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To cite this version:
Sofiane Djebbarri, Jean-Frederic Charpentier, Franck Scuiller, Mohamed Benbouzid. Design and Performance Analysis of Double Stator Axial Flux PM Generator for Rim Driven Marine Current Turbines. IEEE Journal of Oceanic Engineering, Institute of Electrical and Electronics Engineers, 2015, PP (99), 8pp. <10.1109/JOE.2015.2407691>. <hal-01166435>

HAL Id: hal-01166435
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Design and Performance Analysis of Double Stator Axial Flux PM Generator for Rim Driven Marine Current Turbines

Sofiane Djebbari, Jean Frédéric Charpentier, Member, IEEE, Franck Scuiller and Mohamed Benbouzid, Senior Member, IEEE

Abstract—This paper deals with the design and performance analysis of double stator axial flux permanent magnet generators for rim-driven marine current turbines (MCT). Indeed for submarine applications, drive train reliability is a key feature to reduce maintenance requirements. Rim-driven direct-drive multi-stator generators can therefore be a very interesting solution to improve this reliability. In this context, the presented work focus on the design of a double-stator axial flux permanent magnets (PM) generator as a rim-driven direct-drive multi-stator generator. The paper details the models, specifications and an optimization procedure that allow to preliminary design these kind of generators for rim-driven marine turbines. Thereafter, validations with finite elements computations and performance analysis considering particular design of rim driven generators are presented. The obtained results highlight some designs issues of PM generators for rim driven marine turbines. In order to assess the effectiveness of the double stator axial flux PM generator, a comparison with a designed surface mounted radial flux PM generator for rim marine turbines is carried out. The comparison highlights that the double stator axial flux generator presents a better cooling and a reduced active parts cost and mass than the radial flux PM generator.

Index Terms—Marine current turbines, rim-driven, permanent magnets machine, axial flux generators, electromagnetic model, thermal model, immersed gap.
I. INTRODUCTION

Marine renewable energies constitute a very interesting alternative to be combined to other renewable energy sources. Indeed, tidal energy is predictable many years in advance [1-2]. The predictability of tidal currents makes the electrical energy management easier than all other renewable energies. This energy resource allows to limit the visual exposure, the acoustic disturbances and to reduce the environment impacts. However due to the sea immersion, marine tidal power generation requires ultra reliable, salt and waterproof technologies [2-3].

Marine currents kinetic energy can be harnessed using similar technologies as those developed to extract wind energy. This is particularly the case of the firsts developed marine current turbines (MCTs) [4]. Because of tides low speed and to avoid blades cavitations, the turbine rotational speed is typically below 50 rpm. If conventional industrial generators are used, their rated speeds are typically between 1000 and 3000 rpm and multistage gearboxes must be used [5]. Such gearboxes lead to reduce the drive train efficiency and demand high maintenance. This point is particularly penalizing for offshore and underwater technologies. According to literature [6], to make the tidal current energy conversion economically interesting, the MCT should have an approximately 30 years lifespan with maintenance inspections every 5 years. Therefore, MCTs should be highly efficient and reliable.

Direct-drive permanent magnet generators appear as a solution that can fulfill these specific requirements. In direct-drive MCTs, the electrical generator is directly linked to the turbine shaft. This leads to eliminate gearbox and requires the use of low speed generators [7]. In this context, maintenance requirements are significantly reduced and the drive train efficiency is improved. However, the generator active parts mass and cost are expected to be higher if compared with more conventional geared and high speed industrial generators, considering the same rated power.
Regarding MCTs design, with rim-driven topology the generator is placed on the turbine periphery and seems more favorable in term of hydrodynamic behavior than a POD system, where the generator is inserted in a nacelle [8]. Referring to [8], in a rim driven system, the electrical machine volume is less disturbing the water flow. Furthermore, rim-driven technologies naturally imply direct-driven generators and the large generator diameter ensures a reduced active parts mass (in a rim driven system, the internal generator diameter is slightly higher than the turbine blade diameter). As example of industrial rim driven MCT device [4], OpenHydro is probably the most mature technology (fig. 1c). This rim driven turbine has 16 m diameter and 500 kW rated power. It should be pointed-out that the design of such a generator is quite unusual as the active parts are located at the blades periphery (Fig. 1a). Moreover, in previous works of our team a rim-driven MCT demonstrator using a radial flux permanent magnets (RFPM) generator has been designed and tested at the French Naval Academy Research Institute, Brest, France (Fig. 1b) [9-10], the tested rim driven technology has shown an encouraging results.

The presented work has been initiated in [11] and aims to assess the potential of a double stator axial flux permanent magnets (AFPM) generator as a multi-stator generator for a rim-driven MCT technology. Indeed, multi-stator axial flux machines can be interesting solutions for direct-drive turbines. According to literature overview, some MCT and some wind turbines involve axial flux generator technologies [11-12]. C-GEN technology, developed by “Aquamarine Power” company, uses a solution that integrates an air-cored axial generator characterized by a zero cogging torque and high modularity possibilities [13]. In [14], a contra-rotating tidal turbine (CoRMat project) is developed by the University of Strathclyde (Scotland). It includes an axial flux permanent magnets generator. Clean Current Ltd company have also developed marine current turbines based on the use of axial flux generators [15].
In [16], a modular axial flux permanent magnets generator is proposed for wind turbine applications. In comparison with radial flux machines, axial flux machines could enable a better compactness, a better efficiency [17], and high-speed operation ability [18]. In [19], axial and radial flux permanent magnets machines are compared. According to this study, AFPM machines are suitable if the active length is very short and the pole number is high. Because of high diameter, rim-driven generators are characterized by a
very short active length and high pole number. However in AFPM machines the high electromagnetic axial forces between stator and rotor generates a mechanical stress that can make the manufacturing process particularly hard [20]. In order to reduce these axial forces, multi-stator AFPM machines, ironless stator AFPM machines [21] can be considered. It can also be noticed that multi-stator AFPM machines can be more reliable as, if a fault occurs on one of the stators, the generator can operate at a fraction of the rated power using the remaining healthy stators. Regarding to the presented considerations the design of a double stator AFPM generator for a rim-driven MCT is proposed in this paper.

In this paper, a brief discussion about generator/turbine association is given in section I. In section II, the design specifications of an industrial MCT and the geometry of the proposed double stator axial flux permanent magnets machine are described. This set of specifications will be used to perform the design of a double stator AFPM generator for a rim driven MCT. In section III, the double stator AFPM generator electromagnetic design model is described. It consists of a partially inversed electromagnetic model developed for high diameter and high poles number axial flux machines. In section IV, a lumped parameter thermal model of the generator is established considering particularities related to gap immersion. In section V, the models are associated and the constraints are defined in order to formulate a constrained optimization design problem. This problem is solved considering typical MCT specifications. In section VI, the optimization approach will be used to determine a generator geometry that minimizes the active parts material costs under constraints. Both electromagnetic and thermal finite elements simulations are then performed for validation purposes. In addition, a thermal model sensitivity study has been carried-out to validate the immersed generator thermal modeling. In the last part of this paper (section VII), a classical radial flux surface mounted PM generator is designed using similar models and methodology for the same MCT specifications. This design is then used to compare the RFPM and double stator AFPM generators for rim-driven MCTs.

