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To cite this version:
Antonio Giovannini, Alexis Aubry, Hervé Panetto, Hind El Haouzi, Ludovic Pierrel, et al.. Approach for the rationalisation of product lines variety. 19th IFAC World Congress, Aug 2014, Cape Town, South Africa. 19 (1), pp.3280-3291, <10.3182/20140824-6-ZA-1003.02226>. <hal-01081763>
Approach for the rationalisation of product lines variety

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Abstract: The product variety management is a key process to deal with the flexibility requested by the mass customisation. In this paper we show that current variety-modelling methods miss a customer representation: without a proper assessment of the customer, it is not possible to define the product variety that has to be developed to meet the requirements of a customer segment. Here we present an innovative approach to rationalise the product variety, i.e. to link each product variant to the customer profile who needs it. The aim is to optimise the product variety avoiding excesses (variants not related to a customer), lacks (customers not related to a variant) or redundancies (two or more variants proposed to a customer). An overview of customer modelling approaches in the classic product design (non-customisable) is presented. The innovative approach is here developed using system-thinking concepts. A knowledge-based system that uses this approach is designed. Finally the approach is explained using a real industrial case of a quasi-real coil design process.

Keywords: Mass customisation, Product variety, Knowledge representation, Knowledge-based system

1. INTRODUCTION: ABOUT MASS CUSTOMISATION AND PRODUCT VARIETY

For a shirt manufacturer, “what if technology made it possible for every one of the five thousand shirts to be customized while on the assembly line […] produced just as quickly as the five thousand identical shirts, yet at not greater expense?” Starting from these words Davis in (Davis, 1987) introduced for the first time the term mass customisation (MC).

Other definitions can be found in (Tseng et al., 2001) and (Blecker et al., 2004). In these papers, MC is defined as a business approach that aims to fulfil individual customer’s needs having an organizational efficiency of a mass production (MP) company. The MC is explained by comparison also in (Pine II et al., 1993). Authors discuss the change of paradigm needed to move toward MC: if MP or continuous improvement strategies call for low costs and standard goods and services, MC stress on flexibility and quick responsiveness in order to cope with the products customisation.

Another recently introduced concept is the Mass Craftsmanship (MCMS) that is a hybrid form of pure MC and mass personalization, since it is possible to address both wide market and unique requirements. An interesting application in the furniture sector is discussed in (Dassisti et al., 2012), which is mainly similar to that addressed in this paper.

From these definitions, it is clear now the big deal in MC is to timely react to the complexity deriving from the variety of the customer domain. This variety impacts directly the number of products to be manufactured and consequently, the complexity of the manufacturing system and of the planning and scheduling processes (Blecker et al., 2004).

Most of the related works cope with these effects of the product variety. Complementarily, in this paper, the aim is to reason about the origin of this variety, in order to define the right level of customisation to propose, i.e. the number of product variants. For a better understanding, the example of a shoes seller who offered $3 \times 10^{21}$ variants of its shoes is described in (Piller 2003). All together, these shoes can cover 7,000 times the surface of the earth.

In the next section, we formalise the modelling requirements to rationalise the product variety. In the section 3 current variety modelling methods are presented: here, defining a gap between these systems and the customer domain. To understand how to bridge this gap, in the section 4, we focus on the methods typically employed for designing non-customisable products: here the aim is to discuss which method is the more appropriate for expressing formally the variety in the customer domain. Starting from methods discussed in the section 4. A conceptual model that applies a System thinking view on the product variety definition is presented in the section 5. Using this conceptual model as knowledge model, a knowledge-based system is designed in section 6. Finally, section 7 is dedicated to present an application of an industrial case. In the last section, results and future perspectives are discussed.

2. MODELING REQUIREMENTS FOR VARIETY RATIONALISATION

In order to identify the modelling requirements to rationalise the product variety, let us first define two generic sets $X$ and
The set $X$ represents a targeted customer segment. An element of $X$ is a vector of features in the customer domain expressing one customer. The set $Y$ represents the set of product variants defined for the customer segment: an element of $Y$ is a vector of features in the engineering domain expressing one product variant (see Fig. 1a). The function $g$ is the product variety definition function and it has $Y$ as domain and $X$ as codomain. One product variant can correspond to more than one customer. This means that two different element of $Y$ can be related by $g$ to the same element of $X$. In other words, the product variety definition function $g$ can be multivalued (see Fig. 1b).

In order to avoid unnecessary development costs, an engineer should design no more than one variant for each customer in the customers segment: these variants have the same added value for the customer, but can represent different resources consumption for the customizer. This requirement can be formalised by the following property of the configuration function $f$:

$$\forall x_1, x_2 \in X, f(x_1) \neq f(x_2) \Rightarrow x_1 \neq x_2$$

(1)

There exists more than one subset of $Y$ in which $f$ respects this property: the choice of the best one should be done according criteria from economics, sustainability and so on.

