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Characterization of time-varying regimes in remote sensing time series: application to the forecasting of satellite-derived suspended matter concentrations

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Abstract

Satellite data, with their spatial and temporal coverage, are particularly well suited for the analysis and characterization of space-time-varying relationships between geophysical processes. In this study, we investigate the forecasting of a geophysical variable using both satellite observations and model outputs. The studied latent-regime models aim here at identifying time-varying regime

21 shifts within a dataset which is a key of interest for geophysical processes driven by the seasonal
22 variability. As a specific example, we study the daily concentration from 2007 to 2009 of mineral
23 suspended particulate matters estimated from the satellite-derived MODIS, MERIS and SeaWiFS
24 dataset, in coastal waters adjacent to the Gironde River mouth (South West of France). We clearly
25 show that the forecast of the high resolution suspended particulate matter dataset using
26 environmental data (wave height, wind strength and direction, tides and river outflow) and a multi-
27 regime model is significantly improved compared with a classical multi-regression and a Support
28 Vector Regression model. Each regime is here characterized by a regression function and a
29 covariance structure.

30 From an analytical point of view, we compare the results obtained with four models:
31 homogeneous and non-homogeneous Markov-switching models, with and without an
32 autoregressive term, i.e. the suspended matter concentration observed the day before. Inclusion of
33 an autoregressive term is motivated by the strong natural autocorrelation level depicted by
34 geophysical time series, but, one may avoid this term if, for example, the observations are no more
35 available during specific conditions or periods. With the evaluated models, best results are obtained
36 with a mixture of 3 regimes for both autoregressive and non-autoregressive models. Prediction
37 performance at day+1, using the non-autoregressive models and a validation dataset, reached 80%
38 of the observed variance, compared to 32% for a standard single-regime (regression) analysis, and
39 40 % for a Support Vector Regression. Inclusion of an autoregressive term increases results to 93%
40 of explained variance for the mixture model compared to 80% without autoregressive term and 85%
41 using a Support Vector Regression. These results stress the potential of the identification of
42 geophysical regimes to improve the forecasting, or the inversion, of a high resolution geophysical
43 variable using both observations and model outputs. We also show that for short periods of lack of
44 observations (less than 15 days), estimations using the autoregressive term are better than without.
45 In this case the autoregressive term and the transition probabilities between regimes are estimated
46 using available model outputs.

47 Index term: 1) Satellite-derived suspended matter time series analysis. 2) Statistical forecasting. 3)
48 Regime-switching latent regression models. 4) Joint analysis of satellite-derived products and
49 operational model outputs. 5) Gironde river plume.

50 **1 Introduction**

51

52 The forecasting of a geophysical variable using statistical models is an alternative to model-
53 based approaches which typically involve complex simulation and/or assimilation [1, 2]. For
54 instance, coupled hydrodynamic and sediment transport models can be used to estimate the
55 concentration of suspended particulate matters within the water column [3] while statistical
56 approaches may use available satellite and model data to predict the same variable [4]. Many
57 statistical approaches have been proposed and evaluated to forecast or infer a studied variable from
58 predictors. Among them, linear multivariate regression [5] and non-linear (polynomial) multivariate
59 regression [6] are the most known. Numerous specific models dedicated to time-series analysis such
60 as AutoRegressive Moving Average (ARMA) and AutoRegressive Integrated Moving Average
61 (ARIMA) models [7] have also been developed initially to address financial time series. These
62 latest, which aim at studying the behavior of a time series without considering forcing factors, have
63 also been applied to geophysical time series [8]. Non-linear regressions, based on supervised
64 learning strategies, such as Neural Networks [9] and Support Vector Regressions (SVR) [10] may
65 provide relevant alternatives to estimate a variable from predictors. In the context of geophysical
66 studies, they may nevertheless suffer from two major drawbacks. First, though relevant regression
67 performances may be reported, these models are not physically interpretable and may be very
68 sensitive to the training dataset. Second, multi-regime dynamics, often exhibited by geophysical
69 processes driven by the seasonality [11], cannot be addressed by non-linear models, contrary to
70 latent-regime models as demonstrated in our study.

71 We propose here to characterize time-varying relationships between a variable and its forcing
72 parameters using latent-regime models, and hence optimize forecasting results. As an illustration,
73 we address the concentration of inorganic suspended particle matters (SPIM), estimated from
74 satellite data using a regional algorithm [12, 13], and observed in the mouth of the Gironde estuary.
75 In this area, sediments are mainly exported from the Gironde estuary [13, 14] and SPIM
76 concentration clearly depends on the local physical forcing: swell, tide, wind and river discharge. A
77 minimum of energy has to be brought by waves and tides to re-suspend cohesive sediments
78 accumulated at the bottom. Conversely, when sediments have been re-suspended in the water
79 column by wave influence, their settling velocity depends on their size and density [15] and
80 physico-chemical properties [16]. This example stresses that the relationships between the studied
81 variable (SPIM) and the causing factors evolve in space and time and potentially requires advanced
82 statistical methods to identify the underlying geophysical regimes.

