Process-evaluation of tropospheric humidity simulated by general circulation models using water vapor isotopic observations: 2. Using isotopic diagnostics to understand the mid and upper tropospheric moist bias in the tropics and subtropics

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HAL Id: hal-01114749
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Submitted on 10 Feb 2015

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Process-evaluation of tropospheric humidity simulated by general circulation models using water vapor isotopic observations: 2. Using isotopic diagnostics to understand the mid and upper tropospheric moist bias in the tropics and subtropics

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Received 26 July 2011; revised 28 December 2011; accepted 30 December 2011; published 6 March 2012.

[1] Evaluating the representation of processes controlling tropical and subtropical tropospheric relative humidity (RH) in atmospheric general circulation models (GCMs) is crucial to assess the credibility of predicted climate changes. GCMs have long exhibited a moist bias in the tropical and subtropical mid and upper troposphere, which could be due to the mis-representation of cloud processes or of the large-scale circulation, or to excessive diffusion during water vapor transport. The goal of this study is to use observations of the water vapor isotopic ratio to understand the cause of this bias. We compare the three-dimensional distribution of the water vapor isotopic ratio measured from space and ground to that simulated by several versions of the isotopic GCM LMDZ. We show that the combined evaluation of RH and of the water vapor isotopic composition makes it possible to discriminate the most likely cause of RH biases. Models characterized either by an excessive vertical diffusion, an excessive convective detrainment or an underestimated in situ cloud condensation will all produce a moist bias in the free troposphere. However, only an excessive vertical diffusion can lead to a reversed seasonality of the free tropospheric isotopic composition in the subtropics compared to observations. Comparing seven isotopic GCMs suggests that the moist bias found in many GCMs in the mid and upper troposphere most frequently results from an excessive diffusion during vertical water vapor transport. This study demonstrates the added value of water vapor isotopic measurements for interpreting shortcomings in the simulation of RH by climate models.


1. Introduction

[2] Despite continuous improvements in climate models, uncertainties in the predicted amplitude of climate change and in the magnitude of underlying feedbacks remain high [Randall et al., 2007]. Because the water vapor feedback constitutes one of the largest positive feedbacks in climate models [Soden and Held, 2006], assessing the credibility of predicted relative humidity (RH) changes by atmospheric general circulation models (GCMs) is crucial. In addition, RH strongly impacts the formation of cirrus clouds [Luo and Ros sow, 2004], boundary layer clouds [Slingo, 1980; Wetzel et al., 1996; Betts, 2000] and deep convective clouds [Redelsperger et al., 2002; Derbyshire et al., 2004]. Predicting the correct regional changes in RH is thus crucial for a correct prediction of cloud feedbacks, which are still among the largest sources of spread in climate change projections [Bony and Dufresne, 2005; Bony et al., 2006]. Therefore, the credibility of simulated climate change depends
on the ability of atmospheric models to correctly simulate the processes that control RH, although no evidence has been shown so far for a systematic relationship between the behavior of models at present and in the future [John and Soden, 2007].

Most GCMs exhibit a moist bias in the mid to upper tropical and subtropical troposphere compared to a wide range of data sets [Soden and Bretherton, 1994; Salathe and Chester, 1995; Chen et al., 1996; Roca et al., 1997; Chen et al., 1998; Allan et al., 2003; Brogniez et al., 2005; Pierce et al., 2006; John and Soden, 2007; Sherwood et al., 2010; Chung et al., 2011]. Some of these studies suggest this problem can arise from the parameterization of deep convection [Chen et al., 1996, 1998], others suggest it could be related to an underestimated upper tropospheric large-scale circulation [Chung et al., 2011]. This problem has persisted for more than a decade and questions the capacity of GCMs to accurately represent processes controlling RH. The tropical and subtropical tropospheric RH results from a subtle balance between different processes, among which are large-scale radiative subsidence [e.g., Sherwood, 1996; Schneider et al., 2006; Folkins and Martin, 2005], detrainment of condensate from convective clouds and its subsequent evaporation [e.g., Wright et al., 2009], evaporation of the falling precipitation [e.g., Folkins and Martin, 2005] or lateral mixing [e.g., Zhang et al., 2003]. Therefore, the representation of many processes may potentially contribute to the moist bias. Measurements of humidity alone are not sufficient to diagnose which of these processes are the most likely candidates.

The water vapor stable isotopic composition is affected by fractionation during phase changes. Measurements of water vapor isotopologues therefore provide complementary information on the water budget when combined with humidity because they record the integrated history of phase changes within a given air mass [Dansgaard, 1964].

In a companion paper [Risi et al., 2012] (hereafter P1), we have analyzed various data sets (4 satellite, 16 ground-based remote-sensing, 5 surface in situ and 3 aircraft) to document the three-dimensional distribution of the tropospheric water vapor composition and to derive robust characteristics that could be used to evaluate models. For example, we have identified that the $\delta D$ seasonality in the subtropics and mid latitudes (with higher $\delta D$ in summer) was a robust characteristic across all data sets and at all tropospheric levels. We have used these data sets to evaluate the isotopic GCM LMDZ and have identified some biases that are robust compared to all data sets, such as the underestimated seasonality in the subtropics. In addition, we have compared 7 GCMs from the SWING2 (Stable Water INtercomparison Group phase) project, and have shown large discrepancies between models regarding important features of the isotopic distribution: meridional gradient, seasonality, and spatial contrasts in the tropics. This suggests that water vapor isotopic measurements could be used to efficiently discriminate models regarding their representation of the processes controlling RH. Further, we have shown that differences in isotopic behavior are not obviously linked to differences in simulated humidity, confirming that water vapor isotopic composition provides additional information compared to humidity measurements. The goal of this paper is thus to exploit the information provided by the combination of water vapor isotopic measurements, to understand the cause of the moist bias in GCMs.

To do so, the approach is illustrated in Figure 1. First, with the isotopic GCM LMDZ, we perform different sensitivity tests that exhibit a moist bias for different causes. From these simulations, we investigate how the different

<table>
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<tr>
<th>Tools</th>
<th>Steps of the strategy</th>
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<tr>
<td>sensitivity tests with LMDZ</td>
<td>What is the isotopic signature associated with different reasons for a moist bias?</td>
<td>1) identify an observable isotopic diagnostic to diagnose the reason for a moist bias</td>
</tr>
<tr>
<td>isotopic data</td>
<td>Can this isotopic signature be discriminated using observations?</td>
<td></td>
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<tr>
<td>theoretical model</td>
<td>Is this isotopic signature based on simple processes represented by all models?</td>
<td></td>
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<tr>
<td>additional sensitivity tests with LMDZ</td>
<td>Is this isotopic signature robust relative to the model’s physics?</td>
<td></td>
</tr>
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<td>SWING2 outputs</td>
<td>What is the isotopic signature associated with the moist bias in each GCM?</td>
<td></td>
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</table>

Figure 1. Strategy for developing, testing and applying diagnostics based on the isotopic ratio to identify the cause of the moist bias in models. Rectangles describe the different steps of the strategy used in this paper, and circles explain the tools used at different steps.
processes impact the isotopic composition, and how it hurts the agreement with isotopic data sets. This allows us to identify a discriminating diagnostic for the cause of the moist bias that is robust across data sets. Second, we further check the robustness of this diagnostic by creating a theoretical framework to understand the link between the moist bias and isotopic behavior. The framework is used to show that this link can be explained based on simple processes that are represented in all models. We also use additional sensitivity tests to show that the diagnostic does not crucially depend on the model physics. Third, once we have accumulated confidence in the robustness of the diagnostic, we apply it to six other GCMs from the SWING2 project to determine the most frequent cause of the moist bias in models.

We present the LMDZ GCM, the isotopic data sets and the SWING2 database in section 2. We describe the theoretical framework used to interpret the sensitivity tests in section 3. In section 4, we present the sensitivity tests and their impact on RH in section 4. In section 5, we describe the impact of the tests on the water vapor isotopic composition and compare the simulations with the isotopic data. In section 6 we further check its robustness and apply it to SWING2 models. We conclude and propose perspectives for future work in section 7.

2. General Circulation Models and Data Sets

2.1. The LMDZ4 Model and Control Simulation

LMDZ4 (Laboratoire de Météorologie Dynamique-Zoom) [Houbrin et al., 2006] is the atmospheric component of the Institut Pierre-Simon Laplace coupled model: IPSL-CM4 [Marti et al., 2005] used in CMIP3 (Coupled Model Intercomparison Project) [Meehl et al., 2007] and IPSL-CM5A (J.-L. Dufresne et al., Climate change projections using the IPSL-CM5 Earth System Model: from CMIP3 to CMIP5, submitted to Climate Dynamics, 2012) used in CMIP5. It is used with a resolution of 2.5° in latitude, 3.75° in longitude and 19 vertical levels. The physical package includes the Emanuel convective scheme [Emanuel, 1991; Emanuel and Zivkovic-Rothman, 1999], which represents convective systems as an adiabatic updraft, an ensemble of mixed updrafts and downdrafts, and an unsaturated downdraft driven by rain reevaporation. A particular focus had been placed on the parameterization and optimization of microphysical processes, such as the precipitation efficiency $e_r$ representing the proportion of condensate that is converted to precipitation [Emanuel and Zivkovic-Rothman, 1999]. Large-scale condensation is represented by a statistical cloud scheme based on the sub-grid-scale distribution of water vapor [Bony and Emanuel, 2001]. Water vapor and condensate are advected using a second order monotonic finite volume advection scheme [Van Leer, 1977; Hourdin and Armengaud, 1999]. The isotopic version of LMDZ is described in detail by Risi et al. [2010b].

LMDZ is forced by observed sea surface temperatures (SST) and sea ice following the AMIP (Atmospheric Model Inter-comparison Project) protocol [Gates, 1992] from 1978 to 2009. The year 2010 is forced by NCEP (National Center for Environmental Prediction) SSTs [Kalnay et al., 1996] because the AMIP SSTs were not yet available. To facilitate the comparison between simulations and observations on a daily basis, horizontal winds at each vertical level are nudged by ECMWF reanalyses [Uppala et al., 2005] with a relaxation time scale of 1h as in work by Risi et al. [2010b]. This nudging procedure has been shown to enable the model to capture the daily weather and isotopic variability well [Risi et al., 2010b; Vimeux et al., 2011; Gao et al., 2010]. For example, in summer 2006 in average over the tropics, the daily correlation at each grid point for the large-scale vertical velocity at 500 hPa is 0.45 between the ECMWF reanalyses and the nudged simulation, compared to only 0.006 between the ECMWF reanalyses and the free-running simulation.