A subset of $Y$, in which the configuration function respects the defined property (1), is called $Y_1$. If a function $f$ respects the property (1), a customer cannot be related to more than one product variant. In other words, the function $f$ defined from $X_1$ to $Y_1$ is a single-valued function (see Fig. 1d).

If $f$ is the inverse function of $g$ and respects (1) then we can infer that $f$ covers completely $Y_1$: a product variant that is not related with any customer cannot exist. This means that an engineer is not involved in the development of a product variant that will not be sold to any customers.

Starting from these definitions, the set $Y_1$ represents the right product variety for the customer variety $X_1$. From the whole customers segment $X$, the function $g$ allows to identify the set $X_1$ representing the customers that is possible to satisfy. A configuration system that expresses the right level of product variety is a system that uses the configuration function $f$ as in (1) to allow each customer described in $X_1$ to configure only one product variant in $Y_1$.

In the next section, an overview of works on variety modelling, especially for product configuration, is presented. The aim is to verify if the state of the art includes solutions able to model the set $X_1$, $f$ and consequently the set $Y_1$ (i.e. formalisation of the right product variety).

3. CURRENT VARIETY MODELING METHODS

The models that formalise the variety (i.e. set $Y$) in MC are usually named product family (Hong et al., 2008), configurable product model (Aldanondo et al., 2008) or product line (Pohl et al., 2005; Mazo et al., 2012). In this paper we refer to them as product lines (PLs). A PL is the model that expresses the product variety, i.e. set $Y$, that a company offers to a given customer segment in order to fulfil the needs of customers in the segment.

A PL is the base model for every configuration system, used by the customer to select one product variant starting from its needs. In all configuration systems, the customer describes his needs giving some values and preferences to attributes related to the PL variety. An attribute is defined as “an inherent property or characteristic of an entity that can be distinguished quantitatively or qualitatively by human or automated means” (ISO/IEC/IEEE, 2007). Starting from the attributes values, the configuration system is able to define the product variants into the PL variety that are related to the customer needs. For instance, the range of values for the attribute screen size can represent the product variety of a laptop PL.

In the following figure from (Jiao et al., 2007), a complete view of the PLs design and development is shown. The authors define there four main processes for translating the customer needs into design, manufacturing and logistic requirements:

- **Product definition** – how to offer the right variety to the right target market?
- **Product design** – definition of parameters or functional modules (PL attributes) for deriving from the PL the product that fulfils the customer needs
- **Process design** – the management of process variety with process platforms and process configuration methods
- **Supply chain design** – the management of variety on sourcing, manufacturing and distribution strategies.

Here, customer needs represents the customer’s description of the ideal product (e.g. cute, easy to use). Functional requirements concern the features owned by the product, seen as a whole (e.g. colour, size). Design parameters are features characterising product modules, subassemblies and components. Process and logistic variables deal with production and supply chain (not the focus of this paper).
In this section, an overview on PLs modelling solutions and related configuration systems is presented. In Tab. 1, related works are classified according to the above-defined terms related to customer needs, functional requirements and design parameters. The analysed research works are classified according to the semantics of the attributes that expresses the PL variety regarding the customer in current configuration systems. Essentially, we consider here research works that model concepts related to the customer, e.g. customer needs, customer profiles. The analysis of the solutions developed so far allows us to identify a gap between the semantics of these concepts in the cited scientific works and the customer domain representing the set $X$, as formalised in the previous section. This gap prevents the presented configurations system to identify a function $f$ and therefore the set $Y_1$ representing the right product variety.

**Product configuration from design parameters**

In order to configure a product starting from design parameters, the customer is asked to know how components interacts and what the final product features are. Here the required knowledge is technical. For instance, in configuration processes of laptops, the variants description is typically based on memory size (RAM), processor speed, and so on. In each case, the customer has to have a good knowledge about a computer architecture even if its needs concern the ability of the laptop to go on internet, to write some documents, to watch videos, to play videogames and so on.

In this kind of systems, a clear definition of the customer needs as required for the definition of $X$ is not expressed. This lack in the definition of $X$ hinders formalising the configuration function for linking the customers segment with the right level of product variety, i.e. $Y_1$. The effect on the product variety is that, two customers having the same needs, and this representing only one element of the set $X$, can configure two different product variants, as a consequence of their knowledge about the computer architecture. This violates the property (1) causing a lack of control on the level of product variety proposed to the customers.

**Product configuration from functional requirements**

In configuration systems based on attributes described as functional requirement, the customer would be asked to configure the product starting from a holistic view of the product. In this case the customer has to know how the product interacts with its environment to fulfil his needs. For instance, in a heating or cooling system, the power of the system is a property and is not the only one directly related to a room temperature value that can represents a real customer need. In order to reach a temperature target we need to know about room usage, isolation and so on.

Also in this situation, two customers with the same needs, represented as only one element of the set $X$ (see section 2), can configure two different product variants, according to their experience about the usage of these kinds of systems.

