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The Earth as an extrasolar transiting planet

II. HARPS and UVES detection of water vapour, biogenic O$_2$, and O$_3$*

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ABSTRACT

Context. The atmospheric composition of transiting exoplanets can be characterized during transit by spectroscopy. Detections of several chemical species have previously been reported in the atmosphere of gaseous giant exoplanets. For the transit of an Earth twin, models predict that biogenic oxygen (O$_2$) and ozone (O$_3$) atmospheric gases should be detectable, as well as water vapour (H$_2$O), a molecule linked to habitability as we know it on Earth.

Aims. The aim is to measure the Earth radius versus wavelength $\lambda$ – or the atmosphere thickness $h(\lambda)$ – at the highest spectral resolution available to fully characterize the signature of Earth seen as a transiting exoplanet.

Methods. We present observations of the Moon eclipse of December 21, 2010. Seen from the Moon, the Earth eclipses the Sun and opens access to the Earth atmosphere transmission spectrum. We used two different ESO spectrographs (HARPS and UVES) to take spectra and correct for this effect in the data processing. We analyzed the data by three different methods. The first method is based on the analysis of pairs of penumbra spectra. The second method makes use of a single penumbra spectrum, and the third of all penumbra and umbra spectra.

Results. Profiles $h(\lambda)$ are obtained with the three methods for both instruments. The first method gives the best result, in agreement with a model. The second method seems to be more sensitive to the Doppler shift of solar spectral lines with respect to the telluric lines. The third method makes use of umbra spectra, which bias the result by increasing the overall negative slope of $h(\lambda)$. It can be corrected for this with post-processing. The three methods clearly show the spectral signature of the Rayleigh scattering in the Earth atmosphere and the bands of H$_2$O, O$_2$, and O$_3$. Sodium is detected. Assuming no atmospheric perturbations, we show that the E-ELT is theoretically able to detect the O$_2$ A-band in 8 h of integration for an Earth twin at 10 pc.

Conclusions. Biogenic O$_2$, O$_3$, and water vapour are detected in Earth observed as a transiting planet, and, in principle, would be within reach of the E-ELT for an Earth twin at 10 pc.

Key words. Earth – Moon – atmospheric effects – planets and satellites: atmospheres – planets and satellites: terrestrial planets – astrophysics

1. Introduction

Observing planetary transits gives access to a set of properties of the star+planet system (e.g. Winn 2009). The relative size of the planet with respect to the star, given by the depth of the transit light-curve, is one of the most straightforward system observables. Spectrally resolved observations have shown for gaseous giant exoplanets that transit the brightest stars that the transit depth varies with wavelength (the first to report this were Charbonneau et al. 2002; Vidal-Madjar et al. 2003, 2004) which reveals the signature of the planetary atmosphere. At certain wavelengths, the atmosphere indeed absorbs the stellar light and becomes opaque, which makes the planet look larger in front of the star and produces a deeper transit. The atmosphere of smaller terrestrial exoplanets close to or in the habitable zone (HZ) is in principle also accessible by this method (early works by Schneider 1992, 1994, and more recent models by Ehrenreich et al. 2006, 2012; Kaltenegger & Traub 2009; García-Muñoz et al. 2012; Snellen et al. 2013; Bétrémieux & Kaltenegger 2013). Recent simulations show that the next generation of instruments in the infrared or visible domains, that is the James Webb Space Telescope (JWST) and the European Extremely
Large Telescope (E-ELT), should be able to offer a first access to characterizing terrestrial planets in the HZ and detecting biosignatures (here atmospheric O₂ and O₃) and molecules linked to habitability (Rauer et al. 2011; Hedelt et al. 2013; Snellen et al. 2013; Rodler & López-Morales 2014).

In this context, it is of prime interest to observe Earth as a transiting exoplanet. Vidal-Madjar et al. (2010) observed the August 2008 partial lunar eclipse with the high-resolution SOPHIE échelle spectrograph at the 193 cm Haute-Provençal telescope (Perruchot et al. 2008; Bouchy et al. 2009) and showed that the Earth atmosphere thickness versus wavelength can be derived from such observations. Earth observed from the Moon during a lunar eclipse indeed transits in front of the Sun and gives the possibility to study the Earth atmosphere as during a transit. These first observations also allowed one to identify molecular species in the atmosphere, that is water vapour (H₂O), a molecule linked to Earth habitability, biogenic oxygen (O₂), and ozone (O₃). Ozone and oxygen are considered as reliable biosignatures for Earth-like planets (Owen 1980; Léger et al. 1993; Seager et al. 2013) except for terrestrial planets derived from such observations. Earth observed from the Moon in the deep penumbra, the Sun limb (during ingress or egress) – that is, of recording Moon spectra at two different depths in the penumbra (method 1). For these two different positions on the Moon, the solar crescent above the Earth limb as well as the arc of the Earth atmosphere intersecting the solar disk, are different. We have shown (Vidal-Madjar et al. 2010, Eq. (14) therein) that h, the thickness profile of the atmosphere, or the altitude under which the atmosphere can be considered as opaque, can be written

\[
h(l) = \frac{E_A(l)}{E_A(\lambda_0)} - \frac{E_B(l)}{E_B(\lambda_0)} = \frac{F_A(l)}{F_A(\lambda_0)} - \frac{F_B(l)}{F_B(\lambda_0)}
\]

(1)

where E and F are the fluxes during the eclipse and outside the penumbra (almost full-Moon just before or after the eclipse), respectively. Subscripts A and B stand for the two different positions in the penumbra. The value λ₀ is an arbitrary wavelength for which we define h(λ₀) = 0, and the symbols S and L represent geometrical parameters equal to the surface of the Sun crescent above the Earth limb and the length of the arc of the Earth atmosphere intersecting the solar disk for h(λ₀), respectively (see Fig. 4 in Vidal-Madjar et al. 2010). Equation (1) shows that h(λ) can thus be written as a function of differences between the measured fluxes divided by a factor of geometrical values. The numerical values for S are recovered from the measured fluxes too, E(λ₀) and F(λ₀), following Eq. (11) of Vidal-Madjar et al. (2010),

\[
E(\lambda_0) = F(\lambda_0) \times \frac{S}{S_\odot},
\]

(2)

where S_\odot is the surface of the solar disk. At last, once the surfaces S are known, the lengths L can be calculated quite simply from geometrical considerations knowing the apparent diameters of Earth and Sun, so h(λ) can finally be calculated.

Equation (1) above is obtained from the differences between Eqs. (12) and (13) in Vidal-Madjar et al. (2010), each being written for one position on the Moon. These equations can be rewritten, for position A for example,

\[
h(l) = \left(1 - \frac{E_A(l)}{E_A(\lambda_0)} \times \frac{F_A(\lambda_0)}{F_A(l)}\right) \times \frac{S_A}{L_A}
\]

(3)

We note that h(λ) is fully calculable from Eq. (3) above, thus with only one penumbra spectrum (method 2). Nevertheless, because E and F are recorded at different times in the night, the barycentric Earth radial velocity (BERV) leads to a different Doppler shift between the solar and telluric lines in E and F spectra. Since we are interested in the signature of the Earth atmosphere, all spectra are re-aligned on the telluric lines, which slightly shifts the solar lines between E and F. Moreover, the solar lines integrated over the solar crescent seen from the Moon during the partial eclipse are also Doppler-shifted with respect to the lines of the full (un eclipsed) solar disk. The solar lines thus do not cancel out correctly in the ratio \(\frac{E_A(l)}{E_A(\lambda_0)}\) or \(\frac{F_A(\lambda_0)}{F_A(l)}\), and the obtained h(λ) profile is noisier, although the overall shape is correct. With the difference in the left part of Eq. (1), the solar atmosphere the nature of this mixed light in the penumbra is similar to what is observed during a transit of an exoplanet, here Earth in front of the Sun. Nevertheless, as seen from the Moon, Earth is larger than the Sun, and the Earth radius versus wavelength cannot be reconstructed from the transit depth at all wavelengths, as done with transiting exoplanets. The method consists of observing two different positions of the Sun above the Earth limb (during ingress or egress) – that is, of recording Moon spectra at two different depths in the penumbra (method 1). For these two different positions on the Moon, the solar crescent above the Earth limb as well as the arc of the Earth atmosphere intersecting the solar disk, are different. We have shown (Vidal-Madjar et al. 2010, Eq. (14) therein) that h, the thickness profile of the atmosphere, or the altitude under which the atmosphere can be considered as opaque, can be written

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\]

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where E and F are the fluxes during the eclipse and outside the penumbra (almost full-Moon just before or after the eclipse), respectively. Subscripts A and B stand for the two different positions in the penumbra. The value λ₀ is an arbitrary wavelength for which we define h(λ₀) = 0, and the symbols S and L represent geometrical parameters equal to the surface of the Sun crescent above the Earth limb and the length of the arc of the Earth atmosphere intersecting the solar disk for h(λ₀), respectively (see Fig. 4 in Vidal-Madjar et al. 2010). Equation (1) shows that h(λ) can thus be written as a function of differences between the measured fluxes divided by a factor of geometrical values. The numerical values for S are recovered from the measured fluxes too, E(λ₀) and F(λ₀), following Eq. (11) of Vidal-Madjar et al. (2010),

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where S_\odot is the surface of the solar disk. At last, once the surfaces S are known, the lengths L can be calculated quite simply from geometrical considerations knowing the apparent diameters of Earth and Sun, so h(λ) can finally be calculated.