2.2. Data Sets and Comparison Methodology

We focus on evaluating the HDO/H2O ratio as quantified by the variable $\delta D$ in $\%_o$: $\delta D = (R_{\text{SMOW}} - 1) \cdot 1000$, where $R$ is the HDO/H2O ratio of the water vapor and $R_{\text{SMOW}}$ is the Vienna Standard Mean Ocean Water (VSMOW) isotopic ratio [Craig, 1961]. To evaluate the simulated three-dimensional water vapor $\delta D$ distribution from the surface up to the upper-troposphere, we combine various data sets that sample different parts of the atmosphere. We use several satellite data sets, which provide a global coverage: SCIAMACHY (a short-wave infra-red spectrometer) mainly sensitive to the lower troposphere, TES (a nadir-viewing thermal infra-red spectrometer) which is mainly sensitive to the mid-troposphere, and ACE-FTS (an infrared solar-occultation instrument) and MIPAS (a limb infrared sounder) which are sensitive in the upper troposphere and above. In addition, we use ground-based remote-sensing (Fourier Transform Infrared) data sets derived from mid-infrared (NDACC, for which water isotopologue retrievals are performed in the framework of the project MUSICA) or near-infrared (TCCON) solar absorption spectra, and in situ measurements made at the surface and by aircraft. These data sets are listed in Table 1 and described in detail in section 3 of P1. Here we use observations made at lower latitudes (45°N–45°S).

The different data sets show significant differences in their absolute $\delta D$ values, meridional gradients and seasonal amplitudes (section 4.1 of P1), due to the effects of spatiotemporal sampling, instrument sensitivity and measurement errors (section 4.2 of P1). Since remote-sensing data has limited calibration and validation, we will focus the analysis on spatial and temporal variations. It is possible that those variations themselves may be in error, but the use of multiple data sets helps ensure that we draw only conclusions that are robustly supported.

We follow a model-to-satellite approach to estimate what the instruments would observe if operated in the model. First, to take into account the spatiotemporal sampling of the data, we collocate the model output with the data at the daily scale. Second, to take into account the sensitivities of the different remote-sensing instruments to the true state, we apply averaging kernels to model output. Averaging kernels define the sensitivity of the retrieval at each level to the true state at each level. In P1, the model-data comparison methodology for each data set is extensively explained (section 3, Appendix C) and sources of model-data differences are quantified (section 5.1). We will focus the analysis on signals that are larger than these potential
source of errors (i.e. larger than 10 or 20‰) and that are robust across data sets.

2.3. SWING2 Models

[12] We compare seven simulations by six other GCMs participating in the SWING2 inter-comparison project (http://people.su.se/~cstur/SWING2/). Some of them are nudged by reanalyses, some of them are not (i.e. they are free-running) (Table 2). The LMDZ control simulations is one of the SWING2 simulations and has been rigorously compared with each data set through collocation with the data (see P1). Since daily values are not available in the SWING2 archive, it is not possible to collocate other model outputs with the data. Therefore, we use the LMDZ control

| Table 1. The Different Data Sets of Water Vapor Isotopic Composition Used for Model-Data Comparison^a |
|---------------------------------|----------------|----------------|----------------|----------------|----------------|
| Data Set or Network            | Reference              | Level                        | Spatial Coverage or Location; Footprint | Period          | Precision       | Comparison Methodology |
| SCIAMACHY                       | Frankenberg et al. [2009] | total column, mainly sensitive in the boundary layer | global; footprint 120 × 20 km | 2003–2005 | 40‰–100‰, reduced by averaging | collocation |
| TES                              | Worden et al. [2007]     | 600 hPa                       | global; footprint 5.3 × 8.5 km | 2004–2008 | about 40‰, reduced by averaging | collocation, application of kernels |
| ACE                              | Nassar et al. [2007]     | down to 500 hPa               | global, but small number of measurements; limb measurement | 2003–2008 | about 50‰, reduced by averaging | collocation, smoothing |
| MIPAS                           | Steinwagner et al. [2010] | down to 300 hPa               | global; limb measurement | September 2002–March 2004 | about 50‰, reduced by averaging | collocation, application of kernels |
| TCCON network                    | Wunch et al. [2010]      | total column                  | 8 stations: Lauder, Wollongong, Darwin, Park Falls, Pasadena, Lamont, Bremen and Ny Alesund | between 1.5 and 6 years | between 5 and 35‰ | collocation, application of kernels |
| NDACC network                    | Schneider et al. [2010]  | total column and profiles up to 10 km | 8 stations: Arrival Heights, Lauder, Wollongong, Izaha, Jungfraujoch, Karlsruhe, Kiruna and Eureka | between 0.5 and 13 years | 5‰ for total column and 10–25‰ for profiles | collocation, application of kernels |
| GNIP-vapor network               | IAEA web site           | surface                       | 3 stations: Vienna, Ankara, Manaus | between 2 and 13 years | undocumented | collocation |
| Isolated data sets               | Angert et al. [2008]; Risi et al. [2010b] | surface                       | 2 stations: Rehovot and Saclay | daily samples during 1 to 2 years | 1‰ | collocation |
| of daily samples                 | Johnson et al. [2011]; Uemura et al. [2008] | surface at 680 hPa            | Hawaii                                        | 3 weeks | 5 to 10‰ | collocation |
| Piccaro in Hawaii surface samples |                       | surface                       | Southern Ocean                                  | 1 month | 1‰ | collocation |
| Flights in the 60s               | Ehhalt et al. [2005]     | profiles between 1.5 km and 9.2 km | 3 sites in the United States: Nebraska, Santa Barbara and the Death Valley near Costa Rica | a few isolated days | 1‰ | collocation |
| CR-AVE and TC4 campaigns         | Sayres et al. [2010]     | profiles between 475 hPa and 64 hPa | 1 week in winter 2006, 10 days in summer 2007 | 17‰ for ICOS and 50‰ for Hoxotope | 1‰ | collocation |

^aWe detail the levels at which the measurements are performed or are the most sensitive, the location for ground-based data sets, the footprint for satellite data sets, the period over which we use the measurements, the precision specified in the reference papers or calculated in Appendix B of P1, and the methodology that we use for model-data comparison.
simulation as a reference against which we compare the SWING2 models’ monthly outputs.

3. Theoretical Framework to Understand Processes Controlling Humidity and Isotopic Composition

[13] We develop a simple single-column theoretical framework to understand the sensitivity tests with the LMDZ GCM. Given its simplicity, we aim to provide qualitative insights into the main effects on humidity and water vapor isotopic composition of the different micro- and macro-physical processes tested in the experiments, rather than to make quantitative predictions.

3.1. Principle

[14] The theoretical framework components and notations are illustrated in Figure 2a. It is inspired by the last saturation theory as explained by Sherwood [1996]. Sherwood [1996] sets RH to a given value near saturation in convective regions, leading to a fixed profile of specific humidity ($q_s$) in convective regions. Specific humidity is then conserved in the air masses that leave the convective regions and slowly subside, leading to a decrease in RH. This framework is also consistent with the simple single-column model of Folkins and Martin [2005] in which the tropical mid and upper troposphere is moistened by convective clouds detrainment and dried by radiative subsidence outside the clouds. Here we extend these previous frameworks in two ways. First, we calculate the water vapor isotopic composition in addition to the humidity. Second, we take into account additional processes that are crucial for the water budget of GCMs, such as cloud microphysics, water vapor transport at the large-scale and the associated diffusion.

[15] In the real world in convective regions, ascent is concentrated in convective cores and cloud-free regions are subsident [Emanuel et al., 1994], and this was the basis for frameworks such as that of Folkins and Martin [2005]. In GCMs however, water vapor transport by large-scale ascent is resolved by the large-scale advection scheme. The large-scale upward transport of water vapor is partly compensated (and sometimes over-compensated) by the compensating subsidence in the convection scheme [Arakawa and Schubert, 1974]. The proportion of the total upward water vapor transport that is treated by the large-scale advection scheme or by the convection scheme are somewhat arbitrary and model-dependent, but it impacts the vertical distribution of chemical tracers [Lawrence and Salzmann, 2008]. We thus expect an impact on the isotopic composition as well. Contrary to Sherwood [1996] and Folkins and Martin [2005], our goal is to interpret biases in GCMs, and therefore we need to take into account the vertical water vapor transport by the large-scale advection.

[16] To illustrate the water budget in the LMDZ GCM, we consider two regions based on monthly mean large-scale

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**Table 2.** List of the Different SWING2 Models Used in This Study and Their Respective Simulations

<table>
<thead>
<tr>
<th>GCM</th>
<th>Reference</th>
<th>Simulations</th>
<th>Horizontal Resolution</th>
<th>Isotopic Processes During Rainfall</th>
</tr>
</thead>
<tbody>
<tr>
<td>GISS</td>
<td>Schmidt et al. [2007]</td>
<td>free-running and nudged by NCEP</td>
<td>46 x 72</td>
<td>0.004</td>
</tr>
<tr>
<td>ECHAM4</td>
<td>Hoffmann et al. [1998]</td>
<td>nudged by ECMWF</td>
<td>64 x 128</td>
<td>0.003</td>
</tr>
<tr>
<td>LMDZ4</td>
<td>Risi et al. [2010b]</td>
<td>free-running and nudged by ECMWF</td>
<td>72 x 96</td>
<td>0.004</td>
</tr>
<tr>
<td>GSM</td>
<td>Yoshimura et al. [2008]</td>
<td>nudged by NCEP</td>
<td>73 x 144</td>
<td>0.003</td>
</tr>
<tr>
<td>CAM2</td>
<td>Lee et al. [2007]</td>
<td>free-running</td>
<td>64 x 128</td>
<td>0.004</td>
</tr>
<tr>
<td>HadAM</td>
<td>Tindall et al. [2009]</td>
<td>free-running</td>
<td>73 x 96</td>
<td>0.005</td>
</tr>
<tr>
<td>MIROC</td>
<td>Kurita et al. [2011]</td>
<td>free-running</td>
<td>73 x 96</td>
<td>0.003</td>
</tr>
</tbody>
</table>

*a"Free-running" refers to standard AMIP-style simulations [Gates, 1992] forced by observed sea surface temperatures, and whose winds are not nudged. The $\lambda$ parameter refers to the formulation of supersaturation $S_i$ with respect to ice as a function of temperature $T$ following $S_i = 1 - \lambda \cdot T$, involved in the kinetic fractionation during ice condensation [Jouzel and Merlivat, 1984]. The representation of isotopic processes during rainfall for each model is described in the indicated reference, and the calculation of the effective relative humidity around raindrops ($heff$) is also given when available in references.