II. DESIGN FEATURES OF RIM DRIVEN PM MACHINES

A. General design specifications

To carry out a realistic design study, the used specifications are inspired from the Seaflow turbine which is an industrial MCT device. Seaflow has been installed in the north Devon coast of England since 2003 [22]. With 11 m diameter and rotating at 15 rpm for a 2.5 m/sec tidal current velocity developing 300kW rated power. These turbine characteristics are used, in this paper, for the design of PM generators
in a rim-driven context. The configuration of rim-driven system implies that the generator internal radius, the mechanical torque, and the electrical generator rated speed, are constrained by the blade geometrical characteristics and the turbine operating point. If the mechanical and viscous losses are neglected, the electromagnetic torque \( T_{EM} \) of the generator can be considered equal to the turbine mechanical torque \( Q \) as given by relation (1). According to these considerations and to classical design choices of PM generators the given data of table 1 are used for all the studied cases.

\[
\langle T_{EM} \rangle = Q 
\]  

(1)

**Table 1. Design Specifications Set.**

<table>
<thead>
<tr>
<th>Specification</th>
<th>Value</th>
</tr>
</thead>
<tbody>
<tr>
<td>Turbine radius</td>
<td>( R_0 ) 5.5 m</td>
</tr>
<tr>
<td>Turbine torque</td>
<td>( Q ) 191 kNm</td>
</tr>
<tr>
<td>Turbine rated speed</td>
<td>( N ) 15 rpm</td>
</tr>
<tr>
<td>Tidal current velocity</td>
<td>( v ) 2.5 m/s</td>
</tr>
<tr>
<td>Magnet pole-arc to pole-pitch ratio</td>
<td>( \beta_m ) 0.66</td>
</tr>
<tr>
<td>Slot fill factor</td>
<td>( k_f ) 0.65</td>
</tr>
<tr>
<td>Winding coefficient given at the first harmonic</td>
<td>( k_{bl} ) 1</td>
</tr>
<tr>
<td>Electrical angle between phase electromotive force and phase current</td>
<td>( \psi ) 0 rad</td>
</tr>
<tr>
<td>Generator phases number</td>
<td>( m ) 3</td>
</tr>
<tr>
<td>Slot number per pole per phase</td>
<td>( S_{pp} ) 1</td>
</tr>
<tr>
<td>Required generator electrical efficiency</td>
<td>( \eta_{elecmin} ) 0.9</td>
</tr>
<tr>
<td>Maximum allowable temperature in slots</td>
<td>( T_{max} ) 100 °C</td>
</tr>
<tr>
<td>Sea water temperature (ambient condition)</td>
<td>( T_{water} ) 30 °C</td>
</tr>
</tbody>
</table>

In order to evaluate the active parts costs and losses, the set specifications are completed by defining the characteristics of the used active parts materials. The data related to the used active parts materials are then given in Table 2. As magnets materials N\(_d\)FeB magnets are considered for their high energy density, their
high intrinsic coercive field ($H_{cj} > 10^6$ A/m), their high operating temperature, and a low loss of the residual induction (less than 2% per 10 years [23]), these characteristics makes them suitable to enhance generators reliability particularly for marine turbines where high reliable components are necessary.

### Table 2. Active Parts Material Properties.

<table>
<thead>
<tr>
<th>Magnets (NdFeB) [23]</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Residual flux density</td>
<td>$B_r$</td>
</tr>
<tr>
<td>Intrinsic field coercivity</td>
<td>$H_{cj}$</td>
</tr>
<tr>
<td>Operating temperature</td>
<td>-</td>
</tr>
<tr>
<td>Relative permeability</td>
<td>$\mu_{rm}$</td>
</tr>
<tr>
<td>Density</td>
<td>$\rho_{magnet}$</td>
</tr>
<tr>
<td>Price [24]</td>
<td>$C_{magnet}$</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Standard FeSi iron sheets [25]</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Operating frequency</td>
<td>$f_{elec}$</td>
</tr>
<tr>
<td>Maximum flux density value where saturation appears</td>
<td>$B_{sat}$</td>
</tr>
<tr>
<td>Iron sheets thickness</td>
<td>-</td>
</tr>
<tr>
<td>Specific iron losses at 50 Hz</td>
<td>$P_{Fe0}$</td>
</tr>
<tr>
<td>Relative permeability</td>
<td>-</td>
</tr>
<tr>
<td>Thermal conductivity</td>
<td>$\lambda_{iron}$</td>
</tr>
<tr>
<td>Density [26]</td>
<td>$\rho_{FeSi}$</td>
</tr>
<tr>
<td>Price [27]</td>
<td>$C_{iron}$</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Copper at 20°C</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Electric resistivity</td>
<td>$\rho_{Cu}$</td>
</tr>
<tr>
<td>Copper equivalent thermal conductivity</td>
<td>$\lambda_{Copper}$</td>
</tr>
<tr>
<td>Density</td>
<td>$\rho_{copper}$</td>
</tr>
<tr>
<td>Price [24]</td>
<td>$C_{copper}$</td>
</tr>
</tbody>
</table>

**B. Double stator AFPM description**
In order to assess the potential of multi stators machines, a double stator AFPM machine is considered. This machine has two discs (stators) that support the windings (Fig. 3). The rotor magnets are mechanically linked to a rim which surrounds the turbine blades. The rotor and the stator surfaces are considered to be covered by a layer of insulating material in order to separate the active parts from seawater (details of the constitution of the stators and rotor are given in the section III and section IV). To reduce the drag on the whole structure, the stators are inserted in a hydrodynamic shaped hull.

![Fig. 3. 3D view of the double stator AFPM machine (a), 3D sketch of the double stator AFPM machine under a pole pairs width (b).](image)

**III. ELECTROMAGNETIC MODELING**

**A. Geometrical parameters calculation of the double stator AFPM machine**

The electromagnetic topology of an axial flux generator is intrinsically 3D, which makes the electromagnetic modeling more complex. In this paper a simpler approach is considered, where the double stator AFPM generator is assumed to electromagnetically behave as the corresponding linear generator defined at the mean radius (this development is illustrated by Fig. 4). Thereby calculations are done considering the geometry average radius \( R_m \) as shown in Fig. 3b. This simplification is commonly used for the modeling of AFPM generators. In the case of rim driven MCT, this assumption on the geometry is particularly realistic because of the very large value of the generator internal diameter (turbine diameter
$D = 2R_0$ exceeds 10 m for high power MCTs turbines) and because of the large number of poles that characterizes the low speed direct drive generators. Figure 4 illustrates the considered AFPM generator geometry with the corresponding geometrical dimensions defined at the mean radius.

![Diagram](image)

Fig. 4. 2D section of the corresponding linear machine at mean radius: $R_e$, $R_i$, $\beta_t$, and $\beta_m$ are respectively outer and inner radii, teeth pitch ratio, and magnet to pole pitch ratio, $Z_{hm}$, $Z_g$, $Z_{hs}$, $Z_Y$ are respectively the magnet height, air gap height, slot height and stator yoke thickness.

The other geometrical parameters presented in Fig. 4 can be established by simple geometrical relations, these parameters and simple relations are given in table 3.

