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Molecular mechanics investigations of carbon nanotube and graphene sheet interaction

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The interaction between a carbon nanotube (CNT) and a graphene sheet is investigated to describe the contact properties between a CNT atomic force microscope (AFM) tip and a graphite surface. The energy of the whole system is calculated using MM+ molecular mechanical modeling. With the numerical calculations, one explores the sliding motion of the CNT on the graphene sheet either at the CNT apex or with a given CNT length contacting the surface. The aim is to mimic the AFM CNT tip scanning a graphite surface. To do so we calculate the energy barriers, the tips have to overcome to achieve a full translation. The results show that the barrier heights markedly depend on the contact length between the CNT and the graphene but show a weak dependence, if any, on the CNT tube diameter.

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I. INTRODUCTION

In the last decade carbon nanotubes (CNTs) have attracted great interest due to their mechanical and electronic properties. More specifically, their high tensile strength, flexible rigidity, high aspect ratio, and low chemical reactivity make them interesting materials for tips in scanning probe microscopy. Single-wall CNT tip scanning using dynamical AFM imaging has been demonstrated to provide single-molecule profiles of a hydrated protein and DNA molecules with enhanced resolution and reproducibility.

The design of CNT AFM tips (with, in particular, the nanotube attach to the surface, its angle with the surface) is determinant for the AFM image contrast; it depends on the nanotube substrate interaction, thus on the geometry of the contact area between the CNT and the surface. Due to the weak chemical affinity of CNT, AFM experimental studies with CNT AFM tips, show remarkable tip and image stability but many years after early research on the nonlinear behavior of single-wall probes, a quantitative analysis still remains a major challenge.

Experimental measurements are usually done on natural graphite, which is a mixture of ordered AB stacked and disordered turbostratic layered structures, shown in Fig. 3. The equilibrium interlayer distance 3.34 Å and c-axis compressibility 2.7 × 10⁻¹² cm²/dyn of graphite can be measured with good accuracy. The absolute interlayer binding energy, i.e., exfoliation energy is harder to extract; there is only a handful of results in the literature. A heat-of-wetting experiment by Girifalco and Ladd gives an exfoliation energy of 43 meV/atom. A microscopic determination of the interlayer binding through study of collapsed nanotubes yields 35 ± 10 meV/atom. Later experiments on thermal desorption of polyaromatic hydrocarbons give a larger binding energy of 52 ± 5 meV/atom. Concerning interaction between carbon nanotube walls, Kis et al. had performed interlayer force measurements through cyclic telescoping motion of a multiwall carbon nanotube. They showed that the force acting between the core and the outer casing is modulated by the presence of stable defects and generally exhibits ultralow friction, below the measurement limit of 1.4 × 10⁻¹⁵ N/atom and total dissipation per cycle lower than 0.4 meV/atom.

To interpret these experimental values, some theoretical calculations have been carried out on graphene interlayer spacing and binding energy. Trickey et al. in 1992 performed density-functional theory-local-density approximation (DFT-LDA) studies of the binding between two graphene sheets. They obtained an interlayer binding energy that was 50% larger than the experimental ones. Also, an LDA calculation by Jansen and Freeman gave a fairly good answer for the interlayer spacing 3.41 Å but the interlayer binding energy was four times greater than the expected value. The authors explain the difference because of a local density that does not adequately take into account the disper- sive part of the van der Waals interactions. Using the local-density approximation to DFT, within pseudopotential formalism and plane-wave basis, Schabel and Martins found an interlayer spacing and binding energy in excellent agreement with the experimental results. Girifalco and Hodak used an empirical model potential and obtained an interlayer and binding energy also in good agreement with the experiment. In the other hand, Charlier et al. identified various contributions to the interlayer binding and gave the correct interlayer spacing and binding energy.

Other theoretical studies have been dedicated to interaction between carbon nanotube. Using quantum mechanical augmented by an intertwute Lennard-Jones potential, Surján and co-workers have computed interactions of several families of tubes of diameters. Depending on the stacking between tubes, they obtained a rotation barrier in the range 3.9–29.3 meV/Å. Density-functional theory within the local-density approximation has been used to compute the translation and rotation barrier of two concentric bilayered carbon nanotubes. The results gave a translation and rotation barrier equal to 0.23 and 0.52 meV/Å, respectively.