83 From a methodological point of view, “latent regime regressions” also referred as “clusterwise
84 regressions” [17, 18] are particularly appealing to identify such non-linear and multi-regime
85 patterns within a dataset. Each regime is associated with a linear regression and a non-linear
86 relationship is thus estimated as a sum of linear contributions. Regarding the temporal dynamics of
87 these regimes, we here consider Markovian processes [19], which state the transitions in time
88 between two regimes. The standard Hidden Markov Model (HMM) and Non-Homogeneous
89 Markov Model (NHMM) are evaluated [19]. The inclusion of an autoregressive term (HMM-AR)
90 and (NHMM-AR) is also discussed. This aspect is motivated on the one hand by the strong
91 autocorrelation level depicted by geophysical time series [20]. When the observation at $t-1$ is
92 available, it is obvious, considering the strong natural autocorrelation of geophysical data that the
93 forecast at time t should take into account the observation at time $t-1$. Conversely, for specific
94 applications, or if the observations are not available during long periods (such as winter storms, or
95 after a sensor failure), one may need to estimate the variable without using the observations of the

previous days. We discuss here the choice between autoregressive or not autoregressive models for long lack of observation period using forecasting results from $t+1$ to $t+15$.

Model parameter estimation is carried out from a dataset composed of 5862 time series of 1096 points in the mouth of the Gironde estuary in the $[3^{\circ}\text{W}-1^{\circ}\text{E} ; 45-46.5^{\circ}\text{N}]$ area during the period 2007-2009. Validation is performed on the same area for using the data for the year 2010. We used EOFs to reduce the dimension of the space-time observations. This is a usual approach in spatio-temporal statistics [21, 22] although alternatives may be considered such as linear discriminant analysis [23], and, we could also introduce a latent variable to describe the regime at each location and interact with the regimes at other locations. Nevertheless, such models are known to be very difficult to fit on the data and remain a research challenge for statisticians. We infer our mixture model using the expansion coefficients of the first four modes of the EOF which explain 99% of the total variance. The variables used as predictors for the SPIM expansion coefficients (EC) are the wave height issued from a numerical model [24], the wind fields optimally interpolated from satellite observations [25], the tide coefficient [26] and the Gironde fresh water discharge (sum of the Garonne and Dordogne Rivers contributions).

2 Methods

2.1 Markov switching forecast models

We address here the study of a two dimensional scalar geophysical time series Y . In a hidden Markov model framework (HMM; [19]), one states two different processes, the observed process Y and a hidden process Z . The observed process (here the turbidity) is assumed to be temporally dependent of the hidden process. The hidden process Z_t is modeled as a first order Markov chain [19]. At a given time t , the hidden variable $Z_t = k$ is a discrete value which states the regime

119 characterized by a latent [17] regression model with coefficient B_k between the variable Y_t and the
120 predictor X_t . At time t , knowing regime variable Z_t , the observed variable Y_t is modeled as:

$$121 \quad (Y_t | Z_t=k) = X_t B_k \quad (1)$$

122 where $X_t B_k$ is the regression function, which predicts variable Y_t from some predictors X_t for
123 regime $Z_t = k$.

124 Figure 1 shows a graphical representation of the conditional dependencies involved in the
125 model, in the form of the general Directed Acyclic Diagram (DAG). It illustrates the interactions
126 between the variable Y_t , the predictors X_t , the hidden regime Z_t and the covariate S_t which acts on
127 regime switching. X_t may contain lagged values of Y_t (referred as autoregressive terms) and/or
128 exogenous covariates such as wind or wave height. Figure 1 defines a general family of model
129 which encompasses the most usual ones with regime switching. When no covariate is considered
130 i.e., Z_t only depends Z_{t-1} , and, Y_t only depends on $(Y_{t-s} \dots Y_{t-1})$ and Z_t , we retrieve the usual Markov
131 switching autoregressive (MS-AR). If we further assume that $s=0$ (without autoregressive
132 component where Y_t only depends on Z_t) then we obtain the Hidden Markov Models (HMMs).
133 When Z_t does not depend on Z_{t-1} , and the dependence on S_t is parameterized using indicator
134 functions, we obtain the threshold autoregressive (TAR) model which is the other important family
135 with regime switches in the literature. HMMs, MS-AR and TAR have been used in many fields of
136 applications including geosciences [27].

Figure 1: Graphical representation of the various Markov-Switching Models considered in this work: the arrows state the conditional dependencies between the random processes in play, namely hidden regime process Z , observed process Y , prediction process X and regime change covariate process S .

