Impact of Blend Morphology on Interface State Recombination in Bulk Heterojunction Organic Solar Cells


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This work is a re-investigation of the impact of blend morphology and thermal annealing on the electrical performance of regioregular P3HT:PC_{60}BM. The blend is first characterized by combining atomic force microscopy, X-rays diffraction and Time-of-Flight experiments. Then, current-voltage characteristics of photodiode devices are measured in the dark and under illumination. Finally, the existence of exponential tails of electronic gap states is experimentally confirmed by measuring the device spectral response in the sub-band gap regime. This method reveals the existence of a large density of gap states, which is partially reduced by successive annealing steps. The comparison between drift and diffusion simulations and charge transport experiments show that, when band gap tails are properly
taken into account, simulations can satisfactorily reproduce experimental currents under both dark and illumination conditions as a function of voltage and annealing time. This work further confirms the critical impact of tails states on the performance of solar cells.

1. Introduction

Large area, low weight, cost effectiveness and flexibility are some of the exciting promises of printed organic solar cells.\(^1\)–\(^4\) Since the introduction of the organic diode concept by Tang et al in 1986\(^5\), the performances of such devices, produced by printing technologies, have considerably been improved, reaching the record power conversion efficiency of 11.1\%\(^6\).

Bulk HeteroJunction solar cell (BHJ) are one of the most common type of printed organic photovoltaic device.\(^7\) This structure offers not only an excellent tradeoff between optimal charge transfer\(^8\) and exciton dissociation at the donor/acceptor interface\(^9\), but also a good collection of photo-generated carriers.

As pointed out in many papers\(^10\)–\(^13\), the intimate organization of the interpenetrating network composed of the acceptor-like material (fullerene) and the donor-like material (polymer) is of critical importance, directly impacting the cell electro-optical performance. Indeed photon absorption, exciton dissociation and carrier collection are morphology dependent parameters.\(^9,14\)–\(^17\)

For this reason, the optimization of BHJ blend morphology has been considerably investigated, essentially by means of atomic force microscopy (AFM) phase measurement in tapping mode\(^18\) or by transmission electron microscopy (TEM)\(^19,20\), whereas changes in crystallization were usually probed by X-rays diffraction measurements.\(^21\)

In these previous investigations, several parameters impacting the morphology were identified, such as the nature of the solvent\(^22\), the use of solvent additives\(^23,24\), the deposition method\(^25,26\), the polymer/fullerene ratio\(^27,28\), the polymer and fullerene crystallization state
the nature of the fullerene material and one of the most studied, the blend annealing (duration, temperature).

The physical understanding of the relationship between efficiency and morphology was recently improved. Several authors have simulated the performances of such cells, explicitly taking into account morphology and using Kinetic Monte Carlo or 3-D Drift Diffusion approaches. These studies concluded on the existence of an ideal morphology resulting from the competition between exciton dissociation (penalized by too large domains) and Langevin recombinations (enhanced by too narrow domains).

This picture is however still incomplete, as it ignores another significant recombination mechanisms, such as trap-assisted recombination. Indeed, Street and coworkers have pointed out trap-assisted recombination, as one of the major sources of efficiency losses in Poly(3-hexylthiophene-2,5-diyl) (P3HT);[6,6]-Phenyl-C61-butyric acid methyl ester (PC_{60}BM) and Poly[N-9'-heptadecanyl-2,7-carbazole-alt-5,5-(4',7'-di-2-thienyl-2',1',3'-benzo-thiadiazole)] (PCDTBT);[6,6]-Phenyl-C71-butyric acid methyl ester (PC_{70}BM) solar cells. This conclusion was reached using spectral response measurements in the near IR region, probing sub-band gap transitions from trap level states to the HOMO or LUMO bands. However, as measurements were performed in devices featuring a given morphology, little was extracted about the correlation between morphology and trap distribution and density.

In particular, it is well known that either Langevin or trap assisted recombinations mostly occur at the donor acceptor interface. For this reason, it is unclear whether annealing impacts performance mostly by changing the morphology of the blend (i.e. the interface volume fraction) or by modifying the recombination properties of the blend (transport properties, trap concentration).

The aim of this paper is to investigate the impact of morphology on trap assisted recombination in BHJ solar cells. In this contribution, the blend morphology is modified by
successive post-processing thermal treatments at 85°C. Both the blend morphology and the solar cell properties are characterized between each annealing sequence. The spectral response of the device in the near infrared (IR) region is recorded to probe how the band gap states evolve during the experiment. In addition, a numerical model (based on a one-dimensional drift-diffusion formalism), properly calibrated on experiments, is implemented, accounting for the measured exponential trap density of states. The conclusion obtained from comparing experiments and simulations are discussed in the last section of the paper.

2. Experimental Section

The devices had the following general structure: ITO/PEDOT:PSS/P3HT:PC$_{60}$BM/Al. Regioregular poly(3-hexylthiophene-2,5-diyl) (P3HT) and Phenyl-C$_{61}$-butyric acid methyl ester (PC$_{60}$BM) were purchased from Merck. Poly(3,4-ethylenedioxythiophene) (PEDOT:PSS) was purchased from Heraeus with the grade named, CLEVIOS P VP AI 4083. ITO-coated glass substrates were cleaned by successive 10 min. sonication sequences in EDI (water electrodeionization), acetone and isopropanol. A PEDOT:PSS layer used as hole-injection layer was spin-coated at 2000 rpm for 50 seconds to form a 40 nm film on top of the ITO substrate. Then samples were dried at 115°C under nitrogen for 20 minutes. A 50 mg/ml solution of P3HT:PC$_{60}$BM was solubilized in chlorobenzene with a prepared blend ratio of 1:1 (weight ratio). Diiodooctane (DIO) was added to the solution (5% in volume) in order to dissolve selectively the fullerene molecules, preventing C$_{60}$ aggregation$^{[24,44,45]}$. When the chlorobenzene starts evaporating, the fullerene is kept soluble in a semi-crystalline matrix of P3HT by the DIO additive, as its melting point is higher than that of chlorobenzene (169°C vs. 131°C). DIO has been used in all experiments, in particular to improve the degree of crystallinity of P3HT domains (see later).