In recent experiments and theoretical studies, Rao and co-workers, demonstrated that graphene samples prepared by
exfoliation of graphitic oxide or conversion of nanodiamond exhibit significant uptake of \( \text{H}_2 \) and \( \text{CO}_2 \).\(^{21}\) They used DFT calculations with localized orbitals implemented in SIESTA software to interpret their experiments, and obtained a binding energy of \(-0.21\) eV for \( \text{H}_2 \) and \(-0.4\) eV for carbon dioxide. In another paper they also studied binding of DNA nucleobases and nucleosides with graphene.\(^{22}\) The total binding energy obtained by adding the van der Waals term, found thus as \(-0.65\), \(-0.64\), \(-0.638\), and \(-0.34\) eV for Guanine, Adenine, Thymine, and Cytosine, respectively.

Here, we perform calculation of the total energy involved in a CNT-graphene sheet ensemble, with the aim to describe the CNT tips behavior when it scanned on a graphite surface, by using MM+ force field. The MM+ force field is used to calculate the interaction between aromatics molecules.\(^{23}\) For instance, Janelli et al.\(^{24}\) have systematically compared the numerical results obtained with different force-field method with the x-ray structural data dedicated to a study of the influence of the packing forces on the molecular conformation of complex molecules in the solid state. Among different molecular mechanics calculations, MM+ provided better results. The same conclusion was reached in doing ansa-9-meta-cyclophane studies.\(^{25}\) MM+ was also used to calculate various stable structures such as host alcene-octamidocavitands@\( \text{C}_{60} \) (Ref. 26) or biological systems.\(^{27}\) Concerning adsorption studies, MM+ calculations have been found as an appropriate tool to help the experimental finding. For instance, for the study of the deposition of pheniloctane on graphite surface, MM+ gives numerical results in good agreement with the experimental data, in particular, on the relative orientation of the molecule on the graphite surface.\(^{28}\) It has been also widely used to account for scanning tunnel microscope (STM) measurements, MM + calculations on methionine adsorption on the graphite surface have been carried out recently and have helped to find the exact site of adsorption of the molecule on graphite.\(^{29}\) Following the same aim, STM and MM+ calculations were employed to analyze the step of nanoassembly of meso-tetraphenylporphines \( \text{H}_2\text{TPP} \) and it’s cobalt (II) complex on the highly oriented pyrolic graphite.\(^{30}\)

Recent AFM thermal-noise measurements on CNT have shown that the contact between CNTs and a graphite surface can be classified in two categories: either the contact obeys a free sliding condition or else a pinned situation.\(^{31}\) As thermal noise applies a weak forcing, tiny variations can be observed, however the main question remains why similar CNTs may exhibit complete different contact behaviors. The present work aims at providing a step to understand such a difference, in particular, to analyze the parameters governing the height of the barrier that opposes to the CNT tip translation on the graphite.

II. CALCULATION METHOD

Molecular mechanics calculation were performed with the HYPERCHEM program employing the MM+ force field. It is a general force field improved from the MM2 force field first developed by Allinger.\(^{32,33}\) The system total energy is a sum of bond stretching, bond-angle binding, dihedral, improper dihedral, and van der Waals terms.

Unlike other force fields, MM+ describes the interaction of van der Waals by combining an exponential repulsion with an attractive \( 1/\overline{R}^6 \) dispersion interaction. So the van der Waals term is calculated as\(^{34}\)

\[
E_{\text{vdW}} = \sum_{i,j} e_{ij}(2.9 \times 10^5 \exp(-12.5 \rho_{ij}) - 2.25 \rho_{ij}^6),
\]

where \( e_{ij} = \sqrt{e_i e_j} \) and the hardness parameters \( e_i \) determine the depth of the attractive well and are defined for a pair of atoms and \( \rho_{ij} = \frac{R_{ij}}{\overline{e_i e_j}} \), \( r_{ij}^* = r_i^* + r_j^* \), \( r_i^* \) is the van der Waals radius for the atom of type \( i \) and \( R_{ij} \) is the distance between the core of the two atoms.

Structures of CNT and graphene are built with the NANO-TUBE MODELER software.\(^{35}\) In graphene structure the distance between neighboring carbon atoms is 1.41 Å. To do calculations, the default parameters from Goddard and co-workers\(^{36}\) are modified to graphitic systems. \( r_{ij}^* \) is taken to be equal to 3.30 Å and \( e_{ij} \) to 3.66 meV.