In the following equations (2 to 14), X_t and S_t are known, as they are either observations or numerical model outputs. Given (1) the conditional likelihood of the observation Y_t given predictors X_t and regime Z_t is expressed as [17]:

$$P(Y_t | X_t, Z_t = k) \sim N(X_t B_k, \sigma_k) \quad (2)$$

where N represents the Gaussian probability density function with mean $X_t B_k$ and covariance σ_k . Hence, given predictors up to time t we can predict process Y from its expectation conditionally to process X :

$$Y_t = E[Y_t | X_t = k] = \sum_{k=1}^K P(Z_t = k | X_t) \cdot E[Y_t | X_t = k, Z_t = k] = \sum_{k=1}^K P(Z_t = k | X_t) \cdot X_t B_k \quad (3)$$

where K is the number of regimes. $P(Z_t = k | X_t) = \pi_{tk}$ is the posterior probability that the dynamical regime Z at time t is of type k [17].

3 Markov-switching priors

Stating hidden regime process Z as a first-order Markovian process amounts to modeling the transition between successive regimes at time t and time $t-1$. In the simplest case, one assumes homogeneous transitions, i.e. time-independent and context-independent transitions, and the Markovian process is fully characterized by its transition matrix $P(Z_t = k | Z_{t-1} = l)$ for possible pairs of successive regimes (k, l) . In the HMM setting the conditional distribution of Z_t , given the past values Y_s and Z_s for $s < t$, is assumed to depend only on Z_{t-1} (Fig. 1):

$$\pi_{tk} = P(Z_t = k | Y_0 \dots Y_t) = \sum_{l=1}^K P(Y_t | Z_t = k) \cdot P(Z_t = k | Z_{t-1} = l, P(Z_{t-1} = l | Y_0 \dots Y_{t-1})) \quad (4)$$

A NHMM extends this idea by allowing the transition matrix between the hidden states to depend on a set of observed covariates S_t . Hughes and Guttorp [28, 29] highlighted the added value of the NHMM to characterize the links between the large-scale atmospheric measures and the small-scale spatially discontinuous precipitation field. In the NHMM settings, the transition matrix between states $P(Z_t = k | Z_{t-1} = l)$ in (3) is now time-dependent and conditioned by the covariates S_t :

$$\pi_{tk} = P(Z_t = k | Y_0 \dots Y_t, S_t) = \sum_{l=1}^K P(Y_t | Z_t = k, S_t) \cdot P(Z_t = k | Z_{t-1} = l, S_t, P(Z_{t-1} = l | Y_0 \dots Y_{t-1})) \quad (5)$$

with:

$$P(Z_t=k | Z_{t-1}=l, S_t=PS_t | Z_t=k, Z_{t-1}=l) = P(Z_t=k | Z_{t-1}=l) /$$

$$k,l | PS_t | Z_t=k, Z_{t-1}=l) \cdot P(Z_t=k | Z_{t-1}=l) \quad (6)$$

The non-homogeneous transition between states is derived from the likelihood of the covariate S_t given the state transition (Z_t, Z_{t+1}) . We suppose that the probability density function of the covariates during this change of state follows a normal distribution:

$$PS_t | Z_t=k, Z_{t-1}=l = N(\mu_{l,k}, \Sigma_{l,k}) \quad (7)$$

Where N is a multivariate normal distribution with n means $\theta_s = \mu_{l,k}$, $\Sigma_{l,k}$, μ is here of dimension n , the number of covariates used to estimate the transitions. For a 'standard' multivariate gaussian distribution $\Sigma_{l,k}$ is a covariance matrix. In the present application, and to reduce the number of parameters to be estimated, we consider that the predictors are uncorrelated (null covariance) and their relative influence is identical (same variance), i.e. $\Sigma_{l,k}$ is a multiple of the identity matrix.

181

3.1 Estimation of the model parameters

183

The considered models involve two categories of parameters: those of the observation model, θ_k , namely regression coefficient B_k and standard deviation σ_k for each regime (Eq. 2) and those of the Markov-switching prior, namely θ_s (Eq. 5). Given observed Y and X series, we proceed to the estimation of model parameters according to a classical maximum likelihood (ML) criterion using an iterative Expectation Maximisation (EM) procedure [30] expressed here without covariates:

$$L(\theta) = \prod_{t=1}^T P(Y_t | Y_{t-1}, \theta) \quad (8)$$

190 where $\theta = \{\theta_s, \theta_k\}$ is the set of parameters to be estimated. For a given initialization for the
 191 parameters the EM procedure iterates estimation steps (E-step) of the posterior regime likelihood
 192 π_{tk} with the given modes and the maximisation step (M-step) for the update of the parameters given
 193 these posteriors. The algorithm iterates until convergence between steps n and $n+1$, i.e.
 194 $|L\theta(n) - L\theta(n+1)| < 10^{-3}$. The posterior likelihood π_{tk} (Eq 3&4) of the latent regime Z_t , is
 195 estimated in the E-step using the classical forward-backward recursions [31, 32] given series X and
 196 Y and current parameter estimate $\theta_k^{(n)}, \theta_s^{(n)}$. The M-step re-estimates the parameters $\theta_k^{(n+1)}, \theta_s^{(n+1)}$.
 197 For this, it is often possible to break the optimization problem into several lower dimensional
 198 optimization problems which are much quicker to solve [32]. More precisely, for all the models
 199 considered in this paper, it is possible to separate the parameters related to the evolution of the
 200 hidden Markov chain θ_s , and the parameters related to the evolution of the observed process in each
 201 regime θ_k :