As for the systems in the previous subsection, configuration systems based on functional requirements cannot express univocally the right product variety.

**Product configuration from customer needs**

In (Helo et al., 2010), the customizer uses market research. In this case, the manufacturer designs the products and after looks for potential customers for defining a variety in the customer domain. Here, the product variety is defined before defining the customers segment. Doing so it is not possible to guarantee that each product variant meets the requirements of at least one customer in the targeted segment. Moreover, even if the customer does not express his needs as design parameters or functional requirements, he answers also questions about the product (e.g. “which part of the truck do you like most?”). Therefore, also in this case a formalisation of the customers segment, as in $X$, is not feasible.

3.1. The effect of the gap: missing a consistent model of the customer segment

As a consequence of the recognised gap between the current configuration systems attributes and the customer domain, as defined by the set $X$, in current configuration systems, the customer is asked for describing something about the product. The effects of this lack of the definition of the set $X$ are shown in the Fig. 3.

Without a formal definition of a set $X$ representing the customer variety, a formalisation of a unique configuration function $f$, as described above, is never performed. In other words, each customer follows a different $f$ based on his knowledge; therefore the selection of the best variants (according $f_1$ in Fig. 3) cannot be performed on the engineering side. The absence of a unique formalised $f$ implies that a customer, element of $X$, can also configure (according $f_2$ in Fig. 3) a product variant that does not represent the best choice for the enterprise (see the definition of $Y_1$). In the worst case (according $f_3$ in Fig. 3), the customer can select something not included in the available product variety. In summary, without a consistent formalisation of $X$, a definition of a set $Y_1$ representing the right product variety is not possible.

**Fig. 3 – Effects of the gap between configuration systems and the definition of $X$**
The gap between the representation of the product variety and the customer domain - that is not covered by current configuration systems leads to build configuration systems that cannot express the right level of product variety. In order to bridge this gap, we need to understand how to define and formalise the customer variety and what is the knowledge needed for the definition and configuration functions and the set $Y$. In the next section an overview on marketing and engineering methods for the non-customisable product definition processes is presented. The aim is to understand how the link between the customer domain and the product is performed for non-customisable product and then apply this solution to the variety modelling.

4. CUSTOMER MODELING FOR NON-CUSTOMISABLE PRODUCTS DESIGN

Typically the product definition process, for the PLs as well as for simple products, is discussed in the marketing domain and during some engineering phases, i.e. the early design stages.

4.1. Marketing domain

Usually, the solutions to cope with the product definition are in the domain of marketing. We can identify two main approaches: a “attribute-based” and a product “alternative-based” product choice.

The first group is mainly based on the conjoint analysis (Green et al., 1978). This technique represents a milestone: this is an attribute-based method that aims to study the customer behaviour; the customer preferences on product attributes are analysed in order to derive a utility function to be maximised during the design stage. An application can be found in (Balakrishnan et al., 1996): here authors use a genetic algorithm to elaborate the conjoint analysis data for design optimisation.

Another application is suggested in (Tseng et al., 1998), where the designed by customers method is presented. Here authors describe how to integrate in an engineering design the conjoint analysis results. In (Krishnan et al., 2001), authors define a consumer valuation that is calculated from the consumer utility per performance unit. In (Hong et al., 2008), authors represent the formalisation as a customer satisfaction optimization model for solving a configuration problem. A genetic algorithm is deployed for finding a solution. Graphs are used for linking product components features with customer needs. To the second group of methods belongs the decision-based design (Hazelrigg, 1998). For example, in (Wassenaar et al., 2001), authors compare the discrete choice analysis (DCA) with the conjoint analysis. In the former, the customer choice is directly related to product alternatives. The hypothesis here is that for choosing which product to buy is what customer does best. Actually, in (Huffman et al., 1998), authors present experimental results on the customers’ satisfaction in front of product variety. They show how too much variety can be frustrating for the customers and an attribute-based selection is to prefer to an alternative-based, because the first one can simplify the product variety vis-a-vis the customer.

In all described marketing methods the analysis of the customer preferences starts with the evaluation of solutions, represented by product attributes or directly by product alternatives. In this way, the customer is asked to talk about the product. Therefore a formalisation of a unique configuration function $f$, as described above, is never performed. In other words, each customer follows a different $f$ based on his knowledge.

The absence of a unique formalised $f$ implies a lack in the characterisation of the customers segment, i.e. the set $X$. In summary, the usage of this type of methods for the PL definition lead to the cases discussed in the section 3;

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without a consistent formalisation of \( X \), a definition of a set \( Y \) representing the right product variety is not possible.

4.2. Engineering domain

In this section, some of the most known engineering design solutions are briefly introduced. Most of those are related to the concepts of product and process quality.

