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Improvement of a Topological-Physical Model to manage different physical simulations
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ABSTRACT
We present an improvement of a unified topological-physical model which permits topological modifications during physical simulation of soft tissues. Our improvement makes the model more generic, efficient and simpler to update. The main principle of our improvement is to associate information to elements of the model, depending on the underlying physical model. Our modification of the architecture enables to easily integrate different physical models. Moreover, topological operations and physical simulations can be factorized between the different physical models. Our solution is more efficient as it leads to simpler modification algorithms after topological alterations with less changes to apply. In this paper, we present our new solution and illustrate its new properties thanks to several experiments performed on two well-known physical models: Mass-Spring System and Tensor-Mass model. The results present a comparison of our solution with the previous one for the cutting topological operation. Moreover, as our model permits to easily compare several physical models, we performed some simulations to reproduce experiments made on real tissues.

Keywords
Physical Simulation; Mass-Spring System; Tensor-Mass Model; Combinatorial Maps.

1 INTRODUCTION

In medical applications, the actual challenge is to propose physical models which provide interactive simulations with topological modifications (such as cutting). The goal is to simulate surgical operations for training. In computer graphics, the field of soft bodies simulation covers many methods [NMK+06]. The two main approaches, namely Finite Element Method (FEM) and Mass-Spring System (MSS), focus either on accuracy or on the performance of the system with visually satisfactory results. MSS is faster and easier to implement than FEM, but provides less accurate results. However, some papers focus to improve the MSS model by integrating some mechanical properties (such as Young’s modulus and Poisson’s ratio) in the computation of the springs properties [BSSH04, LSH07, BBJ+09].

Furthermore, as an alternative to the classic FEM, the Tensor-Mass (TM) approach has been introduced by Delingette, Cotin and Picinbono [DCA99] and extended by Schwartz [SDR+05]. This approach is based on another way to solve the mechanical equations of the objects, with a direct computation of the forces applied on each node considering the evaluation of the strain energy density. This approach allows to compute elements’ information regardless of the neighborhood of this element.

In this context, this paper proposes an extension of the work of Flechon [FZDJ13, FZDJ14] who proposed a unified topological-physical model (called LCC+MSS) adapted for a mass-spring simulation that handles cutting or piercing simulated objects. Only one model is used to define the topology, the geometry and the physical properties of the simulated object, enabling topological modifications during its simulation by updating on the fly. In this paper, our contributions are:

- The improvement of the efficiency of the topological-physical model for cutting by changing the architecture of the model.
- The improvement of the topological-physical model to manage several physical models. We illustrate this issue by integrating the mass-spring system and tensor-mass model which both naturally allow dynamical topological modifications thanks to a local formulation of the strain.
The use of the topological-physical model to simulate realistic and accurate experiments on soft tissues.

The paper is organized as follows. Section 2 presents the two physical models used. Section 3 presents the unified topological-physical model proposed by Flechon. Section 4 presents our extension of this unified model with discussion in Section 4.3. Section 5 presents some experiments showing that our model can be used to conduct real experiments made on soft tissues and to compare physical models.

2 PHYSICAL MODELS

Mass-Spring System. In computer graphics, mass-spring systems have largely been used to simulate the behavior of deformable objects [TPF91, BFA02]. This physical model is based on the discretization of the object into a set of masses (also called particles) interconnected by springs. Then at each time step, the following main steps are performed for each particle:

1. Computation of the forces applied on the particle due to springs and external forces. Remember that the force involved by a spring connecting particles $i$ and $j$, with stiffness constant $k_{ij}$ and initial length $l_{ij}$, is defined at time $t$ by $F_{ij}(t) = F^e_{ij}(t) + F^v_{ij}(t)$.

2. Computation of the deformation energy according to the acceleration using a numerical integration scheme (for instance the semi-implicit Euler one).

3. Computation of the displacement of a point $X$ inside $E$ with

$$U_E(X) \approx \sum_{j=0}^{n-1} \Lambda_j(X) U_j,$$

where $n$ is the number of 3D nodes $P_j$ defining the element, $U_j$ the displacement of each node $P_j$ from its initial position, and $\Lambda_j(X)$ some interpolation functions defined according to the type of element used for the discretization.

4. Computation of the acceleration according to Newton’s second law (in the same way that for MSS).

5. Computation of the deformation and displacement of the object using a numerical integration scheme (in the same way that for MSS).

