Reconstruction of an optical inhomogeneity map improves fluorescence diffuse optical tomography

Nicolas Ducros¹, Teresa Correia², Andrea Bassi³, Gianluca Valentini³, Simon Arridge², Cosimo D’Andrea^{3,4}

¹ Univ Lyon, INSA-Lyon, Université Claude Bernard Lyon 1, UJM-Saint Etienne, CNRS, Inserm, CREATIS UMR 5220, U1206, F-69621, LYON, France

² Centre for Medical Image Computing, University College London, Malet Place, London WC1E 6BT, United Kingdom

³ Istituto di Fotonica e Nanotecnologie (IFN-CNR) - Dipartimento di Fisica, Politecnico di Milano, Piazza Leonardo da Vinci 32, I-20133 Milan, Italy

⁴ Center for Nano Science and Technology@PoliMi, Istituto Italiano di Tecnologia, Via Giovanni Pascoli, 70/3, 20133 Milano

E-mail: nicolas.ducros@insa-lyon.fr

Submitted in March 2016

Abstract. We propose a new reconstruction algorithm for fluorescence diffuse optical tomography, which is designed for highly heterogeneous objects, such as biological tissues. It is a two-step algorithm that exploits continuous-wave measurements acquired at both excitation and fluorescence wavelengths. First, an optical inhomogeneity map, which depends on both absorption and diffusion coefficients, is obtained from excitation measurements. Second, the fluorescence distribution is reconstructed considering the recovered optical inhomogeneity map. The algorithm includes dimensionality reduction techniques, namely measurement compression and structured illumination, which significantly reduce acquisition and reconstruction times. The algorithm has been tested on experimental data acquired from tissue-mimicking phantoms considering sparsity priors. We demonstrate the feasibility and effectiveness of this new approach that allows the fluorescence reconstruction quality to be improved with respect to that provided by the standard normalized Born method.

Keywords: fluorescence imaging, optical tomography, image reconstruction, heterogeneous objects

1. Introduction

Fluorescence diffuse optical tomography (FDOT), also known as fluorescence molecular tomography (FMT), is an optical technique that allows the 3D reconstruction of the distribution of exogenous fluorescent markers. It has been mainly adopted for *in vivo* preclinical imaging in small animals [1–3]. FDOT consists in illuminating a sample with

light patterns (e.g. points or more complex shapes) and detecting the fluorescence light exiting the sample [4; 5]. Multiple illumination-detection combinations are generally considered for different angles of view of the sample, which improves the spatial resolution of the reconstruction[6–8].

As discussed in [9], tomographic reconstruction of the fluorescent marker distribution generally consists in i) solving the forward problem that describes light propagation through the sample and ii) solving the inverse problem given a forward model. The inverse problem is very ill-posed and thus fluorescence reconstruction highly depends on the accuracy of the forward model itself [10].

The diffusion approximation is generally adopted to solve the forward problem. This partial differential equation, which may be solved by means of the finite element method [11; 12] or the boundary element method [13; 14], requires the knowledge of several optical parameters, principally the absorption coefficient μ_a and reduced scattering coefficient μ'_s at each optical wavelength being measured, as well as the refractive index of the medium, insofar as it affects the determination of correct boundary conditions. One of the major difficulties of FDOT is to estimate the distribution of these optical parameters, which is even more critical when highly heterogeneous objects such as biological samples (e.g. mouse) are considered.

One practical solution has been to assume the sample to be optically homogeneous and consider the ratio between measurements at fluorescence and excitation wavelength. The so-called normalized Born (nBorn) method was originally proposed by Ntziachritos *et. al.* [15] to correct for experimental factors such as detector gains and coupling losses. Interestingly, it also proved efficient to minimize the fluorescence reconstruction artifacts that appear in the presence of optical heterogeneities [16]. Although the state-of-the-art nBorn approach is effective in the case of absorbing heterogeneities, it presents severe limitations when scattering heterogeneities are present [17; 18].

In the last years, FDOT research has focused on multi-modality approaches such as X-ray computed tomography-FDOT (CT-FDOT) [19–21], X-ray phase-contrast CT-FDOT [22], magnetic resonance imaging-FDOT (MRI) [23; 24], single photon emission computed tomography-CT-FDOT [25], or positron emission tomography-FDOT [26]. Traditionally, the volume obtained from the concurrent modality (e.g. CT or MRI) is segmented into different anatomical segments (e.g. organs or tissue types) that can be used to constrain the resolution of the FDOT problem [19–22; 27; 28]. Semi-automatic approaches eliminating the need for prior image segmentation have also been proposed [29]. More recently, the knowledge of the anatomical segments has been exploited to improve the accuracy of the forward model, which results in an improved reconstruction quality. This is usually done by a segment-and-assign strategy, which consists in assigning a couple of optical properties to each of the anatomical segments prior to FDOT reconstruction. In [22], segmentation is performed from a phase-contrast CT scan of the mouse *ex-vivo*, while conventional CT [25; 30] or MRI [23; 31] acquired *in vivo* can be also considered. Segmentation is usually limited to four to six segments. However, choosing the right optical parameters for each segment is very challenging.

Despite many studies, the optical properties of the tissues have not yet been fully established, due to inter-subject variability and measurements being predominantly performed using *ex vivo* tissues. Moreover, anatomical information provided by a non-optical concurrent imaging modality is only partially correlated with the optical parameters.

Therefore, it is highly desirable to recover the optical properties of the heterogeneities from optical measurements, which can be done by performing a diffuse optical tomography (DOT) reconstruction at the excitation wavelength [32–38]. However, continuous wave (CW) measurements at a single wavelength cannot resolve both absorption and scattering coefficients [39]. Although it is possible to reconstruct only the absorption coefficient while assigning prior values to the scattering coefficient [38], effective unmixing of absorption and scattering requires time-resolved/frequency domain or multispectral measurements. Unfortunately, these two approaches show various drawbacks, such as the complexity of the experimental set-up, a lower signal-to-noise ratio, and huge data sets that are difficult to be managed by the inversion algorithms. In practice, FDOT measurements are often performed in CW mode, especially in the case of a multi-modality instrumentation for which technical constraints push towards the use of simple experimental systems

The authors recently proposed the idea to reconstruct the so-called optical inhomogeneity map from CW DOT measurements and then to solve the FDOT problem [40]. The inhomogeneity map, which depends on both the absorption and scattering of the optical heterogeneities, allows the inaccuracies in the homogeneous FDOT forward problem to be corrected. Capitalizing on this work, we propose a new reconstruction method for FDOT, namely the inhomogeneous nBorn (i-nBorn) method, that generalizes the nBorn method. This new method is based on the joint solution of two inverse problems, which are both ill-posed and require the use of regularization schemes to recover an acceptable solution.

In this contribution, we describe a two-step reconstruction algorithm for the i-nBorn method. The first step implements a projected Gauss-Newton algorithm, which can accommodate different types of penalty terms, to reconstruct the sample inhomogeneities. The second step, which includes the inhomogeneity map recovered at the first step in the forward model, consists in the fluorescence image reconstruction using anisotropic diffusion (AD) regularization. To the best of our knowledge, this is the first implementation of the i-nBorn method to be fed up with experimental data.

The algorithm we propose easily integrates the use of structured light illumination and measurement compression, which are dimension reduction approaches that greatly reduce the acquisition and reconstruction times. Structured light is based on the illumination of the object by a small number of light patterns. Patterns can be chosen among natural basis such as Fourier [41] or wavelet [42], using singular value decomposition [43; 44] or applying the compressed sensing paradigm [45]. Different reconstructions schemes have been designed to handle large data sets, e.g. analytic method [46] or matrix free methods [28; 47]. Another approach is measurement

compression, which can be considered as a preprocessing step where the measured images are (wavelet) compressed and the most significant basis function are retained to build the forward model with reduced dimensionality [5; 48].