One of the best approaches oriented to close the gap between customer domain and engineering domain is the design for 6S (Ferryanto, 2007). One of the basic tools for this is the Quality Function Deployment (QFD) method (Ferryanto, 2007). The application of QFD for product design provides an effective methodology for the recursive translation of the voice of customer into customer needs, so as to facilitate their technical specification. QFD allows (1) to analyse the requirements demanded by customers in their own words, (2) to translate the relationships between these and product quality properties, (3) to convert customer requirements into technical ones (Akao, 2004).

The lean production (LP) philosophy is based on the experiences of the Toyota Production System (TPS) (Shah et al., 2007). The LP focus is on the waste minimisation. According authors in (Spear et al., 1999), LP is based on four main rules: (1) all work shall be highly specified as to content, sequence, timing, and outcome; (2) every customer-supplier connection must be direct, and there must be an unambiguous yes-or-no way to send requests and receive responses; (3) the pathway for every product and service must be simple and direct; (4) any improvement must be made in accordance with a scientific method, at the lowest possible level in the organization. Also the lean philosophy, like for design for 6S, has a branch that focuses on the product development. In (Morgan et al., 2006), authors define 13 principles of the lean product development. The first one concerns the characterisation of a customer-defined value for distinguishing the value-added features from the waste. According authors in (Likier et al., 2011), the best way to deploy this principle is to go beyond the QFD performing a Requirement Engineering (RE) process.

Based on theoretical principles from the General Systems Theory (Von Bertalanffy, 1956), in last years a new engineering discipline has been developed: System Engineering (SE). The focus of SE is on the design of complex systems that usually require multidisciplinary exchanges of knowledge and expertise. Main system models are (Pyster et al., 2012):

1. The System requirements model that contains the required system features in order to fulfil customer needs; this model is independent from solution alternatives and from technology;
2. The Logical architecture model that describes how the system functions, i.e. its behaviour for the requirements fulfilment; this model is independent from technology
3. The Physical architecture model that describes the set of elements that perform functions; this model is related to technologies.

The process that performs a translation from customer requirements to system requirements is named RE. The main purpose of RE “is to produce a set of system requirements which, as far as possible, is complete, consistent, relevant and reflect what the customer actually wants” (Sommerville et al., 1997).

All methods described in this section perform an analysis of the customer domain. In QFD, the object described by the “voice of the customer” is not specified. This means that the customer can express some requirements about the product features as well as about his own environment (in which the product has to work) or the required effects in this environment. Despite requirements clustering may help to solve this problem, the application of the QFD for PL definition still lacks of precision: a model representing a variety of the voice of the customer is not possible. Therefore the first formalisation of the variety is only possible on the technical side, according to the product description. This leads to a similar position with the discussed for marketing: an abstraction of the customer needs to obtain a characterisation of the set \( X \) is not possible. A missing definition of \( X \) does not allow assessing the proposed product variety. As mentioned in (Likier et al., 2011), RE allows going much further than QFD. Actually, in SE a better definition of customer needs, customer requirements and system requirements are provided. Already in our initial work (Giovannini et al., 2013), we identified the gap according SE, describing the lack of precision in the definition of customer needs for current configuration systems.

In the next section, an application of these definitions on the variety modelling is discussed. The aim is to identify how to formalise the variety in the customer domain (set \( X \)) and in the engineering domain (set \( Y \)) and what is the nature of the knowledge formalised by the functions \( f \) and \( g \).

5. APPLYING THE SE CONCEPTS TO THE VARIETY MODELING

The proposed approach relates the PL concept to the definitions of System Engineering (Pyster et al., 2012) and concepts of system thinking (e.g. Jackson et al., 1995); the aim is to provide a formal definition of the sets and functions described in the section 2.

5.1. Basic terms from SE

The current section presents the SE concepts that relate, by means of their semantics, the person (generalisation of a customer – element of \( X \)) with the system requirements (elements of the product variety). The following definitions served as a basis for building the conceptual diagram in Fig. 5a.

According to SE terminology, the interaction between the person and its environment is moved by a purpose. The purpose represents “what the system is for, and why the different stakeholders are willing to participate in the system lifecycle” (Blockley et al., 2000). The person who participates to this relationships is a stakeholder, where stakeholder is defined as “a party having a right, share or claim in a system or in its possession of characteristics that meets that party's needs and expectations” (ISO/IEC, 2008). The definition of purpose matches the definition of real needs in (Faisandier, 2013): here the author defined as real needs those needs “that lie behind any perceived needs (defined below) and they are conditioned by the context in
which people live”. In the same paper, the author presents a diagram of the needs lifecycle (Fig 4) that shows the transformations from real needs to a set of consistent requirements. In this figure, real needs are related to stakeholder requirements by perceived needs, expressed needs and retained needs:

- **perceived needs** “are based on a person’s awareness that something is wrong, that there is a lack of something, that there is something that could improve a situation, or that there are business, investment, or market opportunities”
- **expressed needs** “originate from perceived needs in the form of generic actions or constraints, and are typically prioritized”
- **retained needs** “are selected from the expressed needs. The selection process uses the prioritization of expressed needs to achieve something or make solutions feasible”.