Single-walled CNTs, SWNT, of diameters ranging between 0.7 and 2.56 nm and indices \((6,0), (8,0), (9,0), \) and \((5,5), (6,6), (10,10), (20,20)\) corresponding to zigzag and armchair structures, respectively, (see Fig. 2) are used. The ends are opened for \((6,0), (8,0), \) and \((20,20)\) and capped for \((5,5), (6,6), (9,0), \) and \((10,10)\) CNTs. Within the range of...
For each point we do a single-point calculation of the energy of the systems (CNT+graphene) and of the isolated CNT and graphene. The binding energy is obtained as the difference between the total energy of the system and the sum of the energy for each isolated parts (Fig. 1).

\[ E_{\text{binding}} = E_{\text{CNT+graphene}} - (E_{\text{CNT}} + E_{\text{graphene}}). \]

The binding energy depends only on the van der Waals part. The adhesive energy is taken as the lowest value of binding energy. To compute the barrier height, we explore the adhesive energy by moving the tube along its axis and diameter direction by step of 0.2 Å (Fig. 4).

Folding of a graphene sheet along the vector \( \vec{C} \) gives the carbon-nanotube structure, for instance, zigzag and armchair (see Fig. 2).

### III. RESULT AND DISCUSSIONS

#### Influence of the stacking structure

To explore several types of contact between the carbon nanotube and the graphene, we first investigate armchair and zigzag structures deposited along the main axis, then rotate the CNT on the surface with 60° and 90° angles and optimize for each position the equilibrium distance. As showed in Fig. 3, several conformations are found. A translational motion is then performed along the direction of the tube symmetry axis with steps of size 0.2 Å.

The adhesion of the CNT on the graphene is defined as the lowest-energy value giving the equilibrium distance between the CNT and the graphene. For graphite interlayers the calculated distances are found between 2.8 and 4 Å (Refs. 16, 20, 39, and 40) while the equilibrium distances between the CNTs and the graphene sheet are found to be in between 3 and 3.2 Å. In order to mimic the motion of a CNT AFM tip on the graphite, we first investigate the relative translation motion of a SWNTs of 2 nm length on graphene. The number of atoms per tube is 114 for (6,0), 152 for (8,0), 204 for (9,0), 221 for (5,5), 252 for (6,6), 480 for (10,10), and 680 for (20,20). The addressed question is to calculate the potential barrier we need that must be overcome to achieve such a lateral motion. Several configurations are envisioned and some of them are sketched in the Fig. 3. We first look at the
simple translation of a SWNT (9,0) along x and y axes, where x is along the tube-axis direction (Fig. 4).

In Fig. 4, the translation motion along the tube axis shows two barrier heights of 30 and 70 meV. For the second barrier, the SWNT starts from a local minimum of 7 meV. Therefore, the effective value of the second barrier height is reduced to about 63 meV. The lateral force required to pass over the barrier is readily obtained by dividing the distance between the neighboring local minimum and the maximum height of the barrier, which for the two cases is about 1 Å, we thus have 48 and 100 pN, respectively. The lateral motion along the y direction exhibits two identical barrier heights of 57 meV with a distance between minimum and maximum of 1.2 Å. The corresponding lateral force is 76 pN. Note that the calculation investigating the relative rotation of a (10,10) CNT against a fixed one, leads to similar shape of the barrier potential.

The top of the barrier corresponds to a perfect superposition between the aromatic rings. On the contrary, at the location of the minimum of energy, the stacking is such that a carbon atom of the CNT is at the center of a benzene ring of graphene as those shown in Fig. 4(b). These structures are similar to those observed for graphite interlayer.

Changes in the adhesive energy depend both on the CNT graphene relative orientation and on the CNT structure, either zigzag or armchair (see Table I). Therefore, we may also expect that the energy landscape and, in particular, the height of the barriers might also depends on the relative orientation between the two structures. As shown with the results displayed in Figs. 4–6 the energy landscape depends drastically on the relative orientation between the CNT and graphene. For instance, the 90° rotation of the (9,0) CNT modifies the shape of the barrier and leads to a net decrease in the barrier height, much less than $k_BT$, so that the tube may slide on the surface.