Figure 2. (a) Illustration of the simple single-column model developed to interpret the sensitivity experiments. Characteristic profiles of specific humidity and isotopic composition $q_s$, $dDr$ and $dD_{lw}$ in convective plumes are assumed and depend on the precipitation efficiency $\epsilon_p$ in convective clouds and on the humidity and isotopic composition at the lifting condensation level $q_{s0}$ and $dD_0$. The humidity and $dD$ in the convective region, $q_{asc}$ and $dD_{conv}$ are controlled by the balance between moistening by convective detrainment of air from convective plumes, moistening by large-scale ascent, and drying by large-scale condensation in anvil and cirrus clouds. In subsidence regions, the humidity and isotopic composition $q_{subs}$ and $dD_{subs}$ are controlled by the balance between moistening by horizontal mixing with convective regions and drying by large-scale subsidence. Vertical diffusion has also a moistening effect in both regions. (b) Major tendencies involved in the water budget of the troposphere in convective regions ($\omega_{500} < -35$ hPa/d), as diagnosed from the control simulation of LMDZ: vertical transport, convective detrainment, large-scale condensation and the residual from these 3 terms. (c) Same as Figure 2b but for subsidence regions ($\omega_{500} > 35$ hPa/d): vertical transport, large-scale condensation, horizontal advection and the residual from these 3 terms. The “vertical transport” tendency includes both the effect of large-scale vertical advection and compensating subsidence in the convective scheme. (d and e) Same as Figures 2b and 2c but as computed from the simple single-column model. The diffusive term was included as part of the vertical transport term, since in LMDZ it is intrinsic to the advection scheme.
vertical velocity at 500 hPa ($\omega_{500}$) [Bony et al., 2004]. Figure 2b shows the major tendencies involved in the water budget as simulated by the control simulation of LMDZ in regions of large-scale ascent ($\omega_{500} < -35$ hPa/day, i.e. convective regions). We combine the tendencies by large-scale vertical advection and by compensating subsidence in the convective scheme into one single tendency representing the total vertical transport in the environment (i.e. outside convective cores). To first order, in the boundary layer of convective regions, moistening by surface evaporation balances drying by downward vertical transport. In the mid and upper troposphere (between 600 hPa and 200 hPa) of convective regions, the air is moistened by convective detrainment (consistent with Sherwood [1996] and Folkins and Martin [2005]) and by upward vertical transport in the environment. This moistening is balanced by drying by large-scale condensation, which represents condensation in anvils or cirrus clouds associated with convection. In the mid and upper troposphere of regions of large-scale descent ($\omega_{500} > 35$ hPa/day), the air is moistened mainly by horizontal advection from convective regions, and dehydrated mainly by downward vertical transport (Figure 2c). We
develop a theoretical framework that focuses on the mid and upper troposphere and represents these major tendencies in convective and subsidence regions.

3.2. Water Budget in Convective Regions

[17] In the simple framework, we assume that the temporal evolution of \( q \) in regions of large-scale ascent (\( q_{\text{asc}} \)) is driven by four contributions: (1) convective detrainment, (2) total vertical transport in the environment, (3) diffusion associated with this transport due to intrinsic numerical diffusivity of advection schemes, and (4) large-scale condensation:

\[
\frac{dq_{\text{asc}}}{dt} = \left( \frac{dq_{\text{asc}}}{dt} \right)_{\text{dtr}} + \left( \frac{dq_{\text{asc}}}{dt} \right)_{\text{env}} + \left( \frac{dq_{\text{asc}}}{dt} \right)_{\text{diff}} + \left( \frac{dq_{\text{asc}}}{dt} \right)_{\text{cond}} \tag{1}
\]

where we express the tendency due to convective detrainment as:

\[
\left( \frac{dq_{\text{asc}}}{dt} \right)_{\text{dtr}} = k_{\text{dtr}} \cdot \left( q_{\text{dtr}} - q_{\text{asc}} \right) \tag{2}
\]

where \( k_{\text{dtr}} \) is the rate constant of large-scale condensation and \( q_{\text{dtr}} \) is the total cloud water (vapor plus condensate) that is detraining from convective plumes. \( q_{\text{dtr}} \) equals the humidity entrained into the plume minus the precipitation:

\[
q_{\text{dtr}} = q_s - \epsilon_p \cdot (q_{\text{dtr}} - q_s) \tag{3}
\]

where \( q_s \) is the humidity at saturation, \( q_{\text{dtr}} \) is the specific humidity entrained into the plume and \( \epsilon_p \) is the precipitation efficiency in convective updrafts. We neglect the effect of entrainment on \( q_{\text{dtr}} \), as justified by the fact that humidity and isotopic properties of the air detrained from convective plumes is very similar to those in the adiabatic updraft, consistent with the relatively small entrainment in the Emanuel scheme [Derbyshire et al., 2004; Grandpeix et al., 2004]. Therefore, we assume that \( q_{\text{dtr}} \) is the humidity at the lifting condensation level (LCL).

[18] We express the tendency due to vertical transport in the environment as:

\[
\left( \frac{dq_{\text{asc}}}{dt} \right)_{\text{env}} = -w_{\text{env}} \frac{dq_{\text{asc}}}{dz} \tag{4}
\]

where \( w_{\text{env}} \) is the vertical wind speed (positive upward) that sums the large-scale ascending speed and the downward compensating subsidence in the convective scheme. In regions of large-scale ascent, \( w_{\text{env}} \) is always positive.

[19] We express the tendency due to diffusion as:

\[
\left( \frac{dq_{\text{asc}}}{dt} \right)_{\text{diff}} = K_{\text{diff}} \cdot \frac{d^2 q_{\text{asc}}}{dz^2} \tag{5}
\]

where \( K_{\text{diff}} \) is the diffusivity constant associated with vertical water vapor transport.

[20] For the tendency due to large-scale condensation, as is the case in most GCMs, we assume that RH varies at the sub-grid-scale so that condensation starts for a grid average \( q_{\text{asc}} \) lower than the saturation specific humidity (\( q_s \)). As an example, we assume a uniform distribution of RH with a standard deviation \( \sigma_h \). We thus get:

\[
\left( \frac{dq_{\text{asc}}}{dt} \right)_{\text{cond}} = -k_{\text{cond}} \cdot \left( q_{\text{asc}} - q_s \cdot (1 - \sigma_h) \right) \tag{6}
\]

where \( k_{\text{cond}} \) is the rate constant of large-scale condensation.

[21] We substitute equations (2), (4), (5), and (6) into equation (1) and solve it numerically as detailed in section 3.5. At steady state, \( q_{\text{asc}} \) is given by:

\[
q_{\text{asc}} = \frac{1}{k_{\text{dtr}} + k_{\text{cond}}} \cdot \left( k_{\text{dtr}} \cdot q_{\text{dtr}} + k_{\text{cond}} \cdot q_s \cdot (1 - \sigma_h) \right)
- w_{\text{env}} \frac{dq_{\text{asc}}}{dz} + K_{\text{diff}} \cdot \frac{d^2 q_{\text{asc}}}{dz^2} \tag{7}
\]

[22] If the detrainment term dominates, then \( q_{\text{asc}} \) tends toward \( q_{\text{dtr}} \). If the condensation term dominates, then \( q_{\text{asc}} \) tends toward \( q_s \cdot (1 - \sigma_h) \), which is smaller. In practice, \( q_{\text{asc}} \) is bounded between these two extremes, and for reasonable sets of parameters it stays below saturation. \( q_{\text{asc}} \) increases with \( w_{\text{subs}} \) and \( K_{\text{diff}} \) and decreases with \( \sigma_h \).

3.3. Water Budget in Subsidence Regions

[23] We assume that the temporal evolution of \( q \) in subsidence regions (\( q_{\text{subs}} \)) is driven by 4 contributions: (1) horizontal transport from convective regions, (2) downward vertical transport in the environment, (3) diffusion associated with this transport due to intrinsic numerical diffusivity of advection schemes, and (4) large-scale condensation:

\[
\frac{dq_{\text{subs}}}{dt} = \left( \frac{dq_{\text{subs}}}{dt} \right)_{\text{mix}} + \left( \frac{dq_{\text{subs}}}{dt} \right)_{\text{subs}} + \left( \frac{dq_{\text{subs}}}{dt} \right)_{\text{diff}} + \left( \frac{dq_{\text{subs}}}{dt} \right)_{\text{cond}} \tag{8}
\]

where we express the tendency due to horizontal transport from convective region as:

\[
\left( \frac{dq_{\text{subs}}}{dt} \right)_{\text{mix}} = k_{\text{mix}} \cdot (q_{\text{asc}} - q_{\text{subs}}) \tag{9}
\]

with \( k_{\text{mix}} \) the rate constant of horizontal mixing. We express the tendency due to downward vertical transport as:

\[
\left( \frac{dq_{\text{subs}}}{dt} \right)_{\text{subs}} = w_{\text{subs}} \cdot \frac{dq_{\text{subs}}}{dz} \tag{10}
\]

where \( w_{\text{subs}} \) is the vertical wind speed (positive downward) corresponding to the large-scale subsidence. We express the two remaining tendencies in exactly the same way as for convective regions (equations (5) and (6)). We solve equation (8) numerically (section 3.5). In practice, the condensation term is very small due to the dryness of subsidence regions. This term is present only for numerical stability reasons near 100 hPa. Therefore, at steady state, \( q_{\text{subs}} \) is given approximately by:

\[
q_{\text{subs}} = q_{\text{asc}} + \frac{1}{k_{\text{mix}}} \left( w_{\text{subs}} \cdot \frac{dq_{\text{subs}}}{dz} + K_{\text{diff}} \cdot \frac{d^2 q_{\text{subs}}}{dz^2} \right) \tag{11}
\]

[24] It follows that all factors controlling \( q_{\text{asc}} \) also impact \( q_{\text{subs}} \). If the mixing term dominates, then \( q_{\text{subs}} \) tends toward \( q_{\text{asc}} \). If the subsidence term dominates, then \( q_{\text{subs}} \) reflects the value of \( q_{\text{asc}} \) much higher in altitude. In practice, \( q_{\text{subs}} \) is bounded between \( q_{\text{asc}} \) at the same level and \( q_{\text{asc}} \) higher in altitude. In addition to factors controlling \( q_{\text{asc}} \), \( q_{\text{subs}} \) also increases with \( k_{\text{mix}} \) and \( K_{\text{diff}} \) and decreases with \( w_{\text{subs}} \).
3.4. Isotopic Composition

[25] Water vapor isotopic species are treated exactly like normal water during advection, mixing and diffusion, and are assumed to follow Rayleigh distillation during large-scale condensation.