**Table 3. Simple Geometry Parameters Deduced by Basic Geometrical Relations.**

<table>
<thead>
<tr>
<th>Parameter</th>
<th>Formula</th>
</tr>
</thead>
<tbody>
<tr>
<td>Inner radius</td>
<td>$R_i = R_0$</td>
</tr>
<tr>
<td>Radial active length</td>
<td>$\Delta R = R_e - R_i$</td>
</tr>
<tr>
<td>Mean radius</td>
<td>$R_m = (R_e + R_i) / 2$</td>
</tr>
<tr>
<td>Pole pitch ratio</td>
<td>$\tau_p = \pi / p$</td>
</tr>
<tr>
<td>Pole pitch width</td>
<td>$\tau = \tau_p R_m$</td>
</tr>
<tr>
<td>Slot pitch width</td>
<td>$\tau_s = \pi R_m / (S_{pp} \cdot mp)$</td>
</tr>
</tbody>
</table>
The machine is supposed to be supplied with sinusoidal currents. The electromagnetic average torque $\langle T_{EM} \rangle$ can then be obtained by relation (2).

$$\langle T_{EM} \rangle = \frac{4\sqrt{2}}{\pi} k_{B1} \xi_{3D} A_L B_{e\text{max}} S_g R_m \sin\left(\beta_m \frac{\pi}{2}\right) \left|\cos(\Psi)\right|$$  \hspace{1cm} (2)

Where $S_g$ is the air gap area given by $S_g = 2\pi R_m \Delta R$, $A_L$ is the electrical current load, $B_{g\text{max}}$ the maximum air gap flux density. $\xi_{3D}$ is a correction factor that roughly takes into account the magnets three-dimensional flux leakages. The 3D flux leakages mainly depend of the ratio between magnetic air gap ($g_\mu$) and the machine active length ($L_m$) [28]. This correction factor is given by relation (3) that is established for $0.1 < \frac{g_\mu}{L_m} < 4$.

$$\xi_{3D} = 1 - 0.2 \left(\frac{g_\mu}{L_m}\right)$$  \hspace{1cm} (3)

In the case of the considered double stator AFPM generator, $g_\mu = 2Z_{h_r} + Z_{h_a}$ and $L_m = \Delta R$. Then, the external radius $R_e$ of the electrical generator that allowing obtaining the required average electromagnetic torque for the given $A_l$ and $B_{g\text{max}}$ can be derived from equation (2) by solving equation (4).

$$R_e^3 + R_e R_r^2 - R_r^3 - R_s^3 = \frac{\langle T_{EM} \rangle}{2\sqrt{2} k_{B1} \xi_{3D} A_L B_{e\text{max}} \sin\left(\beta_m \frac{\pi}{2}\right) \left|\cos(\Psi)\right|} = 0$$  \hspace{1cm} (4)

It is then obvious that the maximum torque for given Joule losses is obtained by controlling $\Psi$ to zero ($\Psi=0$). This control will be considered for the design rated point.

To determine the minimal value of mechanical air gap $Z_g$ is defined as the distance between the stator teeth and the magnets, a coefficient $k_D$ is introduced (equation 5).

$$Z_g = k_D D_m$$  \hspace{1cm} (5)
This coefficient depends on the structural mass, the electromagnetic stress between the rotor and the iron-cored stator, and several mechanical forces acting on the rotor [20]. According to [21], $k_D$ can be typically set to $1000$ of the mean generator diameter $D_m$ for large direct-drive generators. However rim driven generators are characterized by higher diameters than conventional direct drive generators, because of that it is suitable to enlarge the $k_D$ factor. This factor is considered equal to $2000$ in this study.

For an accurate estimation of magnet height $Z_{hm}$, a 2D formulation that takes into account the interpolar flux leakages is used. Indeed, relation (6) is derived from a 2D model issued from solving the field equations by using the method of separating variables [29]. The calculation is performed considering an equivalent slotless linear generator. The average influence of the slotting effect in the gap permeance is taken into account by considering an additional gap, $Z_{g'}$:

$$Z_{hm} = \frac{\tau}{\pi} \ln \left( \frac{(\mu_m + 1)B_{g\max}}{(\mu_m + 1)B_{g\max}} \left( \frac{e^{\frac{\pi}{\tau}(Z_g + Z_{s})}}{\mu - (\mu_m + 1)} \right)^2 \right)$$

In (6), $\tau$ is the pole width (given in table 3 and fig. 4), $Z_g$ is the mechanical gap, $B_r$ is the magnet residual flux density, $\mu_m$ is the relative permeability of magnets. Relation (7) is valid for open slots generators, it is used in this study to calculate the additional gap $Z_{g'}$ [30]. According to [30], (equation (7)) is more suitable than classical Carter coefficient when the machine magnetic gap is large, which is the case of high diameter rim driven generators.

$$Z_{g'} = \frac{\tau_s}{2\pi} \left[ \beta_s \ln(\beta_s) + (2 - \beta_s) \ln(2 - \beta_s) \right]$$

$\tau_s$ is the slot pitch width (see table 3 and fig. 4). To avoid apparition of saturation in the teeth, a maximum value of the flux density in the soft magnetic materials $B_{sat}$ is fixed. $\beta_s$ is calculated by assuming that this level of flux density will be reached in the teeth for the worst case study where the flux density $B_{g\max}$ created by the magnets and the flux density created by the armature currents at their rated value are summed ($\psi = + \pi/2$) (relation (8)).
\[
\beta_i = \frac{B_{\text{gmax}}}{B_{\text{sat}}} + 2 \frac{\mu_0 \mu_m \sqrt{2} A_i \pi R_m}{Z_{\text{hm}} + 2 \mu_m (Z_g + Z_{g'})} S_{pp} mp B_{\text{sat}} \tag{8}
\]

Where \(\mu_0\) is the air permeability, \(S_{pp}\) is the number of slots per phase per pole (\(S_{pp} = 1\) in this study), \(m\) is the phase number (\(m=3\) in this study) and \(p\) is the pole pairs number (\(p\) is an integer value).

To avoid excessive stator yokes saturation, the minimum yoke thickness \(Z_y\) is calculated by considering that the flux density level \(B_{\text{sat}}\) where saturation appears is reached in the yokes for the maximum magnets flux density \(B_{\text{gmax}}\) summed to the maximum flux density created by the armature windings. In a similar way that for establishing equation (8), this calculation is based on the worst case where the stator and rotor flux are in additive configuration (\(\psi = \pi/2\)). \(Z_y\) is then determined by relation (9).

\[
Z_y = \beta_m \frac{\pi R_m B_{\text{gmax}}}{2p B_{\text{sat}}} + 2 \frac{\mu_0 \mu_m \sqrt{2} A_i \pi^2 R_m}{3 (Z_{\text{hm}} + 2 \mu_m (Z_g + Z_{g'}))} S_{pp} mp^2 B_{\text{sat}} \tag{9}
\]

For a given set values of the linear electric loading \(A_L\) (RMS value), the current density in the copper \(J\) (RMS value) and the slot fill factor \(k_f\), the equation (10) allows to determine the minimum slot height \(Z_{hs}\).

\[
Z_{hs} = \frac{A_L}{k_f J (1 - \beta_i)} \tag{10}
\]

C. Magnet field in magnets and electrical efficiency estimations

The maximum magnetic inverse field \(H_{\text{max}}\) in the magnets is evaluated to ensure that demagnetization is avoided. The expression of \(H_{\text{max}}\) is given in equation (11) for \(S_{pp} = 1\). This expression is established for the case where the stator and rotor flux are subtractive ones (\(\psi = -\pi/2\)) which corresponds to the worst encountered case during generator operation.

\[
|H_{\text{max}}| = \frac{2 \sqrt{2} \pi R_m A_L}{mp S_{pp} (Z_{\text{hm}} + 2 \mu_m (Z_g + Z_{g'}))} + \frac{2 (Z_g + Z_{g'}) B_{\text{gmax}}}{\mu_0 Z_{\text{hm}}} \tag{11}
\]
By considering the machine Joule losses $P_{J_{tot}}$, and the iron losses $P_{Fe_{tot}}$ at the turbine rated operating point (table I), the generator electrical efficiency can be roughly estimated by relation (12).

$$\eta_{elec} = 1 - \frac{P_{J_{tot}} + P_{Fe_{tot}}}{\langle T_{Em} \rangle \Omega}$$

(12)

IV. THERMAL MODELING

A. Thermal network modeling

A lumped parameters model is established to study the steady-state thermal behavior of the stator of the AFPM generator. Only stator copper and iron losses are considered as heat sources in the thermal resistance network model. This thermal model is developed considering heat transfer under a tooth pitch width. Indeed, the heat flows exchanged between slots and teeth are taken into account (2D network). The heat flows pass through the different materials constituting the stator tooth pitch (Fig.5) to be dissipated at last in the stator external sides (gap side and nozzle side). Figure 5 shows a sketch of tooth pitch geometry and the considered heat fluxes. It should be mentioned that only conduction and convection heat transfers are considered. The heat flow is assumed to be fully dissipated to the external sea water area and the immersed gap area in each side of the stator. Furthermore, radial heat transfers and end windings heat losses are not taken into account. Under this hypothesis, the thermal model is \textit{a priori} more pessimistic than the case where the radial heat transfer is considered.