The retained needs represent the stakeholder intentions that still “do not serve as stakeholder requirements, since they often lack of definition, analysis, and possibly consistency and feasibility [...]” RE leads stakeholders from those initial intentions to structure more formal stakeholder requirement statements” (ISO/IEC/IEEE, 2011). Stakeholders requirements are “the requirements for a system that can provide the services needed by users and other stakeholders in a defined environment” (ISO/IEC, 2008). According to authors in (Jackson et al., 1995) the **stakeholder requirements** have to constraint the environment of the system, stating the expected effect on the environment caused by the interaction with the system. Stakeholder requirements are transformed by a RE process into system requirements. System requirements are defined as “the requirements for a system that can provide the services needed by users and other stakeholders in a defined environment” (ISO/IEC, 2008). A detailed analysis of the process for transforming stakeholders requirements into system requirements can be found in (Bouffaron et al., 2012).

System requirements are collected in a system requirement model (SRM), as defined in the previous section. As system requirements, also stakeholder requirements are collected in an appropriate fashion (stakeholder requirements model - RM). This environment is different from the one of person i.e. the person can be part of the system environment. This latter includes “anything affecting a subject system or affected by a subject system through interactions with it, or anything sharing an interpretation of interactions with a subject system” (IEEE, 2002). The system here is the system whose life cycle is under consideration, named the System-of-Interest (SoI) (ISO/IEC, 2008).

Fig 5(a) shows the conceptual model expressing the main definitions from the previous section. Notice that the **stakeholder requirements** are the first statements really structured and consistent, in the customer domain.

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**Fig. 4 – Needs lifecycle (Faisandier, 2013)**

### 5.2. The conceptual model for representing the right variety

**Customer and product variety**

In order to define the sets X and Y, let us now consider a **SoI** referring to a PL so that it has to describe a certain variety interacting with an environment now related to a **customer segment** (see Fig. 5b). A **segment environment** is related to more than one RM. Similarly the **SoI** is related to more than one **SRM**. Since a requirement is unambiguous and measurable (ISO/IEC, 2007) and a **SRM** models consistently a set of system requirements, a **SRM** can represent an element of the set Y. As for **PLs** (see section 3), a set of attributes can describe the variety and similarities between different **SRMs**: this variety can formalise the product variety (i.e. set Y) for the customers segment.

As analogy of **SRM**, the values related to a set of attributes describing the variety between the **RM**s will represent the customer variety, i.e. the set X. This implies that the customer variety is defined by the characterisation of the system environment and the effects that the system has to provide on its environment. The difference between this definition of X and the definition of the set X concerns the feasibility. The **stakeholder requirements** are related to a feasible system (ISO/IEC/IEEE, 2011) therefore every RM has a correspondent **SRM**.

The **PL definition function**

Since the **stakeholder requirements** constraint the environment and the system requirements specify the SoI, the knowledge behind the **PL definition function** g (and consequently f as inverse of g) allows relating attributes concerning the system environment and attributes specifying the SoI. Therefore it represents the knowledge of the interactions between the SoI and its environment. Since the function g is multivalued, more than one **SRM** can be found for a RM.

In this section, we have defined the set X, X1, Y and the definition function g on the basis of terms from SE.
6. KBS FOR PRODUCT LINES DEFINITION AND RATIONALISATION

In this section, we show how to involve the knowledge before defined in the definition or rationalisation of a PL. At this purpose, a knowledge base that uses the concepts just described is used as a core for a Knowledge Base System (KBS). The KBS inferences support the definition of the configuration function $f$ and therefore of the set $Y$, representing the right product variety for the PL.

The first subsection of this paragraph discusses the KB formalisation by means of an ontology. The second subsection describes how the KBS support the definition and the rationalisation of a PL.

6.1. From the conceptual diagram to the knowledge base

Starting from the conceptual diagram just discussed (Fig. 5b), we define an ontology as the core of a KBS for the PL definition and rationalisation. The ontology has been formalised using a description logic (DLLite) (Baader, 2003). DLLite is based on the theory of sets and guarantees the decidability; therefore a verification of the consistency of the modelled artefact can be performed. Moreover DLLite is based on the open world assumption (OWA), thus the knowledge base can be easily extended. In order to translate the conceptual diagram into an ontology we used the mapping rules defined in (Atkinson et al., 2008).

The key knowledge formalised in the ontology is about the function $g$, i.e. about the relationships between attributes representing customer variety and attributes representing product variety. As discussed in the previous section, this implies that the function $g$ describes the interactions between the SoI and its environment.