The 60° rotation of the (9,0) CNT (Fig. 5) shows more complicate energy landscapes. The translation motion along the tube-axis direction exhibits a small bump of 10 meV height and two barrier heights of values 50 and 57 meV with the maxima being separated by a distance of 4.2 Å. The lateral displacement along a direction perpendicular to the CNT axis exhibits symmetric barriers of 30 meV heights. Those values are close to the room-temperature value 25 meV.

When the CNT is rotated by 90°, the barrier heights are drastically reduced with heights much lower than the room-temperature energy. The result is obtained for the two directions, for translation along the tube axis (x) or perpendicular to it (y) (Fig. 6). Those results suggest that the tube may exhibit large fluctuations of the contact area with the graphene.

### IV. EFFECT OF THE TUBE DIAMETER ON THE BARRIER HEIGHT AS THE CNT SLIDES

For the armchair tubes (5,5) and (6,6) (Fig. 7), the energy landscapes are similar to the one obtained with the zigzag structure. The translation motion along the tube axis (x direction) gives a set of barrier heights and periodicity similar to those corresponding to the translation motion along the direction normal to the (9,0) zigzag structure (along the y

![FIG. 5.](image_url) (Color online) Height barrier for a (9,0) CNT rotated of 60° as regard to the graphene. Scheme of the (9,0) CNT rotated of 60° as regard to the graphene potential periodicity linked graphene structure.

![FIG. 6.](image_url) (Color online) Sliding zigzag CNT on armchair direction of graphene.

![FIG. 7.](image_url) (Color online) Barrier-height variation with x displacement for tube (5, 5) (left) and (6, 6) (right).
direction in Fig. 4). A similar behavior is also obtained between a lateral motion along the y direction, armchair structure, and along the x direction for the zigzag structure (results not shown). The increase in the diameter from (5, 5) to (6, 6), leads to an increase in the adhesive energy from −5.16 to −5.34 eV. However, the barrier heights remain nearly equal with a value of 57 meV (Fig. 8). Whatever the involved translational motion involved, along the tube axis or perpendicular to it, the same conclusion is valid for the zigzag and armchair structures with barrier heights often higher than $k_BT=25$ meV. The energy landscape of (5,5) and (6,6) structures show a weak dependence, if any, on the CNT diameter. This result is confirmed with the comparison of barriers heights for the (5,5) and (10,10) structures (Fig. 8).

V. INVESTIGATION OF THE EFFECT OF THE CNT CONTACT LENGTH ON THE RELATIVE MOTION BETWEEN CNT AND GRAPHENE

As expected, an increase in the contact length of the tube on the graphene leads to a corresponding increase in the adhesive energy. But also, the barrier heights are augmented with 35, 45, and 55 meV for 1, 1.5, and 2 nm of contact CNT length, respectively (Fig. 9).

In the Table I, we report the adhesive energy and barrier height per atom calculated for the CNT structures (9,0), (5,5), (6,6), and (10,10). The adhesive energies per atom are within the range 14–26.14 meV/atom, in good agreement with the experiment values from Ref. 12.

In Fig. 8, adhesive energies of CNTs (6,0), (8,0), (9,0), (5,5), (6,6), (10,10), and (20,20) are presented. Values are, respectively, −0.18, −0.19, −0.26, −0.25, −0.33, and −0.40 eV/Å. The equilibrium distances are within the range 3.0–3.2 Å. The results are in a good agreement with Avouris et al. results,37 and C 60 adsorption on graphite results.43 They are slightly larger then the interlayer interactions energies of graphite calculated with Moller-Plesset second-order method (MP2/6-31G*).42 To evaluate the effect of the electronic energy, we compare our results to DFT/LCAO-OO+intermolecular perturbation theory (used to add van der Waals contribution).38,44 Calculations have been realized on the same system with the same method to compute the adhesive energy.45 We obtain some differences in the adhesive energy depend on the diameter. The difference is very small for small diameters and becomes significant up to 0.2 eV/Å for the nanotube (10,10). This difference is due to the electronic energy contribution from atomic orbitals overlapping, which becomes more important with increasing number of atoms of CNT interacting with the surface because of the tube deformation.

Less obvious are the variations in the energy landscape, the barrier heights show a marked increase as a function of the contact length with 35, 45, and 55 meV for 1, 1.5, and 2 nm of contact CNT length, respectively (Fig. 9) (Table II).