In this paper, we used the approach proposed by Faure [FZJM12]. The formulation of the forces applied on each node of the elements was generated thanks to symbolic computation. Thus, the steps (1), (2) and (3) of the simulation loop were replaced by the direct formulation of the force applied on the nodes.
3 LCC+MSS MODEL

3D Linear Cell Complex. The unified topological-physical model (called LCC+MSS) proposed by Flechon [FZDJ13, FZDJ14] used as underlying data structure the 3D Linear Cell Complex (LCC) [Dam12] from the CGAL Open Source geometric algorithms library [The12]. With this topological structure, an orientable object is represented using 3D combinatorial maps (called 3-maps) [Lie94, DL14] as a subdivision of 0-cells (vertices), 1-cells (edges), 2-cells (faces) and 3-cells (volumes). The cells are described by darts, a generalization of half-edges [Män87] to higher dimension, plus pointers between these darts called \( \beta_i \) with \( i \in \{0, 1, 2, 3\} \). The 3D linear cell complex data structure is then obtained by associating to 0-cells the coordinates in \( \mathbb{R}^3 \) of corresponding points.

Fig. 1 represents two adjacent cubes described by a 3-map. Darts are displayed as arrows. \( \beta_1(d) \) is the next dart following dart \( d \) in the same face and the same volume. \( \beta_0(d) \) is the previous dart in the same face and volume. \( \beta_2(d) \) gives the other dart from \( d \) belonging to the same edge, the same volume but not the same face. \( \beta_3(d) \) gives the other dart from \( d \) belonging to the same edge, the same face but not the same volume.

![Two adjacent cubes described by a 3-map](image)

Figure 1: Two adjacent cubes described by a 3-map. Each cube has \( 6 \times 4 \) darts. Purple disks represent vertices associated with points to obtain a 3D LCC.

This representation using darts and pointers describes the cells of an object as well as all the incidence and adjacency relationships. If two i-cells share a common \((i-1)\)-cell, they are adjacent (for example two volumes sharing a common face). If one cell belongs to the boundary of another cell, these two cells are incident (for example a vertex belonging to the boundary of a face). This information is very useful to allow topological modifications during the simulation.

Lastly, any information can be associated with cells thanks to the attribute notion (e.g. a length to edges or a color to faces). We denote by \( i\text{-attribute}(d) \) the attribute associated with the \( i \)-cell containing dart \( d \).

3D LCC for MSS. Flechon added information to a 3D LCC to construct the LCC+MSS model which is suitable for a MSS based on the Baudet formulation for hexahedral mesh [BBJ+09]. This formulation is available for basic hexahedra including four inner springs.

In the LCC+MSS model, a data structure Particle is associated to each 0-cell thanks to a 0-attribute and a data structure Spring is associated to each 1-cell thanks to a 1-attribute. Four additional springs inside each hexahedron are also described by the Spring data structure. But contrary to particles and springs previously described, these inner springs are not associated with any cells of the 3-map, but directly associated to the object.

- The Particle structure stores information related to a particle: its mass, velocity, acceleration and the sum of the forces applied to it. Moreover, it stores the list of the inner springs attached to it.
- The Spring structure stores the physical properties of a spring: its initial length, its stiffness and its two extremities (thanks to two pointers to the two Particle connected by the considered spring).

![Two adjacent cubes described by the LCC-MSS model](image)

Figure 2: Two adjacent cubes described by the LCC-MSS model which is a 3D LCC associated with particles (purple disks), springs (in black) and inner springs (in blue).

Interest of using topological model for physical simulation. The classical data-structure used in MSS simulations is a graph where vertices correspond to particles and edges correspond to springs. This simple model allows to directly and easily compute the forces resulting from the springs and to accumulate these forces on the particles. However, the treatment becomes more difficult for topological modifications. Indeed, it is not possible with such a graph, to directly retrieve the elements of the object, nor all the neighborhood relations between the elements, the springs and the particles when these relations are necessary to implement topological modifications.

For example, to cut an object between two adjacent hexahedra (i.e. two hexahedra sharing a face), particles of the face could need to be duplicated (as we will see later with Fig. 4). To detect if a particle needs to be duplicated or not, we need to search for existence of a path of adjacent elements joining the two cut hexahedra. This is not possible directly in the graph. Thus, a data-structure has to be added to represent elements by
storing indices of its particles and indices of its adjacent elements. Then, we also need to add to each particle the indices of its incident elements. These additional data-structure and links need to be initialized and updated coherently after each operation. Moreover, other data-structures and links will be required to implement another topological modification.