The paper is organized as follows. In Section 2, we introduce the i-nBorn approach that is designed for fluorescence reconstruction in the presence of optical heterogeneities. In Section 3, we present an overview of our reconstruction method, which is based on the resolution of two inverse problems. First, we introduce dimensionality reduction through measurement compression. Then, we formalize the two inverse problems and explain how we solve them. Next, we describe how to build the forward problems. Finally, we provide a detailed description of our algorithm. In Section 4, we discuss the phantom experiments and the figures of merit of the reconstructions. We present our results in Section 5, discuss them in Section 6, and conclude in Section 7.

2. Fluorescence diffuse optical tomography in the presence of heterogeneities

We consider an object domain Ω with absorption coefficient $\mu_a(\mathbf{r})$, $\mathbf{r} \in \Omega$, and reduced scattering coefficient $\mu'_s(\mathbf{r})$, $\mathbf{r} \in \Omega$, that has embedded within it a fluorescent dye. Let $h(\mathbf{r})$, $\mathbf{r} \in \Omega$, be the unknown fluorescence yield, which is related to the concentration of the fluorescent dye. The FDOT image reconstruction problem consists in solving the following inverse problem

$$\Gamma^f = A^f h, \quad (1)$$

where Γ^f is the fluorescence signal measured at the emission wavelength λ^f and A^f is the forward operator.

2.1. nBorn method

The forward operator A^f strongly depends on the optical properties of the object, which are unknown. If the operator A^f is built from estimated optical properties, the resulting model error dramatically degrades the reconstruction quality. A practical way of alleviating this problem has been to normalize data, which leads to the normalized FDOT problem

$$\Gamma^n = A^n h, \quad \text{with } \Gamma^n = \frac{\Gamma^f}{\Gamma^x}, \quad (2)$$

where Γ^x is the signal measured at the excitation wavelength λ^x and A^n is the normalized forward operator computed assuming homogeneous optical properties. Despite the very good results obtained in many configurations, it has been shown that the nBorn method does not compensate for the effect of unknown optical heterogeneities, especially scattering [17; 18].

2.2. Full DOT-FDOT approach

One possibility to improve the nBorn method is to address the full DOT-FDOT problem for which μ_a , μ'_s and h are all recovered and refractive index is assumed known [32–36]. It consists in jointly (either sequentially or simultaneously) solving a pair of inverse problems. When the optical properties of the object are assumed to be the same at λ^x and λ^f we have

$$\Gamma^x = F(\mu_a, \mu'_s) \quad \text{and} \quad (3a)$$

$$\Gamma^n = A^n(\mu_a, \mu'_s)h. \quad (3b)$$

where F is the (non-linear) excitation forward model. The pair of maps (μ_a, μ'_s) may be recovered from the DOT problem of (3a) and then used to build A^n in the FDOT problem of (3b). However, when CW measurements are considered, the DOT problem has no unique solution [39]. Different pairs of maps (μ_a, μ'_s) may satisfy (3a) while resulting into a fluorescence forward model A^n that is subject to model error.

2.3. Inhomogeneous nBorn approach

In a previous work [40], we suggested an approach that allows DOT-FDOT reconstruction to be performed from CW data. The key idea is to recast the forward problem from a solution to a diffusion equation into a solution of the equivalent Helmholtz equation

$$(\nabla^2 + \eta) \Psi = s \quad (4)$$

where η is a scalar optical property with units of reciprocal squared length, defined as $\eta = \nabla^2(\kappa^{\frac{1}{2}})/\kappa^{\frac{1}{2}} + \mu_a/\kappa$, $\kappa = \frac{1}{3}(\mu'_s + \mu_a)^{-1}$ is the diffusion coefficient inside Ω and Ψ and s are the transformed fluence and source terms. The system of equations (3a)–(3b) may now be rewritten as

$$\Gamma^x = G(\eta), \quad (5a)$$

$$\Gamma^n = B(\eta)\Upsilon, \quad (5b)$$

where Υ is a modified fluorescence yield that is given by

$$\Upsilon = \frac{h}{\kappa}. \quad (6)$$

The strategy to recover h is the following. First, the nonlinear problem of (5a) is solved and an optical inhomogeneity map η , which depends on the optical heterogeneities of the medium, is obtained. Second, the η map is used to build the forward model B and the linear problem of (5b) is solved, providing the Υ map. Finally, the unknown fluorescence yield is given by

$$h = \hat{\kappa}\Upsilon, \quad (7)$$

where $\hat{\kappa}$ is chosen, in practice, as an estimate for κ . In this manuscript, we assume κ is slowly varying. Hence, we have the following approximation:

$$\hat{\kappa} \simeq \frac{\hat{\mu}_a}{\eta}, \quad (8)$$

where $\hat{\mu}_a$ is an estimate for the absorption coefficient, chosen as a constant.

3. Reconstruction overview

3.1. Data Acquisition and Compression

The object Ω is illuminated at I view angles. At each angle, a set of J source patterns is projected onto the object. Such an acquisition results in a set of IJ excitation images and IJ fluorescence images. Let $\mathbf{m}_{i,j}^x$ and $\mathbf{m}_{i,j}^f$ be the excitation and fluorescence images, respectively, measured at the i th view after illumination with the j th source pattern. In the following sections, we use a vector representation for the images, i.e. $\mathbf{m}_{i,j}^x \in \mathbb{R}^P$ and $\mathbf{m}_{i,j}^f \in \mathbb{R}^P$, where P is the number of pixels. The normalized fluorescence image is defined by

$$\mathbf{m}_{i,j}^n = \frac{\mathbf{m}_{i,j}^f}{\mathbf{m}_{i,j}^x}, \quad (9)$$

where the division is component-wise (pixel-wise). Each of the IJ excitation images, as well as each of the IJ normalized fluorescence images, are compressed by applying a wavelet transform $\mathbf{D}$ and retaining their K most relevant wavelet components. The data for each forward problem then consists of the IJK retained components stacked into a vector with components

$$\Gamma_{i,j,k} = \langle \mathbf{d}_{i,j,k}^f, \mathbf{m}_{i,j} \rangle, \quad (10)$$

where $\mathbf{d}_{i,j,k}^f \in \mathbb{R}^P$ is the wavelet vector associated with the k^{th} component of the image acquired from the j^{th} illumination pattern at the i^{th} angle.

3.2. Inverse problems

We consider the reconstruction of the unknown quantities $\boldsymbol{\eta} \in \mathbb{R}^N$ and $\mathbf{h} \in \mathbb{R}^N$, where N is the number of voxels, from the measured data $\boldsymbol{\Gamma}^x \in \mathbb{R}^{IJK}$ and $\boldsymbol{\Gamma}^n \in \mathbb{R}^{IJK}$ given the discrete forward models $\mathcal{G}$ and $\mathbf{B}$. The unknown quantities are obtained minimizing the cost functions

$$\mathcal{L}_{\text{dot}}(\boldsymbol{\eta}) = \frac{1}{2} \|\boldsymbol{\Gamma}^x - \mathcal{G}(\boldsymbol{\eta})\|^2 + \alpha \mathcal{R}_{\text{dot}}(\boldsymbol{\eta}) \quad \text{and} \quad (11a)$$

$$\mathcal{L}_{\text{fdot}}(\boldsymbol{\Upsilon}) = \frac{1}{2} \|\boldsymbol{\Gamma}^n - \mathbf{B}\boldsymbol{\Upsilon}\|^2 + \beta \mathcal{R}_{\text{fdot}}(\boldsymbol{\Upsilon}), \quad (11b)$$

where α (resp. β) is a regularization parameter that sets the trade-off between the data fidelity $\frac{1}{2} \|\boldsymbol{\Gamma}^x - \mathcal{G}(\boldsymbol{\eta})\|^2$ (resp. $\frac{1}{2} \|\boldsymbol{\Gamma}^n - \mathbf{B}\boldsymbol{\Upsilon}\|^2$) and the penalty function $\mathcal{R}_{\text{dot}}$ (resp. $\mathcal{R}_{\text{fdot}}$).