![Diagram of thermal network model](image-url)
In order to establish the values of the components given in the thermal network model, each portion of material under the slot pitch width has to be modeled. For heat transfer in the axial direction, an elementary material volume is considered as shown in Fig. 6a, this volume is associated with an axial length $l$, an internal and external radius $R_i$ and $R_e$, a thermal conductivity $\lambda$, and it is subject to a heat dissipation $P_{heat}$. The corresponding thermal modeling is given by Fig. 6b.

The thermal resistances for Fig. 6b configuration are derived from [31-32] and they can be expressed as given in (13).

\[
\begin{align*}
R_{1z} &= \frac{l}{\lambda \alpha (R_e^2 - R_i^2)} \\
R_{2z} &= \frac{l}{\lambda \alpha (R_e^2 - R_i^2)} \\
R_{3z} &= \frac{-l}{3\lambda \alpha (R_e^2 - R_i^2)}
\end{align*}
\]
For heat transfer calculation in the ortho-radial direction (from slots to teeth), elementary parallelepiped materials volumes are considered to model tooth, slot and the tooth to slot insulation material. These volumes can be defined with a width $l_x$ (in the ortho-radial heat flow direction) and a conduction section $S_{\text{cond}}$. The related thermal resistance can then be calculated by (14).

$$R_{\text{cond}} = \frac{l_x}{\lambda S_{\text{cond}}} \quad (14)$$

For all the dissipation surfaces (each lateral face of the stators), a convection coefficient $h_{\text{conv}}$ and a convective area $S_{\text{conv}}$ are considered. The convection thermal resistance is given by (15).

$$R_{\text{conv}} = \frac{1}{h_{\text{conv}} S_{\text{conv}}} \quad (15)$$

The basic relations (13) to (15) are applied to all the part of the stator. They lead to establish the thermal global network of Fig. 7 that models thermal exchanges occurring under a stator slot pitch (Figure 7 elements are defined in the Appendix).
B. Heat sources

For heat sources calculation, both copper and iron losses in slots, teeth and yoke are considered. For an electrical resistivity $\rho_{Cu}$, copper losses can be calculated in each slot as a function of the copper volume per slot ($V_{Cu/slot}$) and the current density $J$ in the copper.

$$P_J = \rho_{Cu} V_{Cu/slot} J^2 \quad (16)$$

Iron losses $P_{Fe}$ (W/kg) can be evaluated in teeth and yoke by the following basic relationship.

$$P_{Fe} = P_{Fe0} \left( \frac{f}{f_0} \right)^b \left( \frac{B_{Fe}}{B_{Fe0}} \right)^c \quad (17)$$

Where $f$ and $B_{Fe}$ are respectively the electrical frequency and the iron flux density of the soft magnetic materials. $P_{Fe0}$ is the iron losses when $f = f_0$ ($f_0$ is the material characteristic frequency). $B_{Fe0}$ is the corresponding characteristic flux density. The values of $b$ and $c$ are set to 1.5 and 2.2 respectively, according to usual soft magnetic materials specifications.

C. Convection coefficients calculation

Figure 8 illustrates the hypothesis taken to represent the water flow and the heat transfer between the machine and the sea water. The water flow is supposed to be perpendicular to a cylindrical-shape nozzle in which the double stator AFPM machine active parts are inserted. The sea water convection coefficients can then be evaluated from this nozzle shape assumption and considering an immersed gap. These coefficients depend on the Reynolds and Prandtl numbers that characterize the water flow inside the machine (in the immersed gap) and outside the machine (external side of the nozzle).
Fig. 8. Hypothesis of cylindrical shaped nozzle and double stator AFPM machine insertion. $D_c$ is the cylindrical shaped nozzle and $h_{ew}$ is the end windings length.

To calculate the convections coefficients inside the gap and outside the generator some parameters related to the water fluid must be defined. The first specification parameter to be fixed is the sea water temperature $T_{water}$. Considering this temperature, the set of following specification parameters are used: water thermal conductivity $\lambda_{water}$ (W/m/K), water mass per volume $\rho_{water}$ (kg/m$^3$), water heat capacity $C_p$ (J/kg/K), and water dynamic viscosity $\nu_d$ (Pa.sec).

For the present study, the sea water temperature is assumed to be equal to 30°C. Considering the above parameters, the thermal diffusivity coefficient $a$ and the water kinematic viscosity $\nu_c$ (m$^2$/sec) can be estimated using relation (18).

$$ \begin{cases} a = \frac{\lambda_{water}}{\rho_{water} C_p} \\ \nu_c = \frac{\nu_d}{\rho_{water}} \end{cases} \tag{18} $$

The Prandtl number can then be estimated by relation (19).

$$ Pr = \frac{\nu_c}{a} \tag{19} $$

Equations (18-19) are used for sea water inside (gap) and outside the generator (nozzle).
For the *Reynold* number, the gap area and the area located outside the nozzle must be distinguished since the water flows are at different speed. The perpendicular current speed \( v \) and the tangential water speed \( v_t \) (that depends on the rated rotating speed and the generator radius) have to be known to calculate *Reynold* numbers (relation (20)).

\[
\begin{align*}
\text{Outside the nozzle} & : \quad \text{Re} = \frac{vD_c}{\nu_c} \\
\text{Inside the immersed gap} & : \quad \text{Re} = \frac{v_t Z_{g_{-\text{eff}}}}{\nu_c} \frac{R_m \Omega Z_{g_{-\text{eff}}}}{\nu_c} 
\end{align*}
\]

(20)

Where \( Z_{g_{\text{eff}}} \) is the mechanical gap between the rotor and the stator resin \( (Z_{g_{\text{eff}}} = Z_g - Z_{\text{rotor resins}} - Z_{\text{stator resins}}) \). \( Z_{\text{rotor resins}} \) and \( Z_{\text{stator resins}} \) are respectively the resin thickness covering the magnets and the stator active parts inside the air gap.

Regarding the convection coefficient calculation on the external side of the nozzle, the nozzle is assimilated to a long cylinder. Considering a turbulent fluid flow on the outside nozzle area and only the forced convection, the average *Nusselt* number can be roughly estimated from relation (21) according to these assumptions.

\[
\bar{\text{Nu}}_{\text{outside}} = \left( 0.4 \text{Re}^{0.5} + 0.06 \text{Re}^{2/3} \right) \text{Pr}^{0.4}
\]

(21)

Relation (21) is given for \( 10 < \text{Re} < 10^5 \) and \( 0.67 < \text{Pr} < 300 \).