The main interest of using a topological model is that we are sure that all the topological relations are described and can be retrieved directly. Existing topological constraints ensure the topological validity of the described objects and can be used to test the consistency of implemented operations. Moreover, we can use many existing and proved topological operations that can serve as basic tool to implement high level operation in our physical simulation.

4 OUR NEW SOLUTION

In this paper, we propose an improvement of the LCC+MSS model. At this time, we consider only hexahedral elements due to the physical models used, but the structure is suitable for any topology. Our model follows two new principles: (1) to store the darts of each element in 3-cells of the 3-map; (2) to associate the physical information directly in the corresponding cells of the 3-map.

4.1 Storing of the darts in their element

For the first principle, we add in each element an array called dart containing all the darts of the element grouped by faces i.e. an array dart\{6\}[4] is associated to each hexahedron. The initialization of these arrays is performed at the construction of the 3-map using the convention given in Fig. 3. With this structure, all points of a given hexahedron can be retrieved thanks to the stored darts. For example, point X0 is obtained from dart[0][3] and point X1 is obtained from dart[4][2]. Moreover, each point of an hexahedron can be retrieved by three different darts. For example X0 can also be retrieved thanks to dart[1][0] and dart[4][1].

![Figure 3: Convention used to store darts of a hexahedron composed of points X_i with i ∈ {0,...,7}. f_j = dart[j][0] with j ∈ {0,...,5} correspond to the first darts of each face (the bolded arrows).](image)

4.2 Storing of physical information in the corresponding cells

The second principle is based on the fact that the physical information associated to the i-cells (with i ∈ {0,1,2,3}) of the 3-map is depending on the physical model chosen. Consequently, the direct association of the physical information to the corresponding cells allows to consider easily different physical models. In this subsection, we present the use of our proposal for a mass-spring system and a tensor-mass model, but any physical model can be envisaged. We terminate this subsection by showing the generic computation of the forces accumulation thanks to this second principle. Naturally, the computation of the acceleration of the object and its integration in order to obtain its velocity and its position is the same for all physical objects who are based on the newtonian dynamics.

Mass-Spring System. For a mass-spring system based on the Baudet formulation [BBJ+09], particles are associated to 0-cells thanks to 0-attributes, springs are associated to 1-cells thanks to 1-attributes, and inner springs are associated to 3-cells thanks to 3-attributes. Indeed, we remember that in the considered MSS, each hexahedron includes 4 inner springs s_i with i ∈ {0,1,2,3}. By convention, we fix spring s_0 (resp. s_1, s_2, s_3) between particles (P_0, P_1) (resp. (P_1, P_2), (P_2, P_3) and (P_3, P_0)) where particles P_i correspond to point X_i with i ∈ {0,...,7} presented in Fig. 3.

To compute the forces involved by springs (supported both by 1-cells and 3-cells), each spring needs to know its two extremity particles which are the parameters of the addForce() function used for this purpose. This can be retrieved thanks to the 3-map and to the dart array, without storing explicitly the link between springs and particles.

- For each spring s associated to a 1-cell, one dart d_1 of the edge is directly known thanks to the 3-map (see Fig. 2). The first particle extremity of the spring is given by 0-attribute(d_1). The second particle extremity of the spring is given by 0-attribute(d_2) with d_1 = other_extremity(d_2) the dart associated with the second extremity of the edge.

- For any inner spring s_i associated to a 3-cell, its two particles extremity are directly retrieved by our convention and the dart array. For example for s_0, its first extremity is 0-attribute(dart[1][0]) and its second extremity is 0-attribute(dart[3][1]).
**Tensor-Mass model.** For the tensor-mass model, nodes are associated to 0-cells thanks to 0-attributes, and the formulation of the forces applied on each node of an element are associated to 3-cells thanks to 3-attributes. In this paper, we only consider hexahedral mesh with a non-linear behavior using the Green-Saint Venant strain-tensor, but it could easily be extended to any topology or physical behavior thanks to the formulation of the forces proposed by Faure [FZJM12].

To compute the forces applied on each element inside the addForce() function, each element starts by computing the displacement of their nodes using their current and initial position. Thanks to the dart array, each node of a 3-cell is retrieved in constant time. Then, the force applied on each node of an element is directly computed using the formulation of forces generated by symbolic computation.