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\]

(3)

We note that h(λ) is fully calculable from Eq. (3) above, thus with only one penumbra spectrum (method 2). Nevertheless, because E and F are recorded at different times in the night, the barycentric Earth radial velocity (BERV) leads to a different Doppler shift between the solar and telluric lines in E and F spectra. Since we are interested in the signature of the Earth atmosphere, all spectra are re-aligned on the telluric lines, which slightly shifts the solar lines between E and F. Moreover, the solar lines integrated over the solar crescent seen from the Moon during the partial eclipse are also Doppler-shifted with respect to the lines of the full (un eclipsed) solar disk. The solar lines thus do not cancel out correctly in the ratio \(\frac{E_A(l)}{E_A(\lambda_0)}\) or \(\frac{F_A(\lambda_0)}{F_A(l)}\), and the obtained h(λ) profile is noisier, although the overall shape is correct. With the difference in the left part of Eq. (1), the solar
lines cancel out much better and the $h(\lambda)$ profile is cleaner. This is discussed in more details in Sect. 7.2.

### 3. An alternative method that approximates $h(\lambda)$ (method 3)

This section describes another method, different from that of Vidal-Madjar et al. (2010), to derive the thickness profile of Earth atmosphere. In a lunar eclipse, the radius of Earth is given by the radius of the umbra. The umbra radius can be calculated geometrically for a solid sphere that casts its shadow to the Moon, but in practice, the Earth atmosphere that scatters light along Earth limb, lead to a blurred edge between umbra and penumbra on the Moon surface. The radiancy profile across the umbra edge has been measured in the past by several observers (especially by Dubois from 1950 to 1980, Danjon 1925; Combaz et al. 1950; Reaves & Walker 1952; Walker & Reaves 1957). The irradiance of the eclipsed Moon as well as the umbra edge have also been modelized (Link 1969; Vollmer & Gedzelman 2008; García-Muñoz & Pule 2011) by an analysis of the light propagation from the Sun to the Moon through the Earth atmosphere. The observed magnitude versus position with respect to the umbra center looks approximately like a hyperbolic function (or sigmoid). The observations mentioned above indicate that magnitude typically drops by about 8 mag from penumbra to umbra, the steepest region being typically 2 arcmin wide (Dubois Pounyrol 1954). Unfortunately, the spatial resolution of published radial photometry across the umbra edge is only about 1 arcmin, and not sufficient to reveal a dependence of the umbra radius with wavelength. To fix the order of magnitude, with an Earth umbra radius of $\approx 43$ arcmin, a variation of 10 km in the Earth radius (of 6371 km) translates into a change of the umbra radius of 4 arcsec.

With ESO’s HARPS and UVES spectrographs, we recorded spectra from deep penumbra to umbra over $\approx 7$ arcmin with HARPS and $\approx 19$ arcmin with UVES. Because the telescope tracked neither the star nor the Moon but the Earth umbra projected to the Moon, we were able to integrate the signal at fixed distances from the umbra edge, while the Moon itself slowly shifted in front of the spectrographs during the exposures. To compare the flux in these spectra taken at different positions in the umbra or in the penumbra, we calculate their corresponding magnitude $-2.5 \log_{10}(E/F)$ relative to the full-Moon spectra recorded before the eclipse. Then we plot for each wavelength the magnitudes versus their distance from the umbra center, as Dubois did. But while Dubois observed at three or four different wavelengths through broadband blue, green, yellow, and red Wratten filters, HARPS and UVES allow to do this now at a much higher spectral resolution. The points follow the same overall shape as Dubois’ profiles (Fig. 1). We fit a hyperbolic function through these points

$$\zeta(r) = a_0 + a_1 \tanh[a_2(r - a_2)],$$

where $\zeta$ is the model giving the magnitude in the radial direction through the umbra edge, $r$ the distance to the umbra center, and $a_i$ the parameters defining the hyperbolic function. The function $\zeta(r)$ varies between $a_0 - a_1$ and $a_0 + a_1$. We may arbitrarily define the abscissa $a_2$ of the inflection point (at ordinate $a_0$) of this function as a measurement of the umbra radius, and thus of the Earth radius at the observing wavelength.

Nevertheless, Fig. 1 shows that the inflection point corresponds to a zone about 3 mag ($\approx 15\times$) fainter than shallower penumbra. But in a real transit, only the beams of light that interact with the top of the atmosphere, and thus only weakly absorbed, leave a signature in the transit. If a beam goes deeper to the atmosphere, it is significantly dimmed and scattered, and finally absent from the transit signature of the planet. Therefore the informations from the 3 mag fainter light we obtain at the inflection point are not those we obtain during a real transit. The inflection point is thus not the best definition of the edge of the Earth’s umbra on the Moon, at least in the context of our Earth-transit analysis. It is more relevant to define a point slightly more in the brighter penumbra for the edge of Earth’s umbra, as shown by the vertical dotted line in Fig. 1, and to build up the Earth radius versus wavelength from this point instead of from the inflection point. More details are given in Sect. 7.3.

We understand that this method makes use of information that is not available in an exoplanet transit: indeed it uses information from spectra of the umbra to build the function $\zeta$, but, as mentioned in the introduction, the photons from the umbra result from highly angularly scattered or refracted beams, which are not available in the observation of an exoplanet transit. Moreover, the umbra photons, especially the red ones, have been refracted by the deepest Earth atmospheric layers, and the Earth shadow is thus shrunk by refraction at these wavelengths, leading to a smaller Earth radius in the red. In other words, the gradient in the altitude profiles measured from blue to red wavelengths will be steeper due to refraction. But we show in Sect. 7.3 that the altitude profiles $h(\lambda)$ obtained by this method can be calibrated (scaled) to the profiles obtained with method 1.

### 4. Observing log

HARPS provides spectra with a spectral resolution of 115 000 and covers the visible range (Table 1, Mayor et al. 2003). UVES was used in dichroic-1 and dichroic-2 modes (DIC1 and DIC2).
In each of these modes, both BLUE and RED arms of the spectrograph are used simultaneously, and with standard settings, two exposures (one in each mode) give a full [3100–10 400] Å spectrum (Table 1, Dekker et al. 2000). The slit width was set to 0.3 arcsec, which gives a spectral resolution of ≈120 000.

Table 2 gives information on the observations made before the eclipse. The daytime cloud fraction contributed to smooth out any relative spectral reflectance differences between the lunar terrains that drifted in front of the spectrograph pair of fibers at a speed of about 0.55 arcsec/s. The shift of the Moon during a given exposure is ≈0.5 arcsec.

Table 3 gives the expected slit positions are indicated in parentheses in the last column.

Table 4 gives series of Moon reference spectra taken with UVES before the eclipse.

Table 5 gives series of n exposures, and measured slit positions in the penumbra (negative values) and umbra (positive values) with respect to the umbra edge given by Guide-9.

Notes. Gaps without data are present in the final spectra due to small gaps between detectors.

Notes. The expected slit positions are given in parentheses in the last column.

Fig. 2. Earth and Sun seen from the Moon deep penumbra where HARPS fiber A was positioned at 07:06:35 UT, at the beginning of the 300 s exposure. Image with Guide-9.

for 2010 Dec. 21 given by Aqua/MODIS for these coordinates is ≥0.7.