In the ontology representing the KB, a class concerning the knowledge just described has been formalised: the class interaction. In this class, individuals describe the mathematical knowledge for calculating values of a required attribute, starting from values of the other attributes related to the interaction. The knowledge about interactions may come from physics, chemistry, experiments, personal experience, etc.. This class relates attributes describing the environmental expected effects and constraints with the system attributes (Fig. 6).

The semantic difference between environmental expected effect and environmental constraints concerns the definition of the purpose shown in the previous section. Actually, a system purpose emerges whenever an unsatisfactory interaction between a person and that person’s environment exists. Consequently a purpose represents something that the system, working in the system environment, has to change. This means that expected effects on the environment are derived starting from a purpose. On the other hand, environmental constraints represent something that the system, working in its environment, has to take into account as some perturbations.

System attributes characterise the product variety. They represents what the system should do to get the environmental expected effects, respecting the environmental constrains.

For instance, we can consider temperature of a room as an environmental expected effect, the room usage and size as environmental constraints and the cooling system power as a system attribute. Interactions in the KB have to describe the mathematical relationships between the values of these attributes.

Environmental effects, constraints and system attributes are all related to the class attribute of the ontology. As discussed in the previous sections, every attribute is a measurable property. Every attribute can be related to different interactions and this relationship is characterised by a domain of validity. Returning to the previous example: if the knowledge contained in the KB is limited to temperature of 24, 25 and 26°C, these three values represent the domain of validity of the attribute along the considered interaction. In other words, if the system attribute is the power of a heating...
system, for defined room characteristics, we know only this information related to maintaining the room temperature at 24, 25 and 26°C.

6.2. Usage scenario for the KBS

Fig. 7 shows the KBS usage scenario. The user selecting the purpose of the SoI in the system performs the first activity. As shown in the conceptual diagram, the purpose for a customer segment is considered as unique. An example of purpose can be “maintain a good air quality in the room”.

Algorithm 1 – interactions retrieval

The KBS retrieves the knowledge about the introduced purpose in the KB. If at least one correspondence is found, the algorithm checks for environment effects derived by the purpose. This algorithm builds a sort of tree of interactions. When an attribute is related to an interaction, the algorithm identifies the other attributes involved in the interaction. Then, for each identified attribute, the algorithm retrieves interactions to which it is related and other attributes are identified. These tasks are iterated until an attribute is an environment constraint or, in the case of system attributes and environment effects, if there are no other interactions related to it. The result of the algorithm is a tree that has as roots the environment effects related to the purpose and as leaves the system attributes and the environmental constraints. Every attribute is related to a validity domain for the related interaction. According the example above, the algorithm would infer attributes on customer variety such as desired temperature, size of the room, usage of the room and so on. On the PL side, possible inferred attributes could be the power of the system, air-filtering features and so on.

When the tree includes alternative paths, more than one PL impacts the same purpose. This implies that a PL is defined by the attributes on the leaves of the tree. In other words, two PL can have the same purpose but cannot be addressed to the same customers segment, i.e. one PL for each customers segment. Returning to the example above, two different PL can affect the air quality in a room, but they can have different interfacing requirements with the environment, e.g. solar heating system, hydraulic system or cogeneration. In this case the customer variety is characterised by attributes that are completely different.

On one tree path built by the algorithm 1, the interactions represent the PL definition function $g$. The set of system attributes and their domain validity describe the variety in the product domain $Y$. The set of attributes for environment effects and constraints and their domain of validity define the variety in the customer domain, i.e. set $X_1$. One element of $X_1$ or $Y$ is a vector that has as component a value for each attribute describing the variety. The multivalued function $g$ transforms a vector of system attributes representing a product variant into a vector of environmental effects and/or constraints representing the customer variety.

The inference algorithm 1 is external to the ontology. This is due to the OWA. Actually we need to make design decision based on the knowledge available at a defined time, i.e. condition on the end of iteration for the tree construction. For this kind of inferences, the closed world assumption (CWA) is required. An external algorithm manipulating the ontology can guarantee the CWA.

Algorithm 2 – PL definition

Starting from a customer segment characterised by certain features, the user should select a PL starting from the customer variety expressed by, i.e. environmental effects, constraints and related validity domains. The latter limits the environments in which the product variants can work for the defined purpose. For instance, if the attribute “room size” has an associated range of validity, this means that we are not able to propose variants that meet the purpose for room sizes outside of that range.

Then the user can further characterise the customer variety defining the values for each attribute, i.e. environment effects and/or constraints. Only values inside the validity domains can be introduced. For instance, if it is known that there exists a minimum room size legally defined, the user can limit the domain validity of the related attribute. It is important to highlight that these characteristics allows determining a finite set representing the customer segment variety. Obviously, if the customer set is unbounded then an assessment of a limited PL variety is not feasible.