Previous results focusing on the interaction energies per length for aligned CNT pairs give barriers in the range 26–33.1 meV/Å for AA and BB structures overlap and much less (4.2–8 meV/Å) for turbostatic structures (see Fig. 3 for the definition of the structures). These results are larger than those we have displayed in Figs. 4–6 because of the strong bind between tubes and the rotation effect which include an important contribution of orbital overlapping. Our results agree quite well with the experimental CNTs measurements investigating the sliding motion between two concentric CNTs, and density-functional theory within LDA approximation of the same system where an estimate of the translation and rotation barriers are, respectively, 0.23 and 0.52 meV/atom (Ref. 20) (see Table I).

VI. MIMICKING AFM CNT TIP SCANNING A GRAPHENE SURFACE

The above methodology might help to simulate the behavior of a CNT AFM tip touching and moving on a graphite surface. Here, only the energy of adhesion is taken into ac-
As indicated with the values reported in Fig. 10, the binding energy of the fullerene is calculated along the CNT axis for the CNT without any torsion, the adhesive energy is less than the fullerene.\textsuperscript{38,43} This difference can be explained by the difference between the CNT and the fullerene diameter size and an additional electrons overlap contribution in DFT.

The structures of the CNT constraint and the graphene are built with the NANOTUBE MODELER software.\textsuperscript{35} In an attempt to be as close as possible to the experimental situations, the binding energy is calculated along the $z$ axis by approaching the CNT and searching the lowest interacting energy at equilibrium distance (Fig. 4). Variation in binding energy of CNT without torsion is reported in Fig. 10 and show an adhesive energy of $-1.37$ eV at an equilibrium distance of 3.2 Å. In the same figure adhesive-energy variation in function of the applied torsion is presented. The results show an adhesive energy around $-1.37$, $-1.39$, $-1.57$, and $-2.43$ eV, respectively, for the CNT without and with 30°, 60°, and 90° torsion. As indicated with the values reported in Fig. 10, the increase in binding energy may be directly connected to an increase in the contact length for the bending CNT. For the tube without any torsion, the adhesive energy is less than the value calculated for the fullerene.\textsuperscript{38,43} This difference can be explained by the difference between the CNT (9,0) and the fullerene diameter size and an additional electrons overlap contribution in DFT.

Then, the minimum energy being reached, a lateral displacement of the CNT is started that corresponds to the $x$ axis, as shown in Fig. 10, when the CNT is perpendicular to the surface or along the direction nearly parallel to the CNT axis for the CNT under torsion. The incremental step motion is 0.2 Å. The CNT without torsion gives a barrier energy of 13.14 meV, for a distance of 1.4 Å between the local minimum and maximum. So that, only a lateral force as low as 15.31 pN is required to induce the lateral displacement. The barrier energy is almost half of the thermal energy $k_BT\sim 25$ meV at $T=300$ K and the tube can slide freely on the graphene.

For the twisted CNT, the barrier heights are, respectively, 12.75, 26.1, and 34.23 meV for 30°, 60°, and 90° torsion (see Fig. 11) with a lateral displacement of 1.4 Å leading to a lateral force of 14.56, 29.82, and 39.2 pN to pass over the barriers. Therefore, as soon as the CNT increases its contact length, it can become trapped in some areas. Both free sliding and pinning of AFM CNT tips\textsuperscript{47–49} have been observed experimentally on a graphite surface using thermal-noise measurements.\textsuperscript{31} As shown in this work, these situations can be explained by a possible increase in the contact length together with a more or less good registry between the CNT and the graphite.

\section*{VII. CONCLUSION}

In this paper, we have calculated the contact interaction between various carbon nanotubes and a graphene surface. The numerical calculations are used to mimic the lateral motion of a CNT AFM tip on a graphite surface. We show that the barrier heights of the lateral motion energy landscape depend very weakly on the tube diameter while it strongly varies with the contact length of the CNT on the surface. Also the barrier heights strongly depend on the relative orientation between the tube and the surface. Therefore the nanotube can slide freely or be trapped at room temperature, depending on how the contact between the CNT and the surface takes place. The bending of a CNT on a surface increases the interaction and the height of the barrier. For applications in AFM, our numerical results show how much the lateral displacement of the CNT AFM tip depends on the contact length between the CNT and the surface and of their relative orientation, thus the angle of the contact with the surface.

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MOLECULAR MECHANICS INVESTIGATIONS OF CARBON…

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