Penalty functions have long been confined to ℓ_2 -norm regularization that promotes the smoothness of the solution [19–22; 49]. More recently, penalty functions based on ℓ_1 -norm have received a lot of attention, since they promote sparse solutions [26; 35; 36; 50; 51]. The DOT problem has also been formulated as a joint sparse recovery problem with a ℓ_0 -norm penalty, which assumes that optical heterogeneities have a small support [52].

In the following we present our minimization framework for both $\mathcal{L}_{\text{dot}}$ and $\mathcal{L}_{\text{fdot}}$. Remind that $\boldsymbol{\eta}$ is required to build $\mathbf{B}$, hence, (11a) has to be solved before (11b).

3.2.1. Solution of the DOT problem The DOT cost function given at (11a) is minimized using a Gauss-Newton algorithm with an inequality constrain of the form $\eta_{\min} \leq \eta$. The Gauss-Newton method is a traditional tool for non linear minimization, which iteratively solves $\min_{\boldsymbol{\eta}} \mathcal{L}(\boldsymbol{\eta})$ starting with an initial guess $\boldsymbol{\eta}^0$ and building new estimates $\boldsymbol{\eta}^{\ell+1} = \boldsymbol{\eta}^{\ell} + \tau^{\ell} \Delta \boldsymbol{\eta}^{\ell}$, where $\Delta \boldsymbol{\eta}^{\ell}$ is the Gauss-Newton step and τ^{ℓ} is the step length.

$$(\mathbf{J}^{\ell\top} \mathbf{J}^{\ell} + \alpha \mathbf{C}^{\ell}) \Delta \boldsymbol{\eta}^{\ell} = -\mathbf{g}^{\ell}, \quad (12)$$

where $\mathbf{J}^{\ell}$ is the Jacobian matrix of $\mathcal{G}$ about $\boldsymbol{\eta}^{\ell}$ and $\mathbf{C}^{\ell}$ is the Hessian matrix of $\mathcal{R}_{\text{dot}}$ about $\boldsymbol{\eta}^{\ell}$. The vector $\mathbf{g}^{\ell}$, which denotes the gradient of $\mathcal{L}$ at $\boldsymbol{\eta}^{\ell}$, is given by

$$\mathbf{g}^{\ell} = -\mathbf{J}^{\ell\top} (\mathbf{\Gamma}^{\text{n}} - \mathcal{G}^{\ell}) + \alpha \nabla \mathcal{R}_{\text{dot}}^{\ell}, \quad (13)$$

where $\mathcal{G}^{\ell} = \mathcal{G}(\boldsymbol{\eta}^{\ell})$ is the forward estimate and $\nabla \mathcal{R}_{\text{dot}}^{\ell}$ is the gradient of $\mathcal{R}_{\text{dot}}$ at $\boldsymbol{\eta}^{\ell}$. Assuming the optical inhomogeneity map to be piecewise constant, we choose

$$\mathcal{R}_{\text{dot}}(\boldsymbol{\eta}) = \text{TV}(\boldsymbol{\eta}), \quad (14)$$

where TV is the total variation semi-norm. To ensure the global convergence of the algorithm, a line search along the direction $\Delta \boldsymbol{\eta}^{\ell}$ is performed, the best step length being retained. The inequality constrain has been implemented considering the fixed-variable method described in [53].

In the following, we denote $\hat{\boldsymbol{\eta}}$ the solution obtained after convergence of the iterative process.

3.2.2. Solution of the FDOT problem The FDOT cost function (11b) is minimized considering the split operator method introduced in [54], considering a regularization penalty of the form

$$\mathcal{R}_{\text{fdot}}(\boldsymbol{\Upsilon}) = \int_{\Omega} p(|\nabla \mathbf{h}|) \, \text{d}\Omega, \quad (15)$$

where p is an edge-preserving potential function. The minimizer of (11b) is the solution of

$$\mathbf{B}^{\top} (\mathbf{B} \boldsymbol{\Upsilon} - \mathbf{\Gamma}^{\text{n}}) = -\beta \mathcal{D}(\boldsymbol{\Upsilon}) \boldsymbol{\Upsilon}, \quad (16)$$

where the right-hand side term is the nonlinear anisotropic diffusion with $\mathcal{D}(\Upsilon) = -\nabla \cdot \left[\exp \left[- \left(\frac{|\nabla \Upsilon|}{T} \right)^2 \right] \nabla \right]$, where the parameter T is the threshold [54–56]. The solution is obtained using the two-step iterative method described in [54].

3.3. Forward problems

In this section, we discuss the calculation of the Jacobian matrix $\mathbf{J}^\ell$, forward estimate $\mathcal{G}^\ell$, and weight matrix $\mathbf{B}$ required in (12), (13), and (16), respectively. All the three quantities require an appropriate model for the propagation of light within the object Ω .

Assuming κ is known on the boundary $\partial\Omega$, we have the following discrete formulation for (4) using a finite element method (FEM) implementation [11]:

$$\mathbf{H}(\boldsymbol{\eta})\boldsymbol{\Psi} = \mathbf{s} \quad (17)$$

where $\mathbf{H}(\boldsymbol{\eta}) \in \mathbb{R}^{N \times N}$ is the Helmholtz operator that only depends on $\boldsymbol{\eta}$, $\boldsymbol{\Psi} \in \mathbb{R}^{N \times 1}$ is the pseudo photon density vector (which is related to the measured data as detailed in appendix A), and $\mathbf{s} \in \mathbb{R}^{N \times 1}$ is the source vector. The propagation operator has been computed using the Matlab TOAST package [57].

The forward estimate $\mathcal{G}^\ell$ is of size $IJK \times 1$. The (i, j, k) th entry of $\mathcal{G}^\ell$ is denoted $\mathcal{G}_{i,j,k}^\ell \in \mathbb{R}$. By definition, it can be computed as

$$\mathcal{G}_{i,j,k}^\ell = \langle \mathbf{d}_{i,j,k}^x, \boldsymbol{\psi}_{i,j}^\ell \rangle \quad (18)$$

where $\boldsymbol{\psi}_{i,j}^\ell$ is obtained solving (17) with $\mathbf{s} = \mathbf{s}_{i,j}$ at iteration ℓ .

The Jacobian matrix $\mathbf{J}^\ell$ is of size $IJK \times N$. The (i, j, k) th row of $\mathbf{J}^\ell$ is denoted $\mathbf{j}_{i,j,k}^\ell \in \mathbb{R}^N$. It may be shown that [9]

$$\mathbf{j}_{i,j,k}^\ell = \boldsymbol{\psi}_{i,j}^\ell \circ \boldsymbol{\psi}_{i,j,k}^\ell, \quad (19)$$

where $\boldsymbol{\psi}_{i,j,k}^\ell$ is the adjoint solution of (17) for $\mathbf{s} = \mathbf{d}_{i,j,k}^x$ at iteration ℓ . The symbol $\circ$ denotes the Hadamard product.

The weight matrix $\mathbf{B}$ is of size $IJK \times N$. The (i, j, k) th row of $\mathbf{B}$ is denoted $\mathbf{b}_{i,j,k} \in \mathbb{R}^N$. As shown in appendix [Appendix A](#), it can be computed as

$$\mathbf{b}_{i,j,k} = \boldsymbol{\psi}_{i,j} \circ \boldsymbol{\psi}_{i,j,k}, \quad (20)$$

where $\boldsymbol{\psi}_{i,j}$ is the solution of (17) with $\mathbf{s} = \mathbf{s}_{i,j}$ at the final iteration of step 1 while $\boldsymbol{\psi}_{i,j,k}$ is the adjoint solution of (17) with $\mathbf{s} = \mathbf{d}_{i,j,k}^n / \boldsymbol{\psi}_{i,j}$ (element-wise division).