5. HARPS data processing

The data processing makes use of so-called s1d reduced data output files directly from the HARPS data reduction software (DRS). The HARPS instrumental response is calibrated with a high signal-to-noise ratio (S/N) G2V star spectrum.

5.1. Correction for the Moon reflectivity

To accurately maintain a given position of the spectrograph with respect to the umbra edge during the exposures, we needed to track the umbra, not the Moon itself. The Moon was thus moving in front of the spectrograph pair of fibers at a speed of about 0.55 arcsec/s. The shift of the Moon during a given exposure contributed to smooth out any relative spectral reflectance differences between the lunar terrains that drifted in front of the

Table 1. HARPS and UVES spectral ranges.

<table>
<thead>
<tr>
<th>Instrument</th>
<th>Range (Å)</th>
<th>Gap (Å)</th>
</tr>
</thead>
<tbody>
<tr>
<td>HARPS</td>
<td>3782–6912</td>
<td>5256–5337.5</td>
</tr>
<tr>
<td>UVES DIC1 BLUE</td>
<td>3055–3885</td>
<td></td>
</tr>
<tr>
<td>UVES DIC1 RED</td>
<td>4788–6806</td>
<td>5750–5821</td>
</tr>
<tr>
<td>UVES DIC2 BLUE</td>
<td>3751–4999</td>
<td></td>
</tr>
<tr>
<td>UVES DIC2 RED</td>
<td>6712–10 426</td>
<td>8544–8646</td>
</tr>
</tbody>
</table>

Table 2. Series of n Moon reference spectra taken with HARPS before the eclipse.

<table>
<thead>
<tr>
<th>Start h:min:ss UT</th>
<th>Exposure (n x s)</th>
<th>Airmass</th>
</tr>
</thead>
<tbody>
<tr>
<td>02:18:26</td>
<td>4 x 30</td>
<td>2.15–2.12</td>
</tr>
<tr>
<td>04:41:20</td>
<td>5 x 45</td>
<td>1.70</td>
</tr>
</tbody>
</table>

Table 3. HARPS exposures and fiber positions in the penumbra (negative values) and umbra (positive values) with respect to the umbra edge given by Guide-9.

<table>
<thead>
<tr>
<th>Start h:min:ss UT</th>
<th>Exposure (s)</th>
<th>Fib. A (arsec)</th>
<th>Fib. B (arsec)</th>
</tr>
</thead>
<tbody>
<tr>
<td>06:43:32</td>
<td>600</td>
<td>-66</td>
<td>41</td>
</tr>
<tr>
<td>06:57:28</td>
<td>450</td>
<td>-204</td>
<td>-98</td>
</tr>
<tr>
<td>07:06:35</td>
<td>300</td>
<td>-232</td>
<td>-125</td>
</tr>
<tr>
<td>07:13:07</td>
<td>900</td>
<td>36</td>
<td>141</td>
</tr>
</tbody>
</table>

Table 4. Series of three Moon reference spectra taken with UVES before the eclipse.

<table>
<thead>
<tr>
<th>Start h:min:ss UT</th>
<th>Exposure (3 x s)</th>
<th>Mode and arm</th>
<th>Mean airmass</th>
</tr>
</thead>
<tbody>
<tr>
<td>02:04:19</td>
<td>3 x 4</td>
<td>DIC2 RED</td>
<td>2.01</td>
</tr>
<tr>
<td>02:18:49</td>
<td>3 x 4</td>
<td>DIC1 RED</td>
<td>1.90</td>
</tr>
<tr>
<td>02:18:56</td>
<td>3 x 40</td>
<td>DIC1 BLUE</td>
<td>1.90</td>
</tr>
<tr>
<td>05:07:25</td>
<td>3 x 4</td>
<td>DIC2 RED</td>
<td>1.56</td>
</tr>
<tr>
<td>05:07:29</td>
<td>3 x 10</td>
<td>DIC2 BLUE</td>
<td>1.56</td>
</tr>
<tr>
<td>05:19:26</td>
<td>3 x 4</td>
<td>DIC1 RED</td>
<td>1.57</td>
</tr>
<tr>
<td>05:19:30</td>
<td>3 x 30</td>
<td>DIC1 BLUE</td>
<td>1.58</td>
</tr>
</tbody>
</table>

Notes. Gaps without data are present in the final spectra due to small gaps between detectors.

Notes. The expected slit positions are given in parentheses in the last column.

1 http://www.projectpluto.com/

2 http://modis.gsfc.nasa.gov/
spectrograph. But different terrains with different albedos were seen by each fiber during the different exposures. To correct each spectrum for the flux variations induced by these albedo variations, we measure the mean lunar reflectivity along the path of the slit across the Moon surface during the exposures at posteriori. The path is reconstructed from the date and telescope coordinates available in the metadata. We build a picture of the Moon as seen during the eclipse from La Silla at a resolution of 1 arcsec/pixel: the reconstructed scene is an orthographic projection of a Clementine albedo map at 750 nm (Eliason et al. 1999) and takes into account the correct libration angles, the correct phase angle (close of zero degree), and a Lambert-Lunar limb-darkening law (McEwen 1996). The mean reflectivity is then measured with Audela-2.0 along the path of each fiber across the lunar surface as shown in Fig. 3.

5.2. Correction for the signature of the atmosphere above the telescope

To correct our eclipse spectra for the signatures of the atmosphere above the telescope, we need a reference transmission spectrum for the atmosphere $T(\lambda)$. To derive $T(\lambda)$, we proceed as in Vidal-Madjar et al. (2010) by calculating the ratio of two full-Moon spectra, $F_1$ and $F_2$, taken before the eclipse at different airmass $AM_1$ and $AM_2 < AM_1$. The ratio can be scaled to $AM = 1$ following

$$T(\lambda) = \left[\frac{F_{AM_1}}{F_{AM_2}}\right]^{1/(AM_1-AM_2)}.$$

We calculate $T(\lambda)$ with $AM_1 = 2.2$ and $AM_2 = 1.7$ (Table 2). Since we are interested only in the accurate measurement of the telluric lines in $T(\lambda)$, the two spectra in Eq. (5) are corrected for the BERV to properly align the telluric lines of both spectra (the solar lines become slightly misaligned). Figure 4 shows the obtained average reference transmission $T(\lambda)$ that we now use in the following data analysis of HARPS data to re-evaluate all eclipse spectra as if they were collected from outside the atmosphere.

6. UVES data processing

The UVES instrumental response is calibrated with the reference star HD 80170 (K5 III-IV, $T_{\text{eff}} = 4537$ K, log $(g) = 2.1$, Randich et al. 1999).

6.1. Correction for the Moon reflectivity

To measure the mean lunar reflectivity along the path of the UVES slit across the Moon surface, we build a picture of the Moon as seen during the eclipse from Paranal, as we did for the HARPS observations. An example of the slit path is shown in Fig. 5.

6.2. Correction for the signature of the atmosphere above the telescope

We can not proceed exactly as with the HARPS data because full-Moon spectra show that the water-vapour lines were.

References:

1. Eliason et al. 1999
2. Hayes & Latham 1975
pointing uncertainty is estimated to be about \( \sigma = 4\% \). The terrain reflectivity fluctuates by \( \sigma = 13\% \) along the path, taking into account a 10 arcsec pointing error in both RA and Dec directions. The mean reflectivity is measured along the path, 330 arcsec long (length of the yellow line). The mean reflectivity is measured along the path, 330 arcsec long (length of the yellow line). The mean reflectivity is measured along the path, 330 arcsec long (length of the yellow line). The mean reflectivity is measured along the path, 330 arcsec long (length of the yellow line).

The slit, 10 arcsec long and perpendicular to the path, remains at \( \approx 936 \) arcsec from the umbra edge, while the slit path over the Moon was \( \approx 330 \) arcsec long (length of the yellow line). The mean reflectivity is measured along the path, taking into account a 10 arcsec pointing error in both RA and Dec directions. The terrain reflectivity fluctuates by \( \sigma = 13\% \) along the path in this bright lunar region, and the error on the mean reflectivity due to pointing uncertainty is estimated to be about \( \sigma = 4\% \).