The heat transfer convection coefficient is proportional to the *Nusselt* number \( \bar{\text{Nu}}_{\text{outside}} \) and is calculated by relation (22).

\[
\bar{\text{h}}_{\text{outside}} = \frac{\bar{\text{Nu}}_{\text{outside}} \lambda_{\text{water}}}{D_c}
\]

(22)

The convection heat transfer coefficient in the immersed gap is calculated knowing the *Nusselt* number in the gap area (\( \bar{\text{Nu}}_g \)) which is given by (23); issued from [33] and takes into account only the forced
convection. It can be noted that with considering only the forced convection the Nusselt number is probably underestimated.

\[
\overline{\text{Nu}}_g = 0.024 \text{Re}^{0.68}
\]  

(23)

Thus, the convection heat transfer coefficient \( \overline{h}_g \) in the flooded air gap can be deduced from (24).

\[
\overline{h}_g = \frac{\overline{\text{Nu}}_g \lambda_{\text{water}}}{Z_{g \text{ - eff}}}
\]

(24)

V. OPTIMIZATION PROBLEM FORMULATION

A. Parameters and design variables

In order to facilitate the distinction between specification parameters and design variables, two specification vectors \( S_m \) and \( S_t \) are introduced as illustrated by relation (25). \( S_m \) and \( S_t \) components remain constant during the optimization procedure. These two vectors summarize the set of specification related to the materials magnetic properties, the material thermal properties and the fixed geometrical parameters (the value of these data are given in tables 1 and 2). An example of \( S_m \) and \( S_t \) vectors is given in relation (25).

\[
\begin{align*}
\left[ S_m \right] &= \left[ T_{EM} \quad R_0 \quad \Omega \quad m \quad s_{pp} \quad \beta_m \quad k_f \quad \psi \quad B_r \quad B_{sat} \quad H_{cf} \right]^T \\
\left[ S_t \right] &= \left[ T_{max} \quad T_{\text{water}} \quad \rho_{\text{Cu}} \quad B_{Fe0} \quad P_{Fe0} \quad \lambda_{\text{water}} \quad \lambda_{\text{materials}} \quad \rho_{\text{water}} \quad C_p \quad u_g \quad v \right]^T
\end{align*}
\]

(25)

For the given specification set \( (S_m \text{ and } S_t) \), the design procedure aims to find a machine that fits as best as possible the objectives and constraints. Using analytical modeling and the study hypotheses, it is possible to fully describe the machine geometry from the knowledge of only four following key design variables: the stator linear electric loading \( A_L \) (Am\(^{-1}\) rms), the copper current density \( J \) (A/mm\(^2\)) in copper, the gap flux density \( B_{gmax} \) (T), and the pole pairs number \( p \). These four parameters are the components of the \( \mathbf{x} \) vector presented in equation (26).
Indeed according to the electromagnetic model given in section III, it is possible for a given vector \( x \), to determine a single vector \( g \) if the specification vector \( S_m \) is known. The scheme of this inversion of the Electromagnetic model is presented at figure 9. The components of \( g \) vector are respectively the external radius, \( R_e \), the magnet height, \( Z_{hm} \), the slot depth, \( Z_{hs} \), the yoke thickness, \( Z_y \), and the teeth width ratio, \( \beta_t \). These parameters associated with the \( x \) and \( S_m \) vectors components allow to fully describe the machine geometry as shown figure 4.

\[
x = \begin{bmatrix} A_l & J & B_{s_{max}} & p \end{bmatrix}^T
\]

(26)

\[
g = \begin{bmatrix} R_e & Z_{hm} & Z_{hs} & Z_y & \beta_t \end{bmatrix}^T
\]

(27)

Fig. 9. Electromagnetic model inputs/outputs.

The thermal model described in previous section allows, for a given vector \( x \) (and then for known geometrical parameters), to calculate the maximum slot temperature when considering thermal specification vector \( S_t \). This thermal model will be associated, in the design optimization process to a non linear constraint. This constraint will ensure that the copper operating temperature is lower than the allowed maximal slot temperature \( T_{max} \).

**B. Optimization procedure**

To achieve the generator optimal geometry, an optimization problem is formulated. The optimization variables are the components of the \( x \) vector that allow determining the machine geometry given by the vector, \( g \), as explained previously. The optimization objective function aims to minimize the total cost of the machine active parts, here denoted \( C(x) \). \( C(x) \) is evaluated considering the generator active parts
masses. The active parts masses are determined from knowing the \( g \) (deduced from \( x \)) and \( S_m \) vectors components and from the costs given in Table 2 (relation (28)).

\[
C(x) = M_{copper}(x)C_{copper} + M_{iron}(x)C_{iron} + M_{magnet}(x)C_{magnet}
\]  

(28)

\( M_i \) and \( C_i \) respectively denote the mass (kg) and the price ($/kg) of each used active parts materials.

To fully define the optimization problem, some constraints must be introduced. The first nonlinear inequality constraint relates to the machine thermal behavior. In fact, the maximal coil temperature must be limited to satisfy the temperature limit that can be supported by the insulation materials in the slots \( T_{max} \), this constraint is given by relation (29). The temperature \( T(x) \) is calculated using the thermal model as presented previously. Another nonlinear inequality constraint limits the magnetic field inside the magnets to avoid their demagnetization, this constraint is introduced by (30). Furthermore, a nonlinear constraint on the minimal electrical efficiency is included to ensure the required electrical efficiency of the optimal generator; this constraint is introduced in the optimization algorithm by relation (31).

\[
T(x) - T_{max} \leq 0
\]

(29)

\[
|H_{max}(x)| - |H_{cj}| \leq 0
\]

(30)

\[
-\eta_{elec}(x) + \eta_{elec,min} \leq 0
\]

(31)

Where \( T(x) \) is the thermal model, \( H_{max}(x) \) is the magnetic model that allows to determine the maximal magnetic field inside the magnets for each values of the vector \( x \) \( H_{max}(x) \) is calculated using relation (11)), \( \eta_{elec}(x) \) is the model function that allow evaluating the electrical efficiency of the generator for a given variables vector \( x \). \( T_{max}, H_{cj} \) and \( \eta_{elec,min} \) are given in table 1.

Otherwise, a nonlinear constraint related to the pole pair number limitation is added to ensure feasible machine shape. To fulfill the machine shape requirements, a first constraint \( (p_{max}) \), given by relation (32),is introduced. This relation relates to the frequency operation limits of the magnetic steel laminations. This condition should be respected to have a realistic estimation of iron losses, given by the utilized iron losses model (given in section III), which is valid in the frequency working range of the iron sheets (table 2). The second constraint is introduced by defining a feasible ratio \( \Re \) (in terms of manufacturing) between the slot heights and the tooth width. The slot shape ratio \( \Re \) is calculated by relation (33).
According to [34] this ratio can be taken in the range $\mathbb{R} \in [\mathbb{R}_{\text{min}}, \mathbb{R}_{\text{max}}] = [4,10]$, to avoid excessive mechanical vibrations. From the upper ratio $\mathbb{R}_{\text{max}}$, another upper limit ($p_{\text{max}2}$) for the pole pair number can be deduced. This second upper limit ($p_{\text{max}2}$) is given by relation (34). The maximum allowable poles pair number is then introduced in the optimization process as a constraint by relation (35). Considering the lower ratio $\mathbb{R}_{\text{min}}$, a last constraint is introduced that fix a lower limit on the poles pair number ($p_{\text{min}1}$), is defined to maintain the ratio $\mathbb{R}$ into the interval $\mathbb{R} \in [4,10]$ during the optimization process. This constraint is established by equations (36) and (37).

\[
p_{\text{max}1} = \frac{2\pi f_{\text{elec}}}{\Omega}
\]

(32)

Where $\Omega$ is the generator rotational speed.

\[
\mathbb{R} = \frac{A_t \times 2pmS_{pp}}{k_J (1-\beta_t) \beta_t \times 2 \pi R}
\]

(33)

\[
p_{\text{max}2} = \frac{\mathbb{R}_{\text{max}} \times \beta_t \times \left(\frac{2 \pi R}{2mS_{pp}}\right)}{\left(\frac{A_t}{k_J (1-\beta_t)}\right)}
\]