[26] The isotopic ratio in convective plumes is constrained by the mass conservation underlying equation (3):

$$R_q = R_0 f + (1 - f) R_v$$

where $f = \frac{w_{up}}{w_{total}}$ is the fraction of vapor that remains after condensation in the cloud, and $R_0$, $R_v$, and $R_q$ are respectively the isotope ratio of the vapor at the LCL, the residual vapor and the accumulated condensate. We assume that $R_q$ follows a Rayleigh distillation: $R_q = R_{0q} f^{\alpha-1}$, where $\alpha$ is the effective fractionation coefficient taking into account both equilibrium and kinetic fractionation consistently with LMDZ simulations [Merlivat and Nief, 1967; Majoube, 1971a, 1971b; Jouzel and Merlivat, 1984]. As a fraction of the condensate precipitates, we obtain the isotopic ratio of the total water in convective plumes [Bony et al., 2008]:

$$R_{dv} = R_0 \frac{1 - \epsilon_p \cdot (1-f^\alpha)}{1 - \epsilon_p \cdot (1-f)}.$$  

[27] If the water balance in convective regions is mainly between large-scale advection and condensation, then $R_{conv}$ is predicted by a Rayleigh distillation. In contrast, if the detrainment term dominates, the isotopic ratio $R_{conv}$ tends toward $R_{dv}$, which is much higher than predicted by a Rayleigh distillation. This is consistent with the effect of convective detrainment on upper tropospheric $\delta D$ evidenced by observational studies [e.g., Webster and Heymsfield, 2003; Sayres et al., 2010]. In practice, $R_{conv}$ is bounded by these two extreme values. In subsidence regions, the isotopic ratio $R_{subs}$ at a given level will be intermediate between $R_{conv}$ at this level and $R_{conv}$ higher in altitude. In addition, $R_{subs}$ increases with vertical diffusion.

3.5. Numerical Application

[28] Equations (1) and (8) and their isotopic counterparts are discretized on the LMDZ vertical grid and solved numerically. We use the annual mean, tropical average temperature profile simulated by LMDZ to calculate profiles of $q_v$ and $\alpha$ that will be used in all calculations. This is justified by the fact that temperature is relatively uniform in the horizontal in the tropics [Sobel and Bretherton, 2000] and are very similar in all our simulations. We assume that in the sub-cloud layer (below the LCL calculated at 925 hPa) RH and $\delta D$ are constant at 80% and $-70\%$ respectively, consistent with the annual mean, tropical-average values simulated by LMDZ. These values are kept constant as a boundary condition throughout the numerical resolution, and this allows us to implicitly account for the effect of surface evaporation. The values of $q$ and $\delta D$ are also relaxed to the value predicted by a Rayleigh distillation above 100 hPa, where almost no convection penetrates. The choice of the upper bound has little impact. The vertical profile of $\epsilon_v$ is exactly the same as in LMDZ: in the control simulation, $\epsilon = 0$ up to 150 hPa above LCL, $\epsilon = 0.99$ above 500 hPa above LCL, and $\epsilon$ varies linearly between these two values from 150 hPa to 500 hPa above LCL [Emanuel and Zivkovic-Rothman, 1999; Bony and Emanuel, 2001]. The vertical profile of $\epsilon_q$ is taken to mimic the behavior of large-scale condensation scheme of LMDZ: $\epsilon_q$ varies linearly from 0 at the surface to 0.4 at 100 hPa.

[29] All other variables were optimized to reproduce the tendencies simulated by LMDZ (Figures 2b and 2c) in the mid and upper troposphere. We calculate $\omega_{up}$ and $\omega_{down}$ by assuming that the profiles of vertical velocity in hPa/day follow a cubic shape with a maximum at 500 hPa. We take $\omega_{up} = 40$ hPa/day and $\omega_{down} = 40$ hPa/day at 500 hPa. We assume that the profile of $k_{dtr}$ follows a Gaussian shape with a maximum at 120 hPa, a standard deviation at 300 hPa and a maximum of 0.2 day$^{-1}$. We assume that $k_{cond}$ equals 0.33 day$^{-1}$. We assume that $k_{mix}$ varies linearly between 0.05 day$^{-1}$ and 1 day$^{-1}$ from 800 hPa to 100 hPa. Finally, $K_{diff}$ is taken so that the diffusion is equivalent to exchanging a thickness $\delta D \cdot dt$ of air between each adjacent level at each time step $dt$, with $\omega_{diff} = 20$ hPa/day. This value was taken as the minimum value to allow numerical stability of the single-column model.

[30] With this set of parameters, the simple single-column model reproduces satisfactorily the vertical profiles of the main tendencies involved in the mid and upper troposphere water balance simulated by LMDZ, though in a simplified way (Figures 2d and 2e). The model fails near the surface, which is neither surprising nor problematic since we focus on mid and upper tropospheric processes. As the model was tuned to reproduce the humidity tendencies for the control simulation, the capacity of the simple framework to predict the RH and isotopic profiles simulated by LMDZ in the different sensitivity tests can be viewed as an independent check of the simple framework.

4. Sensitivity of RH to the Model Physics, Nudging and Resolution

4.1. Sensitivity to Parameterized Processes

[31] Numerous studies have shown that GCMs suffer from a moist bias compared to various data sets in the tropical upper troposphere and in the subtropical mid-to-upper troposphere, following a horse-shoe pattern [Soden and Bretherton, 1994; Salathe and Chester, 1995; Chen et al., 1996; Roca et al., 1997; Chen et al., 1998; Allan et al., 2003; Brogniez et al., 2005; Pierce et al., 2006; John and Soden, 2007; Sherwood et al., 2010; Chung et al., 2011]. As an illustrative example, Figure 3 compares the simulated RH in the control LMDZ simulation with the AIRS (Atmospheric Infra-Red Sounder data) data [Aumann et al., 2003]. Consistent with previous studies and other GCMs, LMDZ exhibits a moist bias throughout the mid and upper troposphere in tropical average (Figure 3a). Figure 3b shows composites of RH at 350 hPa as a function of monthly mean $\omega_{500}$. Due to a clear-sky sampling bias in AIRS [Fetzer et al., 2006], upper-tropospheric RH in deep convective tropical regions could be underestimated by as much as 10–20% [Pierce et al., 2006]. The moist bias seems to be stronger in regions of large-scale ascent than in regions of large-scale descent in Figure 3b, but this is likely an artifact of the clear-sky bias. This does not contradict the fact that in most GCMs, including LMDZ, the moist bias is most pronounced.
in subtropical regions. An accurate comparison of LMDZ with AIRS is beyond the scope of this paper.

To understand the cause of the moist bias, we performed sensitivity tests in which the model physics was degraded in 3 different ways, corresponding to 3 possible causes for a larger moist bias (Table 3). Hereafter, they are referred to as “moist bias” simulations. We conducted tests with a larger rather than smaller moist bias because (1) the goal is to see how isotopic measurements can help understand biases, and (2) since the control simulation is already slightly biased, trying to improve the RH for different causes would lead to error compensations that would make the presentation of the results less straightforward. All these sensitivity tests are nudged by the ECMWF winds, so that the large-scale circulation is similar in all the simulations. This methodology excludes dynamical feedbacks, and thus allows us to focus on differences that are due to physical processes only.

In the “diffusive advection” simulation, we replace Van Leer’s (1977) second-order advection scheme by a simple upstream scheme [Godunov, 1959]. This is the version described by Risi et al. [2010b] and provided to the SWING2 archive. The upstream scheme is intrinsically more diffusive. This leads to a 15% stronger moist bias throughout the tropical troposphere (Figure 3a, green). Additional tests show that most of the moistening in this simulation is due to excessive diffusion in the vertical, rather than the horizontal, advective scheme. In the theoretical framework, this simulation corresponds to an increase in $K_{diff}$. Vertical diffusion moistens the mid and upper-troposphere due to down gradient moisture flux and to the concavity of $q$ profiles as a function of height. The moist bias is strongest in the subsidence region, because the diffusive moistening accumulates in air parcels as they subside from tropical regions (Figure 3b). In the theoretical framework, this is represented by the diffusion term being present in both convective and subsidence regions (equations (1) and (8)).

In the “$\sigma_\nu/10$” simulation, the sub-grid-scale variability in water vapor, which is used to predict large-scale condensation in the Bony and Emanuel [2001] statistical cloud scheme, is divided by 10 at all levels. This reduces the proportion of air in the grid box exceeding saturation. Therefore, large-scale condensation decreases and contributes less to the dehydration of air masses, leading to a

Table 3. Summary of the Four Main Sensitivity Simulations Performed With the LMDZ GCM

<table>
<thead>
<tr>
<th>Name</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>Control</td>
<td>Control simulation described with the actual AR4 version of LMDZ4.</td>
</tr>
<tr>
<td>Diffusive advection</td>
<td>Same as control but a simple upstream scheme [Godunov, 1959] is used rather than the second order advection scheme [Van Leer, 1977; Hourdin and Armengaud, 1999]. This is the simulation described by Risi et al. [2010b] and provided to SWING2.</td>
</tr>
<tr>
<td>$\sigma_\nu/10$</td>
<td>Same as control but the sub-grid-scale variability in water vapor used to predict large-scale condensation and nebulosity is divided by 10.</td>
</tr>
<tr>
<td>$\epsilon_\nu/2$</td>
<td>Same as control but the precipitation efficiency in both the convective and large-scale precipitation schemes was divided by 2.</td>
</tr>
</tbody>
</table>
stronger moist bias by about 15% in the upper troposphere (Figure 3, blue). This is consistent with the theoretical framework, in which dividing $\sigma_h$ by 10 leads to an increase in the lower bound for $q_{asc}$ toward saturation. The effect of $\sigma_h$ is largest in regions of large-scale ascent (Figure 3b), because this is where the large-scale condensation scheme plays a significant role. In subsidence regions, its effect is smaller.

Finally, in the “$\epsilon_p/2$” simulation, the precipitation efficiency $\epsilon_p$ in the convective scheme was divided by 2. Therefore, a higher proportion of the condensate evaporates into the environment rather than precipitates, significantly moistening the atmosphere by 5 to 10% (Figure 3a, cyan). This is consistent with the theoretical framework, in which the increase in $\epsilon_p$ leads to an increase of $q_{dir}$, which constitutes the upper bound for $q_{asc}$. Again, the effect is largest in regions of large-scale ascent (Figure 3b), because this is where convective detrainment plays a significant role.

The large sensitivity of RH to micro- and macrophysical cloud processes seems to contradict some earlier studies. Sherwood [1996] argued that cloud processes act to bring the convective column close to saturation, and have thus very limited quantitative effect of RH [Sherwood and Meyer, 2006]. However, at the scale of a GCM grid box, the atmospheric column is not necessarily close to saturation in convective regions. Therefore, there is room for modulation of the RH by cloud processes. Then, since RH in convective regions serves as an initial condition for the RH in other dynamical regimes through large-scale transport and subsidence, RH modulations in convective regions by cloud processes propagate to other regimes. Using a simple backtrajectory model, Dessler and Sherwood [2000] had shown that the large-scale circulation alone could explain to first order the observed RH distribution in the upper troposphere. They showed an influence of both sub-grid-scale heterogeneity and condensate detrainment, consistent with our study, but they discarded these processes on the basis that each of them individually worsen their simulation. In GCMs however, both these processes play a simultaneous role (Figure 2b) and the degree to which they compensate each other is not fully understood.