$$202 \quad \theta = \underset{\theta_s}{\operatorname{argmax}} \sum_{t=0}^T \log(P(Z_t = k | Z_{t-1} = l, S_t, \theta_s(n)) P(Z_t = k, Z_{t-1} = l | Y_0..Y_T, S_t, \theta(n))) \quad (9)$$

$$203 \quad \theta_k = \underset{B_k}{\operatorname{argmin}} \sum_{t=0}^T P(Z_t = k | Y_0..Y_T, \theta(n)) (Y_t - B_k X_t)^2 \quad (10) \quad \sigma_k(n+1) = \sum_{t=0}^T P(Z_t = k | Y_0..$$

$$204 \quad Y_T, \theta(n)) (Y_t - B_k X_t)^2 \quad (11)$$

205

206 **3.2 Forecasting application**

207

208 The considered multi-regime regression models are applied to the short-term forecasting of
 209 series Y . More precisely, at a given time t , we aim at predicting variable Y at time $t+dt$. We
 210 typically assume that prediction variables X and covariates S , typically numerical simulations, are
 211 available up to time $t+dt$ whereas the variable Y is only known up to time t . θ is estimated using
 212 $X_{0..t+dt}$ and $S_{0..t+dt}$ (for inhomogeneous transitions). Thus, Y_{t+dt} is given by the conditional

213 expectation of variable Y_{t+dt} given observations series up to time t and predictor series up to time $t+$
214 dt :

215
$$(12)$$

216 For HMM and NHMM it resorts to:

217
$$(13)$$

218 For autoregressive models HMM-AR and NHMM-AR, i.e. X_{t+dt} contains Y_{t+dt-1} which is not
219 available, is estimated using Y_{t+dt-1} , X_{t+dt-1} and Y_{t+dt} . Estimated Y_{t+dt} resorts to:

220
$$(14)$$

221 It might be noted that these predictions actually account for the uncertainties in the
222 determination of the underlying regimes. Contrary to deterministic methods, confidence interval
223 and uncertainties on Y_{t+dt} can be derived [33] which is a key issue for modeling considerations.

224

225 **3.3 Model performance estimation**

226

227 A key issue in practice, which has received lots of attention in the last few years, is the problem
228 of model selection which aims at finding the "optimal" number of predictors and covariates [31].
229 Hereafter, we have chosen to use both the Bayes Information Criterion (BIC) and the explained
230 variance (EVAR) as a first guides. BIC index generally permits to select parsimonious models
231 which fit the data well [34]. It is defined as:

232
$$BIC = -2 \log^*(L) + p \cdot \log(S) \quad (15)$$

233 Where L is the likelihood of the data, p is the number of parameters and S is the number of
234 observations. The likelihood which is an output of the backward-forward recursions performed in
235 the E-step. We also use the classical explained variance, EVAR, to characterize the model
236 relevance:

$$237 \quad \text{EVAR} = 1 - \frac{\text{var}(Y_{t+1} - \hat{Y}_{t+1})}{\text{var}(Y_{t+1})} \quad (16)$$

238 BIC and EVAR are partially linked [34]. BIC tends to penalize complex models whereas
239 explained variance criterion only qualifies the result and may lead to the over-parameterization of a
240 model that typically lead to errors when other dataset are tested using the same parameterization.
241 Therefore we consider both BIC and EVAR to assess the model performance.

242 The choice of the predictors and the covariates is performed here as follows. We first select as
243 predictors the variable showing a significant correlation with the studied variable. Given these
244 predictor datasets, we tested all the possible configurations and chose the predictors which provide
245 the lower BIC on the training dataset and the greatest EVAR using the training (EVAR_train) and
246 the validation dataset (EVAR_valid).