(34)

\[
p - \min\left(p_{\text{max}1}, p_{\text{max}2}\right) \leq 0
\]

(35)

\[
p_{\text{min}1} = \frac{\mathbb{R}_{\text{min}} \times \beta_t \times \left(\frac{2 \pi R}{2mS_{pp}}\right)}{\left(\frac{A_t}{k_J (1-\beta_t)}\right)}
\]

(36)

\[
-p + p_{\text{min}1} \leq 0
\]

(37)

At last, upper and lower bounds are introduced as linear constraints to restrict the optimization space and then to obtain feasible solution (relation (38))
\[
\begin{bmatrix}
A_{t_{\text{min}}} \\
J_{\text{min}} \\
B_{g_{\text{max}}} \\
P_{\text{min}} \\
\end{bmatrix}
\leq
\begin{bmatrix}
A_{t} \\
J \\
B_{g_{\text{max}}} \\
P \\
\end{bmatrix}
\leq
\begin{bmatrix}
A_{t_{\text{max}}} \\
J_{\text{max}} \\
B_{g_{\text{max}}} \\
P_{\text{max}} \\
\end{bmatrix}
\] (38)

These bounds are set to \( LB = [20000 \, (A/m), 1 \, (A/mm^2), 0.1 \, (T), 50 ]^T \) and \( UB = [150000 \, (A/m), 10 \, (A/mm^2), 1 \, (T), 500 ]^T \).

Relation (39) summarizes the formulation of the optimization problem presented previously:

\[
x^* = \min_{x \in X} \| C(x) \|
\]
\[
T(x) - T_{\text{max}} \leq 0
\]
\[
\left| H_{\text{max}}(x) - |H_{\text{c}}| \right| \leq 0
\]
\[
-\eta_{\text{elec}}(x) + \eta_{\text{elec}} \leq 0
\]
\[
p - \min(p_{\text{max}}^1, p_{\text{max}}^2) \leq 0
\]
\[
-p + p_{\text{min}} \leq 0
\]
\[
LB \leq x \leq UB
\] (39)

VI. RESULTS ANALYSIS

A. Optimization analysis

Considering the given specifications of Tables 1 and 2 and the proposed models and methodology the optimization process is performed with SQP (sequential quadratic programming) algorithm. This optimization algorithm is available under MATLAB \textit{fmincon} function. Figure 10 illustrates the optimization algorithm evolution up-to the optimal solution \( x^* \) convergence. Figure 11 gives the total active parts cost (objective function), the electrical efficiency and the slots temperature evolution during the optimization iterations.
This figure clearly shows that cost minimization and efficiency decrease are strongly correlated: constraint relating to the efficiency is here first saturated. The other constraints are not saturated: the final conductors temperature is about 45°C (for 100°C allowed) and the final magnetic coercive field is about 0.538 MA/m (for 1.208 MA/m allowed). This clearly shows that the temperature constraint related to the maximum slot temperature ($T_{\text{max}}$) cannot be saturated because the electrical efficiency constraint is saturated first. This is due to the good cooling related to the subsea generator immersion. Furthermore, as it is observed in Fig. 10, when the active parts cost is minimized, the pole pair number $p$, the current load $A_L$, and the copper current density are increased whereas the air gap flux density created by magnets is decreased. However, even if increasing $A_L$ and $J$ lead to lower active parts cost, these variables cannot be increased because of electrical efficiency constraint saturation.
Fig. 11. Objective function and main nonlinear constraints evolution during the optimization iterations.

B. Electromagnetic design discussion

The design parameters corresponding to the optimal double stator AFPM machine solution is obtained with the previously described procedure, the obtained optimal machine is summarized in Table 4.

<table>
<thead>
<tr>
<th>$x^*$</th>
<th>Current density</th>
<th>$J$</th>
<th>3.8</th>
<th>A/m² (rms)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Stator linear electric loading</td>
<td>$A_L$</td>
<td>58078</td>
<td>A/m (rms)</td>
</tr>
<tr>
<td></td>
<td>gap flux density</td>
<td>$B_{gmax}$</td>
<td>0.295</td>
<td>T</td>
</tr>
<tr>
<td></td>
<td>Pole pair number</td>
<td>$p$</td>
<td>448</td>
<td>-</td>
</tr>
<tr>
<td>$g^*$</td>
<td>Inner radius</td>
<td>$R_i$</td>
<td>5.5</td>
<td>m</td>
</tr>
<tr>
<td>Parameter</td>
<td>Symbol</td>
<td>Value</td>
<td>Unit</td>
<td></td>
</tr>
<tr>
<td>--------------------------------------------------</td>
<td>--------</td>
<td>--------</td>
<td>--------</td>
<td></td>
</tr>
<tr>
<td>Outer radius</td>
<td>$R_e$</td>
<td>5.538</td>
<td>m</td>
<td></td>
</tr>
<tr>
<td>Active length (radial thickness)</td>
<td>$\Delta R$</td>
<td>4.48</td>
<td>cm</td>
<td></td>
</tr>
<tr>
<td>Mean radius</td>
<td>$R_m$</td>
<td>5.519</td>
<td>m</td>
<td></td>
</tr>
<tr>
<td>Polar arc width defined at mean radius</td>
<td>$\tau$</td>
<td>3.87</td>
<td>cm</td>
<td></td>
</tr>
<tr>
<td>Magnet to pole width ratio</td>
<td>$\beta_m$</td>
<td>0.66</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>Teeth pitch ratio</td>
<td>$\beta_t$</td>
<td>0.248</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>Stator yoke thickness</td>
<td>$Z_y$</td>
<td>0.5</td>
<td>cm</td>
<td></td>
</tr>
<tr>
<td>Slot height</td>
<td>$Z_{hs}$</td>
<td>3.07</td>
<td>cm</td>
<td></td>
</tr>
<tr>
<td>Magnets thickness</td>
<td>$Z_{hm}$</td>
<td>1.2</td>
<td>cm</td>
<td></td>
</tr>
<tr>
<td>Air gap (magnet/stator)</td>
<td>$Z_g$</td>
<td>11</td>
<td>mm</td>
<td></td>
</tr>
<tr>
<td>Temperature in the slots</td>
<td>$T_c$</td>
<td>45.7</td>
<td>°C</td>
<td></td>
</tr>
<tr>
<td>Electrical efficiency</td>
<td>$\eta_{elec}$</td>
<td>0.9</td>
<td>-</td>
<td></td>
</tr>
<tr>
<td>Maximum magnetic field inside magnets</td>
<td>$H_{max}$</td>
<td>0.538</td>
<td>MA/m</td>
<td></td>
</tr>
</tbody>
</table>

Fig. 12a gives a scale drawing of obtained double stator AFPM generator active parts volume. Figure 12b shows a zoom on the active parts drawn at the scale. As expected the resulting double stator AFPM machine is characterized by a thin axial and radial thickness, which complies with the requirements of rim-driven marine turbines [11].
For validation purposes, 3D finite elements (FE) computations have been performed for the obtained optimal rim driven generator using Maxwell 3D® software (Fig. 13). In this case, a difference of about 4% is found between calculated electromagnetic torque and the required one which is acceptable at this predesign step. In addition, finite elements calculations also show that the calculated axial machine magnetic circuit is not saturated as illustrated in Fig. 13. In fact, saturating the magnetic circuit to reduce iron volume is not an issue for rim drives because the part of the iron mass is not significant compared to...
the total marine turbine mass. Furthermore, in this kind of rim driven structures, the electrical generator is characterized by a large magnetic gap and a small machine active length that lead to high 2D and 3D flux leakages.

