 90, 98^\circ$; $\delta = 120, 132, 150, 158^\circ$.

Here it can be observed that for a given depth of dislocation the main features of the dislocation remain unchanged except for a rotation. It can therefore be concluded that when the dislocation lies deeply inside the crystal the orientation of the image depends very strongly on the orientation of the line while this is not the case when the dislocation lies close to the entrance surface.

7.2. Discussion

The variation of the orientation dependence of the image with the depth of the dislocation can be understood by reference to the variations with depth of the dynamical image. Fig. 12 compares the dynamical images of the dislocation for two orientations of its projection on the photographic plate and two positions of the Borrmann triangle, one for which the dislocation lies very close to the entrance surface and the other for which the dislocation lies close to the exit surface. In the former case the orientation of the dynamical image is seen to be practically normal to the section pattern, whatever the orientation of the dislocation. This is because when Z tends towards 0 in

Fig. 12. Variation of the dynamical image with depth and orientation of the dislocation in its slip plane. $D_1D_2D_3D_4$ projection of the dislocation on the plane of incidence $i_1b_2i_3b_4$. $i_1''b_2''i_3''b_4''$ projections of the dislocation on the photographic plate for two orientations of the dislocation in the slip plane. Note that the dynamical images (dashed lines) are close to the projection of the dislocation when it lies close to the exit surface and close to the trace of the plane of incidence when the dislocation is near the entrance surface.

(6.3), δ' tends towards 90° whatever the value of δ . On the contrary, when the dislocation lies close to the exit surface, Z tends towards 1 and δ' is practically equal to δ .

7.3. Application

It so happens that with the geometry of the dislocations studied here the dislocation image does not differ very much from a straight line (see Fig. 7). This is because the angle α of the projection of the dislocation on the plane of incidence with the normal to the crystal surface is close to 90° . It is therefore possible to measure the orientation δ' of the dynamical image either on an experimental or on a simulated topograph and to compare it with the value calculated from (6.3), (6.4) or (6.5) according to the geometrical situation. This is done in Figs. 13(a) to 13(d).

The values calculated for five different orientations φ of the dislocations are plotted in terms of the depth of their intersection with the direct beam in Figs. 13(a) and (b) for $\bar{3}\bar{3}\bar{3}$ reflection and in Figs. 13(c) and (d) for $3\bar{3}\bar{3}$. The values measured on the simulations performed for the same orientations and various depths of the dislocation are represented in Figs. 13(a) and (c). The agreement is seen to be very good with the calculated curves. Figs. 13(b) and (d) represent the values measured on experimental topographs taken at successive positions of the entrance slit for the two dislocations labelled 1 and 6 in Fig. 1. It can be seen that close to the entrance surface the dislocations are of 60° type and that close to the exit surface dislocation 1 makes an angle of about 80° with the Burgers vector and dislocation 6 an angle of about 98° , in agreement with the observations made on traverse topographs. It can also be observed that the depth at which the dislocations start rotating away from the 60° orientation seems to be different depending on whether it is measured on the $\bar{3}\bar{3}\bar{3}$ or on the $3\bar{3}\bar{3}$ reflection. This is easily understood from Figs. 7(a) and (b): for the same depth z_1 of the intersection of the dislocation with the direct beam, the part of the dislocation that lies within the Borrmann triangle is situated below this depth in the former case and above it in the latter. It is a different part of the dislocation, with a different orientation, that is therefore giving rise to the dynamical image in each case, which explains the observed result.

8. Variation of the contrast with the sign of the Burgers vector

In order to try to determine the sign of the Burgers vector whose direction was shown to be $\frac{1}{2}[01\bar{1}]$ by usual topographic techniques (Lefeld-Sosnowska & Zawadzka, 1978), computer simulations were made for both $\frac{1}{2}[01\bar{1}]$ and $\frac{1}{2}[0\bar{1}1]$ Burgers vectors, for many values of the depth of the dislocation and for both $\bar{3}\bar{3}\bar{3}$ and $3\bar{3}\bar{3}$ reflections. An example is given in Fig. 14 for

Fig. 13. Variations of the angle δ' between the dynamical image and the trace of the beam on the section pattern with the depth of the dislocation for several orientations ϕ of the dislocation in the slip plane (ϕ is the angle with the Burgers vector). (a) $\bar{3}\bar{3}\bar{3}$ reflection. The curves represent the values calculated according to (6.3) and the error bars to the values measured on the simulations. When the dislocation is so deep that it intersects the direct beam only, the orientation of the dynamical image becomes constant (6.4). The limiting value for the depth is here equal to 341 μm . (b) $\bar{3}\bar{3}\bar{3}$. The curves are the calculated ones according to (6.3) and (6.4) and the rectangles represent the values measured on the experimental topographs for two different dislocations, labelled 1 and 6 in Fig. 1. The sizes of the rectangles give the error bars. (c) and (d) Same thing for the $\bar{3}\bar{3}\bar{3}$ reflection.