**Generic forces accumulation.** Thanks to this new way to associate physical information to a LCC, the forces applied on the object are easily computed by performing a loop on all the relevant i-cells, that is the i-cells affected by the force computation (e.g. the 1-cells and 3-cells for MSS; the 3-cells for MT) and calling the appropriate addForce() function on the associated physical information. In practice, it consists to iterate through all the enabled i-attributes (i.e. the attributes which are associated to cells of the 3-map).

### 4.3 Comparison with previous solution

As recalled in Section 3, the initial definition of the LCC+MSS topological-physical model [FZDJ13] associates physical entities to cells (similarly than in our new solution), except for inner springs which are not associated with elements. Moreover, each spring stores its two extremity particles to be able to accumulate the force of this spring to the particles.

**Improvement for cutting.** With this previous solution, extremity particles of springs may have to be updated after a cutting. For example in Fig. 4, the cut of the two top hexahedra leads to the split of particles $v_1$ and $v_2$ into four particles $v_1, v'_1, v_2, v'_2$. But after this cutting, springs of the top-right hexahedra are still associated with original particles $v_1$ and $v_2$ instead of particles $v'_1$ and $v'_2$ (see Fig. 4(a)). To solve this problem after the cutting, a post-processing is applied to update the incorrect extremities of springs (see Fig. 4(b)).

The solution proposed [FZDJ13] is to update all the springs having as extremity the particles involved in the cutting. This requires to store in each particle the list of the springs touching it. Then, when a particle is duplicated due to a cutting, an iteration is performed through this list to update the extremities of the springs to point to the new particles. Moreover, the list of springs is split in two parts: the first part for springs incident to $v_1$ and the second one for springs incident to $v'_1$ (the new particle). This treatment requires a complex and time consuming processing.

![Figure 4](image.png)

Figure 4: In the LCC+MSS model (pictures from [FZDJ13]), the cutting involves the updating of the spring extremities. (a) The bold segments represent the inner springs wrongly attached to particle $v_1$ after the cutting. (b) The same springs updated after a post-processing step.

With our new solution, as the darts of an element are constant whatever the topological modification applied on its neighbor elements, no change is required for cutting. For example, the darts of the two hexahedra split in Fig. 4 are still valid after the cutting. Moreover, as springs and inner springs extremities are only defined by using the darts of the hexahedra, they are still valid after the cutting without any updating. Thus our algorithms with topological modifications are simpler than Flechon and our method is faster (as shown in our experiments in section 5) than Flechon.

**Improvement for any physical models.** Another advantage of our proposal concerns the ease to consider several physical models as presented in previous subsection. Indeed, as physical information are associated with cells thanks to the 3-map, the same algorithm is used to accumulate forces regardless of the physical model used (in our actual implementation, for both mass-spring system and tensor mass model).

Moreover, the 3-map and the dart array are up to date after cutting without any need of post-processing. Thus, only physical properties concerning by the cutting (like the mass) have to be updated. This simplifies the integration of new physical models in our system.

### 5 RESULTS

In this section, we present results obtained in a Intel®i5 4690 CPU, 4 cores @3.50 GHz with 16 Go RAM. For the following tests, we consider a gravity put to $g = -9.8 \text{ m.s}^{-2}$ and beams with a density $\rho = 1000 \text{ Kg.m}^{-3}$, a Young’s modulus $E = 400 \text{ KPa}$ and a Poisson’s ratio $\nu = 0.3$.

**Time for cutting.** We start by a comparison in time for cutting between our approach and that of
Flechon [FZDJ13]. In Fig. 5, the curves represent the time in seconds involved to cut a beam compared to the number of faces disconnected. We consider beams discretized in $200 \times 200 \times 2$, $400 \times 400 \times 2$, $600 \times 600 \times 2$ and $800 \times 800 \times 2$ elements of size $1 \times 1 \times 1$ m with a cutting according to the Z axis.

In Table 1, more complex meshes are used for the comparison in time (in ms) for cutting: a frog (2,354 elements), an elephant (125,754 elements), a mushroom (27,000 elements) and a giraffe (85,405 elements).