![Image](image.png)

**Fig.13.** Flux density distribution 3D mapping (a), mesh of the double stator AFPM machine under a pole width (b).

### C. Thermal model validation and discussion

In order to estimate the thermal resistance network model accuracy, a 2D finite elements computation is performed for the final optimal machine geometry. In this case, FEMM software that allows solving the heat transfer equation in steady-state operation is used [35]. Figure 14 shows the obtained temperature mapping under a slot pitch width. The analytical slots temperature evaluated by the lumped parameter model is very close to the one obtained with finite element. The difference is here lower than 1% (45.7°C for the analytical calculation and 45°C for the numerical computation). It should be noted that same heat transfer convection coefficients are introduced in both analytical thermal model and numerical software.
The heat transfer convection coefficients are however issued from basic hydrodynamic formula described in section IV. The accuracy of their estimation is therefore not fully guaranteed. For that purpose, the influence of these coefficients variation on the calculated slots maximal temperature has been studied. Figure 15 gives a mapping of this coils temperature according to the heat transfer convection coefficients values calculated by relations (18 to 24). Figure 15 clearly shows that the convection coefficients variations do not strongly affect the slots maximal temperature. The temperature variation is less than 10% when the outside heat transfer convection coefficient exceeds 600 W/K/m² ($h_{\text{outside}} > 600\text{W/K/m}^2$) when the calculated one is 4059 W/K/m². Indeed, it is related to the large values of the convection coefficients due to the good cooling related to generator immersion in the sea water. In fact, these high values of convection coefficients lead to very small values of convection thermal resistances that can be neglected referring to conduction thermal resistance of the insulation materials. Otherwise, Fig. 15 clearly underlines that the slots temperature is even less sensitive to the air gap heat transfer coefficient ($h_g$).
Fig. 15. Sensitivity of the maximal slot temperature versus the convection coefficients variations.

Table 5 gives the machine heat flow repartition between the nozzle external area and the immersed gap. It shows that 25% of the total heat flow produced by the losses is evacuated through the gap and only 5% of the heat flow is exchanged between slots and teeth. The small proportion of heat flow exchanged from slots to teeth is due to the small temperature difference between slots and teeth. However, even if an immersed gap allows a significantly better cooling, the presence of water in the gap leads to additional losses related to water viscosity that are not taken into account by the proposed models. In fact, the considered immersed gap has some advantages and inconvenient that are resumed in table 6.

**Table 5. Exchanged Heat Flow Proportions.**

<table>
<thead>
<tr>
<th>Heat Flow Description</th>
<th>Value</th>
<th>Unit</th>
</tr>
</thead>
<tbody>
<tr>
<td>Immersed gap convection coefficient ($\bar{h}_g$)</td>
<td>4059.4</td>
<td>W/K/m²</td>
</tr>
<tr>
<td>Outside convection coefficient ($\bar{h}_{outside}$)</td>
<td>5042.6</td>
<td>W/K/m²</td>
</tr>
<tr>
<td>Outside heat flow</td>
<td>10965</td>
<td>W/m²</td>
</tr>
<tr>
<td>Heat flow exchanged with the immersed gap</td>
<td>3748.8</td>
<td>W/m²</td>
</tr>
<tr>
<td>Slot to tooth heat flow</td>
<td>693</td>
<td>W/m²</td>
</tr>
</tbody>
</table>
Table 6. Qualitative comparison of flooded and waterproof air gaps.

<table>
<thead>
<tr>
<th></th>
<th>advantages</th>
<th>inconvenient</th>
</tr>
</thead>
<tbody>
<tr>
<td>Immersed gap</td>
<td>☑ better thermal cooling</td>
<td>☐ Higher viscous losses and frictions in the gap</td>
</tr>
<tr>
<td></td>
<td>☑ No use of special nozzle to ensure gap waterproof</td>
<td>☐ Need of special fluid bearings</td>
</tr>
<tr>
<td></td>
<td></td>
<td>☐ Resin inside the gap to cover magnets and stator active parts</td>
</tr>
<tr>
<td>Waterproof gap</td>
<td>☑ Less viscous and friction losses</td>
<td>☐ Reduced gap thermal exchanges</td>
</tr>
<tr>
<td></td>
<td>☑ No resin and special fluid bearings in the gap</td>
<td>☐ Use of reinforced waterproof nozzle</td>
</tr>
</tbody>
</table>

VII. DOUBLE STATOR AFPM AND RFPM MACHINES COMPARISON

The aims of this section is to compare the studied double stator AFPM generator solution with a more conventional solution based on the use of radial flux permanent magnets generator for the same rim-driven specifications. For comparison purposes, a radial flux machine design is performed using a similar methodology and the same specifications as for the double stator AFPM generator. The radial flux generator design procedure implies similar electromagnetic and thermal models. These models have the same level of complexity and accuracy than the ones used to design the axial flux topology.

A. Sizes and active parts comparison

A similar design optimization approach as in section V is carried-out to optimize the RFPM machine with considering the same design specifications. The used RFPM generator is based on classical design options, with surface mounted magnets as shown in Fig.16a. The resulting machine is compared to the previously optimized double stator AFPM generator. Table 7 gives a comparison between the both RFPM and double stator AFPM generators geometry and performances main parameters. In Table 7, the volume dimensions of the two generators (RFPM and double stator AFPM generators) are also presented for comparison purposes. End-windings are included by considering a simple half cylinder end-winding geometry [36]: the end-winding diameter is considered equal to the pole arc width. From Table 7 analysis, the following conclusion can be drawn: a double stator AFPM generator appears to be more compact than
the RFPM generator when considering the active parts volume sizes. However this difference is not really significant because both machines are characterized by very large diameters. Figure 16 shows slots, magnets, and yoke dimensions, of the two optimized generators.

### Table 7. Double Stator AFPM and RFPM Generators Comparison.

<table>
<thead>
<tr>
<th></th>
<th>RFPM generator</th>
<th>Double stator AFPM generator</th>
<th>units</th>
</tr>
</thead>
<tbody>
<tr>
<td>Pole pair number</td>
<td>267</td>
<td>448</td>
<td>-</td>
</tr>
<tr>
<td>Inner radius</td>
<td>5.5</td>
<td>5.5</td>
<td>m</td>
</tr>
<tr>
<td>Generators radial thickness (with end windings for the axial generator)</td>
<td>8.2</td>
<td>6.67</td>
<td>cm</td>
</tr>
<tr>
<td>Axial length (with end windings for the radial generator)</td>
<td>13.2</td>
<td>11.74</td>
<td>cm</td>
</tr>
<tr>
<td>Magnet thickness</td>
<td>8.6</td>
<td>12</td>
<td>mm</td>
</tr>
<tr>
<td>Current density in copper</td>
<td>3.663</td>
<td>3.8</td>
<td>A/mm² (rms)</td>
</tr>
<tr>
<td>Stator linear Electric loading</td>
<td>76981</td>
<td>58078</td>
<td>A/m (rms)</td>
</tr>
<tr>
<td>Maximum gap flux density</td>
<td>0.250</td>
<td>0.295</td>
<td>T</td>
</tr>
<tr>
<td>Active length</td>
<td>7.3</td>
<td>4.48</td>
<td>cm</td>
</tr>
<tr>
<td>Magnet to pole width ratio</td>
<td>0.66</td>
<td>0.66</td>
<td>-</td>
</tr>
<tr>
<td>Teeth pitch ratio</td>
<td>0.235</td>
<td>0.248</td>
<td>-</td>
</tr>
<tr>
<td>Yoke thickness</td>
<td>2.95</td>
<td>0.5</td>
<td>cm</td>
</tr>
<tr>
<td>Slot height</td>
<td>4.23</td>
<td>3.07</td>
<td>cm</td>
</tr>
<tr>
<td>gap thickness (magnets to stator distance)</td>
<td>22</td>
<td>11</td>
<td>mm</td>
</tr>
<tr>
<td>Maximum temperature in the slots</td>
<td>49.5</td>
<td>45.7</td>
<td>°C</td>
</tr>
<tr>
<td>Electrical efficiency</td>
<td>0.9</td>
<td>0.9</td>
<td>-</td>
</tr>
<tr>
<td>Maximum magnetic field inside magnets</td>
<td>0.5888</td>
<td>0.538</td>
<td>MA/m</td>
</tr>
</tbody>
</table>
According to Fig. 18, the calculated double stator AFPM generator is more compact than the RFPM machine in terms of active parts mass (25% reduction of the active parts mass). Regarding the costs comparison, the double stator AFPM generator presents active parts cost reduction of about 20% (fig. 17). This can be explained by the higher poles number of the double stator AFPM machine (Table 7). Indeed, poles number is higher with the axial machine because the copper volume is distributed over two stators. Then it becomes possible to find a higher pair pole number that matches a feasible tooth shapes (to satisfy the constraint on the tooth shape factor). For both machines, a significant part of copper is used in the end-windings (more than 50% of the total copper volume is in the end windings in the both cases). This high volume is due to the small machine active length related to rim-driven generator integration (very high diameter). For the presented costs comparison, the inactive materials are not taken into account. This assumption is justified by the fact that these materials price would be much lower than the price of active materials (permanent magnets and copper) even if the active parts mass is lower than the generator and the MCT turbine structural masses [21].
Fig. 17. Comparison of double stator AFPM and RFPM generators active parts costs.