The P3HT:PC$_{60}$BM blend layer was spin-coated at 800 rpm for 3 minutes in air. The typical thickness of the active layer was 330 nm (measured by mechanical profilometer). Note that
this large value of the active layer, prejudicial for solar cell performances, is needed in this work, in order to keep the level of dark current low. Indeed, it would no longer be possible to measure accurately the EQE at low photon energy if the dark current is too large.

No post-annealing treatment was done after this initial step. Finally, 100 nm thick aluminum cathode contacts were evaporated via shadow mask in a vacuum chamber under a pressure of $10^{-6}$ mbar. Samples were stored one day in a nitrogen-filled glove box and then encapsulated with a glass cover. The device area was 3.14 mm$^2$.

For thermal annealing, the encapsulated photodiode was annealed in nitrogen on a hot plate at 85°C. This low temperature was selected to prevent the C$_{60}$ diffusion usually observed at higher temperatures.$^{[13]}$

3. Experimental results

3.1. Physical characterization of blend morphology

AFM tapping mode measurements were performed on the surface of P3HT:PC$_{60}$BM blends for different annealing steps in order to monitor the average domain width evolution with annealing. Topography and phase were both recorded during tip scan and results are reported in Figure S1. Phase measurement is known to reveal crystallized regions$^{[18,46]}$, taking advantage here of the easily observable fibrous aspect of P3HT. The average width of the P3HT domains is extracted from AFM phase images using an autocorrelation procedure, performed numerically on the raw data. In accord with Dante et al.$^{[18]}$, we measure an average domain width increase during annealing (Figure 1). Moreover, this domain growth is found to follow the kinetics introduced by Alam et al.$^{[47]}$ given by:

$$\langle W(t) \rangle = \langle W_0 \rangle + (D_{ct} t)^n$$

(1)
Here $\langle W_o \rangle$ is the initial average domain width, $D_{eff}$ is the effective diffusivity of organic/polymer material and $n$ is the “Lifshitz-Slyozov” power exponent associated with spinodal decomposition. The following parameters were found by fitting the experimental data:

$$\langle W_o \rangle = 9.96 \text{ nm} \quad D_{eff} = 6.41 \times 10^{-4} \text{ nm.s}^{-1} \quad n = 1$$

This result not only further confirms the validity of Equation 1, but also provide a simple way to estimate the increase in average domain width during the thermal annealing experiments.

X-rays diffraction (XRD) experiments using the Bragg Brentano (0/20) reflection diffraction geometry and a cobalt radiation ($\lambda=1.789$ Å) were performed on P3HT:PC$_{60}$BM films deposited on ITO-coated glass in order to estimate the average growth of P3HT crystallites in the transverse direction, i.e. perpendicular to the substrate. The raw data were corrected by subtracting the background given by the ITO-coated glass substrate reference. The intense (h00) reflections along the $q_z$ direction indicate the formation of a lamellar structure with the side chains oriented out of the plane of the substrate, as illustrated in Figure 2.a. This result is typical of semi-crystalline π-conjugated polymers film such as P3HT. The (0k0) reflections corresponding to the π-π interchain stacking period was not visible on spectra, which confirms its in-plane orientation$^{[48]}$ (see Figure S2 for complete XRD spectra). The coherence length (crystallite size) is measured on the (100) reflection peak using a Pseudo-Voigt peak shape function for fitting and the Scherrer formula. The inter-chains distance $a$ is found equal to 16.5 Å from peak analysis, a value coherent with values typically reported in the literature for P3HT.$^{[31]}$ In Figure 2.b, the coherence length of the P3HT extracted from the (100) peak is reported as function of the annealing time.

We conclude from these observations that the internal structure of P3HT fibrils as seen by AFM consists in a self-organization of P3HT chains in a lamella like structure whose
stacking period is given by the position of the (100) Bragg peak. The in-plane organization has also been confirmed by AFM phase measurements. Moreover, the coherence length $L_c$ corresponding to the average size of P3HT crystallites in the transverse direction (perpendicular to the substrate) was also extracted. Only a weak increase was determined during the post annealing treatment, moving from 10.4 nm to 13.8 nm, and indicating that the crystallite growth is anisotropic in character since it differs noticeably from the observation made for in-plane morphology as observed by AFM. In summary, P3HT lamellae evolves into a larger scale organization in the (001) direction when introducing annealing.

The P3HT crystallite size evolution versus annealing can thus be deduced from the combination of both AFM and X-rays measurements. With an average crystallite volume approximately given by $L_c \pi \left( \frac{w(i)}{4} \right)^2$, and given that $L_c$ appears almost constant under annealing, the results indicate that the crystallites volume increases by a factor 9 during the full duration of the process and its perimeter by a factor of 3.

It has to be noticed that the existence of a third phase in P3HT/PCBM blends, composed of amorphous finely intermixed regions, has been recently reported\cite{77-82}. AFM and X-rays diffraction technics are not suitable for the characterization of this third phase. Indeed, in our work, the characterization of the blend morphology has been limited to the monitoring of the pure P3HT domain. In principle, additional morphology characterization (such as 2-D X-ray scattering in grazing incidence geometry (GIWAXS) as performed in \cite{80}) would be needed to further quantify the importance of this third phase. However, the appearance of vibronic bands on the P3HT:PCBM absorption spectra at 550 nm and 600 nm (see Figure S3) is an first order indication of a large presence of pure P3HT crystalline phase, as expected when an additive has been used, as suggested in the work of Vongsaysy et al.\cite{83}. 