247

248 **4 The data**

249

250 **4.1 The studied variable**

251

252 Non-algal SPM concentrations (SPIM) are estimated using an analytical algorithm [12] defined
253 as the difference between total SPM and phytoplankton biomass, the latter derived from Chl-a. It
254 incorporates mainly mineral SPM and smaller amounts of organic SPM not related to living

255 phytoplankton. This method to derive non-algal SPM from remote-sensing reflectance is based on
 256 the inversion of a simplified equation of radiative transfer, assuming that chlorophyll concentration
 257 is known. This merged dataset consists of fields of non-algal surface SPM concentrations, derived
 258 from the Sea-viewing Wide Field-of-view Sensor (SeaWiFS), the Moderate Resolution Imaging
 259 Spectroradiometer (MODIS) and the Medium Resolution Imaging Spectrometer (MERIS) sensors,
 260 provided by the Ocean Colour TAC (Thematic Application Facility) of MyOcean, and interpolated
 261 with a kriging method [35] for the period 2007–2009 over the Gironde mouth river from 3°W-1°E ;
 262 45-46.5°N. Finally 5682 continuous time series of 1096 days compose our initial dataset of mineral
 263 suspended matters concentration.

264 We first account for the space-time variability of the dataset, previously detrended and centered
 265 for each time series [37] using a EOF decomposition [21], expressed here using the matrix form:

$$266 \quad \text{Cov}(\text{SPIM}) = \text{UVU}^t \quad (17)$$

267 where U is a here 5682*5682 matrix containing the spatial modes (Eigenvectors) of the
 268 covariance decomposition (ordered by percentage of explained variance). Associated with each
 269 spatial mode k, its expansion coefficient (also referred in the literature as principal component) is
 270 the time evolution of the kth mode:

$$271 \quad \text{EC_SPIM}_{k,t} = \text{SPIM}_t * U_k \quad (18)$$

272 Figure 2 shows the four first spatial modes of the EOF decomposition. Figure 3 depicts the four
 273 associated time series EC_SPIM_{i=1,4}. The first mode (Fig.2a) comprises 85% of the total variance. It
 274 clearly addresses the seasonal cycle as shown in Fig. 3a where the switch between winter (high
 275 values of EC_SPIM₁ correspond here to high values of SPIM observed in winter) and summer
 276 periods is clearly visible. The variability around the seasonal mean is captured by the other modes
 277 (Fig.2 c-e & Fig 3 c-e). Mode 2 refers to the inter-annual and the intra-seasonal variability in the
 278 shoreward gradient and represents 7% of the total variance. Mode 3 addresses some North-South

279 gradients and represents 4% of the total variance and mode 4 is clearly influenced by the Gironde
 280 river (Fig. 2d), which brings sediments during water outflow, and represent 3% of the variance. By
 281 construction, EOF decomposition imposes the orthogonality [21] of the spatial modes (Fig. 2).

282 Figure 2: spatial modes of the EOF decomposition of the SPIM observed from satellite from
 283 2007-2009 in the Gironde mouth river. From left to right and top to bottom the first four EOF
 284 modes account respectively for 85, 7, 4 and 3% of the total variance.

Figure 3: EOF decomposition of the SPIM observed from satellite from 2007-2009 in the Gironde mouth river: from left to right and top to bottom, the expansion coefficients (EC_SPIM_{1-4}) associated with the first four EOF modes depicted in Fig. 2, i.e. the time evolution of the spatial modes. The reconstruction of the SPIM variable from the estimated ECs is performed as:

$$SPIM_t = k EC_SPIM . Uk \quad (19)$$

The total explained variance using the 4 first modes is shown Fig. 4. On average, the explained variance represents 99 % of the total variability on the areas with some local minima of 60% observed at the very near-shore and the Southwestern part of the area.

Figure 4: Variance explained by the four first modes of the EOF decomposition of the suspended matters.

4.2 Predictors and covariates

The predictors X are the variables used in the estimation of Y and Z any time (Eq. 13 & 14). We used here wave height (WH) daily means of the Wave Watch 3 model (WW3; [24, 36]) provided by the IOWAGA and PREVIMER programs, Western and Northern winds interpolated from QuickSCAT and ASCAT observations in conjunction with ECMWF forecasting [25], provided by Ifremer, tide index (SHOM, 2000) at Bordeaux and the flow measurement of river la Gironde. Similarly to the SPIM data, all the data were log transformed. For the wind data which is signed, the transformed log variable was signed negatively a posteriori to the log transformation. The WH first mode of the EOF decomposition explained 98 % of the total variance, 93% for the Northern wind

307 (WND1), and 96% for the Western wind (WND2). Covariates are the normalized predictors used in
308 the estimation but considered at $t-2$. This lag has been estimated as the optimal time-lag using BIC
309 and EVAR results on the training dataset.