4. Material and methods

4.1. Experimental set-up

In the following paragraph a brief description of the experimental set-up is reported. A more detailed description can be found in [42; 58]. The light emitted by a diode

Figure 1. Bottom view of the epoxy resin phantoms used in the experiments. Phantom 1 is depicted on the left and phantom 2 on the right. Both phantoms are cylinders of diameter 20 mm and height 80 mm. Red full line (—) indicates absorbing inclusions, green dashed line (--) fluorescence inclusions, and orange dotted line (···) scattering inclusions. The diameter and length of inclusions 1 to 5 are reported in Table 1 and 2. The paths $\mathcal{P}_1$ and $\mathcal{P}_2$ are used to plot profiles in Fig. 6.

inclusion	1	2	3	4
$\varnothing$ (mm)	4	2	2	2
L (mm)	30	21	21	30
μ_a (mm ⁻¹)	0.20	0.02	0.20	0.02
μ'_s (mm ⁻¹)	1.00	1.00	1.00	1.00
η (mm ⁻²)	0.72	0.06	0.72	0.06
dye	no	yes	no	yes

Table 1. Inclusions in phantom 1. The diameter ($\varnothing$), length (L), and optical properties of the heterogeneities are reported.

inclusion	1	2	3	4	5
$\varnothing$ (mm)	4	2	2	2	2
L (mm)	30	21	21	30	21
μ_a (mm ⁻¹)	0.02	0.02	0.20	0.20	0.02
μ'_s (mm ⁻¹)	5.00	1.00	1.00	1.00	1.00
η (mm ⁻²)	0.30	0.06	0.72	0.72	0.06
dye	no	yes	no	no	yes

Table 2. Inclusions in phantom 2. The diameter ($\varnothing$), length (L), and optical properties of the heterogeneities are reported.

laser (wavelength of 630 nm, power ≈ 10 mW) is spatially modulated by means of a digital micromirror device (DMD) (Discovery 1100 - ALP1, Vialux), which creates different patterns that are projected onto the sample surface through an objective lens. The sample is placed on a motorized rotational stage in order to acquire multiple views. In particular, measurements have been carried out on biological tissue mimicking phantoms. The light exiting the sample surface is collected by an objective lens ($f = 50$ mm, $f\# = 2.8$, Nikon Co.) and projected on a low noise 16-bit cooled (-40 °C) CCD camera (Versarray 512, Princeton Instruments). In order to discriminate fluorescence from excitation light, a high-pass filter (RG-695, Schott) in conjunction with an interference filter (XF 3076, Omega) have been inserted in front of the objective lens.

The phantom is an epoxy resin cylinder of diameter 20 mm and height 80 mm. Appropriate concentrations of toner powder and TiO_2 particles have been added to the resin so as to simulate the absorption and scattering parameters of biological tissues. The optical properties of the phantom have been measured by means of a time-resolved diffused optical spectroscopy system [59]. The following values have been obtained at 630 nm: $\mu_a = 0.02 \text{ mm}^{-1}$ and $\mu'_s = 1 \text{ mm}^{-1}$. In order to simulate inclusions, cylindrical holes have been drilled into the phantom at different positions (see Fig. 1). The diameter and length of the inclusions are reported in Table 1 and 2. Each of the inclusions can be independently filled with a liquid solution whose optical properties differ from the background. In the case of absorbing/scattering inclusions, the solution is made of ink and intralipid® and by changing their concentrations it is possible to modify the absorption and scattering coefficients, respectively. Fluorescent inclusions have been obtained filling the holes with a fluorescent dye (Nile Blue dye concentration of $30 \mu\text{M}$). In particular, two phantoms of increasing complexity have been prepared, as shown in Fig. 1. The optical properties of the inclusions for both phantoms are reported in Table 1 and 2. In the first phantom, two absorbing cylindrical inclusions (labels 1 and 3 according to Fig. 1) and two fluorescent inclusions (labels 2 and 4) have been inserted. In the second phantom, two absorbing inclusions (labels 3 and 4), one scattering inclusion (label 1), and two fluorescent inclusions (labels 2 and 5) have been inserted.

Measurements at both excitation and fluorescence wavelengths have been carried out in transmission every 18° , resulting in $I = 20$ views. For simplicity, only $J = 1$ uniform source pattern has been considered at each view angle.

4.2. Practicalities

Mesh The mesh used to solve the Helmholtz-like equation consists of 42886 tetrahedral elements connected by 7468 vertices and is displayed in Fig. 2a. It was obtained considering the DMD-CCD-based method proposed in [42], which can handle any convex sample without requiring any extra device. The main steps are the following. First, uniform illumination patterns were projected onto the sample and the resulting shadow images were recorded rotating the sample with a step angle of 1° . Then, the obtained

stack of shadow images was filtered backprojected, which results in a 3D volume that was thresholded to get a binary volume indicating the volume occupied by the sample. Finally, the *iso2mesh* mesh generator was employed [60] to compute the mesh from the binary volume.

Illumination/detection areas The illumination and detection areas (see Fig. 2 c and d) are determined from the shadow images. For each measurement angle, the detection area is chosen as a rectangle that fits within the sample. To avoid camera saturation during excitation measurements, the detection area is narrower than the phantom diameter. The retained size was $34 \text{ mm} \times 17 \text{ mm}$. For each view, the illumination area is obtained by symmetry on the opposite side of the object (see Fig. 2b). Illumination and detection areas all start 2 mm away from the top of the phantom.

Image preprocessing The recorded excitation and fluorescence images are of size 256×256 (see Fig. 2c and 2d). All of them are cropped to the detection area and resampled so as to get 128×64 rectangular images. Then, the fluorescence images are wavelet transformed (Daubechies 4 wavelet basis) using the *wavelab* software [61]. Finally, for each image, the $K = 64$ most significant wavelet basis are retained to build the detection patterns $\mathbf{d}_{i,j,k}$ introduced in (10).

Reconstruction The grid we consider to reconstruct both the inhomogeneity and the fluorescence maps is regular and consists of $N = 30 \times 29 \times 59$ voxels of size $(0.75 \text{ mm})^3$. Note that this grid differ from the grid where the binary volume used to create the mesh is defined. We chose $\mu_a = 0.02 \text{ mm}^{-1}$ and $\mu'_s = 1 \text{ mm}^{-1}$ to build the weight matrix of the nBorn method. The initial guess for η required by the i-nBorn method was obtained considering the same values, i.e. choosing $\eta^0 = 3\mu_a(\mu_a + \mu'_s) \approx 6 \times 10^{-2} \text{ mm}^{-2}$. The estimate of the absorption coefficient $\hat{\mu}_a$ was set to 0.02 mm^{-1} while the optimization bound $\eta_{\min}$ was set to $\frac{1}{2}\eta^0$.

4.3. Performance metrics

The reconstruction quality has been assessed by means of three main objective performance metrics. First, the Pearson correlation has been considered as a global metric that indicates how well two volumes are linearly correlated. Given the ground-truth h^{true} and reconstructed fluorescence distribution h^{rec} , the Pearson correlation ρ is defined by

$$\rho = \frac{\text{cov}(h^{\text{rec}}, h^{\text{true}})}{\sigma(h^{\text{rec}})\sigma(h^{\text{true}})}, \quad (21)$$

where cov is the covariance and σ the standard deviation. A large ρ indicates a high correlation between the images.

Second, the contrast-to-noise ratio (CNR) has been considered. It is defined by

$$\mathcal{C}_{\text{roi,back}} = \frac{\mu_{\text{roi}} - \mu_{\text{back}}}{(w_{\text{roi}}\sigma_{\text{roi}}^2 + w_{\text{back}}\sigma_{\text{back}}^2)^{1/2}}, \quad (22)$$

Figure 2. a) Mesh of the object b) Detection and illumination areas for the first view angle c) image at excitation wavelength d) image at fluorescence wavelength. The rectangles in (c) and (d) indicate the detection area.

where μ_{roi} (μ_{back}) and σ_{roi} (σ_{back}) are the average and standard deviation of h^{rec} in the region-of-interest Ω_{roi} (background Ω_{back}) and w_{fluo} (w_{back}) is the ratio of the volume occupied by the two fluorescent inclusions (the rest of the volume).

We define the global CNR $\mathcal{C}$ by choosing

$$\Omega_{\text{roi}} = \Omega_A \cup \Omega_B \quad \text{and} \quad \Omega_{\text{back}} = \Omega \setminus \Omega_{\text{roi}}, \quad (23)$$

where Ω_A (resp. Ω_B) is the support of the first (resp. second) fluorescent inclusion. The larger the CNR, the better.