<table>
<thead>
<tr>
<th>Mesh</th>
<th># faces cut</th>
<th>Flechon</th>
<th>Our model</th>
</tr>
</thead>
<tbody>
<tr>
<td>Frog</td>
<td>112</td>
<td>4.0</td>
<td>2.0</td>
</tr>
<tr>
<td>Elephant</td>
<td>592</td>
<td>14.5</td>
<td>7.6</td>
</tr>
<tr>
<td>Mushroom</td>
<td>987</td>
<td>32.2</td>
<td>17.7</td>
</tr>
<tr>
<td>Giraffe</td>
<td>5210</td>
<td>176.3</td>
<td>91.6</td>
</tr>
</tbody>
</table>

Table 1: Comparison of time (in ms) for cutting.

We observe that our method is nearby twice as fast than the LCC+MSS model as less information has to be updated in our approach to take into account a topological modification of the object.

**Precision.** Fig. 6 presents a comparison for the traction test between the results obtained using the MSS and the MT approach compared to the analytic solution with beams discretized in $5 \times 5 \times 20$ and $10 \times 10 \times 40$ elements. We consider the analytic solution given by

$$y = \frac{\rho glh}{24EI} \left(4Lx^3 - 6L^2x^2 - x^4\right)$$

with $L = 1$ m the length, $h = 0.25$ m the height, $l = 0.25$ m the thickness of the beams and $I = lh^3/12$ the inertia moment. Fig. 7 presents a visual comparison of the equilibrium state obtained with the $10 \times 10 \times 40$ MSS beam and the $10 \times 10 \times 40$ MT beam.

As expected, we observe that the MT simulation is closest to the analytic solution than MSS simulation. This experiment shows the interest of having several physical models in a same software to simply comparisons between different simulations.

**Time of execution.** Fig. 8 presents a comparison in time for the traction test performed on beams with several discretization. The aim was to vary the number of elements of size $0.025 \times 0.025 \times 0.025$ m. We present sequential and parallel time with a parallelization of the simulation’s loop performed using the Intel®TBB (Threading Building Blocks) C++ template library for task parallelism. Four threads were involved for the parallel time. We obtained an average speedup of 1.45 for the MSS and 2.73 for the MT.

The MT simulation is slower than the MSS simulation due to the more complex physical equations. However its parallelization has a better speedup than the MSS one. This is due to the fact that MT uses only once type of attribute for the physical information (associated with 3-cells), while MSS uses two different types of attributes (1-cells for springs and 3-cells for inner springs) requiring two different loops.
Figure 8: Comparison in time for the MSS and MT simulation performed in sequential or in parallel with TBB.

Illustrations of cutting. Fig. 9 and 10 show cutting made during a MT or a MSS simulation of meshes subject to the gravity. These pictures show that our model allows topological modifications of the objects during their physical simulation.

Figure 9: Cutting made during a MT simulation of a beam (subject to gravity) fixed to its two extremities.

Figure 10: Cutting made during a MSS simulation. Some particles were fixed and the gravity was applied. The density of the letters was put to $\rho = 200 \text{ Kg.m}^{-3}$.

Fig. 11 shows several cuts applied on a giraffe mesh (with no simulation) that contains 85,405 elements. The different parts were separated by hand to obtain a proper visualization.

6 REPRODUCE REAL EXPERIMENTS

In this section, we present the use of our model to simulate experiments performed on real tissues. Firstly, we explain the original experiments made on porcine tissues [NNP12]. Secondly we present our simulation and the preliminary results obtained with the MSS and the MT model. Note that the comparison between two physical models in this simulation is possible thanks to our improvement of the physical-topological model.

Experiment. The original experiments were performed on a porcine liver disks of $2 - 3.7$ mm thickness and diameter of approximately 15 mm. Fig. 12 presents a schematic picture of the experiment. The disks of porcine tissues were glued between the plates of a rotational rheometer. Then, the top plate was rotating at a frequency varied from 0.1 Hz to 2 Hz, while the bottom one was constrained. This experiment is equivalent to a local deformation of the porcine disks.

Figure 11: Ten successive cuts on a giraffe mesh.

Figure 12: Schematic representation of the experiments made on porcine tissues [NNP12].
The authors [NNP12] of the original experiments derived a non-linear model from the results obtained with the experiments. However, since we only consider the linear case, the following equations are modified accordingly.