310

311 **5 Results**

312

313 We summarize in Table 1 the prediction performance for the first four ECs of the SPIM issued
314 from four models: HMM, NHMM, HMM-AR, and NHMM-AR. The number of considered modes
315 for the mixture varies from 1 to 3. The one-mode models refer to a simple multivariate regression
316 analysis. For each configuration we provide the BIC and EVAR_train on the training dataset
317 (2007-2009) and EVAR_valid on the validation dataset (2010). Note that the selection of the
318 predictors and resulting covariates is achieved as a prior step as described in Section 2.6. The first
319 mode of the EOF decomposition explains 85% of the total variance. EC_WH₁ and EC_WND2₁
320 (respectively the expansion coefficient of the first EOF of the Western winds) are identified as
321 being the relevant predictors. This mode captures the mean seasonal variability of the SPIM, which
322 is mainly driven by WH and the North Atlantic storms and at a second order by the Western winds.
323 For EC_SPIM₁, when no autocorrelation term is used, the best fit is obtained for a 3-regime
324 NHMM model (BIC= 9873, EVAR_train=90% and EVAR_valid=85%). When a first order
325 autocorrelation term is added, the best fit is issued from a 3-regime HMM-AR model: BIC= 7997,
326 EVAR_train = 98% and EVAR_valid = 97%. The lag-1 autocorrelation value is 0.85 for
327 EC_SPIM₁, and therefore the weight given Y_{t-1} is important compared to the other covariates,
328 EC_WH₁ and EC_WND2₁. This stresses the fact that when available first autoregressive term
329 should be included to enhance the performances

pas
clair

330 The second mode of the EOF decomposition of the SPIM variability explains 7% of the total
 331 variance. The selected predictors are the first mode of the Western wind, the tide, and the river
 332 flow. The variability captured by EC_SPIM₂ relates to the local Westward wind, which is not
 333 captured by the WH model, and the very coastal variability introduced by the tide and the river
 334 outflow. For the non-AR models the selected model was the three-regime NHMM. It is interesting
 335 to note in this case that EVAR_{valid} increased from 50 to 73% between the HMM and the NHMM,
 336 highlighting the contribution of the non-homogeneous transition model. By contrast, the HMM-AR
 337 performed slightly better than the NHMM-AR.

niveau de contribution des variables complémentaires

338 Table 1: Model performance for each EOF mode of the SPIM variability. For each
 339 configuration we report the BIC (a) and the explained variance (EVAR_{train}, b) for the training
 340 dataset (2007-2009), and the explained variance (EVAR_{valid}, c) for the validation dataset (2010).
 341 In bold are highlighted for each EC the selected configurations (see § 5.2).

EC_SPIM	Number of modes, M					
	1	2	3	1	2	3
1	HMM (a) 11183 (b) 37 (c) 32	HMM 10037 84 70	HMM 9874 85 75	HMM-AR 8157 92 91	HMM-AR 7986 95 93	HMM-AR 7997 98 97
	NHMM 11184 37 34	NHMM 10037 84 71	NHMM 9873 90 85	NHMM-AR 8171 92 90	NHMM-AR 7994 92 94	NHMM-AR 8018 98 97
2	HMM 9403 18 12	HMM 8579 67 33	HMM 8129 76 50	HMM-AR 7167 90 87	HMM-AR 7098 91 89	HMM-AR 7075 92 91
	NHMM 9451 18 12	NHMM 8614 67 44	NHMM 8152 79 73	NHMM-AR 7188 89 88	NHMM-AR 7383 90 87	NHMM-AR 7070 92 90
3	HMM 8840 12 7	HMM 8222 57 44	HMM 7844 68 72	HMM-AR 6723 85 84	HMM-AR 6632 86 91	HMM-AR 6630 88 92

	NHMM 8866 11 16	NHMM 8246 59 45	NHMM 7862 75 76	NHMM-AR 6745 88 86	NHMM-AR 6673 88 91	NHMM-AR 6703 88 92
4	HMM 8248 18 28	HMM 7596 60 63	HMM 7285 71 72	HMM -AR 6398 85 86	HMM -AR 6416 85 86	HMM -AR 6313 86 86
	NHMM 8276 18 28	NHMM 7628 62 59	NHMM 7267 70 75	NHMM-AR 6426 85 83	NHMM-AR 6445 85 83	NHMM-AR 6357 86 85

342

343 The third mode of the EOF decomposition of the SPIM variability explains 4% of the total
344 variance. It captures some inter-annual and intra-seasonal variability of the latitudinal gradient of
345 the SPIM. The selected predictors are EC_WH₁, EC_WND1₁ (Northern) and the tide. Once again,
346 three-regime NHMM and HMM-AR provide the best results.

347 Regarding the fourth mode of the EOF decomposition of the SPIM variability, which accounts
348 3% of the total variance, EC_WH₁, EC_WND2₁, the tide and the river flow are selected as
349 contributive predictors. We reconstruct 75 % of EC_SPIM₃ variance of the validation dataset using
350 a three-regime NHMM and 86% using a three-regime HMM-AR. We note that globally, the three
351 indices (BIC, EVAR_train and EVAR_valid) tend to select the same models.