Fig. 5. Example of a path of the UVES slit across the reconstructed Moon image during the 600 s exposure in the umbra. The slit, 10 arcsec long and perpendicular to the path, remains at \( \approx 936 \) arcsec from the umbra edge, while the slit path over the Moon was \( \approx 330 \) arcsec long (length of the yellow line). The mean reflectivity is measured along the path, taking into account a 10 arcsec pointing error in both RA and Dec directions. The terrain reflectivity fluctuates by \( \sigma = 13\% \) along the path in this bright lunar region, and the error on the mean reflectivity due to pointing uncertainty is estimated to be about \( \sigma = 4\% \).

Fig. 6. Part of the spectrum showing the ratio of a high airmass over a low airmass UVES full-Moon spectra. The oxygen B and A bands at 6960 and 7600 Å respectively, are in absorption as expected, but the water vapour bands at 7200 and 8200 Å appear in emission, showing that the amount of water vapour along the line of sight was higher when the airmass was lower, indicating that the amount of water vapour above Paranal increased during the first part of the night, before the eclipse. To calculate this ratio, the spectra are aligned by cross-correlation to match the radial velocity of the telluric lines, so the solar lines do not properly cancel out in the ratio, and appear with a wing in emission and the other in absorption.

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We estimate the precipitable water vapour (PWV) in our spectra by using the spectral-fitting method described in Querel et al. (2011). This method compares the measured spectrum with a reference spectrum where varying the reference water-vapour content. The reference spectrum is generated using an atmospheric model configured with the local environmental parameters at the time of measurement (ambient temperature, pressure, elevation, etc.). A comparison is then made over several small spectral intervals (\( \pm 2-5 \) nm) where the only significant features are caused by absorption by water vapour. A least-squares fit is performed between the measured data and reference spectra for a range of PWV values. The reference spectrum with the smallest fit residual represents the water-vapour content (or PWV) most similar to that of the measured spectrum. Since this absorption is along the line-of-sight and assuming an isotropic distribution of water vapour above the telescope, the absorption must then be corrected back to zenith by dividing the best-fit PWV by the airmass of the measurement.

Table 6 indicates that three hours before the eclipse started the PWV measured on the full-Moon spectrum was about 6.4 mm for an airmass of 2. The PWV for airmass \( = 1 \) was therefore 3.2 mm. Later in the night, and just before the penumbra ingress, we find that PWV increased to 8.00 mm at airmass \( = 1.56 \), indicating the increase of moisture above the telescope. The reduced PWV for airmass \( = 1 \) is thus 8.00/1.56 = 5.1 mm before the eclipse started. Immediately after the eclipse observations, we observed HD 80170 and measured a reduced PWV of 5.71 mm. We therefore assume that during the eclipse, the PWV at zenith remains within the [5.1; 5.7] mm range and we chose the mean value 5.4 mm as the reference PWV at airmass \( = 1 \) during the eclipse. PWV values of 5 mm are relatively high for Paranal, and we understand that assuming such a high water vapour content is isotropic and constant above the telescope for three hours (the duration of our observations) may be a strong assumption. Nevertheless, it is the best we can do and the whole process of data reduction leading to \( h_r(\lambda) \) assumes the stability of the PWV above Paranal during the observations (this is obviously also true for the HARPS observations at La Silla).

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Table 6. Measured PWV before the eclipse and at the end the observation, and reduced PWV for airmass \( = 1 \).

<table>
<thead>
<tr>
<th>h:min UT</th>
<th>PWV (mm)</th>
<th>Airmass</th>
<th>PWV (mm) at zenith</th>
</tr>
</thead>
<tbody>
<tr>
<td>02:05 and 02:18</td>
<td>6.43</td>
<td>2.01</td>
<td>3.20</td>
</tr>
<tr>
<td>05:08 and 05:21</td>
<td>8.00</td>
<td>1.56</td>
<td>5.14</td>
</tr>
<tr>
<td>08:23 and 08:32</td>
<td>5.95</td>
<td>1.04</td>
<td>5.71</td>
</tr>
</tbody>
</table>

Notes. 1: full-Moon before penumbra ingress, DIC2 and DIC1 observations, respectively. 2: full-Moon before penumbra ingress, DIC2 and DIC1 observations, respectively. First contact with penumbra occurred at about 05:28 UTC. 3: HD 80170 at the end of the eclipse observation, DIC1 and DIC2 observations, respectively.

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full-Moon spectra $F$ for which we know the value of PWV (Table 6),

$$T_{\text{H}_2\text{O}}(\lambda) = \left( \frac{F(\text{PWV} = 8.00)}{F(\text{PWV} = 6.43)} \right)^{5.4/(8.00-6.43)}.$$  

(6)

To derive a spectrum for pure water vapour (i.e. without the lines from other elements or molecules), $T_{\text{H}_2\text{O}}(\lambda)$ is calculated only when water-vapour absorption is present ($T \leq 99\%$) in the water-vapour synthetic spectrum computed to measure the PWV. To avoid $T_{\text{H}_2\text{O}}(\lambda)$ to become too noisy in the deepest absorption bands of water vapour, the spectrum is not calculated when water-vapour transmission becomes $T \leq 2.5\%$.

The transmission spectrum for $\text{O}_2$ for airmass $=1$ is obtained by taking into account the variation of airmass AM between the two $F$ spectra (Table 6), as done by Vidal-Madjar et al. (2010):

$$T_{\text{O}_2}(\lambda) = \left( \frac{F(\text{AM} = 2.01)}{F(\text{AM} = 1.56)} \right)^{1/(2.01-1.56)}.$$  

(7)

And as for $T_{\text{H}_2\text{O}}$, $T_{\text{O}_2}$ is calculated only when $\text{O}_2$ absorption is present ($99.9\% \geq T \geq 2\%$) in a $\text{AM} = 1$ MODTRAN$^2$ synthetic spectrum.

Once $T_{\text{H}_2\text{O}}$ and $T_{\text{O}_2}$ are known, we can correct our spectra simply by the division

$$s = \frac{S}{(T_{\text{H}_2\text{O}} \times T_{\text{O}_2})^{\text{AM}}}.$$  

(8)

where $s$ is the corrected spectrum and $S$ is a full-Moon or eclipse spectrum acquired at airmass AM. The final $T(\lambda)$ spectrum for Paranal is shown in Fig. 7. The continuum shows neither the Rayleigh nor the ozone signature in this spectrum (on the opposite of what is obtained with HARPS, Fig. 4) because the UVES reduction pipeline automatically removed from all spectra tabulated values for the Rayleigh and ozone signatures at the corresponding airmass of the observation. Of course, the additional Rayleigh and ozone signatures present in the eclipse spectra and produced by the light path through the limb of the Earth atmosphere have not been removed by the UVES pipeline.

To calculate $T_{\text{H}_2\text{O}}$ and $T_{\text{O}_2}$, the full-Moon spectra are aligned with a cross-correlation to match the radial velocity of the telluric lines.

### 7. Results and discussion

#### 7.1. Results from Eq. (1) (method1)

From the HARPS data, we build five pairs of penumbra spectra suitable for Eq. (1), [98; 204], [125; 232], [66; 125], [66; 204], and [66; 232] where the numbers in brackets are the positions described in Table 3. The possible pair [66; 98] is not used: it and [66; 232] where the numbers in brackets are the positions in the penumbra spectra (Table 6), as done by Vidal-Madjar et al. (2010):

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The penumbra spectra are affected by the wavelength-dependent solar limb darkening $L_D(\lambda)$ (Hestroffer & Magnan 1998). Equation (1) makes use of geometrical parameters $S$ and $L$ for two different solar crescents visible above Earth. The solar $L_D(\lambda)$ makes the crescents fainter than the mean solar brightness. The size of the solar crescents estimated from the penumbra spectra fluxes is thus underestimated if the penumbra fluxes are not corrected for the solar LD. To correct for this effect, we first evaluate the size of the solar crescents (parameters $S$ and $L$) from the flux ratio (penumbra/full-Moon) at $\lambda = 5798.8$ Å which allows us to evaluate an average LD that affects each solar crescent following Hestroffer & Magnan (1998). For these crescent sizes and the LD obtained at $\lambda = 5798.8$ Å, a wavelength-dependent limb darkening $L_D(\lambda)$ is then re-evaluated from the low spectral resolution model of Hestroffer & Magnan (1998). It covers the spectral ranges [3033–3570] and [4160–10990] Å, with a spectral resolution of a few tens (we do a linear interpolation between 3570 and 4160 Å). The model is then used to calculate the LD-corrected penumbra spectra $E_\gamma(\lambda)/L_D(\lambda)$ and $E_B(\lambda)/L_D(\lambda)$ from which new $S$ and $L$ are evaluated for $\lambda_0$ with Eq. (2). Equation (1) is then evaluated again to derive the final $h(\lambda)$ profile.