3.2. Time of flight mobility measurements

Performance improvements due to annealing have sometimes been attributed to carrier mobility improvements.\textsuperscript{[21]} To address this assumption in the context of the present work, carrier mobility was measured using the time of flight (TOF) technique,\textsuperscript{[49]} which is well suited for mobility measurements in disordered organic systems such as π-conjugated polymers.\textsuperscript{[50]} The technique, however, cannot be directly applied on the solar cell samples used in this study, as it requires layer thicknesses at least ten times larger than the optical absorption length (approximately 90nm for P3HT:PC\textsubscript{60}BM at 530nm, taking an extinction coefficient of 0.45\textsuperscript{[51]}). Samples used in our TOF experiments were approximately 1 μm thick, i.e. 3 times thicker than the solar cell active layer used in this work. Except for the active layer thickness, the TOF samples fabrication procedure is identical as described in Process details section.

TOF measurements were performed using a 532 nm, 35 μJ/cm\textsuperscript{2}, 1ns laser beam. The laser intensity was attenuated by insertion of neutral density filters. A chopper was used to select a laser pulse every second. The measured signal was averaged over 50 acquisitions. Both electron and hole mobilities were extracted from TOF signals.

The resulting electron and hole mobilities are plotted for several annealing times and square root of applied electric field in Figures 3.a and 3.b. Interestingly, the mobility is not significantly modified by annealing. These results appear consistent with the previously mentioned X-ray experiments, which showed basically no evolution with temperature of the crystallite size in the transverse direction (i.e. the photo-generated transport direction in this case).

Similar results were obtained by Mandoc et al.\textsuperscript{[52]} On the other hand, Mihaiiletchi et al.\textsuperscript{[21,53]} reported a hole-mobility improvement of 4 orders of magnitude for similar measurements. This discrepancy is presumably due to differences in sample preparation (solvent, additive, solid contents). In our work, absorption spectroscopy (See Figure S3) and
X-rays diffraction measurements reveal that the ratio of the volume of crystallized P3HT to the total volume is approximately equal to 60% before annealing. Although this ratio was not specified in the work of Mihailetchi et al., the extreme low value of their hole mobility before annealing ($\sim 10^{-8} \text{ cm}^2\cdot\text{V}^{-1}\cdot\text{s}^{-1}$, compared to $\sim 10^{-4} \text{ cm}^2\cdot\text{V}^{-1}\cdot\text{s}^{-1}$ in our work) suggests a much lower concentration of crystallized P3HT fraction before annealing. Moreover, mobility in that work was not measured by TOF, but extracted from an I-V curve fitting using a space charge limited current (SCLC) model, which renders a quantitative comparison with mobility values reported in our work questionable.

Finally, experiments show a decreasing mobility with electric field for both electrons and holes, which is rather unexpected for most polymers, but typical of energetic and spatial disorder in P3HT material.[54,55] Experiments can be fitted by the model proposed in[56]: this empirical model is then used to calibrate numerical simulations.

3.3. Impact of morphology on I-V and visible EQE measurements

Photocurrents, External Quantum Efficiency (EQE), as well as dark currents were measured after each annealing step in order to monitor the impact of annealing on diode performances.

First, photocurrent measurements in short circuit condition were performed at two different wavelengths, 440 nm and 620 nm, corresponding to the absorption peak of PC$_{60}$BM and P3HT, respectively. As each radiation probes a different molecule, the experiment helps quantify the domain evolution of the polymer and fullerene separately. As previously mentioned, the annealing temperature is kept at 85°C in order to prevent the vertical phase segregation of PC$_{60}$BM, known to appear when the temperature exceeds a certain value.[13] The appearance of this segregation can be detected by monitoring the external quantum efficiency measuring the relative amplitude of PC$_{60}$BM and P3HT peaks.
The external quantum efficiency as a function of the annealing time is reported on Figure 4.a. Both curve at 440nm (fullerene absorption) and 620nm (polymer absorption) exhibits a similar “bell shape” curve. A closer look to Fig. 4a reveals that the two curves follow a similar trend in the first part of the curve (low domain regime), but differs after the maximum. Similar wavelength dependency of the EQE versus annealing has been previously reported in the literature [84]. It can suggest that the annealing induces a similar change in both polymer and fullerene domains, at least for short annealing time.

An alternative explanation, consistent with the conclusions of the next section, is that the mechanisms impacting the EQE are not the same in the first and the second part of the curve, and thus are not impacted in the same way by the size of fullerene and polymer domains.

During the first 580 minutes, the EQE at 440nm (620nm) is improved from 15% (8%) up to 37% (47%). After this optimal annealing time, the EQE drops off when additional annealing steps are performed. This drop is usually attributed to the degradation of the exciton dissociation rate, when the domain size exceeds the exciton diffusion length.[57]

The first regime is less well understood, in part because it is somehow difficult to obtain such small values of domain size, especially without introducing additives such as DIO to get an improved interpenetrating network. Some authors attribute this first regime to an excess of Langevin recombination, occurring in blends with large interfacial volume ratio.[11] Others authors attribute this effect to the increase of percolation path connecting both electrodes, making more favorable the carriers collection.[33] As mentioned previously, the photocurrent improvement is sometime also attributed to an enhancement of transport properties induced by polymer crystallization.[30] However, this later assumption appears in contradiction with the TOF mobility measurements reported above. In addition, the absorption spectra indicate an excellent thermal stability, suggesting that the crystallization of the blend occurs mostly during the deposition step and not during the post-thermal treatment (see
**Figure S3.** The use of additive such as DIO is most likely the cause of such stability. Our interpretation will be discussed in the next section.