Figure 4. Comparison of annual mean water vapor $\delta D$ simulated by the control simulation and by the three moist bias simulations. (a) Vertical profiles of tropical (30°S–30°N) average $\delta D$. (b) Zonal mean $\delta D$ at 350 hPa. (c) Tropical average $\delta D$ at 350 hPa as a function of annual mean, tropical average $q$ at 350 hPa.
other affects the simulated RH. To summarize, while large-scale circulation is the major control on RH spatial variations in a given model, there is a wide margin for variations in mean RH associated with the representation of cloud processes.

4.2. Sensitivity to the Nudging and Resolution

[37] To assess the relative importance of uncertainties related to large-scale circulation in simulating RH, we compared the control simulation with nudged wind fields to a free-running simulation (i.e. without nudging). The effect on RH is however smaller (<5%) than the effect of the model physics (Figure 3, pink).

[38] Strong gradients of RH arise in the tropics and subtropics because the timescale of mixing processes is longer than that of radiative subsidence [Pierrehumbert, 1998; Zhang et al., 2003]. A higher resolution may improve the simulation of RH by GCMs [Sherwood et al., 2010]. We thus performed free-running and nudged simulations at a higher horizontal resolution (1.25° in latitude / C2 / 2.5° in longitude). The impact of resolution is slightly stronger for the free-running simulation, because it allows the model to create its own finer scale circulation. The RH is decreased by 2–3% in the subtropics, where the RH gradients are the strongest. This impact is much smaller than that of physical processes (Figure 3).

[39] Therefore, improving the representation of large-scale circulation or improving horizontal resolution has a smaller effect on the RH simulation than changing the model physics. Since the large-scale circulation is relatively well simulated in GCMs, the uncertainties that remain are related to the models physics. Therefore, while the large-scale circulation is the main control on RH, it is not the major source of uncertainty. This is confirmed by the fact that reanalyses models also exhibit the moist bias [Salathe and Chester, 1995; Chen et al., 1998].

[40] We thus mainly focus on the sensitivity tests which are designed to test to the model physics.

[41] Coarse vertical resolution has also been suggested to contribute to the moist bias [Pope et al., 2001]. We expect the vertical advection to be less diffusive at finer vertical resolution, with an effect opposite to the “diffusive advection” simulation. The simulation at higher vertical resolution (39 vertical levels rather than 19) indeed leads to a decrease in RH of about 5% (Figure 3a, dashed red). Since this simulation provides redundant information compared to the

Figure 5. Illustration of how the simple theoretical model captures the behavior of $q$ and $\delta D$ for the sensitivity simulations, at 350 hPa as an example. Diagrams of $\delta D$ versus log($q$) are shown so that Rayleigh distillation follows approximately a straight line. On each subplot, the mechanisms for the control simulation is shown in red. The vertical profile in the convective region between 350 hPa (circle) and 225 hPa (square) follows the thick line. In subsidence regions, the humidity and $\delta D$ (star) reflect a mixture between the air from convective regions at the same level and from levels above, and is further affected by vertical diffusion, following the hand-drawn dashed line. These markers and lines are shown also for the three moist bias simulations: diffusive advection (Figure 5a, green), $\sigma_q/10$ (Figure 5b, blue) and $\epsilon_q/2$ (Figure 5c, pink). Note that log($q$) values of −2.5, −2, −1.5, −1, −0.5 and 0 correspond to $q$ values of 0.08, 0.14, 0.22, 0.37, 0.61 and 1 g/kg.
“diffusive advection” simulation, we focus on the latter for the sake of brevity.

5. Isotopic Fingerprint of Different Causes for the Moist Bias

[42] The goal of this section is threefold. First, we compare the isotopic behavior associated with the different causes of a moist bias in our sensitivity tests. If the isotopic behavior is significantly different between the simulations in a way that is complementary to the behavior of RH, then this isotopic behavior could be used as a diagnostic for the moist bias. Second, we interpret the isotopic behavior using the theoretical framework, to check that we understand the processes at play. Third, we compare the simulations to the data, to identify which one most closely matches the observations and to assess to what extent the isotopic measurements can help discriminate between the different simulations.

5.1. Zonal, Annual Means

[43] Figure 4a compares tropical mean profiles of $\delta D$ for the control and moist bias simulations. In all moist bias simulations $\delta D$ is higher than in the control between 500 and 200 hPa. The increase in $\delta D$ is the strongest in $\epsilon_\rho/2$ in the upper troposphere. Figure 4b compares the zonal mean $\delta D$ at 350 hPa. The level 350 hPa is chosen as representative of the upper troposphere where the isotopic differences between the tests are the strongest. Most of our analysis focuses on this level. In the “advective diffusion” and “$\epsilon_\rho/10$” simulations, upper tropospheric $\delta D$ increases at all latitudes (Figure 4b), whereas in the “$\epsilon_\rho/2$” simulation, the $\delta D$ increase is concentrated in the tropics, consistent with the convective detrainment acting mainly in the tropics. The increase in $\delta D$ does not obviously relate to the increase in $q$ or RH following Rayleigh distillation: the increase in tropical $\delta D$ is largest in the “$\epsilon_\rho/2$” simulation, although the increase in $q$ or RH is smallest for this simulation (Figure 4c). This shows that $\delta D$ is particularly sensitive to convective detrainment and provides additional information compared to traditional humidity variables.

[44] To understand the $\delta D$ increase in the moist bias simulations, in Figure 5 we illustrate the results of the theoretical framework (section 3) at 350 hPa in a $\delta D$ versus log ($q$) diagram, in which Rayleigh distillations are approximately straight lines. The solid red arrow shows the $\delta D$ profile in convective regions from 350 hPa (red circle) up to 225 hPa (red square) for the control case. In convective regions, $\delta D$ decreases as $q$ decreases with altitude, but less steeply than predicted by Rayleigh distillation, due to convective detrainment of condensate [e.g., Moyer et al., 1996]. Then, as explained in section 3.3, $\delta D$ in subsidence regions at 350 hPa is a mixture between $\delta D$ in convective regions at 350 hPa and $\delta D$ in convective regions higher up (e.g. 225 hPa). The dashed red arrow shows the effect of mixing the air at 350 hPa and 225 hPa, combined with the effect of vertical diffusion. The red star shows the resulting $\delta D$ at 350 hPa in subsidence regions. Since mixing lines are curved in a way that leads to higher $\delta D$ compared to Rayleigh lines [e.g., Brown et al., 2008; Galewsky and Hurley, 2010; Noone et al., 2011], $\delta D$ in subsidence regions is higher for a given $q$ than in convective regions. Vertical
diffusion also contributes to the $\delta D$ increase, since diffusion acts like mixing.

[45] We now use the theoretical framework to interpret the $\delta D$ difference between the sensitivity tests. When vertical diffusion is stronger (here, we take $w_{\text{diff}} = 80 \, \text{hPa/d}$ compared to $20 \, \text{hPa/d}$ in the control), convective regions are slightly moistened and have a significantly higher $\delta D$ due to the curvature of mixing lines (Figure 5a, green). In subsidence regions, the $\delta D$ is even further increased, due to the additional diffusion along the way. In the “$\sigma_p/10$” simulation, the distillation curve in convective regions remains approximately the same, but since large-scale condensation is less efficient, the distillation does not go as far as in the control (Figure 5b, blue). $q$ and $\delta D$ are thus higher in convective regions and this signature is conserved during the subsidence, leading to higher $q$ and $\delta D$ everywhere. In “$\epsilon_p/2$”, more condensate is detrained from convective towers, so that $\delta D$ in convective regions is much higher, especially in the upper troposphere where detrainment is largest (Figure 5c, cyan). This higher $\delta D$ is then conserved during subsidence in subsidence regions.

[46] To summarize, the increase in $\delta D$ associated with the moistening has a very different cause in each of the three sensitivity tests. As a result, for a given increase in $q$ relatively to the control, the $\delta D$ increase is very different between the tests (Figure 4c). In particular, the theoretical model is able to predict that for “$\sigma_p/2$”, $\delta D$ is 3–4 times more sensitive to changes in $q$ than for “advective diffusion” or “$\sigma_p/10$”.

Figure 7. Comparison of water vapor $\delta D$ simulated by the control simulation and the by three moist bias simulations, binned into dynamical regimes. (a) Vertical profiles of the difference between composite of monthly mean $\delta D$ in regions of large-scale ascent (tropical grid cells where $\omega_{500} < -35 \, \text{hPa/d}$) and composite of monthly mean $\delta D$ in subsidence regions (tropical grid cells where $\omega_{500} > 35 \, \text{hPa/d}$). The variable $\omega_{500}$ refers to the large-scale vertical velocity at 500 hPa, with negative (positive) values in regions of large-scale ascent (subsidence). (b) Composites of monthly mean $\delta D$ at 350 hPa as a function of $\omega_{500}$ over the tropics. The annual mean, tropical average was subtracted to focus on contrasts between dynamical regimes. (c) Composite of monthly mean $\delta D$ at 350 hPa in convective regions minus that in subsidence regions, as a function of the same difference for $q$. The difference in $q$ was normalized and expressed in % as follows: $(q_{\text{asc}} - q_{\text{subs}})/(q_{\text{asc}} + q_{\text{subs}}) \cdot 200$. 
5.2. Variations With Dynamical Regime

In the tropics, it is convenient to examine model output as a function of dynamical regime characterized by the monthly mean large-scale vertical velocity $\omega_{500}$ [Bony et al., 2004]. Figure 7a shows profiles of $\delta D$ differences between tropical regions of large-scale ascent and descent, and Figure 7b shows $\delta D$ at 350 hPa as a function of $\omega_{500}$. The sensitivity tests show very different behaviors, both quantitatively and qualitatively. The only common feature between all simulations is that at the surface, convective regions have a lower $\delta D$ than subsidence regions (Figure 7a). Strong precipitation events have long been observed to be associated with a lower $\delta D$ in the precipitation and the surface vapor (i.e. amount effect [Dansgaard, 1964]), and this has been shown to involve processes restricted to the lower troposphere such as rain re-evaporation or unsaturated downdrafts [Lawrence et al., 2004; Risi et al., 2008, 2010a; Field et al., 2010]. In contrast, from 900 to 200 hPa in the control simulation, $\delta D$ is lower in regions of large-scale subsidence than in regions of large-scale ascent, by up to 50‰ around 500 hPa. This is expected from the simple model (Figure 5, stars versus circles), since the low $\delta D$ values found in the upper troposphere of large-scale ascent regions are largely conserved during subsidence. The decrease of $\delta D$ as $\omega_{500}$ increases is the strongest for $\omega_{500} > 10$ hPa (Figure 7b).