The mean altitude profile from the five pairs of fibers obtained from Eq. (1) is shown in Fig. 8. The profile is shifted upward by $\approx$30 km to have an altitude of 23.8 km in the [4520–4540] Å domain, as predicted by Ehrenreich et al. (2006). The profile shows the large bump due to ozone Chappuis band centered around 5900 Å and peaking here at about 38 km, and the oxygen $\gamma$ and $B$ bands at 6300 and 6900 Å, respectively. Water vapour also appears around 6500 Å at an altitude above 25 km. The increase of $h(\lambda)$ in the blue due to Rayleigh scattering is visible as a negative slope between 4000 and 5000 Å (Ehrenreich et al. 2006; Kaltenegger & Traub 2009). The blue part of the profile shows many residual solar absorption lines that bias the binned profile towards lower altitudes. Numerous solar lines are visible, for example H$\beta$ at 4861 Å and H$\alpha$ at 6563 Å. The Fig. 9 is a zoom on the Na I doublet. The $\approx 2$ Å-wide
photospheric wings of the solar Na lines are still visible. The presence of all these solar features indicates that the solar signature is not properly removed from the Na I profiles. The profile shows the large bump due to ozone at 5892.9 Å, the oxygen γ-band at 5584.5 Å and the water-vapour band around 6500 Å.

Fig. 8. Altitude profile with HARPS as obtained from Eq. (1) (method 1). A 10 Å bin is superimposed in light-blue over the full-resolution profile. The profile shows the large bump due to ozone at 5892.9 Å, the oxygen γ-band at 5584.5 Å and the water-vapour band around 6500 Å.

The expected increased of $h(\lambda)$ in the blue due to Rayleigh is visible as a negative slope between 4000 and 5000 Å. Oxygen and water-vapour absorption spectra at arbitrary scale are shown.

Fig. 9. Zoom in the Na I doublet region of the altitude profile from Fig. 8 with HARPS and method 1. The ≈2 Å-wide photospheric wings of the Na lines are still present, showing that the solar signature is not properly removed from this $h(\lambda)$ profile. A residual solar line of Ni I is visible at ≈5892.9 Å (Wallace et al. 2011).

Vidal-Madjar et al. (2010) observe the same type of solar residuals in the SOPHIE data (residual wings of the Na I doublet) and the explanation invoked is the Ring effect. The depth of solar Fraunhofer lines in scattered light is lower than in direct sunlight. This effect is known as the Ring effect (Grainer & Ring 1962) and is mainly induced by rotational Raman scattering (Vountas et al. 1998). The line filling-in for forward scattering (as experienced by the photons that interact with the Earth atmosphere and are scattered towards the eclipsed Moon) is about 2.1% and 3.8% of the continuum for single and multiple scattering, respectively, for the Ca II K line (Vountas et al. 1998). Kattawar et al. (1981) report a filling-in of 2.5% at 6301.5 Å for a Fe I line. Brinkmann (1968) calculates a filling-in of about 1.7 in the center to 1.9% in the wings for a hypothetical line at 4000 Å, underlying the continuous and smooth effect across the line profile, which is also measured by Pallamraju et al. (2000). Brinkmann (1968) reports observations showing a decrease of the filling-in with wavelength by a factor of 2 between 4383 and 6563 Å, and more recent measurements (Pallamraju et al. 2000, Fig. 3 therein) shows that the Ring effect decreases approximately linearly by a factor of ≈3 from 4285 to 6560 Å for a given line strength (normalized depth to continuum x width).

Several methods exist to correct for the Ring effect (Wagner et al. 2001). The simplest is that of Noxon et al. (1979), which consists of subtracting a small constant, close to 2%, from the spectrum. This was the solution applied in Vidal-Madjar et al. (2010) where a constant is empirically adjusted to remove the residual solar Na I lines (the constant was 4% and 0.6% of the continuum in the Na I region, for the deepest and the shallowest positions in the penumbra, respectively). We also correct this Ring effect in our data.

We observed that removing a Ring value $x_p$ from the shallower spectrum in the penumbra and $x_p > x_{sh}$ to the deepest only (all spectra were corrected from the instrumental response, so Noxon’s approach applies correctly). The Ring signature is thus, as expected, stronger in the deeper spectrum ($x_p > x_{sh}$), where collected photons have been more scattered in Earth atmosphere than photons collected in the shallower penumbra. In our empirical correction for the Ring effect, we therefore only apply a correction on the spectrum in the deepest positions in the penumbra. We consider empirical Ring corrections following: i) Noxon et al. (1979); ii) Noxon et al. (1979) except in deep telluric bands ($T < 0.5$) where the Ring effect is negligible because Raman-scattered photons are strongly absorbed (Sioris & Evans 2000); iii) a $\lambda^{-2}$ power law to mimic the chromatic dependance observed by Pallamraju et al. (2000) or Brinkmann (1968); iv) a $\lambda^{-2}$ power law subtracted except in deep telluric bands ($T < 0.5$); and v) a subtraction of the reciprocal of the spectrum (Johnston & McKenzie 1989) that mimics the Ring spectrum. Here again, the obtained Ring spectrum is not removed from deep telluric lines ($T < 0.5$).

We observe that removing $\approx1\%$ of the continuum at 5880 Å to the deepest spectrum of each pair reduces the solar residuals over the full altitude profile (Fig. 10) and slightly reduces the
Fig. 10. Altitude profile with HARPS and method 1 without Ring correction (upper panel) and different empirical Ring corrections. The amount of correction is 1% of the continuum at 5880 Å: i) Noxon et al. (1979); ii) Noxon et al. (1979) except in deep telluric bands (T < 0.5) where the Ring effect is negligible because Raman-scattered photons are strongly absorbed (Sioris & Evans 2000); iii) a λ^2 power law to mimic the chromatic dependence observed by Pallamraju et al. (2000) or Brinkmann (1968); iv) a λ^2 power law subtracted except in deep telluric bands (T < 0.5); and v) a subtraction of the reciprocal of the spectrum (Johnston & McKenzie 1989), which mimics the Ring spectrum. Here again, the obtained Ring spectrum is not removed from deep telluric lines (T < 0.5). The Na I doublet peaks at ≈5890 Å for all types of Ring corrections tested.

Na wings (Fig. 11). The correction also leads to the rise of the Na lines to altitude values of ≈80 km, a value in agreement with the literature (Plane 2003; Moussaoui et al. 2010). Nevertheless, the width of the terrestrial Na I peaks are observed to be ≈0.4 Å. This is larger than the ≈0.2 Å observed for the other telluric lines, but might be induced by the presence of the strong Na I line in the solar spectrum. The extraction process of h(λ) is then more disturbed in the case of the Na I lines, easily inducing a change in the width, particularly because the solar lines cannot be perfectly positioned in all spectra since these have been Doppler-shifted to have the telluric lines aligned. An additional effect is the limb-darkening effect that changes the shape of the solar Na I lines emitted by different size crescent above the Earth limb. This is also why the broad Na I stellar wings are not perfectly corrected in the presented extraction procedure, which only includes a low spectral resolution limb-darkening model. Finally, we also note that only the Na I lines are detected in Fig. 10, not the strong Mg I triplet at ≈5170 Å nor Hα, for example, produce a peak in the altitude profile. We therefore conclude that the terrestrial Na layer is detected.

Interestingly, García-Muñoz et al. (2012) point out that the lunar eclipse of 16 August 2008 occurred only four days after the maximum of the Perseid meteor shower. It is indeed known that meteor showers can temporarily increase the amount of sodium in the atmosphere by a factor up of 10 (Plane 2003; Moussaoui et al. 2010). This corroborates the detection of the sodium layer by Vidal-Madjar et al. (2010) in August 2008. Nevertheless, the Geminid meteor shower maximum occurs on December 13. It is an active meteor shower, with a particle density similar to that of the Perseids, that might have increased the sodium absorption during the eclipse of 21 December 2010. Nevertheless, our observations just show that the Na layer is indeed present, as during our first observations in August 2008. Since we have only one measurement, it is unfortunately not possible to detect any change of the atmospheric Na I content, either in 2008 or in 2010, and thus to confirm a link with any meteor shower.