Photocurrent was measured as function of incident light flux in order to determine the main recombination mechanism operating in the solar cell. Indeed, the dominant mechanism, Langevin-type recombination versus trap assisted recombination, can be distinguished by monitoring the slope of the photocurrent function of the incident light power. Langevin-type recombination is known to be a second order mechanism, leading to nonlinear curves at high light power, whereas trap assisted recombination is a first order mechanism, and thus does not affect the linearity of photocurrent versus light flux curves.[43]

Results plotted in **Figure 4.b** do not show any non-linearity, suggesting that Langevin recombination is not the dominant mechanism in these samples, at least for the range of light flux investigated in this experiment. This point will be further investigated by simulation in the final section. Moreover, both the dependence of the photocurrent with annealing duration, and the poor value of quantum efficiency reported without initial annealing suggests that recombination mechanisms are indeed present, mostly trap assisted recombination. This point will be further confirmed by others experiments in the following section.

Normalized photocurrents versus applied voltage are plotted in **Figure 4.c**, for each annealing step. The photocurrent normalization consists in dividing by the illuminated current density value at -5V, according to:

\[
I_{\text{norm}} = \frac{I_{\text{light}}(V_a) - I_{\text{dark}}(V_a)}{I_{\text{light}}(-5V) - I_{\text{dark}}(-5V)}
\]  

(2)

This procedure is performed in an attempt to simplify the visual comparison of each curve. As in the EQE experiments, the voltage dependence of the current density improves (*i.e.* reduced) with annealing time before reaching an optimal annealing point (580 minutes annealing). Note that the built-in voltage seems almost unchanged during the successive steps, suggesting that contact work functions are not affected by annealing.
Finally, the dark current is recorded for each annealing step (Figure 4.d). The dark current density decreases continuously with annealing, scaling by more than 2 decades. Such a trend has been reported in only few other works, presumably because the dark current is typically not a figure of merit of solar cell devices.\cite{58} Moreover, optimized organic solar cell have typically very thin active layers (~100nm), and consequently may suffer from additional leakage current induced by pinholes. In some publications, the dependence of the dark current on annealing has been attributed to the reduction of the shunt resistance, possibly burned out by annealing\cite{29} or to a better contact selectivity, induced by changes in the vertical phase composition profile.\cite{59}

To summarize, current-voltage characteristics under dark and illumination show two main trends: the improvement of the photocurrent dependence on the electric field, and the drop in the reverse dark current.

3.4. Infra-red EQE measurements

Following the work of Street et al., IR spectral response experiments were also performed in order to probe the density of states in the energy gap.\cite{40,42} Regions of the absorption curves corresponding to bulk absorption (transition from the HOMO to the LUMO bands of the same semiconductor), charge transfer band-to-band across the donor/acceptor interface, exponential absorption tail, and deep state charge transfer are indicated in Figure 5, while the specifics of these transitions are represented in Figure 6. The optical band gap of P3HT is 1.8eV whereas the optical band gap of the PC_{60}BM is 2.4eV.

The most interesting part of the spectral response, below 1.6 eV in the regime of charge transfer through gap states, exhibits a marked exponential dependence on photon energy, consistent with an exponential density of states in the band tails. Furthermore, this part of the spectral response is in large part reduced by annealing. The contribution from these gap state-mediated transitions drops with the annealing time. To quantify this effect, a band
tail characteristic energy $E_0$ is extracted using an exponential fit of the IR spectral response experiment (discussed below, see Equation 5). The fitting procedure consists in fitting every spectral response versus photon energy curves in the 1.1 eV - 1.5 eV range. As shown in Figure 7, this characteristic energy $E_0$ decreases with annealing time, which indicates a drastic reduction of the density of trap states within the band gap of the blend layer.

### 3.5. Validation of the band tail characteristics energy extraction

As mentioned above, the characteristic energy extracted from EQE has been plotted on Figure 7. EQE is only an indirect bulk measurement, which does not directly monitor the density of states into the gap. Indeed, according to\[^{[60]}\], the absorption coefficient (which is one of the EQE component) for photon energy below the gap is related to the HOMO and LUMO band tails density of states according the following formula (Equation 3):

$$
\alpha(h\nu) = C \frac{V_F}{h\nu} \int_{E_{\text{HOMO}}}^{E_{\text{LUMO}}} N_{\text{HOMO}}(E) N_{\text{LUMO}}(E + h\nu) \, dE
$$

(3)

where $V_F$ is the heterojunction interface volume fraction and $C$ a constant. The absorption coefficient can be divided into a sum of three different contributions: band-to-band transition; band-to-tail or tail-to-band transitions and tail-to-tail transition. Taking into account the characteristic energy $E_0$ of the respective HOMO and LUMO band tails, the density of states into the gap are given by Equation 4 and Equation 5:

$$
N_{\text{HOMO, tail}}(E) = N_{\text{H, tail}} \exp\left(-\frac{E - E_{\text{HOMO}}}{E_{0,\text{H}}}ight) \quad E_{\text{HOMO}} < E < E_{\text{LUMO}}
$$

(4)

$$
N_{\text{LUMO, tail}}(E) = N_{\text{L, tail}} \exp\left(-\frac{E - E_{\text{LUMO}}}{E_{0,\text{L}}}ight) \quad E_{\text{HOMO}} < E < E_{\text{LUMO}}
$$

(5)

where $N_{\text{H, tail}}$ and $N_{\text{L, tail}}$ are the density of states at the tail band edge, $E_{0,\text{H/L}}$ band tail characteristics energy of the HOMO and LUMO band tail population, and $E_{\text{HOMO}}$ the HOMO energy, $E_{\text{LUMO}}$ the LUMO energy.
Computing Equation 3, for photon energy between $E_g$ and $E_g/2$ (1.6eV and 0.8eV) the band-to-tail absorption is found to be dominant over the tail-to-tail transition. In this case, the absorption coefficient indeed exhibits a $\exp(h\nu/E_0)$ dependence, where $E_0$ is the highest band tail characteristics energy between the HOMO and LUMO band. For photon energy below $E_g/2$, Equation 3 shows that absorption only depends on tail-to-tail transition. In this regime, again, an $\exp(h\nu/E_0)$ dependence is found, with however a different $E_0$ parameter (except if identical band tail characteristics energy are assumed for both the HOMO and LUMO). However, note that this regime of photon energy was not accessible in our experiments.