In the “$\sigma_p/10$” simulation, the contrast between convective and subsidence regions is slightly weaker, with higher $\delta D$ in subsidence regions. In the “$\sigma_p/2$” simulation, the decrease of $\delta D$ as $\omega_{500}$ increases is similar to the control for $\omega_{500} > 20$ hPa/d. However, for $\omega_{500} < 20$ hPa/d, $\delta D$ decreases as $\omega_{500}$ decreases throughout the entire troposphere. Similarly, in the “diffusive advection” simulation, $\delta D$ decreases as $\omega_{500}$ decreases for $\omega_{500} < 20$ hPa/d. In addition, contrary to all other simulations, $\delta D$ does not decrease with $\omega_{500}$ for $\omega_{500} > 20$ hPa/d. Even in strongly subsiding regions, $\delta D$ is always higher than in convective regions throughout the free troposphere.

We notice that the spread in our simulations is not obviously linked to the behavior of $q$: “advective diffusion” exhibits the most negative $\delta D$ difference between convective and subsidence regions, but not the weakest contrast for $q$ (Figure 9). We also checked that the isotopic behavior is not related to how the precipitation rate varies with $\omega_{500}$. This
shows again that $\delta D$ provides complementary information on the relative magnitude of processes contributing to the moisture balance.

[51] We use the simple theoretical framework to explain the different isotopic behavior. In the “diffusive advection” simulation, the stronger vertical diffusion in subsidence regions leads to a stronger $\delta D$ increase than in the control. If the diffusion is sufficiently strong, it can overcome the effect of subsidence, leading to higher $\delta D$ in subsidence regions than in convective regions (Figure 5a). In the “$\sigma_{h}/10$” simulation, $q$ and $\delta D$ are higher at all levels in convective regions, so this signal is preserved during subsidence (Figure 5b). Hence, the $\delta D$ contrast between convective and subsidence regions is similar to that in the control. Finally, in the “$\epsilon_{p}/2$” simulation, the vertical gradient in $\delta D$ in the convective region is weaker than in the control, due to the effect of condensate detrainment in the upper troposphere (Figure 5c). Therefore, the effect of subsidence on the $\delta D$ is weaker, leading to the weaker contrast between subsidence and convective regions. In addition, the very low $\delta D$ in very convective regions can be due to the much weaker convective mass fluxes in the “$\epsilon_{p}/2$” simulation than in the control. Indeed, since most of the condensate detains rather than precipitates, the model has to produce precipitation by an alternative means, i.e. by large-scale condensation. Therefore, in convective regions, large-scale condensation is stronger and convective detrainment fluxes are smaller in the “$\epsilon_{p}/2$” simulation than in the control, explaining why $\delta D$ is so low in convective regions in the “$\epsilon_{p}/2$” simulation.
Model – data difference of zonal mean JJA-DJF variations

![Figure 10](image)

Figure 10. Same as Figure 6 but for model-data differences of zonal mean seasonal variations (JJA-DJF). Note that two kinds of differences (model-data and JJA-DJF) have been compacted into the $\Delta \delta D$ notation.

[52] Figure 8 shows that even after taking into account spatiotemporal sampling and instrument sensitivity corresponding to the different data sets, the main $\delta D$ characteristics of our simulations remain. The isotopic data could thus help discriminate which of these very distinct behavior better represents the real atmosphere. In the lower and mid troposphere, the control simulation has the best agreement with SCIAMACHY and TES, whereas the “diffusive advection” and “$\epsilon_p/2$” simulations exhibit excessively low $\delta D$ values in convective regions. (Figures 8a and 8b). In the upper troposphere however, none of the simulations is able to match the strong increase in $\delta D$ in regimes of large-scale ascent.

5.3. Seasonal Variations

[53] In the tropics and the subtropics, much of the seasonal variations are associated with seasonal variations in dynamical regimes. When ascending motions are more frequent, $\delta D$ is expected to be higher as explained in section 5.2. In the control simulation, at all latitudes, upper tropospheric $\delta D$ is higher in summer than in winter (Figures 9a and 9b). This is consistent with more frequent ascending motions in summer than in winter due to the location of the inter-tropical convergence zone. In the subtropics in both hemispheres, the seasonality is very weak, or even reversed, in the subtropics in both hemispheres (20°S–30°S and 20°N–30°N). This is consistent with the $\delta D$ being higher in subsidence regions than in convective regions in this simulation.

[55] Therefore, the understanding of isotopic variations across dynamical regimes (section 5.2) allows us to understand the different behaviors of our simulations in terms of isotopic seasonality. Again, the different isotopic behaviors are not obviously related to those in humidity (Figure 9c), showing the added value of isotopic measurements to discriminate between the simulations.

[56] At all levels, the control simulation underestimates the isotopic seasonality in the subtropics (Figure 10). This is robust in the comparisons between the model and all data sets (in situ, ground-based remote-sensing and satellites). The robustness of this result is further discussed in P1. Therefore, the underestimated or even reversed seasonality in the “diffusive advection” simulation worsens the model-data agreement. Compared to ACE for example, the $\delta D$ seasonality is more underestimated in the “diffusive advection” simulation than in the control by 40–50‰ in the Northern subtropics (Figures 10d and 10e). The magnitude of this difference is unlikely to be affected by absolute calibration problems in the data since we are looking at variations. In addition, it is larger than any additional sources of model-data comparison uncertainties detailed in P1. Therefore, the deterioration of the simulated subtropical seasonality in the “diffusive advection” simulation is robustly constrained by the comparison with the ACE data. It is also observable in the subtropics at 600 hPa compared to TES (Figure 10c) and compared to MIPAS at 350 hPa (Figure 10f) and at 250 hPa (Figure 10g), except for MIPAS in the Northern Hemisphere.

[57] To measure the degree to which our simulations capture the $\delta D$ seasonality in the subtropics and lower
midlatitudes, we calculate the ratio of the simulated JJA-DJF variations to the observed JJA-DJF variations, at different levels, in different hemispheres and compared to different data sets (Table 4, zonal mean seasonal variations and seasonal variations (JJA-DJF)). Although there is no consensus on which simulation performs the best, the “advective diffusion” simulation has the lowest seasonality in 20 of these metrics, corresponding to the worst model-data agreement in 19 of these metrics. For example, for the average over 20°S–30°S and over 20°N–30°N, the “advective diffusion” simulation has the worst underestimate of the seasonality compared to all satellite data sets except when compared to MIPAS in the Northern Hemisphere. Between 20°S–45°S and 20°N–45°N, this is also the case for all of the aircraft data sets and at all ground-based remote-sensing stations except at Pasadena.

To summarize, in LMDZ, when a moist bias is due to excessively diffusive vertical advection, the isotopic seasonality in the subtropics is distinctly lower. This can be robustly identified by comparison with almost all data sets, especially with ground-based remote-sensing and ACE data sets.

5.4. Spatial Variations

Spatial variations partially reflect variations in dynamical regimes. Spatial variations in the control simulation and in the SCIAMACHY, TES and MIPAS data sets are extensively discussed in P1. To measure the degree to which simulations reproduce spatial patterns of annual mean $\delta D$, we calculate the spatial correlations between simulated and observed annual mean $\delta D$, and the ratio of the simulated spatial standard deviation to the observed spatial standard deviation of annual mean $\delta D$ (Table 4, spatial variations of annual mean). To measure the degree to which simulations reproduce spatial patterns of $\delta D$ seasonality, we calculate the same metrics for JJA-DJF variations (Table 4, spatial variations of seasonal variations (JJA-DJF)). No consensus emerges regarding the best or worst performing simulation. The control simulation is most frequently the best in capturing the spatial patterns (as quantified by correlations). In