It can be seen from Fig. 10 that the Ring correction is not homogeneous across the full spectral range: the Hα line remains undercorrected, while lines in the bluer part of the h(λ) profile are overcorrected. We therefore adopt the simplest Noxon

Fig. 11. Same as Fig. 10 but zoomed-in on the Na I doublet region of the altitude profile without Ring correction (upper panel) and different empirical Ring corrections.

See for example the IMO (International Meteor Organization) data at http://www.imo.net/live/geminids2012/ and http://www.imo.net/live/perseids2012/
final altitude profile obtained with HARPS, method 1, and with a Noxon correction for the Ring effect, except in the deep telluric lines (Sioris & Evans 2000). A 10 Å bin is superimposed in light-blue over the full-resolution profile; 30 and 100 Å bins are shown too, shifted upwards for clarity. The Na I peaks are visible near 5900 Å. Oxygen and water-vapour absorption spectra at arbitrary scale are shown. The altitude profile has been shifted to have an altitude of 23.8 km in the [4520–4540] Å domain, as predicted by Ehrenreich et al. (2006) (dots and dashes in green – dashes to improve the visibility of the curve around 6000 Å).

The model is flatter than the observed profile, which peaks at about 35 km near 6000 Å, about 8 km above the model. This difference might be a refraction effect that amplifies the observed profile, as with method 3, although this effect is weaker here because we use only penumbra spectra. If the profile is calculated only with the two pairs [98; 204] and [125; 232] (Table 3), leaving out the spectrum from the deepest penumbra at only 66 arcsec from the umbra, the observed profile is indeed flatter (but noisier): it still peaks at 35 km, higher that the altitude expected from the model, but the lowest altitude at 6900 Å becomes ≈17 km instead of 12.

We note that our observations of the 2008 eclipse agrees better with the model (Vidal-Madjar et al. 2010, Fig. 9 therein) although SOPHIE fibers were between ≈100 and 250 arcsec from the umbra edge, as for HARPS. The additional bins in Fig. 12 show that the B-band is barely detectable in the 30 Å bin, while the broad O$_3$ Chappuis band and Rayleigh slope in the blue remain visible in the 100 Å bin. Figure 13 shows zooms in the Na I lines and the O$_2$ γ and B band regions. Oxygen shows up very clearly, with peaks reaching $h = 35–40$ km. Some water-vapour peaks are visible but weak, which is not surprising because of the high altitude at which they are detected and also because of the lower strength of the water-vapour absorption in the HARPS wavelength range compared with $\lambda > 7000$ Å. We detect neither Li (6708 Å) nor Ca II (Hunten 1967; Plane 2003).

With UVES, the coordinates of the telescope indicate that the telescope unfortunately did not move in the penumbra between the exposures in order to record spectra at 90 and 180 arcsec from the umbra edge as expected, but instead stayed ≈200 arcsec from the umbra (Table 5). The different recorded spectra are very similar and the result from Eq. (1) is noisy, especially in the blue. Residuals from spectral orders are also visible above 7000 Å. There is nevertheless a spectrum taken in UVES DIC2 configuration, while the telescope was thought to be in the umbra, but was too close to the Moon edge and left the moon about 20 s after the exposure started. The exposure was then stopped, but the telescope coordinates indicate that the telescope was in fact in the penumbra. The exposure time for that unexpected exposure is only about 21 and 38% of what was required for the BLUE and RED exposures, respectively. The altitude profile obtained with UVES is shown in Fig. 14. The overall shape agrees better with the model of Ehrenreich et al. (2006), but the altitude observed in the UV is far higher than that of the model. Moreover, we had to shift the DIC1 BLUE profile by –110 km to connect it to the DIC2 BLUE profile. The DIC2 RED profile has also to be shifted by 35 km to be connected to the altitude obtained for the DIC1 RED profile. The oxygen bands are barely visible and the water-vapour bands appears in absorption. We did not consider any Ring correction for this noisy profile. Note also that the model of Ehrenreich et al. (2006) shown in the figures of this paper does not include water vapour.

### 7.2. Results from Eq. (3) (method 2)

The HARPS spectra are now used with Eq. (3) to calculate $h$ from only one penumbra spectrum. The eclipse spectra are corrected for limb-darkening and Ring effect as for method 1. When the profile is calculated with the spectra in Eq. (3) aligned on the telluric lines, the solar lines become consequently slightly misaligned, which generates noise in the profile (Fig. 15 upper panel). We therefore build a composite profile where all lines – telluric and solar – are aligned. The composite uses two different profiles, one aligned on the telluric lines and a second aligned on the solar line. In the first profile, every misaligned solar line is recognized with the help of a synthetic G2 spectrum and replaced by its aligned residual taken from the second profile. Some solar lines are missing in the G2 spectrum in the most crowded telluric bands, therefore some residual noise due
Fig. 13. Zooms on the HARPS final altitude profile from method 1 (Fig. 12) with a Noxon correction for the Ring effect, except in the deep telluric lines (Sioris & Evans 2000). Oxygen and water vapour absorption spectra at arbitrary scale are shown. Oxygen shows up very clearly. Water vapour is barely visible around 6500 Å above 25 km and weak lines are visible in the higher Na I D1 D2 region. Note that our Noxon correction does not completely remove the wings of the Na I solar lines. The wings disappear with a stronger correction, but the two Na I peaks then reach an altitude well above 100 km which is not realistic.

Fig. 14. Final altitude profile obtained with UVES and method 1. No Ring correction is applied. A 10 Å bin is superimposed in light-blue on the full-resolution profile. Reference oxygen and water-vapour absorption spectra obtained with UVES are shown at arbitrary scale. The altitude profile has been shifted to have an altitude of 23.8 km in the [4520–4540] Å domain, as predicted by Ehrenreich et al. (2006) (green dashed line, no water vapour in the model).

Fig. 15. Altitude profile with HARPS and Eq. (3) (method 2). Only the spectrum of the deepest penumbra, taken at 66 arcsec from the umbra, is used here (Table 3). Shallower penumbra spectra give similar but noisier profiles. A 10 Å bin is superimposed in light-blue on the full-resolution profiles. The upper panel shows the profile obtained with the HARPS spectra aligned on the telluric lines. Solar lines are consequently misaligned and generate noise in the profile. The lower panel shows a composite profile showing the profile calculated with the spectra aligned on the telluric lines, except when a solar line is present, where the profile from spectra aligned on the solar lines is used. Oxygen and water-vapour absorption spectra at arbitrary scale are shown. The green dashed line is the model of Ehrenreich et al. (2006).
spectra of 0.5% of the continuum at 5880 Å. When we subtract a Ring effect of 1% as we did for HARPS, the profile does not change, except from the oxygen A and B bands which peak at 150 km.

Qualitatively speaking, the overall shape of the profile from 3000 to 7000 Å is in acceptable agreement with the model, with the ozone Chappuis bump at 6000 Å and a Rayleigh increase of $h$ in the blue and near UV. The DIC2 BLUE altitude is set to $h = 23.8$ km in the [4520–4540] Å domain, as predicted by Ehrenreich et al. (2006). The other parts of the profile need to be shifted by about ±6 km to be properly continuously connected to the DIC2 BLUE profile.

7.3. Results from the umbra edge radiance profile (method 3)

With method 3, we make use of all available umbra and penumbra spectra. The penumbra spectra are corrected from the limb-darkening in the same way as for method 1 and 2. For each sampled wavelength in the HARPS spectra, we fit a sigmoid curve (Eq. (4)) through the eight available measured points (position, magnitude) in the umbra and deep penumbra region (Table 3). An example of the obtained fit is shown in Fig. 1. We now need to define the radius of the umbra edge $r_e$ from which we build the Earth atmosphere thickness $h(\lambda)$ simply given by

$$h(\lambda) = r_e(\lambda) \times \frac{r_u}{r_u} + cte,$$  \hspace{1cm} (9)

where $r_e$ is expressed in arcmin, $r_u = 42.7$ arcmin is the umbra radius from the ephemeris, and $r_u = 6371$ km is the Earth radius. The constant $cte$ is set to give $h = 23.8$ km at [4520–4540] Å.