In conclusion, it is not possible to extract separately from spectral response measurement both the value of the HOMO and LUMO band tail characteristic energy $E_{0,HOMO}$ and $E_{0,LUMO}$. Only the highest band tail characteristic energy is obtained where band-to-tail or tail-to-band transitions are dominant over the other contributions.

4. Discussion

Let us summarize the experimental results reported in the previous section. The dependence of I-V characteristics on annealing time both in illuminated and dark conditions was measured. Results obtained show the existence of a preferred morphology in term of short circuit current, together with constant improvement of the fill factor and decrease of the dark current with annealing. Moreover, the blend morphology was characterized by combining AFM and X-rays diffraction experiments, leading to an accurate description of the P3HT domain evolution versus annealing. Electrons and holes mobilities were measured by TOF experiments, indicating no significant evolution of the transport properties with annealing duration.

The density of states in the gap of the materials was found to significantly depend on annealing duration, as shown spectral response measurements.
In this section, experimental I-V curves obtained both in illuminated and dark conditions are investigated using Drift and Diffusion simulations, carefully calibrated using previously presented characterization results. In particular, the aim of this section is to demonstrate that the dependence of the electrical response (both in dark and illuminated conditions) on annealing is consistent with band tail DOS reorganization.

4.1. Drift diffusion simulations and calibration

The transport of electrons and holes into the blend is modelled using the extensively used effective semiconductor approach proposed by Kostler et al.\cite{61}. Simulations parameters can be found in previous publications\cite{62–65}, and are reported in Table 1. Electron and hole mobilities are modelled by field-dependent analytical expressions, obtained by fitting TOF experiments. Both mobilities are taken independent of the annealing duration, in agreement with experiments.

The polymer semiconductor is assumed to be intrinsic. In agreement with experiments, the exponential band tail density of states is included, following the model proposed by Urbach et al.\cite{66} and used in amorphous silicon photodiodes.\cite{67}

For the sake of simplicity, the characteristics energy and band tails amplitude of both HOMO and LUMO bands are assumed equal in the simulation. No additional deep traps are implemented in the code. Trap assisted recombination and occupation probability of the tail states are described by the Shockley-Read-Hall formalism (see Figure S4 for details).

Moreover, the HOMO-band-tail-states are assumed to be donor-like while the LUMO-band-tail states are proposed to be acceptor-like:\cite{68}; the charge induced by the possible ionisation of these states is accounted into the self-consistent solution of the Poisson equation. Note that trap-assisted recombinations are computed in this work without using any analytical approximations, such as the popular Taylor and Simmons approximation.\cite{69}
The blend morphology is taken into account in the simulation by adjusting both the electron and holes generation and recombination terms. Following\textsuperscript{[70]}, the generation term is modified to account for the poor exciton dissociation occurring in blend with too large P3HT and PC\textsubscript{60}BM domains. Similarly, as electron and holes are supposed to recombine mostly at the heterojunction interface, the recombination term is assumed proportional to the interface volume fraction \( V_F \). Both terms depend on the P3HT average domain size \( <W> \), which is deduced from the AFM experiments.

Langevin recombination is also included in these simulations, using the well-known \( \gamma(np-n_i^2) \) formula. Contrary to several previous works\textsuperscript{[71,72]}, the Langevin prefactor \( \gamma \) is given by its theoretical expression \( \gamma = e(\mu_n+\mu_p)/\varepsilon \), which constitutes an upper estimation of the Langevin recombination.

The resulting electron (hole) continuity equation is given by:

\[
\nabla \cdot \Phi_n = \frac{2L_{\text{ex}}}{\langle W \rangle} \tanh \left[ \frac{\langle W \rangle}{2L_{\text{ex}}} \right] G - V_F R_{\text{SRH}} - V_F \gamma \left( np - n_i^2 \right)
\]

where \( \Phi_n \) is the flux of electrons (holes), \( L_{\text{ex}} \) the exciton diffusion length, \( G \) the optical generation rate and \( R_{\text{SRH}} \) the recombination rate defined from the SRH formalism.

4.2. Comparison between experimental photocurrent and simulations

Experimental photocurrents versus applied voltage curves are compared with simulation for various annealing times. As seen in Figure 8, using the calibration explained for Figure 4.c, all the data are nicely reproduced by the simulation. Note that only one single fitting parameter is used here: the trap concentration at the band edge \( N_0 \). This parameter is fixed at the same value for the all the curves.

If the band tail characteristics energy \( E_0 \) is arbitrary kept constant in the simulation, the photocurrent field-dependence remains almost unchanged, despite the interface volume fraction \( V_F \), underlying the critical impact of the band tail density of states on photocurrent.

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Similarly, the spectral response under short circuit condition is simulated versus annealing, and plotted together with experimental data on Figure 4.a. The simulation parameters are the same as in Figure 8. Simulations qualitatively reproduce the “bell shape” observed in the experiments, and confirm the interpretation of the two part of the curve: exciton dissociation limited at large domain size, and trap assisted recombination at small domain size.

Note that simulations have been performed for a different light power condition than experiments. Indeed, the power used in simulation is 250 W/m², instead of ~0.3 W/m² in experiments. This difference however do not impact the comparison, since the short circuit current is indeed linearly dependent on the light power (as confirmed in experiments, see Figure 4.b).