### Table 4. Quantitative Metrics to Compare the Model-Data Agreement Between the Different LMDZ Simulations

<table>
<thead>
<tr>
<th>Feature</th>
<th>Metric</th>
<th>Region</th>
<th>Data Set</th>
<th>Level</th>
<th>Control</th>
<th>Diffusive Advection</th>
<th>$\sigma_{10}$</th>
<th>$\sigma_{30}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>Zonal mean seasonal variations (JJA-JF)</td>
<td>amplitude ratio</td>
<td>20°N–30°N</td>
<td>SCIAMACHY total column</td>
<td>0.67</td>
<td>0.40</td>
<td>0.41</td>
<td>0.60</td>
<td></td>
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<tr>
<td></td>
<td>amplitude ratio</td>
<td>20°N–30°N</td>
<td>TES 600 hPa</td>
<td>1.02</td>
<td>0.27</td>
<td>1.14</td>
<td>0.57</td>
<td></td>
</tr>
<tr>
<td></td>
<td>amplitude ratio</td>
<td>20°N–30°N</td>
<td>MIPAS 350 hPa</td>
<td>0.51</td>
<td>2.12</td>
<td>0.21</td>
<td>0.26</td>
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<tr>
<td></td>
<td>amplitude ratio</td>
<td>20°N–30°N</td>
<td>ACE 350 hPa</td>
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<td>0.07</td>
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</tr>
<tr>
<td></td>
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<td>MIPAS 250 hPa</td>
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</tr>
<tr>
<td></td>
<td>amplitude ratio</td>
<td>20°N–30°N</td>
<td>ACE 250 hPa</td>
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<td></td>
<td>amplitude ratio</td>
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<td></td>
<td>amplitude ratio</td>
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<td>ACE 250 hPa</td>
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<td>0.72</td>
<td>0.72</td>
<td>0.98</td>
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</tr>
<tr>
<td>Seasonal variations (JJA-JF) at all subtropical and midlatitudes</td>
<td>amplitude ratio</td>
<td>Wollongong (34.41°S)</td>
<td>NDACC total column</td>
<td>0.72</td>
<td>0.51</td>
<td>0.64</td>
<td>0.74</td>
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</tr>
<tr>
<td>(15°S–45°S and 15°S–45°N)</td>
<td>amplitude ratio</td>
<td>Pasadena (34.2°N)</td>
<td>NDACC total column</td>
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<td>0.30</td>
<td>0.60</td>
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<tr>
<td></td>
<td>amplitude ratio</td>
<td>Izaña (28.30°N)</td>
<td>TCCON total column</td>
<td>2.72</td>
<td>1.71</td>
<td>2.50</td>
<td>2.86</td>
<td></td>
</tr>
<tr>
<td></td>
<td>amplitude ratio</td>
<td>Oklahoma (36.6°N)</td>
<td>TCCON total column</td>
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<td>0.28</td>
<td>0.30</td>
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<tr>
<td></td>
<td>amplitude ratio</td>
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<td>0.45</td>
<td>1.0</td>
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</tr>
<tr>
<td></td>
<td>amplitude ratio</td>
<td>Death Valley (36°N)</td>
<td>Ehhalt 350 hPa</td>
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<td>0.39</td>
<td>0.39</td>
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</tr>
<tr>
<td></td>
<td>amplitude ratio</td>
<td>Nebraska (41.83°N)</td>
<td>Ehhalt 350 hPa</td>
<td>0.93</td>
<td>0.69</td>
<td>0.83</td>
<td>0.89</td>
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<tr>
<td>Spatial variations of annual mean</td>
<td>standard deviation ratio</td>
<td>45°S–45°N</td>
<td>SCIAMACHY total column</td>
<td>0.42</td>
<td>0.48</td>
<td>0.43</td>
<td>0.59</td>
<td></td>
</tr>
<tr>
<td></td>
<td>standard deviation ratio</td>
<td>45°S–45°N</td>
<td>TES 600 hPa</td>
<td>0.85</td>
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<td>0.80</td>
<td>1.07</td>
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<tr>
<td></td>
<td>standard deviation ratio</td>
<td>45°S–45°N</td>
<td>MIPAS 250 hPa</td>
<td>0.25</td>
<td>0.46</td>
<td>0.32</td>
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</tr>
<tr>
<td></td>
<td>correlation</td>
<td>45°S–45°N</td>
<td>SCIAMACHY total column</td>
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</tr>
<tr>
<td></td>
<td>correlation</td>
<td>45°S–45°N</td>
<td>TES 600 hPa</td>
<td>0.93</td>
<td>0.91</td>
<td>0.92</td>
<td>0.86</td>
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</tr>
<tr>
<td></td>
<td>correlation</td>
<td>45°S–45°N</td>
<td>MIPAS 250 hPa</td>
<td>0.54</td>
<td>0.61</td>
<td>0.51</td>
<td>0.72</td>
<td></td>
</tr>
<tr>
<td>Spatial variations of seasonal variations (JJA-JF)</td>
<td>standard deviation ratio</td>
<td>45°S–45°N</td>
<td>SCIAMACHY total column</td>
<td>0.31</td>
<td>0.40</td>
<td>0.31</td>
<td>0.46</td>
<td></td>
</tr>
<tr>
<td></td>
<td>standard deviation ratio</td>
<td>45°S–45°N</td>
<td>TES 600 hPa</td>
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<td>0.99</td>
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<td></td>
<td>standard deviation ratio</td>
<td>45°S–45°N</td>
<td>MIPAS 250 hPa</td>
<td>0.33</td>
<td>0.36</td>
<td>0.37</td>
<td>0.44</td>
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</tr>
<tr>
<td></td>
<td>correlation</td>
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<td>SCIAMACHY total column</td>
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<td>0.45</td>
<td>0.44</td>
<td>0.43</td>
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</tr>
<tr>
<td></td>
<td>correlation</td>
<td>45°S–45°N</td>
<td>TES 600 hPa</td>
<td>0.73</td>
<td>0.61</td>
<td>0.61</td>
<td>0.63</td>
<td></td>
</tr>
<tr>
<td></td>
<td>correlation</td>
<td>45°S–45°N</td>
<td>MIPAS 250 hPa</td>
<td>0.47</td>
<td>0.13</td>
<td>0.39</td>
<td>0.53</td>
<td></td>
</tr>
<tr>
<td>Daily variability</td>
<td>standard deviation ratio</td>
<td>Izaña (28.30°N)</td>
<td>ground-based remote-sensing</td>
<td>4.2 km</td>
<td>0.69</td>
<td>0.40</td>
<td>0.51</td>
<td></td>
</tr>
<tr>
<td></td>
<td>correlation</td>
<td>Izaña (28.30°N)</td>
<td>ground-based remote-sensing</td>
<td>4.2 km</td>
<td>0.39</td>
<td>0.45</td>
<td>0.42</td>
<td></td>
</tr>
</tbody>
</table>

*For each feature that we try to evaluate, we look at different metrics, regions, data sets and/or levels. To evaluate the seasonality, we calculate the ratio of amplitude as the amplitude of seasonal variations (JJA-DJF) for the simulation divided by that for the data, in average over the specified region or at the specified site. To evaluate spatial variations, we calculate the standard deviation ratio as the standard deviation in the simulation divided by that in the data, and the correlation between the simulation and the data. The same applies to evaluate daily variations at Izaña. For each metric, the simulation with the lowest (resp. highest) seasonality, standard deviation or correlation is highlighted in bold (resp. in italic).
Despite the nudging, GCMs have difficulties in capturing the timing of the subtropical synoptic and intraseasonal variations. Figure 11a shows the comparison of daily data for the year 2007 at 4.2 km, when LMDZ captures best the timing of humidity modulations. The data features very strong intraseasonal variations, with peak-to-peak variations in $q$ of 4 g/kg and in $\delta D$ of 150‰ in summer (Figures 11a and 11b). In the control simulation, the $q$ fluctuations are slightly underestimated and the air is on average too moist (consistent with section 5.1). The magnitude of $\delta D$ fluctuations is also slightly underestimated.

In moist bias simulations, annual mean $q$ and $\delta D$ are higher (Figure 12, consistent with section 5.1). In the “diffusive advection” simulation, the standard deviations of fluctuations are 25% weaker for $q$ and 45% weaker for $\delta D$ than in the control. This is associated with an underestimated slope of $\delta D$ vs $q$ (Figure 11a). This is consistent with the accumulating effect of continuous vertical diffusion during subsident transport from the tropics to Izaña. $q$ and $\delta D$ thus increase most strongly during the driest periods, when air travels for a longer period. Hence the lower variability in $q$ and $\delta D$. In addition, due to the curvature of mixing lines (Figure 5a), diffusion increases $\delta D$ much more strongly for a given increase in $q$ than predicted by Rayleigh distillation. Hence the lower slope of $\delta D$ vs $q$.

In contrast, in the “$\sigma/10” and “$\epsilon/2” simulations, $q$ and $\delta D$ are mainly affected in convective regions where most of the large-scale condensation and convective detrainment take place. The increases in $q$ and $\delta D$ in convective regions are preserved to some extent in subsidence regions, but the slopes of $\delta D$ vs $q$ are not as strongly affected as for the “diffusive advection” simulation (Figures 12b and 12c).

Therefore, the tests exhibit different daily variations in the subtropics, and these are consistent with the predictions from the theoretical framework under different dynamical regimes. The control simulation captures best the timing and amplitude of $\delta D$ variations, while the “diffusive advection” simulation underestimates $\delta D$ fluctuations the worst (Table 4, daily variability). Therefore, this remote-sensing data set, combined with all the other data sets documenting isotopic seasonality, can robustly identify the shortcoming in the numerical scheme used to account for vertical transport in models. This result can be obtained from both daily and seasonal mean data.

### 6. Isotopic Seasonality in the Subtropics: as a Diagnostic for the Moist Bias

We have shown that different processes potentially explaining the moist bias commonly seen in GCMs have a different isotopic signature, in the annual mean, seasonal cycle and intraseasonal variability, as summarized in Table 5. We have also shown that this isotopic signature provides complementary information compared to humidity variables. Compared to the data, the most pronounced isotopic bias is the underestimated or reversed $\delta D$ subtropical seasonality in the “diffusive advection” simulation. This can be seen at all mid and upper tropospheric levels and in most data sets (section 5.3). Therefore, we focus on using the isotopic seasonality as an observable diagnostic to understand the cause of the moist bias in GCMs. In the next section, we...
describe the way in which the seasonality diagnostic is used (section 6.1), check its robustness (section 6.2) and then apply it to the SWING2 models (section 6.3).

6.1. The Isotopic Seasonality Diagnostic

Figure 13a shows the subtropical (20°N–30°N) δD seasonality at 350 hPa as a function of tropical (30°S–30°N) annual-mean RH, for the different simulations. As explained earlier, the seasonality is reversed (green square). This is not the case for the other causes for a moist bias considered in the sensitivity tests (blue and cyan squares). In the δD seasonality versus RH diagram, we will use the slope S between different simulations to diagnose the cause of a moist bias, as illustrated by arrows on Figure 13a. A slope S of the order of −2 to −4‰/% indicates a moist bias that is due to excessively diffusive advection.

We also plot on Figure 13a the approximate position of the data based on AIRS and ACE. The position is subject to large errors for δD because of the sampling mismatch between the observations and monthly mean model outputs. ACE has a much weaker seasonality than MIPAS (P1), so

Table 5. Summary of How Different Causes for a Moist Bias in LMDZ Affects the Isotopic Behavior

<table>
<thead>
<tr>
<th>Cause of Moist Bias</th>
<th>Tropical Mean δD</th>
<th>δD Seasonality in the Subtropics</th>
<th>Intraseasonality in the Subtropics</th>
</tr>
</thead>
<tbody>
<tr>
<td>Excessive diffusion during water vapor transport</td>
<td>overestimated in the mid and upper troposphere</td>
<td>underestimated or reversed in the mid and upper troposphere</td>
<td>under estimated variability of δD due to underestimated q-δD slope</td>
</tr>
<tr>
<td>Underestimated sub-grid-scale variability of water vapor detrainment</td>
<td>overestimated in the upper troposphere with a stronger slope of δD change versus q change.</td>
<td>unaffected</td>
<td>unaffected</td>
</tr>
</tbody>
</table>

Figure 12. Probability density function (PDF) for the joint q − δD distribution at 4.2 km at Izaña. The scale for q is logarithmic: log(q) values of −0.4, −0.2, 0, 0.2, 0.4 and 0.6 correspond to q values of and 0.40, 0.82, 1, 1.22, 1.49 and 1.82 g/kg. The PDFs were calculated from all years of data and binned into bins of 0.05 log(g/kg) and 24% and lines correspond to densities of 0.5% (thinnest lines or lightest colors), 1.5% (medium lines and colors) and 4% (thickest lines and darkest colors). For clarity, the PDF for the control simulation (red) is compared to (a) the data (gray), (b) sensitivity tests with diffusive advection (green), (c) σ_q/10 (blue) and (d) c_q/2 (cyan).
that ACE likely provides a lower bound for observed $\delta D$ seasonality. Despite these limitations, based on the consensus that emerged from section 5.3 and Figure 4, the control simulation likely lies between the data and the "diffusive advection" simulation. This suggests that the cause of the moist bias in the control simulation is likely excessively diffusive advection.

The diffusivity of an advection scheme is an intrinsic and unwanted property that cannot be tuned. One way to reduce the diffusion during vertical advection is to increase the vertical resolution. To test whether this solves consistently the moist-bias and the underestimated $\delta D$ seasonality, we add on Figure 13a the simulation with higher vertical resolution. This simulation is drier and has a stronger seasonality, following a slope similar to that of the "diffusive advection" simulation. This suggests that our $\delta D$ seasonality diagnostic can detect moist biases that are due to excessive diffusion in a consistent way, be they caused by too diffusive an advection scheme or by too low a vertical resolution.