As explained in Sect. 3, the inflection point abscissa $a_2$ of the fit is not the best estimate of $r_e$ (in our context of Earth transit analysis, at least). To explore the impact of $r_e$ on $h(\lambda)$, we write $r_e$ such that

$$\zeta(r_e) = a_0 + c \times a_1.$$  \hspace{1cm} (10)

For the inflection point, the coefficient $c$ in front of half-amplitude $a_1$ of the tanh function is $c = 0$ and $\zeta(a2) = a_0$, Positive values of $c$ lead to positions on the penumbra side of the inflection point. Figure 19 shows a set of altitude profiles built for different positions across the umbra edge, with $-0.6 < c < 0.9$ as shown in Fig. 20. The profiles versus $c$ change substantially: for $c = -0.6$, the profile is built from data on the umbra side of the inflection point, and the bump from the ozone Chappuis band is almost invisible. The mean negative slope of the profile also underlines the effect of refraction that shrinks the Earth umbra at redder wavelengths. This effect decreases when $c$ increases to positive values, with the profiles built from data on the penumbra side of the inflection point. The broad Chappuis band is detected. We finally define the umbra radius such as $\zeta(r_e) = a_0 + 0.6 \times a_1$ ($c = 0.6$). For this value, the noise in the altitude profile is close to minimum, and the bias from shallow umbra (that is, the mean negative slope of $h(\lambda)$) is reduced. With this definition, Fig. 20 puts the umbra edge at...
about 1 arcmin in the penumbra side with respect to the inflection point, and about one magnitude fainter than the penumbra at 4 arcmin from the inflection point. This choice is consistent with our reasoning developed Sect. 3.

The result with HARPS and method 3 is shown in Figs. 21 and 22. Wide and narrow features of the Earth atmosphere are visible (Rayleigh, ozone Chappuis band, oxygen $\gamma$ and $B$-bands). Water vapour is not detected, suggesting it is not present above 12 km. Compared with the profile obtained with method 1 (Fig. 12), the profile with method 3 shows a stronger negative slope from blue to red, leading to an altitude range about ≈3.3 times larger than with method 1. We attribute this effect to the fact that method 3 makes use of umbra spectra. The light in the umbra is reddened by Rayleigh scattering in the deep Earth atmospheric layers and refracted towards the umbra center. Therefore the umbra edge in red light is more refracted towards the umbra center than at blue wavelengths. The umbra radius (Earth radius on the Moon) is thus smaller in the red than in the blue.

![Fig. 18. Zooms on the oxygen $A$ and $B$-band regions of the UVES profil shown in Fig. 17 (method 2). An oxygen absorption spectrum at arbitrary scale is shown.](image1)

![Fig. 19. Altitude profiles obtained with HARPS and method 3 for different positions across the umbra edge, given by parameter $c$ in Eq. (10) and shown in Fig. 20.](image2)

![Fig. 20. Positions across the umbra edge used to build the altitude profiles shown in Fig. 19.](image3)
Fig. 21. Altitude profile obtained with HARPS and method 3. The left vertical axis is the measured altitude, set to 23.8 km at [4520–4540] Å. The right vertical axis is the corrected altitude, if one considers the lowest region of $h$ close to altitude 12 km as in Fig. 12 and again $h = 23.8$ km at [4520–4540] Å. The horizontal dotted line represents the altitude 23.8 km. The light-blue line is a 10 Å bin superimposed on the full-resolution profile. Oxygen and water-vapour absorption spectra at arbitrary scale are shown.

Fig. 22. Zooms on the HARPS altitude profile from method 3 shown in Fig. 21. The left vertical axis is the measured altitude, set to 23.8 km at [4520–4540] Å. The right vertical axis is the corrected altitude, if one considers the lowest region of $h$ close to altitude 12 km as in Fig. 12 and again $h = 23.8$ km at [4520–4540] Å. Oxygen and water-vapour absorption spectra at arbitrary scale are shown. Water vapour is not detected above 16 km, suggesting that the amount of water vapour is too low to absorb enough to be visible at this altitude. The sodium layer Na I is not detected.

Fig. 23. Measured magnitude across the umbra edge with UVES at 10000 Å. The horizontal error bars are 20 arcsec long and represent the typical pointing error of the telescope. Vertically, the $2\sigma$ error bars are the magnitude errors given by the UVES pipeline and the evaluated error in the local Moon albedo. The solid line is the model from Eq. (4) fitted through the data with parameter $a_3$ set to the mean value of $a_3$ found for the HARPS data. The vertical dotted line marks the edge of the umbra following our definition.

blue, due to refraction and Rayleigh scattering. This effect amplifies the measured altitude range across the full visible spectrum. To correct for this effect, the right vertical axis of Fig. 21 is calibrated with the method 1 result, by setting the altitude for two different points, that is, the lowest region of $h$ at altitude 12 km and $h = 23.8$ km at [4520–4540] Å.
We process the UVES data in the same way. Nevertheless, since we have less observations points with UVES than with HARPS, it is not possible to keep four free parameters for the fitting function, the sigmoid $\zeta$. We have to fix the $a_3$ parameter to the mean value obtained with HARPS. The parameter $a_5$ describes the steepness of the fit near the inflection point and is quite stable for HARPS at visible wavelengths: in the $[6500–6900]$ Å range, its average value is $\mu = 9.88 \times 10^{-3}$ with an RMS of $\sigma = 2.2 \times 10^{-4}$. We fix $a_3$ to that mean value for UVES. An example of the fit through the UVES observations at 10 000 Å is shown in Fig. 23. Figure 24 shows the altitude profile obtained with UVES, showing the same features as for HARPS, with clear oxygen $A$ and $B$ bands, and water-vapour bands up to 10 000 Å. As with the HARPS profile (Fig. 21), the profile obtained with UVES displays a strong global negative slope. Here the profile is $\approx 4.5$ times larger than with method 1. The right axis in Fig. 24 is calibrated considering that the lowest region of $h$ is close to altitude 0 km and again that $h = 23.8$ km at $[4520–4540]$ Å. The factor of 4.5 is larger than with HARPS ($\approx 3.3$) maybe because the slit positions with UVES are deeper in the umbra than with HARPS (see Tables 5 and 3).

In the blue ($\lambda \leq \approx 4300$ Å), the signal in the umbra spectra is weak and the altitude profile becomes noisy and unexpectedly decreases. Oxygen and water-vapour absorption spectra at arbitrary scale are shown.

The Figs. 25 and 26 show zooms in the UVES full profile shown in Fig. 24. In Fig. 25, the three oxygen bands are clearly detected. Note that the core of the oxygen line for the $A$-band could not be calculated because the signal in the line core is too weak. The sodium layer is not detected, and no water vapour appears above 19 km near the sodium lines. At $\lambda > 7000$ Å in Fig. 26, water vapour appears very well, even at an altitude higher than 20 km, because the water-vapour absorption bands become stronger in these longer wavelengths. Water vapour indeed presents a vertical distribution in the Earth atmosphere and is thus also present at higher altitudes but with lower volume densities. The altitude at which it is detected (where an optical thickness of about 1 is reached for a grazing line of sight) is of course higher in the stronger bands.

It is worth noting that the residuals of the Na I lines are very similar apart from the noise for HARPS and UVES (Figs. 22 and 25 respectively). This is expected because HARPS and UVES observed roughly the same solar crescents and thus experienced the same Doppler shift of the solar lines of the crescents that induced these residuals in the altitude profile. Note also that no correction of the Ring effect is implemented in method 3, either for HARPS or UVES. All spectra are indeed used here, all at different depths in the penumbra and umbra. A simple empirical approach cannot reasonably be considered. A physical model of the Ring effect is much needed, taking into account the path length through the Earth atmosphere for the different positions observed in the umbra and penumbra.

### 7.4 Possibilities with a future giant telescope

We analyze how our results can be extrapolated to what a future ground-based giant telescope might be able to detect in the visible transmission spectrum of an Earth-like exoplanet observed in transit. We use a full model of the future E-ELT, a 39 m telescope. The focal instrument has the same throughput, pixel sampling, and detector characteristics as the EPICS instruments. The model takes into account the photon noise from the star, the thermal and readout detector noises, the zodiacal noise, and...
the absorption of the local atmosphere above the telescope (see Hedelt et al. 2013 for a detailed description of the model).