4.3. Non geminate Langevin versus SRH mechanism

As previously mentioned, recombinations in organic solar cells are usually attributed to either Langevin or Shockley-Read Hall (SRH) mechanisms. The SRH recombination rate is usually proportional to carrier density n, while the Langevin rate is proportional to the square of the carrier density n². For this reason, assuming standard value for the Langevin prefactor γ, this later mechanism typically dominates only at high light flux (> 1sun) in P3HT/PC₆₀BM blend [72] or in forward bias beyond the built-in potential (OLED device).[73,74] In the literature, this point has been the source of debate.[40,75,76]

In practice, the dominant mechanism can be discriminated by measuring the linearity of the photodiode current as function of light flux. Trap-assisted recombination keeps a linear relation between the short circuit current density and the light intensity, whereas Langevin type recombination induces nonlinear effects at high light flux (recombination term proportional to the square of the carrier density).
Numerical simulations were performed to estimate the dominant mechanism in our system (Figure 9). It turns out that for the level of traps considered in this work and extracted from experiments, SRH is always the dominant mechanisms, at least for light power lower than 250 W/m² (the maximum light power value used in this work). However, in the optimum morphology condition, Langevin can be as high as 60 % of SRH, suggesting that this former mechanism cannot be ignored. It is likely that, in well optimized blends based on polymers more advanced than P3HT, e.g. low band gap polymers, Langevin might be the most effective recombination mechanism.

4.4. Reverse dark currents

Dark currents were also investigated (see Figure 10.a). In this regime, as there is no light-induced charge generation, only the recombination term is effective. In forward bias, trap states located deeply in the gap help in the recombination of electrons and holes injected into the device (as the carrier concentration in the semiconductor exceeds the intrinsic carrier concentration). In reverse bias however, deep states help in the electron-holes pair generation process. The SRH recombination rate in this latter case is directly proportional to $N_t n_i^2$ (with $N_t$ the trap states concentration), which explains the high dark current level observed at large deep states concentration, i.e. at low annealing time. During the annealing treatment, the reorganization of the band tail DOS induces a lowering of the density of trap states, explaining the drop of the reverse dark current.

In the reverse bias regime, if the model reproduces quite well the amplitude of the dark current versus annealing, the field dependence is not well captured. This difference originates from the transport model in the drift-diffusion approach, which does not account for hopping transport through deep states. This limitation can be partially removed following the approach of Hurkx et al.[68], which accounts for trap assisted tunnelling from the trap state to the HOMO or LUMO bands as illustrated in Figure S4. When this new approach is implemented, the
agreement between experiments and simulations in the negative bias regime appears significantly improved (see Figure 10.b). Note that the dark injection from contacts into the trap states is not taken into account in this model. The good agreement between simulations and experiments lead to the conclusion that this effect can be neglected.

4.5. Charge transfer state recombination versus SRH mechanism

Charge transfer state (CT) recombination has recently been extensively investigated in the literature [85-87] and should be discussed as a possible alternative explanation of the impact of thermal annealing on the performance of organic solar cells. This third mechanism implies geminate recombination [88] and depends mostly on the organization of the fullerene phase with respect to polymer domains. The group of Richard Friend [87] has demonstrated recently that the presence of pure domains of fullerene, at least 5 nm in size, suppress entirely this CT recombination. In this work, the introduction of annealing temperature leads to an improvement of the device performances, which could be attributed to a change in the fullerene domains organization and thus to a possible diminution of the CT state recombination.

This effect is certainly present in our results, especially at low electric field, where charge transfer state recombinations are more efficient. Note that it is partially included in our simulation, where the Onsager Braun model is implemented. This approach is however not completely satisfactory, as it does not include any morphological dependence of the recombination probability [86].

We believe however that the morphology dependency of CT recombination can not explain all our experimental results, and that our hypothesis (SRH recombination) is also needed, as discussed in this paper. Let us summarize the arguments in favor of SRH versus CT recombinations.
First of all, EQE experiments at low energy clearly indicate the presence of shallow and deep traps into the gap, and allow quantifying the impact of thermal annealing on their concentration. This effect is unlikely to be explained by pure CT recombination. Moreover, our model, accounting only for the morphology dependency of generation, non geminate langevin and SRH recombination, can nicely reproduced I-V curves under illumination at all temperature annealing. There are no fitting parameters in these simulations: mobility, domain size and traps concentrations have all been extracted from complementary experiments (Time of Flight for mobility, AFM and X-ray diffraction measurement for the domain size and EQE at low energy for the traps concentration). Last but not least, the same model also explains, again without additional fitting parameters, the impact of annealing on the dark currents, where obviously CT recombinations are absent (no light). These conclusions, in the case of P3HT/PCBM blends, are consistent with other works\textsuperscript{[88],[89]}. All these facts support the analysis presented here, if even more investigation is needed to quantify more accurately the impact of CT recombinations.

The origin of the traps observed here through infra red EQE measurements is not known. Different hypothesis are evoked in the literature. The band tail states may originate from the polymer chain disorder inside the active layer\textsuperscript{[42],[90]}, confirmed by UPS measurement\textsuperscript{[91]} and by quantum chemistry simulations\textsuperscript{[92]}. Defects can also induce traps, however not usually “band tails”. Localized traps may originate from polymer chain scission\textsuperscript{[93]} or impurities such as oxygen\textsuperscript{[94]} or metallic residues\textsuperscript{[95]}.

5. Conclusions

In this work, trap assisted recombinations have been investigated, focusing in particular on the impact of thermal annealing durations in the classical P3HT:PC\textsubscript{60}BM solar
cells. Interestingly, while the spectral response versus annealing time exhibits a bell curve with an optimum value, the dark currents however are monotonously reduced by annealing. The second part of the spectral response (i.e. decrease of the efficiency) is interpreted in term of blend morphology change. Indeed AFM and X-rays diffraction measurements have revealed that the growth of P3HT domains occurs in the 2D longitudinal directions. When the average polymer domain width exceeds the exciton diffusion length, the solar cell efficiency gets lower because of the exciton dissociation rate limitation.