Once the values for attributes of a customer variety are introduced, the algorithm 2 uses the interactions retrieved by the algorithm 1 for calculating constraints in terms of system attributes. These attributes limit the border of a space that represents the variety that the PL has to express in order to meet all requirements in the defined customer segment. Each system attribute and related validity domains represent respectively the dimensions and the limits of the space. Moreover, a validity domain for environmental effects and constraints can be characterised by a tolerance: the latter can allow making discrete a continuous interval; in each case, the space defined by the system attributes should be discrete. Notice that, on the product variety, a variant represents a physical object; therefore a product variety defined by continuous intervals would be nonsense.

Even if limited, this space still does not represent the portion of the set $Y_1$ defining the right product variety. Actually, $Y_1$ represents the codomain and image (property 3) of the configuration function $f$, where $f$ respects the property (2).

To respect the property (2), the configuration function has to relate each customer with only one product variant. This implies that, in order to respect the property, only one product variant should be chosen. Since for the customer all these variants are equally fulfilling his needs, the most reasonable decision is to choose the best product variant for each identified environmental effect: for instance, an optimisation criteria could represent the lowest resource consumption for the development and the manufacturing of the related product. If the property (2) is respected, the set of product variants defined by system attributes and values represents the set $Y_1$, expressing the right product variety.
Algorithm 3 – PL rationalisation

When the aim is the rationalisation of an existing PL, the results of the algorithm 1 are used by another algorithm. This time, the user introduces values also for system attributes. These values represent the variety expressed by the existing product line. The algorithm 3 uses these values and the interaction in the tree to infer the coverage of the PL on the defined customer segment. The ranges of values for the attributes describing the customer variety define this coverage. Comparing these ranges with the defined customer segment, this algorithm allows to highlight lacks, redundancies and/or excess of variety in an existing PL: a lack represents a part of the defined customer segment that is not covered by the PL; a redundancy in the PL means that it is possible to identify more than one variant for a distinct customer; an excess of variety represents a part of the PL variety that cover customers outside the customer segment defined by the user.

7. CASE STUDY

In this section, an application of the proposed approach is presented. The aim of this case study is to show how the KBS should handle domain knowledge in order to rationalise the product variety.

The case study presented in typical of the major part of companies producing mature products, where the revenue is strongly dependent on scale economies more than on innovation lips. In such a kind of scenario, the careful definition of tacit and explicit customer requirements became a critical asset for revenue margins. The challenge for any company in mature market scenario is to increase the worthiness of money spent by customer, by providing satisfaction of the tacit customer’s expectations in terms of product quality and reliability, while maintaining a high level of profitability. The mass craftsmanship paradigm is here thus implemented by applying the methodology proposed to solve this apparent contradiction.

KBS scenario

The KBS should allow the selection of a purpose for the PL. The analysed PL has as purpose the “room air-cooling”. In the KB, this purpose is related to some attributes representing the desired environmental effects for cooling the room, i.e. the room temperature. The algorithm 1 defines a tree of interactions for this attribute. The retrieved equations are the following:

\[ q_{td} = U_0 F_{2a} A_{0} n r \left( t_{a1} - t_{a2} \right) - \left( t_{a2} - t_{a1} \right) \ln \left( \frac{t_{a2} - t_{a1}}{t_{a1} - t_{a2}} \right) \]

\[ A_a = \frac{Q}{V_a} \]

\[ q_{td} = P_a = P_r = P_s \]

\[ F_s = \frac{A_0}{A_n} N_r \]

\[ U_0 = \frac{1}{\left( \frac{1}{n f_a} \right) + \left( \frac{B}{f_r} \right)} \]

\[ P_a = 0.018 A_n V_a (t_{a1} - t_{a2}) \]

\[ P_r = \rho_r Q c_r (t_{r1} - t_{r2}) \]

\[ Q^2 k = P_{st} \]

\[ B = \frac{A_3}{A_1} \]

Notice that more than one attribute can be related to the selected purpose; this should not affect the algorithms effectiveness. The tree has no alternative path and the attributes on the customer side (i.e. environmental effects and constraints) are: the room temperature \( (t_{a1}) \), the fluid type \( (p_r, c_r) \), and input output temperatures \( (t_{r1}, t_{r2}) \), the static pressure \( (P_{st}) \) of the duct and the power \( (P_s) \) to be provided to the room depending on building features and the room usage. The attributes on the engineering side (i.e. system attributes) are the fan \( P_{st}/air \) flow characteristic \( (k) \), the air velocity \( (V_a) \), the external coil surface \( (A_0) \), the internal coil surface \( (A_i) \), the number of coil rows \( (N_r) \), the coil air heat exchange \( (f_a) \), the coil fluid heat exchange \( (f_r) \), the fin efficiency \( (\eta) \), where the last three properties are the result of the interaction of the water and air flows with the coil geometry.