Last, the relative quantification factor $\mathcal{Q}$ is introduced as a measure of the quantitiveness of the reconstruction. We define

$$\mathcal{Q} = \min \left(\frac{\mathcal{C}_A}{\mathcal{C}_B}, \frac{\mathcal{C}_B}{\mathcal{C}_A} \right), \quad (24)$$

where $\mathcal{C}_A$ (resp. $\mathcal{C}_B$) is the CNR of inclusion A (resp. B), which is obtained choosing $\Omega_{\text{roi}} = \Omega_A$ (resp. $\Omega_{\text{roi}} = \Omega_B$) and $\Omega_{\text{back}} = \Omega \setminus (\Omega_A \cup \Omega_B)$. The closer the relative quantification is to 1, the better.

4.4. Choice of the regularization parameters

The reconstruction quality dramatically depends on the choice of the regularization parameters α and β given in (11a) and (11b), respectively. While the best α has been chosen from visual inspection, β has been chosen by optimizing an objective performance metric, which enables fair comparisons of the reconstructions. The retained performance metric is the global CNR.

5. Results

The fluorescence distribution h was reconstructed from the same data sets considering both the i-nBorn method and the state-of-the-art nBorn method. The nBorn method

Figure 3. Optical inhomogeneity maps (in mm^{-2}). a) ground truth in phantom 1, b) reconstruction in phantom 1, c) ground truth in phantom 2, b) reconstruction in phantom 2. Slices at increasing z are displayed from top left to bottom right. Sparsity priors (14) and (15) were considered.

requires to solve (2), which is an ill-posed inverse problem that requires regularization. To ensure fair comparison between the nBorn and the proposed i-nBorn method, we solve (2) and (5b) the same way, i.e., minimizing a cost function of the form (11b). To show the universality of our approach, not only the sparsity priors promoted by the regularizers given by (14) and (15) were considered, but also more classical regularity priors of the form $\mathcal{R}_{\text{dot}}(\boldsymbol{\eta}) = \|\Delta\boldsymbol{\eta}\|_2^2$ and $\mathcal{R}_{\text{fdot}}(\boldsymbol{\Upsilon}) = \|\boldsymbol{\Upsilon}\|_2^2$ [19–22; 49].

Slices of the inhomogeneity maps reconstructed in both phantoms are shown in Fig. 3. Three-dimensional rendering (Volume Viewer ImageJ plugin) of the fluorescence reconstructions in phantom 1 and phantom 2 are reported in Fig. 4 and 5, respectively. For both phantom reconstructions, the fluorescence profiles obtained along paths $\mathcal{P}_1$ and $\mathcal{P}_2$ (refer to Fig. 1 to localize the paths) are depicted in Fig. 6 considering sparsity priors as well as regularity priors. Finally, the performance metrics introduced in section 4.3 were used to evaluate reconstructions in both phantoms considering the two approaches. The metrics are reported in Table 3 for reconstructions performed with sparsity priors and in Table 4 for reconstructions performed with regularity priors.

In phantom 1, we observe a clear advantage of the proposed approach over the standard nBorn method as can be observed visually in the 3D rendering of Fig. 4 and in the profiles of the top row of Fig. 6. In particular, the nBorn reconstruction is unable to resolve separately the two inclusions as our proposed approach does. This is quantitatively confirmed with the increase of the global CNR of the reconstructed volume $\mathcal{C}$ and its correlation with the ground truth ρ (see Table 3 and Table 4). Specifically, we observe a 36 % increase (resp. 23 %) of ρ and a 42 % increase (resp.

Figure 4. Fluorescence reconstructions in phantom 1. a) ground truth, b) standard nBorn reconstruction, c) reconstruction obtained with the proposed i-nBorn algorithm. Sparsity priors (14) and (15) were considered.

Table 3. Performance metrics of the fluorescence reconstructions considering sparsity priors, i.e., $\mathcal{R}_{\text{dot}}(\boldsymbol{\eta}) = \text{TV}(\boldsymbol{\eta})$ and $\mathcal{R}_{\text{fdot}}(\boldsymbol{\Upsilon})$ given by (15)

Phantom	method	ρ	$\mathcal{C}$	$\mathcal{Q}$
—	perfect	1	∞	1
1	nBorn	0.305	2.28	0.85
1	proposed	0.416	3.25	0.72
2	nBorn	0.197	1.96	0.17
2	proposed	0.274	2.79	0.79

28 %) of $\mathcal{C}$ for the sparsity (resp. smooth) priors. Improvements are obtained for both prior types, which suggests the i-nBorn method outperforms the standard nBorn method regardless the penalty functional chosen for regularization. A small decrease of 15 % (resp. 1 %) of the relative quantification $\mathcal{Q}$ is observed in phantom 1 with sparsity (resp. smooth) priors.

In phantom 2, similar results are obtained. As shown in Fig. 5 and in the bottom row of Fig. 6, the two fluorescent inclusions cannot be separated considering nBorn-based reconstruction while they can be well discriminated and localized by means of the proposed method. Specifically, we observe a 39 % increase (resp. 11 %) of ρ

Figure 5. Fluorescence reconstructions in phantom 2. a) ground truth, b) standard nBorn reconstruction, c) reconstruction obtained with the proposed i-nBorn algorithm. Sparsity priors (14) and (15) were considered.

Table 4. Performance metrics of the fluorescence reconstructions considering regularity priors, i.e., $\mathcal{R}_{\text{dot}}(\boldsymbol{\eta}) = \|\Delta\boldsymbol{\eta}\|_2^2$ and $\mathcal{R}_{\text{fdot}}(\boldsymbol{\Upsilon}) = \|\boldsymbol{\Upsilon}\|_2^2$

Phantom	method	ρ	$\mathcal{C}$	$\mathcal{Q}$
–	perfect	1	∞	1
1	nBorn	0.343	2.58	0.96
1	proposed	0.424	3.31	0.95
2	nBorn	0.211	2.11	0.37
2	proposed	0.235	2.36	0.87

and a 42 % increase (resp. 12 %) of $\mathcal{C}$ for the sparsity (resp. smooth) priors. The advantage of the proposed method is even more evident due to the higher complexity of the absorbing/scattering heterogeneities distribution. Beyond the higher number of heterogeneities and their variability –both absorbing and scattering inclusions are present, the distance between the two fluorescent inclusions is smaller in phantom 2 than in phantom 1 (see Fig. 1). For this phantom, we observe a dramatic increase of the relative quantification $\mathcal{Q}$, which is increased by a factor of 3.7 for sparsity priors and by a factor of 1.37 for smooth priors.

Finally, we remark that the relative quantification is much better in phantom 1 than

Figure 6. Reconstructed fluorescence profiles considering the nBorn approach (green line marked with $\triangleright$) and our method (red line marked with $\times$). The phantom profiles are provided for comparison (blue solid line marked with $\circ$). In (a) and (b), the sparsity priors $\mathcal{R}_{\text{dot}}(\boldsymbol{\eta}) = \text{TV}(\boldsymbol{\eta})$ and $\mathcal{R}_{\text{fdot}}$ given in (15) are considered. In (c) and (d), the smooth priors $\mathcal{R}_{\text{dot}}(\boldsymbol{\eta}) = \|\Delta\boldsymbol{\eta}\|_2^2$ and $\mathcal{R}_{\text{fdot}}(\boldsymbol{\Upsilon}) = \|\boldsymbol{\Upsilon}\|_2^2$ are chosen. Profiles are plotted along path $\mathcal{P}_1$ (see (a) and (c)) and path $\mathcal{P}_2$ (see (b) and (d)). For each of the four cases, the reconstructed fluorescence distributions have been normalized to a unit marker quantity such that $\int h(\mathbf{r}) d\Omega = 1 \mu\text{mol}$.

in phantom 2 when the standard nBorn method is considered while the proposed i-nBorn algorithm tends to provide similar quantification capabilities whatever the complexity of the phantom and the priors used in the reconstruction algorithm.