Fig. 18. Comparison of double stator AFPM and RFPM generators active parts masses.
B. Thermal behavior comparison

Regarding the thermal behavior of the double stator AFPM machine, the estimated maximal slots temperature is about 45°C whereas the temperature is 49.5°C in the corresponding radial machine (Table 7). This result confirms that the double stator AFPM generator has a better thermal behavior. This is due to the current load distribution on the two stators.

C. Achieved results versus required efficiency

In both axial and radial generators design cases, the constraints on the electrical efficiency are saturated. Therefore, the influence of the minimal electrical efficiency value is studied (Figs. 19 and 20).

Figure 19 gives a Pareto front of the considered objective function (active parts cost function) as a function of the electrical efficiency. It is interesting to note that the Pareto curve shows that the generator electrical efficiency presents two limit values (Fig. 19 curve bounds). The minimal efficiency limit value corresponds to the minimum active parts cost. This lower limit is reached when the temperature constraint is saturated (for an efficiency of 0.9). In this case the current density \( J \) in the copper and the stator linear electric loading \( A_L \) reach their maximum allowable values. According to Fig. 20, the maximal efficiency limit corresponds to the maximal active parts cost and this upper bound matches the minimal losses (balance between Joule and iron losses). Thus for direct-drive permanent magnet machines the iron losses cannot be neglected when the generator is designed with a maximal electrical efficiency strategy, even if the generator speed is low.


VIII. CONCLUSION

This paper is devoted to the design and performance analysis of axial flux permanent magnet generators for rim-driven marine current turbines. Thermal and inverse electromagnetic analytical models are described and integrated in an optimal design strategy that allows designing direct drive rim driven AFPM generators. This original strategy aims to minimize the active parts costs and takes into account a minimal efficiency constraint and marine context specifications. The achieved axial flux generator design has been validated by both thermal and magnetic finite elements computations. These computations validate the used analytical models. Results analysis allows underscoring some design issues for rim drives marine turbines generators. Furthermore and for comparison purposes, a radial flux generator has been optimally designed with similar design models and with the same specifications. The comparison of the two topologies mainly shows that the double stator axial flux permanent magnets generator has a lower cost, a lower mass and better cooling performance.
REFERENCES


**APPENDIX**

\[
P_{12} = \text{Joule losses in a slot;}
\]

\[
P_{23} = \text{Iron losses in the yoke under a slot width;}
\]

\[
P'_{12} = \text{Iron losses in the tooth under a tooth width;}
\]

\[
P'_{23} = \text{Iron losses in the yoke under a tooth width;}
\]

\[
R_{11} = \text{Thermal convection resistance in the flooded air gap (under a slot width;)
}\]
\[ R_{12} = \text{Thermal conduction resistance of the resin (under a slot width)}; \]
\[ R_{13} = \text{Thermal conduction resistance of the insulation material (under a slot width)}; \]
\[ R_{14} = \text{Thermal resistance of the lower part in T scheme of slot (under a slot width)}; \]
\[ R_{15} = \text{Thermal contact resistance } R_{3z} \text{ in the T scheme of slot (under a slot width)}; \]
\[ R_{21} = \text{Thermal resistance of the upper part in T scheme of slot (under a slot width)}; \]
\[ R_{22} = \text{Thermal conduction resistance of the insulation (under a slot width)}; \]
\[ R_{23} = \text{Thermal contact resistance (between yoke and insulation)}; \]
\[ R_{24} = \text{Thermal resistance of the lower part in the T scheme of yoke (under a slot width)}; \]
\[ R_{25} = \text{Thermal contact resistance } R_{3z} \text{ in the T scheme of yoke (under a slot width)}; \]
\[ R_{31} = \text{Thermal resistance of the upper part in T scheme of yoke (under a slot width)}; \]
\[ R_{32} = \text{Thermal contact resistance (between yoke and hull)}; \]
\[ R_{33} = \text{Thermal conduction resistance of the hull (under a slot width)}; \]
\[ R_{34} = \text{Thermal convection resistance with sea water (outer side of the hull)}; \]
\[ R_{ct1} = \text{Thermal contact resistance } R_{3z} \text{ in the T scheme of the slot part (slot to tooth heat transfer)}; \]
\[ R_{ct2} = \text{Thermal contact resistance } R_{3z} \text{ in the T scheme of the tooth part (slot to tooth heat transfer)}; \]
\[ R_{Cu} = \text{Thermal resistance of the lower part in T scheme of the slot part}; \]
\[ R_{isot} = \text{Thermal resistance of the insulation (between slot and tooth)}; \]
\[ R_{eclt} = \text{Thermal contact resistance (between insulation/tooth surface)}; \]
\[ R_{fer} = \text{Thermal resistance of the lower part in T scheme of the tooth part}; \]
\[ R'_{11} = \text{Thermal resistance in the flooded gap (under a tooth width)}; \]
\[ R'_{12} = \text{Thermal conduction resistance of the resin (under tooth width)}; \]
\[ R'_{13} = \text{Thermal contact resistance (between insulation/tooth surface)}; \]
\[ R'_{14} = \text{Thermal resistance of the lower part in T scheme of a tooth (under a tooth width)}; \]
\[ R'_{15} = \text{Thermal contact resistance } R_{3z} \text{ in the T scheme of tooth (under a tooth width)}; \]
\[ R'_{21} = \text{Thermal resistance of the upper part in T scheme of tooth (under a tooth width)}; \]
\[ R'_{22} = \text{Thermal resistance of the lower part in T scheme of yoke (under a tooth width)}; \]
\[ R'_{23} = \text{Thermal contact resistance } R_{3z} \text{ in the T scheme of yoke (under a tooth width)}; \]
\[ R'_{31} = \text{Thermal resistance of the upper part in T scheme of yoke (under a tooth width)}; \]
\[ R'_{32} = \text{Thermal contact resistance yoke/insulation surface (under a tooth width)}; \]
\[ R'_{33} = \text{Thermal conduction resistance of the hull (under a tooth width)}; \]
\[ R'_{34} = \text{Convection resistance with sea water (outer side of the hull) under a tooth width}. \]
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