The user has to characterise the customer segment introducing a range of values for each environmental constraint and effect. For instance we can consider 21°C-25°C C for the room temperature; only water as cooling vector (fluid)
Starting from the retrieved equations and ranges of values, the algorithm 2 should limit the values of the system attributes. In this case, considering the attributes range for static pressure \((P_s)\) (0-60 Pa) range of values, it is possible to add two more constraints to the retrieved equation \(Q^2k = P_{st}\), where \(Q\) is the airflow rate and \(k\) is the corrective constant depending on the fan type. Let us consider for a moment this interaction as the only one in the tree. This means that the environmental constraint can be fulfilled by couples of values for the airflow and the fan type. From the customer point of view, the choice of two couples of values generating the same static pressure makes no differences. Therefore engineers have to choose only the best one (e.g. on the basis of economic reasons) in order to preserve the property (2), i.e. one variant for each customer. Defining a tolerance values for the environment constraints and effects (e.g. \(\pm 0.1\) for \(\alpha_1\)), the constraints can support the definition of discrete intervals of system attributes and consequently a finite number of product variants. Variants should be selected defining some optimisation criteria to the defined constraints. The algorithm 3 for the PL rationalisation requires also the system attributes to be filled. Here the user has to describe the existing PL variety according to the inferred system attributes. The algorithm 3 should use the interactions retrieved by the algorithm 1 for projecting the PL variety on the customer segment. The algorithm should highlight lacks, excess and/or redundancies in terms of values for the static pressure, the room temperature and so on.

The object of the case study is inspired by the works on the Trane fan-coils PL, named UniTrane\(^{TM}\) FCD (Fig. 8). Trane is a company that designs, develops and commercialises heating and cooling systems. For confidentiality reasons, the knowledge we use to instantiate the ontology is not coming from the Trane PL, but the domain knowledge in (American Society of Heating, 2012) is typically formalised as mathematic formulas, describing physics principles and experimental relationships. An examples is the following:

\[
q_{ctd} = U_0F_sA_aN_r \left(\frac{(t_{a1} - t_{r2}) - (t_{a2} - t_{r1})}{\ln \frac{(t_{a1} - t_{r2})}{(t_{a2} - t_{r1})}}\right)
\]

where \(q_{ctd}\) is the sensible cooling capacity of a coil, \(U_0\) is the overall coefficient of heat transfer for sensible cooling (without dehumidification), \(F_s\) is a coil shape coefficient, \(A_a\) is the coil face area, \(N_r\) is the coil rows number, \(t_{a1}\) and \(t_{a2}\) are the input and output air temperatures, \(t_{r1}\) and \(t_{r2}\) are the input and output fluid temperatures.

In the ontology, this is an individual belonging to the class interaction. All variables in the formulas represent the attributes related by the interaction. Each attribute is marked as being an environmental constraint (customer variety), an environmental effect (customer variety depending on the purpose) or a system attribute (product variety). In the formula above: \(q_{ctd}, U_0, F_s, A_a\) and \(N_r\) are system attributes, \(t_{a1}\) is an environmental effect (approximation of the room temperature), \(t_{a2}\) is a system attribute and the fluid temperatures \((t_{r1}, t_{r2})\) are environmental constraints.

8. CONCLUSIONS AND PERSPECTIVES

In this paper an approach for the rationalisation of the product variety has been presented. Initially, a formal definition of the requirements for the rationalisation is proposed. Related concepts have been identified by means of a conceptual model based on system engineering (SE) terminology: customer has been represented as environment and the relationship with product as an interaction between the system and its environment. Concepts have been formalised and extended in an ontology for representing PL definition knowledge. Finally a scenario of usage for this ontology in a knowledge-based system (KBS) has been shown.

The whole approach defines a brand new point of view on product variety. In literature it is usually seen as a source of complexity for manufacturing, planning and scheduling systems. Several works are focused on how to cope with this complexity. In this paper we dealt with the customer variety, representing the causes of the product variety and consequently of this complexity. Linking the product variety with the customer domain, we showed that a system for defining only the rationalised PL variety can be defined. On the manufacturing side, the aim is to delete the unjustified variety and therefore to reduce the unjustified complexity. On the customer side, the aim is to define configuration systems that do not require a product-related knowledge for configuring the right product.

It is important to highlight the consequence on the configuration systems discussed. On one hand these are completely customer-oriented: the customer is asked to describe its environment and what he expects from the product. On the other hand, all optimisations in configuration
system (e.g. price) are moved on the engineering side: a customer should represent a problem; only on the engineering side, appropriate algorithm can be deployed to identify the best solution (e.g. from a resources consumption point of view).

Future perspective of the present research concerns the development of the algorithms to finalise the structure of the KBS. A larger KB, even with knowledge from different domains, will be used to test the algorithm two. Moreover a more complex PL will be treated: according to the presented approach, the more complex the system-environment interactions are, the more complex is the implementation of the approach. Finally, an integration of this work with the proposal in (Giovannini et al., 2012) will be envisaged; the aim is to take into account the PL variety in an enterprise network.

9. REFERENCES


Atkinson, Colin and Kiko, Kilian (2008), A Detailed Comparison of UML and OWL.