6. Discussion

Our approach represents a simple and effective way to experimentally capture the optical inhomogeneities needed to accurately model light propagation within biological tissues. We demonstrated that an optical inhomogeneity map can be recovered from CW measurements in tissue mimicking phantoms. Even without discriminating absorbing from scattering inclusions, the proposed method proved efficient to improve the quality of the fluorescence reconstructions. In particular, an increase of the CNR and correlation of the reconstruction with the ground truth is observed in all our measurements. The dramatic loss of quantification capabilities, which has already been reported elsewhere for the nBorn approach in the presence of complex phantoms [17], can be alleviated considering our approach. This could be a fundamental step towards applications such as follow-up studies in oncology.

It is worth noting that, in this study, only one illumination pattern was considered per view angle, which allowed the acquisition time to be drastically reduced compared to standard illumination schemes based on point source scanning. While the nBorn approach failed to provide satisfactory reconstruction with such an illumination scheme, the i-nBorn provided improved resolution, which could contribute to the emergence of fast acquisition schemes.

These results confirm the importance to incorporate the optical heterogeneities into the forward model involved in FDOT reconstructions [30; 31; 37; 38; 62]. They are consistent with those showing that the nBorn method only partially compensates the fluorescence reconstruction errors due to the presence of optical heterogeneities, especially in the presence of scattering inclusions [17; 18]. The advantage of the proposed i-nBorn algorithm is particularly evident in the case of phantom 2 that contains both absorbing and scattering heterogeneities as well as close fluorescent inclusions. It is worth noting that also in the simpler phantom 1, the nBorn method is outperformed by our approach. We anticipate that the advantage of the proposed approach over the standard nBorn method would be even stronger if an anatomical prior obtained by a concurrent anatomical modality is available.

The i-nBorn method can be understood as a generalisation of the standard nBorn method. Indeed, the i-nBorn method is equivalent to the nBorn method for homogeneous samples. The nBorn method provides a preliminary fluorescence reconstruction that can be improved by reconstructing the optical inhomogeneity map of the sample. It is worth reminding that the two advantages offered by the nBorn normalization, namely independence to experimental gains and optical inhomogeneity compensation, are preserved by the i-nBorn method.

As commonly assumed (see for instance [2–8]), the optical properties of the sample were considered to be the same at both excitation and fluorescence wavelengths. For applications where strong variations of optical properties are encountered, the inhomogeneity map can be reconstructed at both wavelengths. However, this comes at the cost of an extra acquisition that consists in illuminating the sample at the fluorescence wavelength. In our phantoms, μ_a is constant while μ'_s shows a decrease of about 10% between 633 nm and 700 nm [63]. Although the decrease of μ'_s is neglected, our results show that the recovered fluorescence distribution is in very good agreement with the ground truth distribution, which suggests that our method is robust to optical properties variations.

It is important to note that our method is not primarily designed to output an optical map. The inhomogeneity map we recover aims at correcting for the artefacts that occur in the fluorescence images due to inaccuracies of the homogeneous forward model. Demonstrating such a model correction effect is beyond the scope of this paper but it is one of the future works that we would like to carry out. Other ideas to correct for inaccuracies are to use an approximation error model or marginalize out errors [64; 65].

Finally, it is worth mentioning that the possibility to localize optical heterogeneities by means of CW measurements, even without discriminating between absorbing and scattering inclusions, can be of interest for different applications based on optical contrast, e.g. optical oxymetry [66] and mammography [67].

7. Conclusion

In this paper, we demonstrated the feasibility and advantage of a novel FDOT reconstruction algorithm, which is designed for highly heterogeneous samples. We showed that the inaccuracies of the homogeneous forward model affect the fluorescence images, unless they are corrected for. By reconstructing an optical inhomogeneity map from CW measurements, it is possible to fit the inaccuracies and improve the fluorescence reconstruction quality. Further studies would help to establish the limits of use of the i-nBorn method and provide *in vivo* validations. In particular, we believe that the i-nBorn method together with the proposed algorithm can be of particular interest in combination with non-optical techniques, such as MRI and CT. In such a multimodal scheme, the non-optical modality would provide high resolution *a priori* about the localization of the optical heterogeneities, while DOT measurements could provide an *in situ* optical characterization of the inhomogeneities. The combination of both types of optical information could be a fundamental step towards improved 3D resolution and quantification of fluorescence markers *in vivo*.

Acknowledgments

The research leading to these results has received funding from LASERLAB-EUROPE (grant agreement no. 284464, EC's Seventh Framework Programme). This work was performed within the framework of the LABEX PRIMES (ANR-11-LABX-0063) of Université de Lyon, within the program "Investissements d'Avenir" (ANR-11-IDEX-0007) operated by the French National Research Agency (ANR).

Appendix A. Proof of the weight matrix formula

The pseudo photon density ψ obeys the following coupled equations [40]:

$$\mathcal{H}\psi^x = s \text{ in } \Omega \quad (\text{A.1a})$$

$$\mathcal{H}\psi^f = \psi^x \Upsilon \text{ in } \Omega. \quad (\text{A.1b})$$

where $\mathcal{H}$ is the Helmholtz operator with Robin boundary conditions on $\partial\Omega$. The optical properties are assumed to be the same at both excitation and fluorescence wavelengths.

Let Σ be the portion of object surface viewed by the camera. Measurements are obtained from the photon density by means of the $\mathbb{R}(\Omega) \rightarrow \mathbb{R}(\Sigma)$ measurement operator $\mathcal{M}$. We have

$$m = \mathcal{M}\psi. \quad (\text{A.2})$$

Any compressed measurement Γ^n is the projection of the uncompressed measurement m^n onto some detection pattern d . We have:

$$\Gamma^n = \langle m^n, d \rangle_\Sigma \quad (\text{A.3})$$

where $\langle \cdot, \cdot \rangle_\Sigma$ denotes the L^2 -inner product, i.e. $\langle f, g \rangle_\Sigma = \int_\Sigma f(\mathbf{x})g(\mathbf{x}) d\mathbf{x}$. By definition of m^n , we have

$$m = \left\langle \frac{m^f}{m^x}, d \right\rangle_\Sigma \quad (\text{A.4})$$

Using (A.2), we have

$$m = \left\langle \frac{\mathcal{M}\psi^f}{\mathcal{M}\psi^x}, d \right\rangle_\Sigma \quad (\text{A.5})$$

$$= \left\langle \mathcal{M}\psi^f, \frac{d}{\mathcal{M}\psi^x} \right\rangle_\Sigma. \quad (\text{A.6})$$

Introducing the Green's operator of the Helmholtz Eqs. (A.1) leads to

$$m = \left\langle \mathcal{M}\mathcal{G}^f[\psi^x\Upsilon], \frac{d}{\mathcal{M}\psi^x} \right\rangle_\Sigma. \quad (\text{A.7})$$

By definition of the adjoint operator $\mathcal{G}^{f*}$, we have:

$$= \left\langle \psi^x\Upsilon, \mathcal{G}^{f*}\mathcal{M}^* \left[\frac{d}{\mathcal{M}\psi^x} \right] \right\rangle_\Omega \quad (\text{A.8})$$

Isolating Υ that is the quantity of interest, we obtain

$$m = \left\langle \psi^x\mathcal{G}^{f*}\mathcal{M}^* \left[\frac{d}{\mathcal{M}\psi^x} \right], \Upsilon \right\rangle_\Omega \quad (\text{A.9})$$

The operator $\mathcal{G}^f$ being self adjoint, we obtain

$$m = \left\langle \psi^x\mathcal{G}^f\mathcal{M}^* \left[\frac{d}{\mathcal{M}\psi^x} \right], \Upsilon \right\rangle_\Omega \quad (\text{A.10})$$

In practice, a measurement may be modelled as

$$\mathcal{M}\psi = f(\mathbf{r})\psi(\mathbf{r}), \quad \forall \mathbf{r} \in \Sigma \quad (\text{A.11})$$

where $f \in \mathbb{R}(\Sigma)$ depends on the optical properties, the geometry of acquisition and some gain factors. By definition of the adjoint operator that satisfies $\langle \mathcal{M}\psi, m \rangle_\Sigma = \langle \psi, \mathcal{M}^*m \rangle_\Omega$, $\forall \psi \in \mathbb{R}(\Omega)$, $m \in \mathbb{R}(\Sigma)$, we have

$$\mathcal{M}^*m = \begin{cases} f(\mathbf{r})m(\mathbf{r}), & \forall \mathbf{r} \in \Sigma \\ 0 & \forall \mathbf{r} \in \Omega \setminus \Sigma \end{cases} \quad (\text{A.12})$$

Inserting (A.11) and (A.12) into (A.10) leads to :

$$m = \left\langle \psi^x\mathcal{G}^f \left[\frac{d|_\Omega}{\psi^x} \right], \Upsilon \right\rangle_\Omega \quad (\text{A.13})$$

where $d|_\Omega = d$ for $\mathbf{r} \in \Sigma$ and 0 for $\mathbf{r} \in \Omega \setminus \Sigma$. Discretizing the previous equation completes the proof.