6.2. Robustness of the Diagnostic With Respect to Large-Scale Circulation, Isotopic Representation, Diagnostic Definition and Model Physics

Before we apply the slope diagnostic to all GCMs, we check that aspects of the model simulations that are unrelated to the model physics have relatively little impact. First, we recall that sensitivity tests to the nudging and to the horizontal resolution have a comparatively small impact on both RH and $\delta D$. On Figure 13b (pink), these tests are very close to the control simulation (dashed red circle). This suggests that differences in RH or in $\delta D$ seasonality between different models are more likely due the model physics than to differences in the large-scale circulation.

Second, we investigate the impact of differences in the isotopic representation. All SWING2 models use the same equilibrium fractionation coefficients and make similar assumptions during condensation processes (i.e. closed system during liquid condensation and Rayleigh fractionation during ice condensation). Isotopic differences between models can however arise from differences in diffusivity coefficients [Cappa et al., 2003; Merlivat, 1978], in kinetic fractionation during ice condensation [Jouzel and Merlivat, 1984] or in the representation of isotopic fractionation during rain re-evaporation. Diffusivity coefficients have been shown to affect deuterium excess with very little effect on $\delta D$ [Mathieu et al., 2002; Yoshimura et al., 2010]. Regarding ice condensation, in all models the supersaturation over ice $S_i$ varies with temperature $T$ following $S_i = 1 - \lambda \cdot T$, where $\lambda$ is a tunable parameter. Among all SWING2 models, $\lambda$ varies from 0.003 (e.g. ECHAM, GSM [Hoffmann et al., 1998; Yoshimura et al., 2008]) to 0.005 (HadAM [Tindall et al., 2009]) and is set to 0.004 in LMDZ (Table 2). As an extreme test, we tried $\lambda = 0$ (Figure 13b, purple circle). Although it affects annual mean $\delta D$ in the upper troposphere, it has a very limited effect on $\delta D$ seasonality. Regarding isotopic parameterization during rain re-evaporation, there is a wide diversity among models (Table 2). To encompass this diversity, we performed two additional tests with no post-condensation at all [e.g., Field et al., 2010] and with very strong kinetic fractionation respectively (Figure 13b, purple triangles). To represent strong kinetic effects, we change parameter $\phi$ from 0.9 to 0.7 when calculating the effective
Figure 14. Slope of the seasonal difference in $\delta D$ versus RH, as in Figure 13, as a function of height for the different sensitivity tests compared to the control. Slopes are shown only where the RH of the two simulations differs by more than 1%. Solid lines: the control simulation and the moist bias simulations are those described in sections 2.1 and 4.1. Dashed lines: same as solid, but both the control and the sensitivity simulations were modified to test the robustness to the model physics. Dashed green: both the control and “diffusive advection” simulations were redone with $\epsilon_p/2$. Dashed blue: both the control and “$\sigma_h/10$” simulations were redone with diffusive advection. Dashed cyan: both the control and “$\epsilon_p/2$” simulations were redone with diffusive advection.

RH around raindrops ($h_{\text{eff}}$) as a function of simulated RH ($h$) following $h_{\text{eff}} = \phi + (1 - \phi) \cdot h$ [Bony et al., 2008; Risi et al., 2010b]. These tests have much smaller impacts than the sensitivity tests to the model physics. Therefore, we conclude that the details of the isotopic implementation is likely not the major factor contributing to the $\delta D$ seasonality dispersion between models.

[71] We now check the robustness of our diagnostic with respect to altitude. Figure 14 shows the slope $S$ between various pairs of simulations as a function of altitude. The slope between the control and the “diffusive advection” simulation is much more negative than for the other tests from 500 to 150 hPa (solid green). The diagnostic is thus robust with respect to altitude.

[72] We also checked the robustness with respect to the geographical domain. We tested different subtropical domains for $\delta D$ seasonality (20°N–30°N, 15°N–30°N, 20°N–35°N, 25°N–35°N) and different tropical domains for annual-mean RH (30°S–30°N, 25°S–25°N and 20°S–20°N). The slopes $S$ range within $[-3.1, -2.5]$, $[-0.6,0]$ and $[-1.0, -0.3]$ for the “diffusive advection”, “$\sigma_h/10$” and “$\epsilon_p/2$” simulations respectively. Therefore, whatever the choice of the geographical domain, the behavior of the “diffusive advection” can be clearly distinguished from that of the other simulations.

[73] Finally, the robustness of the slope diagnostic with respect to model physics is a necessary condition to apply the diagnostic to all GCMs. The ability to understand the isotopic behavior of the tests with a simple theoretical framework, which involves simple physical processes that are represented in all GCMs, suggests the applicability of these diagnostics to all GCMs. As an additional check, we calculated the slopes $S$ for pairs of simulations with a modified physics. For example, when $\epsilon_p$ is divided by two in both the control and “diffusive advection” simulations, the effect of diffusive advection is a deterioration of the seasonality following the same slope $S$ of about $-2$ to $-4\%$ (Figure 14, dashed green). Similarly, when $\sigma_h$ is divided by 2 in both the control and “$\sigma_h/10$” simulations, or when using the diffusive advection scheme in both the control and “$\epsilon_p/2$” simulations, the slopes $S$ characterizing the sensitivity to $\sigma_h$ and $\epsilon_p$ remain much less negative than $-2\%$ between 500 and 150 hPa (Figure 14, dashed blue and cyan).

Therefore, the isotopic diagnostic is robustly related to the source of the bias and relatively independent of other aspects of model physics.

6.3 Application to SWING2 GCMs

[74] Figure 15b shows the $\delta D$ seasonality versus RH diagram for the other SWING2 simulations (black markers). As expected, all models are too moist. Models show a very wide spread in $\delta D$ seasonality, spanning more than 70‰, with variations even in the sign. Isotopic observations can thus discriminate between models despite the large uncertainties in the data sets. The spread in our LMDZ seasonality tests (about 40‰) is of the same order of magnitude as that in SWING2 models. Most models plot around the line connecting the control and “diffusive advection” simulations (dashed green). Models with the driest troposphere exhibit the strongest (and presumably most realistic: Figure 4) $\delta D$ seasonality (e.g. Had-AM), while the moistest models exhibit the worst reversed seasonality (e.g. CAM, GSM).

This suggests that in many GCMs, excessive diffusion during vertical advection is a likely cause of the moist bias, and the major source of RH dispersion between models.

[75] This result is robust with altitude (Figure 15b): the correlation among models in this diagram is lower than $-0.7$ from 600 to 250 hPa, and at all these levels the corresponding slope $S$ among models is between $-2$ and $-4\%$. This value corresponds to the slope $S$ characterizing the “diffusive advection” simulation at these levels (Figure 15a).

[76] Some GCMs deviate from the “diffusive advection” line (e.g. GISS, MIROC) suggesting that other processes may be responsible for the moist bias in some models. For example, Wright et al. [2010] suggest that excessive rainfall evaporation in the GISS model may contribute to its moist bias. However, errors in large-scale circulation are not likely to be the major source of the moist bias and of the spread between models. The small effect of nudging the large-scale circulation in LMDZ is supported by the equally small effect
for the GISS model (dashed gray circle). In addition, the best performing model for RH and δD seasonality is Had-AM, which happens to be run in a free-running mode, while the worst performing model is GSM, which happens to be run in a nudged mode and with the highest horizontal resolution. This further supports the suggestion that the representation of physical processes and advection numerics are larger sources of uncertainties on RH than the large-scale circulation. While it has been shown that nudging might improve the simulation at high latitudes [e.g., Yoshimura et al., 2008; Risi et al., 2010b], a correct large-scale circulation does not guarantee that the tropical and subtropical RH and isotopic distribution are realistic.

7. Conclusion

We show that different processes affecting RH in GCMs impact the water vapor isotopic composition differently. Water vapor isotopic measurements can thus be used as an observational diagnostic to detect and understand causes of RH biases in GCMs. This study proposes an approach to practically do so. The isotopic sensitivity to various physical processes is first understood using sensitivity tests and a simple framework. An isotopic diagnostic based on observations is then designed, and its robustness with respect to the data set used and other aspects of the model physics and isotopic representation is checked. This diagnostic is finally applied to a wider range of models to diagnose the reason for their bias.

[78] As an example, in this study we aim at understanding the reasons for the moist bias in the tropical mid and upper troposphere that has persisted in GCMs for more than a decade. We show that the isotopic seasonality in the subtropics can robustly discriminate simulations in which the moist bias is due to excessively diffusive vertical advection. Applying this isotopic diagnostic to an ensemble of GCMs suggests that excessive diffusion during vertical advection is the most frequent cause of moist bias in GCMs. However, our approach bears some limitations: (1) the lack of validation of upper-tropospheric isotopic data sets, (2) the limited number of our sensitivity tests to the model physics, leaving some other possible sources of moist bias unexplored, (3) the limited subset of GCMs with an isotopic representation and (4) the absence of similar sensitivity tests in the other isotopic GCMs to further check the universality of our diagnostic.

[79] Although it has long been recognized that the large-scale circulation controls the spatial distribution of RH to first order [Sherwood, 1996; Pierrehumbert and Roca, 1998], our study highlights the importance of uncertainties related to parameterized processes controlling RH and advection numerics. If excessive diffusion during vertical advection is indeed the most frequent cause of moist bias in GCMs, this problem can be solved by improving the advection scheme, or alternatively by increasing the vertical resolution. This is consistent with sensitivity to vertical resolutions in other GCMs [Pope et al., 2001; Roeckner et al., 2006].
et al., 2006], and supports the importance of vertical resolution [Tompkins and Emanuel, 2007]. It would be interesting to apply our isotopic diagnostic to more models, in particular those for which other causes for the moist biases have been hypothesized but which did not participate in SWING2 (e.g. Geophysical Fluid Dynamics Laboratory model [Chung et al., 2011]).

Acknowledgments. We thank Debra Wunch, Vanessa Sherlock, Nicholas Deutscher, David Griffith, Paul Wennberg, and Kimberly Strong for detailed comments on the manuscript. DeWAT data of MIPA have been provided by ESA. The ACE mission is supported mainly by the Canadian Space Agency. We thank the Anderson Group at Harvard University for providing water vapor measurements from space, and thank Debra Wunch, Vanessa Sherlock, Nicholas Deutscher, Paul Wennberg and Kimberly Strong for detailed comments on the manuscript. DeWAT data of MIPA have been provided by ESA. The ACE mission is supported mainly by the Canadian Space Agency. We thank the Anderson Group at Harvard University for providing water vapor measurements from space.

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