352

353 **5.1 Example with the estimation of EC_SPIM₁**

354

355 We report in Figure 5 the temporal evolution of the three regimes of the NHMM for EC_SPIM₁.
356 In table 2 are shown the corresponding coefficients for each predictor and the intercept. The first
357 regime (light grey), characterized by high SPIM levels (intercept of 65), is referred as a ‘winter
358 regime’. The ‘winter regime’ also strongly relates to the wave height (WH regression coefficient of
359 0.6). Dark grey periods (regime 3) are identified as a ‘transition regime’, and medium grey (regime

2) identified as the ‘summer regime’. For regimes 2 and 3, the coefficients for WH decrease respectively to 0.12 and 0.09. In summer the energy brought by waves is not sufficient enough to re-suspend massively the sediments. It might be noticed that for all regimes the wind conditions show a small but significant effect on EC_SPIM_1 . When an autocorrelation term is added (HMM-AR, table 2), the AR(1) coefficient value is 0.86 for the regime 1 (winter), and 0.9 for regime 2 and 3 which underlies the natural higher autocorrelation level of SPIM when the concentration is low.

Figure 4 compares the prediction of EC_SPIM_1 using a single multivariate regression (green) and the proposed multi-regime NHMM. In this case the explained variance value (Table 1) is of 37% for the multivariate regression model compared to 85% for the three-regime NHMM.

Figure 5: Estimation of the EC_SPIM_1 (in black) using EC_WH_1 , EC_WND2_1 and a single regression (green) and a 3 regime NHMM (red). The nuances of grey in the background highlight the temporal distribution of the regimes.

374 Table 2: Estimated regression parameters for each of the three regimes of the NHMM and the
 375 HMM-AR for the first mode of the SPIM EOF decomposition: regression parameters involve an
 376 intercept and the regression coefficients of the wave height and western wind velocity.

	EC_WH ₁	EC_WND ₂	Intercept	
NHMM	(1, winter) 0.6037	-0.0632	65.0672	variance expliqué par chaque terme
	(2, summer) 0.0910	0.0006	-61.6442	
	(3, transition) 0.1210	0.0100	-24.6578	
	EC_WH ₁	EC_WND ₂	Intercept	AR(1)
HMM-AR	(1) 0.2383	-0.0033	4.4694	0.86
	(2) -0.0050	0.0168	-3.9531	0.90
	(3) 0.0354	0.0035	0.6079	0.90

377

378 Figure 6 illustrates the non-homogeneous transition used in the NHMM between the ‘transition’
 379 ($Z_t=3$) and ‘winter’ ($Z_t=1$) regimes. The probability of switching from regime 3 to 1 increases with
 380 wave height covariate WH_1 with a probability of switching close to zero when WH_1 is negative and
 381 a probability close to one for large WH_1 values.

382

383 Figure 6: Non-homogeneous transition between ‘transition regime’ ($Z_t=3$) (light grey Fig. 5)
 384 and ‘winter regime’ ($Z_t=1$) (light grey Fig. 5) as a function of the wave height covariate WH_1 .

385 **5.2 Forecasting of the SPIM on the 2010 validation dataset**
386

387 We forecast SPIM fields from the reconstructed ECs and the selected models (Table 1 & Eq.
388 19). Figure 7a&7b compare EVAR_valid of the initial field (SPIM) using the three-regime NHMM
389 and NHMM-AR models selected in Table 1 for their results. On average we were able to predict at
390 t+1 80% of the variance using the NHMM (Fig. 7a) and 90% using the NHMM-AR. The spatial
391 distribution of the error is not homogeneous. Fig. 7a shows that EVAR_valid value is of 90% in the
392 Northern part with nevertheless poorer results in the South. Fig. 7b shows that the AR₁ component
393 of the model increases EVAR for the whole area.

394 We also consider the results of a standard multi-regression analysis. If only one regime is
395 considered NHMM and HMM resort to a standard multivariate regression and NHMM-AR and
396 HMM-AR to a standard multivariate regression including an AR₁ coefficient the transition
397 probabilities being equal to 1. Fig. 7c shows the obtained results with the standard multivariate
398 regression and Fig 7d the standard multivariate regression including an AR₁. From Fig. 7c to 7a, the
399 gain in explained variance is in mean about 250% (from in mean 32% Fig. 7c to 80% Fig. 7a) while
400 for the AR models, the gain is about from 11% (from in mean 83% Fig. 7d to 93% Fig. 7b).

401

Figure 7: Explained variance for the 2010 validation dataset reconstructed using the selected 3-regime NHMM (a) and NHMM-AR (b), compared with the standard multivariate regression without AR_1 (c) and including an AR_1 (d).

To consider the model forecast performances, we report the short-term forecast results at different time steps (cf. Eq.13 & 14). For the HMM-AR and NHMM-AR (Eq. 14) is the estimated value, the observation being not available (see § 3.2). Table 3 synthesizes the explained variance statistics using 3 regimes and the four tested models for the forecasting at $t+1$, $t+5$ and $t+15$ and the validation 2010 dataset (Eq. 19).