On the other hand, this work demonstrates that the initial improvement of the spectral response is not correlated to any carrier mobility improvement as confirmed by Time-of-Flight experiments, where mobilities for both hole and electron have been extracted and found unchanged during the annealing steps.

The impact of thermal annealing durations on the trap assisted recombination rate has been investigated to explain both dark and light current changes. First, the existence of exponential band tails into the gap has been experimentally confirmed by measuring the device spectral response in the IR regime. Such method revealed the existence of large density of states into the gap, largely reduced by the successive annealing steps.

All these results (mobility, bandtails) have then been used to calibrate Drift and Diffusion simulations. It turns out that electrical and optical simulations can satisfactory reproduce illuminated and dark experimental currents at the same time, versus voltage and annealing time. These simulations highlight the predominance of the band tail states reorganization in the improvement of the solar cell characteristics. Recombinations assisted by trap states are lowered by annealing, which lead to an improvement of the solar cell efficiency and a decrease of the reverse dark current (thermal generation from trap states). This approach constitutes a powerful physical model, able to explain the existence of an ideal morphology for photogenerated currents, and at the same time, able to capture the constant reduction of dark current induced by annealing. An optimum in term of quantum efficiency is
found between the band tail states reorganization and the coarsening of the blend morphology as function of thermal annealing duration.

6. Experimental Section

**Opto-electrical characterization:** Encapsulated devices were characterized in ambient air. Opto-electrical measurements are performed on a dedicated optical bench. The devices are placed in a light shielding box and can be illuminated by a specific optical head controlling the size of the spot light on the device and insuring in-line measurement of the light power. All light sources are placed outside of the shielding box and connected to the optical head by a liquid light-guide.

Current-voltage (I-V) characteristics were measured with a Keithley 2636A in darkness and under illumination (irradiance of 200 W/m²) obtained from a quartz tungsten halogen lamp (LOT-Oriel 250W QTH light source).

For photodiode linearity measurement, the irradiance is reduced by insertion of different optical densities. Photocurrents were recorded as function of incident light power.

For spectral response measurement, a 1/4m grating spectrometer (LOT-Oriel Cornerstone 130) with a resolution of 20 nm was used. The EQE measurements were performed at zero-bias voltage to get the lowest dark current. The incident light power was measured with a calibrated photodiodes: silicon sensor for wavelengths below 900 nm and an InGaAs sensor up to 1.7µm.

**AFM characterization:** AFM phase measurements of the blend surface were performed in air on specific separated samples using a Veeco Multimode AFM in tapping mode. AFM tips (super sharp silicon tip purchased from NanoSensors) with 2 nm radius and resonance 300 kHz frequency were used in order to identify the different phases on fine blend morphology. This insured clear distinction between crystalized and amorphous region on the blend surface.
The detector side of the AFM had an aluminum coating in order to improve the signal detection.

Supporting Information
Supporting Information is available from the Wiley Online Library or from the author.

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The authors are grateful to Simon Charlot for photodiodes preparation and discussions regarding solar cell fabrication. The work done at CEA was supported by ISORG. Work in Princeton was supported in part by the National Science Foundation (DMR-1005892).

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Figure 1. Average domain width extracted from AFM images versus annealing time. Symbols refer to experiments; line to a fitting obtained using the theoretical law proposed in the work of [47].

\[ \langle W \rangle = \langle W_0 \rangle + (Dt)^n \]

\( \langle W_0 \rangle = 9.96 \text{ nm} \)

\( D = 6.41 \times 10^{-4} \text{ nm/s} \)

\( n = 1 \)
Figure 2. a). Schematic representation of the orientation of ordered P3HT domains with side chains perpendicular to the substrate; b). Coherence length extracted from X-rays diffraction spectra at the identified (001) peak using the Scherrer formula.
Figure 3. Electron (a) and Hole (b) mobility extracted from time-of-flight measurements, for different annealing times, plotted against the square-root of the electric field. The hole
mobility is extracted by illuminating the device from the aluminum cathode electrode, whereas for the electron mobility, the device is illuminated from the glass substrate side.

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**Diagram a)**

- **External Quantum Efficiency**
  - Graph showing data for wavelengths $\lambda = 440$ nm and $\lambda = 620$ nm, along with numerical simulation data.
  - $x$-axis: Annealing time (s)
  - $y$-axis: External Quantum Efficiency

**Diagram b)**

- **Photocurrent density (A/cm²)**
  - Graph showing data with and without annealing, and linear fit with $\alpha = 1$.
  - $x$-axis: White light power (lm)
  - $y$-axis: Photocurrent density (A/cm²)

**Legend**
- **w/o annealing**
- **5.10^5 s at 85°C**
- **linear fit $\alpha = 1$**
Figure 4. a). Photodiode External Quantum efficiency measured in short circuit condition versus the 85°C annealing duration. The device quantum efficiency is measured at two different wavelengths, corresponding to the maximum absorption of the polymer and the
fullerene respectively (620 nm and 440nm). b) Measured photocurrent density in short circuit condition versus white light power (halogen quartz lamp) for two different annealing durations. Different optical densities are used to modulate the light power. A linear function (line) has been also plotted to visually confirm the linearity of the curves over more than 5 decades. c) Experimental normalized photocurrent versus applied voltage for different annealing durations. The photocurrent normalization consists in dividing by the illuminated current density value at -5V. The illumination is performed by white light from halogen quartz lamp. d) Measured dark current-voltage characteristics, after different 85°C annealing duration. Contrary to the photocurrent, the dark reverse current keeps on decreasing with successive annealing steps.