References

- [1] Cherry S R 2004 *Physics in Medicine and Biology* **49** R13–R48
- [2] Ntziachristos V, Bremer C and Weissleder R 2003 *European radiology* **13** 195–208 ISSN 0938-7994 URL <http://www.ncbi.nlm.nih.gov/pubmed/12541130>
- [3] Stuker F, Ripoll J and Rudin M 2011 *Pharmaceutics* **3** 229–274 ISSN 1999-4923 URL <http://www.mdpi.com/1999-4923/3/2/229/>
- [4] Chen J, Venugopal V, Lesage F and Intes X 2010 *Opt. Lett.* **35** 2121–2123 URL <http://ol.osa.org/abstract.cfm?URI=ol-35-13-2121>
- [5] Ducros N, D’andrea C, Valentini G, Rudge T, Arridge S and Bassi A 2010 *Opt. Lett.* **35** 3676–3678 URL <http://ol.osa.org/abstract.cfm?URI=ol-35-21-3676>
- [6] Zacharakis G, Ripoll J, Weissleder R and Ntziachristos V 2005 *IEEE Transactions on Medical Imaging* **24** 878–885 URL [GotoISI://000230218800007](http://ieeexplore.ieee.org/xpl/articleDetail.jsp?tp=&arnumber=150100384)
- [7] Lasser T, Soubret A, Ripoll J and Ntziachristos V 2008 *Medical Imaging, IEEE Transactions on* **27** 188–194 ISSN 1558-254X
- [8] Ducros N, Bassi A, Valentini G, Schweiger M, Arridge S and D’Andrea C 2011 *Opt. Lett.* **36** 1377–1379 URL <http://ol.osa.org/abstract.cfm?URI=ol-36-8-1377>
- [9] Arridge S R and Schotland J C 2009 *Inverse Problems* **25** 123010 (59pp) URL <http://stacks.iop.org/0266-5611/25/123010>
- [10] Mozumder M, Tarvainen T, Arridge S, Kaipio J P, d’Andrea C and Kolehmainen V 2015 *submitted* URL <http://arxiv.org/abs/1501.00384>
- [11] Schweiger M, Arridge S R, Hiraoka M and Delpy D T 1995 *Medical Physics* **22** 1779–1792 URL <http://link.aip.org/link/?MPH/22/1779/1>
- [12] Guven M, Zhou L, Reilly-Raska L and Yazici B 2010 *Medical Imaging, IEEE Transactions on* **29** 230–245 ISSN 0278-0062
- [13] Grzywacz T, Sikora J and Wojtowicz S 2008 *Magnetics, IEEE Transactions on* **44** 1374–1377 ISSN 0018-9464
- [14] Elisee J, Gibson A and Arridge S 2010 *Biomedical Engineering, IEEE Transactions on* **57** 2737–2745 ISSN 0018-9294
- [15] Ntziachristos V and Weissleder R 2001 *Opt. Lett.* **26** 893–895 URL <http://ol.osa.org/abstract.cfm?URI=ol-26-12-893>
- [16] Soubret A, Ripoll J and Ntziachristos V 2005 *Ieee Transactions on Medical Imaging* **24** 1377–1386 URL [GotoISI://000232236800013](http://ieeexplore.ieee.org/xpl/articleDetail.jsp?tp=&arnumber=150100384)
- [17] Pyka T, Schulz R, Ale A and Ntziachristos V 2011 *Opt. Lett.* **36** 4329–4331 URL <http://ol.osa.org/abstract.cfm?URI=ol-36-22-4329>
- [18] Abascal J F P J, Aguirre J, Chamorro-Servent J, Schweiger M, Arridge S, Ripoll J, Vaquero J J and Desco M 2012 *Journal of Biomedical Optics* **17** 036013–1–036013–9 URL [+http://dx.doi.org/10.1117/1.JBO.17.3.036013](http://dx.doi.org/10.1117/1.JBO.17.3.036013)

- [19] Schulz R, Ale A, Sarantopoulos A, Freyer M, Soehngen E, Zientkowska M and Ntziachristos V 2010 *IEEE Transactions on Medical Imaging* **29** 465–473 ISSN 0278-0062
- [20] Guo X, Liu X, Wang A, Tian F, Liu F, Zhang B, Hu G and Bai J 2010 *Biomedical Engineering, IEEE Transactions on* **57** 2876–2883 ISSN 0018-9294
- [21] Liu X, Guo X, Liu F, Zhang Y, Zhang H, Hu G and Bai J 2011 *Biomedical Engineering, IEEE Transactions on* **58** 2139–2143 ISSN 0018-9294
- [22] Mohajerani P, Hipp A, Willner M, Marschner M, Trajkovic-Arsic M, Ma X, Burton N, Klemm U, Radrich K, Ermolayev V, Tzoumas S, Siveke J, Bech M, Pfeiffer F and Ntziachristos V 2014 *Medical Imaging, IEEE Transactions on* **33** 1434–1446 ISSN 0278-0062
- [23] Zhang X, Toronov V Y and Webb A G 2006 *Review of Scientific Instruments* **77** 114301–114301–8 ISSN 0034-6748
- [24] Stuker F, Baltes C, Dikaiou K, Vats D, Carrara L, Charbon E, Ripoll J and Rudin M 2011 *IEEE Transactions on Medical Imaging* **30** 1265–1273
- [25] Solomon M, Nothdruff R E, Akers W, Edwards W B, Liang K, Xu B, Suddlow G P, Deghani H, Tai Y C, Eggebrecht A T, Achilefu S and Culver J P 2013 *Journal of nuclear medicine : official publication, Society of Nuclear Medicine* **54** 639–46 ISSN 1535-5667 URL <http://www.ncbi.nlm.nih.gov/pubmed/23447655>
- [26] Zhang B, Liu S, Cao X, Liu F, Wang X, Luo J, Shan B and Bai J 2013 *Multimedia, IEEE Transactions on* **15** 1031–1038 ISSN 1520-9210
- [27] Baritiaux J C, Hassler K and Unser M 2010 *Medical Imaging, IEEE Transactions on* **29** 1075 –1087 ISSN 0278-0062
- [28] Baritiaux J C, Hassler K, Bucher M, Sanyal S and Unser M 2011 *Medical Imaging, IEEE Transactions on* **30** 1143 –1153 ISSN 0278-0062
- [29] Holt R W, Davis S and Pogue B W 2013 *Opt. Lett.* **38** 2407–2409 URL <http://ol.osa.org/abstract.cfm?URI=ol-38-14-2407>
- [30] Tan Y, Cao Z and Sajja H K, Lipowska M and Wang Y A Y L and Jiang H 2013 *Journal of X-Ray Science and Technology* **21** 4352 URL <http://doi.org/10.3233/XST-130365>
- [31] Zhang J, Chen D, Liang J, Xue H, Lei J, Wang Q, Chen D, Meng M, Jin Z and Tian J 2014 *Biomed. Opt. Express* **5** 1861–1876 URL <http://www.osapublishing.org/boe/abstract.cfm?URI=boe-5-6-1861>
- [32] Hielscher A, Klose A and Hanson K 1999 *Medical Imaging, IEEE Transactions on* **18** 262–271 ISSN 0278-0062
- [33] Ntziachristos V, Hielscher A H, Yodh A G and Chance B 2001 *Ieee Transactions on Medical Imaging* **20** 470–478 URL [GotoISI://000169452900002](http://www.ncbi.nlm.nih.gov/pubmed/11694529)
- [34] Tan Y and Jiang H 2008 *Appl. Opt.* **47** 2011–2016 URL <http://ao.osa.org/abstract.cfm?URI=ao-47-12-2011>