The long term forecasting results are globally better with the NHMM. At $t+15$ using the NHMM we are able to forecast 74% of the variance for 2010, compared with 40% for the HMM. In this case where the covariates and predictors (mode outputs for which the short term predictions are assumed to be available) are used in the estimation of the regime transition probability. For autoregressive models, at $t+15$, we were able to forecast 75% of the 2010 variance with the NHMM-AR compared with 70% with the HMM-AR. For the NHMM-AR the covariates help in the estimation of both and. At $t+15$ NHMM and NHMM-AR show equivalent results underlying the maximal time-step to consider for the between these two models.

Table 3: Validation results on year 2010. Explained variance (Eq. 16) for the forecast at $t+1$, $t+5$ and $t+15$ of the 2010 validation dataset.

EVAR for the 2010 validation dataset	
HMM $(t+1)$ 73 $(t+5)$ 63 $(t+15)$ 40	HMM-AR 93 80 70
NHMM $(t+1)$ 80 $(t+5)$ 77 $(t+15)$ 74	NHMM-AR 93 82 75

SVR model was also evaluated to evaluate the performances of a non-linear model on the studied dataset. To perform the comparison, we train the SVR model (<http://www.csie.ntu.edu.tw>) for each EC using the same training dataset (2007-2009) and performed forecasting using the same validation dataset (2010). We used the setting as following: model epsilon-SVR ($s=3$), linear or polynomial kernel ($t=0$ or 1) and the same inputs (predictors, covariables) for each EC. Parameters c and g [10] were optimised for each EC using the training dataset and the cross validation mode. On the 2010 validation dataset, better forecast results reached 40% at $t+1$ of the EVAR (without AR) and 85% with an AR coefficient. The results were significantly worse than those obtained using the time-varying models for increasing time steps. The SVR can address non-linear relationships, it cannot nevertheless deal with multi-regime processes. By contrast, the latent-regime model addresses by nature multi-regime processes and can approximate non-linear relationships as a series of linear models.

6 Discussion

We investigated the relevance of four regime-switching latent regression models, namely HMM, NHMM, HMM-AR and NHMM-AR to characterize time-varying linear relationships between the high resolution inorganic suspended matter concentration (SPIM), estimated from 2007 to 2009 using MODIS, SeaWiFS and MERIS data in a coastal area, and its forcing conditions, i.e. the wave height, the Northern and Western winds, the tides and the river flow. The estimated regimes are then used to forecast the SPIM using the independent year 2010 dataset, from $t+1$ to $t+15$.

An optimal number of three distinct geophysical regimes were needed to capture the different dynamics and optimize forecasting performance. Autoregressive and non-homogeneous model showed better performances. With the evaluated models and the 2010 validation dataset we were able to forecast at $t+1$ 80 % of the variance explained using a NHMM and 93 % using a NHMM-AR. In the latest case the strong natural autocorrelation of the studied signal is an important predictor to consider. The explained variance on the prediction at $+1$ for a standard multivariate regression was of 32% and 80% (with an AR_1 term). Using a SVR we were able to forecast at $t+1$ respectively 40% and 85% (with an AR_1) of the explained variance.

As illustrated for the first SPIM EOF component (Figure 5), the proposed multi-regime setting allowed us to identify three seasonally varying relationships between the observed turbidity, the wave height and the wind. We did not drive the model to account for seasonal regimes but we identified three seasonally-discriminated regimes, with two leading factors: the mean SPIM level (intercept) and the Western wave height. These regimes identified directly physical behaviors, here the minimum of energy to be brought by the Western swell to re-suspend the sediments. This is regarded as a key feature of the latent-regime model compared to other non-linear regression models, such as Neural Networks [38] or SVR [10] which cannot address multi-regime

relationships and ~~are~~ hardly interpreted in general. Using our dataset the non-linear SVR was not able to retrieve the regime changes.

Regarding long-term forecast performance, at $t+15$ best results obtained were of 74% of explained variance for the NHMM and 75% for the NHMM-AR. For short period, typically from 1 to 15 days, when the observed Y is not available, NHMM-AR provided the best results. In this case the predictors and covariates are used in the estimation of both and . At $t+15$ NHMM and NHMM-AR showed similar results underlying the maximal time-step to consider, when no observation of Y is available, for the choice between these two models.

In the future, we will address the forecasting of the chlorophyll-a using satellite-derived observations such as the photosynthetic available radiation, the temperature, the suspended matters (as index of available nutrients) and light attenuation [39]. In this more complicated case, second order relationships between the variable and its predictors have to be evaluated, the chlorophyll-a dynamic being not anymore a passive result of the forcing conditions, as expected with the SPIM, but having its proper characteristics depending on each phytoplankton specie. Extensions of the considered latent regime setting to other inverse problems in satellite sensing data analysis are also under investigation, such as latent regime inversion procedures for satellite-derived chlorophyll-a concentration to account for different water types (turbid or not turbid) and/or the presence of specific phytoplankton species.

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