a dislocation depth of 330 μm . It can be seen that no difference in contrast can be detected between the two orientations of the Burgers vector, although on a false color display which enhances small contrast differences a small difference in intensity of the Kato fringes can be observed between the top and the bottom parts of the image. This difference reverses when changing the sign of either the Burgers vector $\mathbf{b}$ or the diffraction vector $\mathbf{h}$ and remains constant when $\mathbf{h}\cdot\mathbf{b}$ is also constant. When the depth of the dislocation is smaller the differences are slightly more visible, even on black and white displays. For instance, Fig. 15 shows a $\bar{3}\bar{3}\bar{3}$ simulation for a dislocation depth of 44 μm and a $\frac{1}{2}[0\bar{1}1]$ Burgers vector. This simulation, calculated with an entrance slit of 12 μm , is to be compared with the first topograph of Fig. 4(b) calculated for the same reflection and the same dislocation depth but a $\frac{1}{2}[01\bar{1}]$ Burgers vector and with the first topograph of Fig. 4(a), which is an experimental one. It can be seen that it is very difficult to determine which is the correct Burgers vector even if a careful examination of the original seems to indicate that $\frac{1}{2}[01\bar{1}]$ is slightly more likely.

This situation is very different from that studied by Epelboin (1974) with a dislocation having a different geometry and a thicker crystal where the intermediary image is very important. A marked difference was then observed in the contrast when changing the sign of the Burgers vector. That the dislocation images studied in the present paper are not very sensitive to the sign of the Burgers vector seems to be because for such a small crystal thickness the intermediary image has very few fringes. Indeed, on simulations performed

Fig. 14. Variation of the contrast with the sign of the Burgers vector. Simulated topographs. Depth: 330 μm . (a) $\bar{3}\bar{3}\bar{3}$, $\mathbf{b} = \frac{1}{2}[01\bar{1}]$; (b) $\bar{3}\bar{3}\bar{3}$, $\mathbf{b} = \frac{1}{2}[0\bar{1}1]$; (c) $\bar{3}\bar{3}\bar{3}$, $\mathbf{b} = \frac{1}{2}[01\bar{1}]$; (d) $\bar{3}\bar{3}\bar{3}$, $\mathbf{b} = \frac{1}{2}[0\bar{1}1]$.

Fig. 15. Simulated topograph. Depth: 44 μm , $\bar{3}\bar{3}\bar{3}$, Burgers vector $\frac{1}{2}[01\bar{1}]$, opposite to that of the simulated image of Fig. 4(a). Width of the entrance slit: 12 μm .

with the same geometry of dislocation but a thicker crystal, the intermediary image is very visible and changes markedly when changing the sign of the Burgers vector.

9. Sensitivity of the Kato fringes to small variations of the depth of the dislocation

Fig. 16 compares the five topographs calculated for an incident point source that have been used to simulate the first topograph of Fig. 4(b), which corresponds to a slit width of 12 μm . They have been calculated for lateral translations of the crystal with respect to the entrance slit of 2.4 μm each time. Since the dislocation is inclined with respect to the crystal surfaces, the depth of its intersection with the direct beam changes for each position of the slit and takes the successive values of 30.7, 37.4, 44, 50.7 and 57.3 μm . It can be seen that as the depth of the dislocation changes the shape of the Kato fringes is modified, as is to be expected, and is very sensitive even to small changes.

10. Conclusion

This study, as several others before, has confirmed that dislocation images on section topographs can be simulated with very good agreement, which is highly improved when the width of the entrance slit is taken into account and that computer experiments are a very fruitful tool for the investigation of the mechanism of image formation.

The drastic variation of the contrast of the image with its depth inside the crystal has been shown by systematic studies both experimentally and with simulations and has been explained by simple geometrical considerations. When the dislocation lies close to the entrance surface the orientation of its image is normal to the axis of the section pattern and practically does not depend on the orientation of the dislocation but the distance over which *Pendellösung* fringes are deformed does depend strongly on this orientation. On the contrary, for the part of the dislocation that is close to the exit surface, its orientation depends primarily on that of the dislocation since it lies very close to the projection of the dislocation on the photographic plate.

A new feature in the dislocation image has been analysed. It is a concentration of intensity along the

projection of the dislocation on the photographic plate and is due to the propagation of energy along the reflected direction from points of the dislocation that are situated *inside* the Borrmann prism. It merges into the direct image for points of the dislocation that are very close to the direct beam, and seems to be the limit of the intermediary image.

An attempt has been made to determine the sign of the Burgers vector from comparison between experimental topographs and simulations made for the two opposite signs of the Burgers vector, the magnitude and direction of which were already known by usual topographic techniques. However, very small differences only have been observed and this is probably because the crystal is rather thin and the fringes of the intermediary image are not well separated. From the scant evidence, the Burgers vector has been assumed to be $\frac{1}{2}[01\bar{1}]$.

The further developments of this work will consist on one hand in a systematic study of the influence of orientation on all the features of the dislocation image in relation to the relative variations of equal strain and equal strain gradient surfaces and on the other in a study of the influence of absorption in order to analyse the various components of the image that are known to have very different absorption dependence.

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Fig. 16. Topographs simulated with a point source corresponding to successive positions of the crystal translated by 2.4 μm intervals parallel to its entrance surface. The corresponding depths of the dislocation are equal to 30.7, 37.4, 44, 50.7, 57.3 μm from left to right, respectively. These topographs were added to calculate the simulation of Fig. 4(a)1 with an entrance slit of 12 μm .

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