We define a set of ten filters i) to sample the Chappuis band and the Rayleigh continuum; and ii) to isolate the most interesting narrow features in the profile shown in Fig. 24, that is, the oxygen A and B bands, and the water vapour around 9500 Å. The low spectral resolution 10 Å bin in this figure shows that the oxygen A-band peaks about 20 km above the lowest altitude around 10 200 Å. The Earth radius is thus 0.3% larger and the transit 0.6% deeper through a filter that isolates the oxygen A-band. The Earth transit depth is 8.3 × 10−5, and the transit variation at that spectral resolution for the O2 band represents 7.5 × 10−7 of the stellar flux.

According to Porto de Mello et al. (2006), there are 33 solar-type stars within 10 pc, 13 of which are reasonably similar to the Sun in terms mass, age, metallicity, and evolutionary status. Considering that the transit probability of an Earth twin in front of its star is about 1%, we understand that the probability of detection is low, even if all stars have a planet in their habitable zone. The Darwin All Sky Star Catalogue (Kaltenegger et al. 2010) lists 878 single FGK stars within 30 pc, a number fully consistent with the 33 solar-type stars numbered by Porto de Mello et al. (2006) for a 27 times smaller volume. Nevertheless, although the probability of transit detection significantly increases with 878 targets, the flux for a star at 30 pc will be 9 times fainter than at 10 pc meaning that 9 times more transits will be necessary to reach the same S/N as for a target at 10 pc.

We consider an earth at 10 pc transiting a G2V star observed during a full night of 8 h (an Earth-like 13 h single transit being longer than the night). The simulation assumes that the atmosphere above the telescope is perfectly stable. The simulation results are given in Table 7 and shown in Fig. 27. The result shows that transit photometry through the defined filters allows in principle the detection of the O2 A-band with a detection level of ≈2.3 σ. The oxygen B and water-vapour bands will be more difficult to detect and will require more than one transit to reach a detection level >2σ. This is also true for the ozone Chappuis band, which is blended with the Rayleigh scattering.

It is encouraging to see that the E-ELT will beat the photon noise in only one single transit to identify oxygen in the visible range on a terrestrial planet transiting a solar-type star at 10 pc. But it will be extremely difficult, at least at low spectral resolution, to detect the 7.5 × 10−7 flux variation in the O2 band through the slightly fluctuating atmosphere above the telescope.

We considered broadband and narrow-band photometry, with a spectral resolution of up to ≈170. But it is worth noting that at a much higher spectral resolution (of the order of ≈104), the telluric lines become distinct from those of an exoplanet as soon as its radial velocity is sufficiently different from the BERV. Under these conditions, ground-based detection at high spectral resolution of O2 or H2O in an exoplanet atmosphere becomes easier, especially by cross-correlating the transit spectrum and an O2 or H2O spectrum, respectively (Vidal-Madjar et al. 2010; Snellen et al. 2013; Rodler & López-Morales 2014).

8. Summary and conclusion

We have described the analysis of the observations of a lunar eclipse used as a proxy to observe Earth in transit. The results fully confirm those obtained with SOPHIE and the observation of the August 2008 eclipse (Vidal-Madjar et al. 2010) and extend the observed h(λ) profile towards the near infrared thanks to the UVES data. They agree well with the models (Ehrenreich et al. 2006; Kaltenegger & Traub 2009; Snellen et al. 2013; Bétrémieux & Kaltenegger 2013). The Rayleigh increase in the blue is visible. Biogenic oxygen and ozone are also well visible.

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**Table 7.** Transit of an Earth twin at 10 pc observed for 8 h by the E-ELT, at low spectral resolution and assuming no atmospheric perturbations.

<table>
<thead>
<tr>
<th>Filter</th>
<th>λ range (Å)</th>
<th>h (km)</th>
<th>S/N</th>
<th>δ h ± 1-σ error (km)</th>
</tr>
</thead>
<tbody>
<tr>
<td>O3 + Rayl. 1</td>
<td>5000–5500</td>
<td>19.9</td>
<td>11.3</td>
<td>17.2 ± 3.0</td>
</tr>
<tr>
<td>O3 + Rayl. 2</td>
<td>5500–6100</td>
<td>19.2</td>
<td>12.3</td>
<td>16.5 ± 2.9</td>
</tr>
<tr>
<td>O3 + Rayl. 3</td>
<td>6300–6800</td>
<td>15.0</td>
<td>8.6</td>
<td>12.3 ± 2.9</td>
</tr>
<tr>
<td>O2–B</td>
<td>8685–9005</td>
<td>17.6</td>
<td>2.5</td>
<td>14.8 ± 6.4</td>
</tr>
<tr>
<td>Rayl. 4</td>
<td>7360–7560</td>
<td>8.9</td>
<td>3.1</td>
<td>6.2 ± 3.2</td>
</tr>
<tr>
<td>O2–A</td>
<td>7590–7650</td>
<td>23.2</td>
<td>3.7</td>
<td>20.5 ± 5.9</td>
</tr>
<tr>
<td>Rayl. 5</td>
<td>7750–8100</td>
<td>7.2</td>
<td>3.3</td>
<td>4.5 ± 2.9</td>
</tr>
<tr>
<td>Rayl. 6</td>
<td>8450–8800</td>
<td>5.3</td>
<td>2.3</td>
<td>2.6 ± 2.8</td>
</tr>
<tr>
<td>Water vapour</td>
<td>9300–9600</td>
<td>8.7</td>
<td>3.1</td>
<td>6.0 ± 3.2</td>
</tr>
<tr>
<td>Window</td>
<td>10 100–10 400</td>
<td>2.7</td>
<td>1.0</td>
<td>0 ± 2.6</td>
</tr>
</tbody>
</table>

**Notes.** The S/N is calculated through ten different filters. The last filter “Window” is for the atmospheric window. The filter widths range from 40 Å for the O2 B to 600 Å for one of the filter sampling the Chappuis band. The values of h are taken from the 10 Å bin of the UVES profile (Fig. 24). The value δh is the altitude difference to the atmospheric window measured by the E-ELT.
in the atmosphere altitude profiles, and are therefore relevant detectable biosignatures to look for during transits of Earth-like exoplanets in the [4000–10 500] Å range. The oxygen A and B bands show up clearly with HARPS or UVES.

Water vapour is well detected at $\lambda > 8000$ Å with UVES because water-vapour absorption is stronger at these wavelengths. Therefore even low densities of water vapour at these altitudes are detected. Water vapour is seen at an altitude of up to 20 km around 9500 Å. Moreover, Rayleigh scattering and ozone absorption are essentially absent above 8000 Å, therefore we are also able to probe deeper layers in the Earth atmosphere where low-altitude water vapour is also present at higher densities. In HARPS data at $\lambda < 7000$ Å water vapour appears above 25 km with method 1 but remains below 25 km with method 2 and below 12 km with method 3, because water-vapour absorption is weaker in the visible range.

The results from UVES are nevertheless less reliable than those of HARPS, because the PWV was not stable during the beginning of the night when the calibration spectra were recorded on the full-Moon before the eclipse, which compromised the quality of the eclipse observation. Although we were able to recover the water-vapour content in the calibration spectra a posteriori, the results for the detection of water vapour in the altitude profiles with UVES are not coherent between method 1, 2 and 3. This underlines the difficulties of these observations which were made through the local atmosphere above the telescope, while our goal was to measure atmospheric features at a planetary scale. Lunar eclipse observations done from space, either at low or high spectral resolution, would not suffer from the telluric pollution, with the additional benefit of an access to UV and the prominent Hartley band of ozone.

Another bias in the recovering of the Earth atmosphere profile from a lunar eclipse is the effect of refraction in method 3 that makes use of refracted light from the umbra. We have shown that this effect can be partially corrected with the results from method 1, but the profiles – either from HARPS or UVES – still show a residual negative slope with respect to the profile from method 1 or 2.

Finally, these results provide input for the preparation of future observations with the next generation of giant telescopes. We showed that the E-ELT observing in the visible range at low spectral resolution and in the absence of atmospheric perturbations is in principle able to detect the O$_2$ A-band in the atmosphere of a transiting Earth twin. It will be extremely challenging in practice through the atmosphere. If we overcome this difficulty, especially with high spectral resolution spectroscopy, the O$_2$ signature may then be increasing from year to year (from transit to transit), as will the enthusiasm of the observers.

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