- [35] Prakash J, Dehghani H, Pogue B and Yalavarthy P 2014 *Medical Imaging, IEEE Transactions on* **33** 891–901 ISSN 0278-0062
- [36] Prakash J, Shaw C, Manjappa R, Kanhirodan R and Yalavarthy P 2014 *Selected Topics in Quantum Electronics, IEEE Journal of* **20** 74–82 ISSN 1077-260X
- [37] Wu L, Zhao H, Wang X, Yi X, Chen W and Gao F 2014 *Appl. Opt.* **53** 6970–6982 URL <http://ao.osa.org/abstract.cfm?URI=ao-53-30-6970>
- [38] Gremse F, Theek B, Kunjachan S, Lederle W, Pardo A, Barth S, Lammers T, Naumann U and Kiessling F 2014 *Theranostics* **4** 960–971 URL <http://dx.doi.org/10.7150/thno.9293>
- [39] Arridge S R and Lionheart W R B 1998 *Opt. Lett.* **23** 882–884 URL <http://ol.osa.org/abstract.cfm?URI=ol-23-11-882>
- [40] Correia T, Ducros N, D’Andrea C, Schweiger M and Arridge S 2013 *Opt. Lett.* **38** 1903–1905 URL <http://ol.osa.org/abstract.cfm?URI=ol-38-11-1903>
- [41] D’Andrea C, Ducros N, Bassi A, Arridge S and Valentini G 2010 *Biomed. Opt. Express* **1** 471–481 URL <http://www.opticsinfobase.org/boe/abstract.cfm?URI=boe-1-2-471>
- [42] Ducros N, Bassi A, Valentini G, Canti G, Arridge S and D’Andrea C 2013 *Journal of Biomedical Optics* **18** 020503–020503 URL [+http://dx.doi.org/10.1117/1.JBO.18.2.020503](http://dx.doi.org/10.1117/1.JBO.18.2.020503)
- [43] Wang D, Liu X, Liu F and Bai J 2010 *Information Technology in Biomedicine, IEEE Transactions on* **14** 1346–1354 ISSN 1089-7771
- [44] Mohajerani P and Ntziachristos V 2013 *Opt. Lett.* **38** 2324–2326
- [45] Jin A, Yazici B and Ntziachristos V 2014 *Image Processing, IEEE Transactions on* **23** 2609–2624 ISSN 1057-7149
- [46] Konecky S D, Panasyuk G Y, Lee K, Markel V, Yodh A G and Schotland J C 2008 *Opt. Express* **16** 5048–5060 URL <http://www.opticsexpress.org/abstract.cfm?URI=oe-16-7-5048>
- [47] Zacharopoulos A D, Svenmarker P, Axelsson J, Schweiger M, Arridge S R and Andersson-Engels S 2009 *Opt. Express* **17** 3042–3051 URL <http://www.opticsexpress.org/abstract.cfm?URI=oe-17-5-3042>
- [48] Rudge T J, Soloviev V Y and Arridge S R 2010 *Opt. Lett.* **35** 763–765 URL <http://ol.osa.org/abstract.cfm?URI=ol-35-5-763>
- [49] Hyde D, Miller E, Brooks D and Ntziachristos V 2010 *Medical Imaging, IEEE Transactions on* **29** 365–374 ISSN 0278-0062
- [50] Cao X, Zhang B, Liu F, Wang X and Bai J 2011 *Opt. Lett.* **36** 4515–4517 URL <http://ol.osa.org/abstract.cfm?URI=ol-36-23-4515>
- [51] Shaw C B and Yalavarthy P K 2012 *Journal of Biomedical Optics* **17** 086009–086009 URL <http://dx.doi.org/10.1117/1.JBO.17.8.086009>

- [52] Lee O K, Kim J M, Bresler Y and Ye J C 2011 *Medical Imaging, IEEE Transactions on* **30** 1129–1142 ISSN 0278-0062
- [53] Kim D, Sra S and Dhillon I 2010 *SIAM Journal on Scientific Computing* **32** 3548–3563 (Preprint <http://epubs.siam.org/doi/pdf/10.1137/08073812X>) URL <http://epubs.siam.org/doi/abs/10.1137/08073812X>
- [54] Correia T, Aguirre J, Sisniega A, Chamorro-Servent J, Abascal J, Vaquero J J, Desco M, Kolehmainen V and Arridge S 2011 *Biomed. Opt. Express* **2** 2632–2648 URL <http://www.opticsinfobase.org/boe/abstract.cfm?URI=boe-2-9-2632>
- [55] Black M, Sapiro G, Marimont D and Heeger D 1998 *Image Processing, IEEE Transactions on* **7** 421–432 ISSN 1057-7149
- [56] Douiri A, Schweiger M, Riley J and Arridge S R 2007 *Measurement Science and Technology* **18** 87 URL <http://stacks.iop.org/0957-0233/18/i=1/a=011>
- [57] Schweiger M and Arridge S 2014 *Journal of biomedical optics* **19** 040801 ISSN 1560-2281 URL <http://www.ncbi.nlm.nih.gov/pubmed/24781586>
- [58] Ducros N, D’Andrea C, Bassi A, Valentini G and Arridge S 2012 *Physics in Medicine and Biology* **57** 3811 URL <http://stacks.iop.org/0031-9155/57/i=12/a=3811>
- [59] Bassi A, Farina A, D’Andrea C, Pifferi A, Valentini G and R C 2007 *Opt. Express*, **15** 1448214487.
- [60] Fang Q and Boas D 2009 Tetrahedral mesh generation from volumetric binary and grayscale images *Biomedical Imaging: From Nano to Macro, 2009. ISBI '09. IEEE International Symposium on* pp 1142–1145 ISSN 1945-7928
- [61] <http://statweb.stanford.edu/~wavelab/> URL <http://statweb.stanford.edu/~wavelab/>
- [62] Koenig A, Planat-Chrtien A, Hassler K, Bucher M, Coutard J G, Herv; L, Brambilla M, Josserand V, Coll J L, Vats D, Dikaiou K, Rudin M and Dinten J M 2012 Validation of an xct/fdot system on mice URL <http://dx.doi.org/10.5402/2012/735231>
- [63] Pifferi A, Torricelli A, Cubeddu R, Quarto G, Re R, Sekar S K V, Spinelli L, Farina A, Martelli F and Wabnitz H 2015 *Journal of Biomedical Optics* **20** 121304 URL <http://dx.doi.org/10.1117/1.JBO.20.12.121304>
- [64] Tarvainen T, Kolehmainen V, Kaipio J P and Arridge S R 2010 *Biomed. Opt. Express* **1** 209–222 URL <http://www.opticsinfobase.org/boe/abstract.cfm?URI=boe-1-1-209>
- [65] Kolehmainen V, Tarvainen T, , Arridge S R and Kaipio J P 2010 *International Journal for Uncertainty Quantification* **1** 117
- [66] Ferrari M and Quaresima V 2012 *NeuroImage* **63** 921–35 ISSN 1095-9572 URL <http://www.ncbi.nlm.nih.gov/pubmed/22510258>
- [67] Pifferi A, Farina A, Torricelli A, Quarto G, Cubeddu R and Taroni P 2012 *J. Near Infrared Spectrosc.* **20**