The model is represented by the relaxation modulus $G(t)$ and the stress-strain relationship $\sigma[\varepsilon(t)]$. We have:

$$G(t) = \frac{K}{\Gamma(1-n)} t^{-n}$$

with $K$ the consistency, $n$ the linear constitutive index and $t$ the time [KM09, NVP10]. The Gamma function is defined by

$$\Gamma(x) = \int_0^\infty t^{x-1} e^{-t} dt.$$

Considering the experiments made on liver tissues, we used as values $K = 861$ Pa s$^n$ and $n = 0.1138$ [NNP12]. The stress-strain relationship is defined for the linear case by

$$\sigma[\varepsilon(t)] = \int_0^t G(t-t')\dot{\varepsilon}(t') dt',$$

where $\sigma$ represents the stress, $\varepsilon(t)$ the strain and $\dot{\varepsilon}$ a constant strain rate. We considered the same three strain rates as the authors [NNP12] with $\dot{\varepsilon} \in \{0.0151 \text{ s}^{-1}, 0.133 \text{ s}^{-1}, 0.67 \text{ s}^{-1}\}$.

**Simulation.** We used our model to reproduce the experiments by simulation. We assumed that locally the tissue is represented by a rectangular block of infinitely long plates. The bottom of the tissue did not move and the top of the tissue only moved on the abscissa $X$. For this, we applied a direct displacement to the top particles and studied the response of the tissue. The simulated tissue consists of 3,751 particles with $10 \times 10 \times 30$ volumes (see Fig. 13). The unit of a cube is 1 mm.

Figure 13: MSS composed of $10 \times 10 \times 30$ hexahedra to reproduce the experiments made on tissues.

As in the LCC+MSS model of Flechon, the formulation of Baudet [BBJ+09] is used to compute the stiffness constant according to Poisson’s ratio and Young’s modulus to integrate physical parameters into the MSS.

**Results.** We considered porcine liver which is a non-compressible tissue with $E = 1000$ Pa, $\nu = 0.499$ and $\rho = 1000$ Kg/m$^3$. The gravity force is set to zero as it is negligible in the real experiment. As we performed a shear experiment in the linear case, the strain is small enough to be negligible. For this reason, we consider the stress-time relationship to analyse our simulations.

Fig. 14 shows the stress according the time obtained for the MT model and the MSS model. For the simulations, the stress is computed by dividing the force applied on the object by the area of the top plate of the tested tissue (in our case 300 mm$^2$).

![Figure 14: Evolution of stress in time for respectively the MT model (top) and the MSS model (bottom) for three different strain rates.](image)

As expected, we observe that MT and MSS have a linear behavior for small deformations.

In the future work, we will improve the MSS solutions by implementing volume preservation and applying some correction forces. We also want to implement a new damping solution to ensure the correctness of the model for linear case.
7 CONCLUSION AND PERSPECTIVE

In this paper, we presented an improvement of the LCC+MSS model proposed by Flechon [FZDJ13]. Our improvement is based on two new principles: (1) to store the darts of each element in the 3-cells of the 3-map; (2) to associate the physical information directly in the corresponding cells of the 3-map.

Thanks to these two new principles, our model allows simpler algorithms since no more modifications are required for topological modification operations. Secondly, our model gives better results since less operations are required. Lastly, our model is more generic since it is now easier to add a new physical model while keeping all the existing operations. We have illustrated these improvements in our experiments with better results obtained for cutting than the previous model.

Moreover, two different physical models (namely the mass-spring system and the tensor-mass model) have been presented who are both based on the same unified topological model. With these two physical models, we have illustrated the generic computation of the accumulation of the forces thanks to our two new principles.

In future work, we are considering adding others physical models to easily compare the results of simulations. The most interesting would be to implement the Finite Element Method and give thought to the Position Based Dynamics approach, like the one of Müller [MHHR07]. According to the MSS, we plan to include the volume preservation constraint in order to improve its precision.

The most interesting would be to implement the Finite Element Method and give thought to the Position Based Dynamics approach, like the one of Müller [MHHR07]. According to the MSS, we plan to include the volume preservation constraint in order to improve its precision.

We plan to study the work of Aubert [AB97] which created a space deformation model (called DOGME), to deal with the volume preservation, and the more recent article of Duan [DHC+14] who treats about preserving volume by position corrections. Furthermore, to improve the precision of our simulations, it is also important to take a deeper look into constraining the particles to distribute correctly the acting forces. Lastly, we want to extend our simulation of soft tissues to the case of non-linear mechanical behavior to consider bigger deformations. All these future work will benefit of our new solution of the LCC+MSS model allowing to define simpler and more efficient algorithms to perform topological modifications during simulation for any kind of physical objects.

Acknowledgments

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8 REFERENCES


2014.