**Figure 5.** Spectral response measured at short circuit condition as function of the photon energy. Spectral wavelength ranges from 380nm up to 1400nm. Different regimes are identified in the figure: bulk absorption for photon energy higher than 1.9eV, band to band charge transfer for photon energy between 1.9eV and 1.6eV and transition between energy levels located inside the gap and HOMO or LUMO bands below 1.6eV (see Figure 6 for details).
Figure 6. Schematic drawing of the different transitions occurring in a BHJ solar cell.
Figure 7. Band tail characteristic energy $E_0$ extracted from spectral response experiments in the IR regime versus annealing duration using an exponential fitting law.
Figure 8. Comparison between experimental and simulated photocurrent I-V curves for the different annealing steps. The evolution of the interface volume fraction $V_f$ (extracted from AFM images) is taken into account in the simulation, as well as the evolution of the band tail characteristic energy $E_0$ (extracted from EQE experiments).
Figure 9. Calculation of the ratio between the SRH recombination and the Langevin recombination terms at short circuit condition as function of the annealing time. For high band tail states, Langevin recombination can be neglected whereas for optimized efficiency, the Langevin term is of the same order of magnitude than the SRH term.
Figure 10. Dark current density versus applied voltage, for several annealing duration using simple trap assisted recombination model a) or using trap assisted recombination model accounting for tunneling b). Parameters are the same of figure 15.

Table 1. Simulation parameters used in this work.

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<td>Effective mass (m^*)</td>
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Supporting Information

**Title:** Impact of blend morphology on interface state recombinations in bulk heterojunction organic solar cells

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((Optional Dedication))

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**Figure S1.** Atomic Force Microscope (AFM) phase measurement in tapping mode performed on the P3HT:PC$_{60}$BM blend surface, obtained with different annealing duration (2min, 60min, 100min and 580min). The blend layer was spin coated on the ITO coated glass substrate.
Figure S2. XRD spectra for the different annealing step. (100), (200) and (300) are identified on every spectrum. The coherence length on the (100) peak is extracted using the Scherrer formula.
Figure S3. Absorption spectra of P3HT:PC$_{60}$BM blend layer with 95% of CB and 5% of DIO. The crystallization order of the film is unchanged along with the annealing.

Langevin recombination is described by the following formalism:

$$R_L = \frac{q}{\varepsilon_r \varepsilon_0} \frac{(\mu_e + \mu_h)}{2} (np - n_i^2) \quad (1)$$

With $n_i$ the intrinsic carrier concentration, $\mu_{eh}$ the carrier mobility, $q$ the elementary charge, $\varepsilon_r$ the dielectric constant of the polymer and $\varepsilon_0$ the dielectric constant in the vacuum.

The recombination rate in the Shockley Read Hall formalism is given by the following relation:

$$R_{SRH} = N_t \frac{np - n_i p_i}{\frac{1}{C_n} (n + n_i) + \frac{1}{C_p} (p + p_i)} \quad (2)$$

With $N_t$ the trap density of states, $C_p$ and $C_n$ the capture cross section of the trap states taken as equal (Taylor and Simmons approximation). The electron $n_i$ and hole $p_i$ trapped density are defined by:

$$n_i = N_c \exp \left( \frac{E_l - E_i}{k_BT} \right) \quad (3)$$
\[ p_i = N_v \exp \left( - \frac{E_i - E_{HOMO}}{k_B T} \right) \]  \hspace{1cm} (4)

With \( E_i \) the energy trap depth with respect to the band edge.

The probability of occupation of the trap level at the energy \( E_i \) is given by:

\[ f(E) = \frac{n + p_i}{n + n_i + p + p_i} \]  \hspace{1cm} (5)

Exponential band tail states distribution are implemented for both the HOMO and the LUMO in agreement with the experiments:

\[ N_{HOMO,\text{tail}}(E) = N_{H,\text{tail}} \exp \left( - \frac{E - E_{HOMO}}{E_{0,H}} \right) \] \[ E_{HOMO} < E < E_{LUMO} \]  \hspace{1cm} (6)

\[ N_{LUMO,\text{tail}}(E) = N_{L,\text{tail}} \exp \left( - \frac{E - E_{LUMO}}{E_{0,L}} \right) \] \[ E_{HOMO} < E < E_{LUMO} \]  \hspace{1cm} (7)

where \( N_{H,\text{tail}} \) and \( N_{L,\text{tail}} \) are the density of states at the tail band edge, \( E_{0,H/L} \) band tail characteristics energy of the HOMO and LUMO band tail population, and \( E_{HOMO} \) the HOMO energy, \( E_{LUMO} \) the LUMO energy.

To correctly simulate the reverse dark current, the trap assisted tunnelling mechanism is implemented. This additional mechanism induces a field dependence thermal generation. In the formalism of Hurkx et al, a field-effect function \( \Gamma_n, \Gamma_p \) is introduced:

\[ \Gamma_{n,p} = \frac{\Delta E_{n,p}}{k_B T} \int_0^1 \exp \left( - \frac{\Delta E_{n,p} u - K_{n,p} u^{3/2}}{k_B T} \right) du \]  \hspace{1cm} (8)

And, \[ K_{n,p} = 4 \frac{\sqrt{2m^* \Delta E_{n,p}}}{q \hbar |E|} \]  \hspace{1cm} (9)

With, \( \Delta E_{n,p} \) the energy difference between the trap level and the band edge, \( E \) the local electric field and \( m^* \) the effective mass.
The capture cross section in the SRH recombination formalism is modified as follow in order to account for tunneling emission via trap state.

\[ C_{n,p} = \frac{V_m \Gamma}{1 + \Gamma_{n,p}} \]  

(10)

The following schematic illustrates the mechanism introduced to correctly reproduce the reverse dark current field dependency.

Figure S4. Description of the electrical model implemented in the numerical code in order to simulate the electrical losses (recombination assisted by traps and Langevin).
Figure S5. Band tail density of states in the blend band gap with the occupation probability of the energy state. The gap states are described by an exponential density. $E_{f,p,n}$ represents the quasi Fermi level energy.