Mechanical noise limit of a strain coupled magneto(elasto)electric sensor operating under a magnetic or an electric field modulation

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Abstract—The mechanical noise limit of a strain coupled Magneto(elasto)Electric (ME) composite has been investigated when a magnetic or an electric field modulation is applied to sense a low frequency magnetic field and access DC field measurement capabilities. The sensitivity and noise of such a composite sensor was derived from constitutive equations based on the piezoelectric and ferromagnetic material properties. The analysis was used to evaluate the equivalent noise floor of the composite sensor and to explain the origin of noise by constituting a mechanically coupled electromagnetic model. Experimental measurements revealed a good fit with the proposed model. For example, an equivalent magnetic noise level of ~60 pT/Hz @ 1Hz with DC capability was achieved by using an appropriate field modulation.

Index Terms—Magnetoelastic effects, Magnetic noise, Signal modulation, Magnetic field sensing

I. INTRODUCTION

MAGNETOELECTRIC (ME) composites have the potential for detecting very small low frequency magnetic fields on the order of a few pT/Hz. Passive detection methods are based on the direct strain-coupled ME effect [1], [2]. The detection performance for this passive mode is limited by the dielectric loss contributions to the equivalent noise. In order to avoid this limit, field modulation methods can be applied for magnetic field sensing. The principle of operation is based on the field-dependent couplings between the magnetization, strain and electric polarizations [3], [4], [5].

A ME composite can be driven at a given excitation frequency by using a sine wave magnetic field signal. This field produces both an induced magnetization and an induced strain in the ME composite. This magnetization and strain can be modulated by a low frequency magnetic field via any magnetic, mechanical or electric nonlinearities. First, the induced magnetization is able to produce an electromotive force in a pick-up coil surrounding the ME composite. Thus, the low frequency magnetic field can be recovered from the pick-up coil by means of a voltage amplifier in association with a synchronous detector. This method is named M/M. Secondly, this magnetic field induced strain is transferred to the piezoelectric layers where electric charges are generated. A charge amplifier in conjunction with a synchronous detector serves to recover the low frequency magnetic field from the inter-digital electrodes. This is the M/E modulation [6], [7].

Across electrodes deposited on the piezoelectric layer, an electric field can also be applied to drive the ME composite. Serving as an excitation signal, this electric field produces a strain via the piezoelectric effect. This strain can be transferred onto the ferromagnetic layers resulting in a magnetization change (via the 90° domain wall motion). By using a pick-up coil, the induced electromotive-force can be sensed by a voltage amplifier, which is the E/M detection mode. This is the converse ME modulation [8], [9]. Finally, the magneto-dielectric (or magneto-capacitance) described as a change in the dielectric constant as a function of an applied magnetic field can also be used for field sensing. In this E/E detection mode, low frequency magnetic fields can be measured from the change of the sensor capacitance at a given excitation frequency which is controlled by the low frequency reference magnetic field [10], [11], [12].

II. THEORETICAL ANALYSIS

Illustrated in Fig. 1 is a multi-push-pull structure of a ME composite. The sensing element is made up of two Metglas layers of dimensions 80×10×0.075 mm², and a piezoelectric layer of 40×10×0.2 mm³ with 5 piezoelectric macro-fibers, separated by two Kapton layers. Each Metglas layer is obtained by stacking three foils of 80×10×0.025 mm³. Interdigital electrodes are attached on both top and bottom faces of the piezoelectric layer using epoxy resin. The central-to-central space between inter-digital electrodes is 850 μm [13], [14].

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Because the ME composite is fabricated for sensing very low amplitude magnetic signals (~pT to nT range), the amplitudes of either the magnetic or the electric excitation field have to be sufficiently strong (~μT magnitude). These implementations result in linear responses for small signals and nonlinear responses for small signal and excitations when used as a mixer. In order to analyze both the linear and nonlinear effects, the constitutive equations for the magnetic, electric and mechanical states are introduced by

\[
\begin{align*}
D &= d_{33,p}T_p + \varepsilon^T E \\
S_p &= s_{33}E_T + d_{33,p}E
\end{align*}
\]

and

\[
\begin{align*}
B &= d_{33,m}T_m + \mu^T H \\
S_m &= s_{33}H_T + d_{33,m}H
\end{align*}
\]

where \( D \), \( E \), \( T_p \), \( S_p \) are the electric field, electric induction, mechanical stress and mechanical strain in the piezoelectric layer; \( H \), \( B \), \( T_m \), \( S_m \) are the magnetic field, magnetic induction, mechanical stress and mechanical strain in the ferromagnetic layer; \( d_{33,p} \) and \( s_{33} \) are the piezomagnetic and flexiblility coefficients in the piezoelectric layer; \( d_{33,m} \) and \( s_{33,m} \) are the piezomagnetic and flexibility coefficients in the ferromagnetic layer; \( \varepsilon^T \) and \( \mu^T \) are the electric permittivity and permeability of the piezoelectric and ferromagnetic layers under a constant stress.

These constitutive equations yield the coupling equations for the magnetic, electric and mechanical parameters in the ME composite [15, 16, 17]

\[
\begin{align*}
F &= \varphi_m H + \varphi_p E \\
&+ j\omega\left(\mu^T HV_m - \Psi_l\right) = 0 \\
&+ j\omega\left(\varepsilon^T EV_p - Q_l\right) = 0 \\
&+ j\omega C_{EH} F = (v_1 + v_2)
\end{align*}
\]

The first equation in (2) represents the relation between the mechanical force \( F \), the magnetic field \( H \) and the electric field \( E \). Corresponding to a magnetic and an electric field, the force appearing at a given point of the ME composite can be calculated with the magnetoelastic coupling \( \varphi_m = d_{33,m}A_m / s_{33} \) and the piezoelectric coupling \( \varphi_p = d_{33,p}A_p / s_{33} \). \( A_m \) and \( A_p \) are the section area of the magnetic and piezoelectric layers, respectively. The second equation binds the mechanical force \( F \), the magnetic field \( H \) and the magnetic flux \( \Psi \) (= \( B \times A_m \)) in the ferromagnetic layers. The coefficient \( \mu^T \) is the permeability under a constant strain which can be defined by \( \mu^T = \mu^T \left(1 - k_{33,m}^2\right) \), where \( k_{33,m} \) is the elastic coupling coefficient of the magnetostrictive layer. \( s_{EH}^2 = s_{33} \) is the mechanical capacity of the ME composite with

\[
s_{33} = \left(\frac{n}{s_{EH}^2} + \frac{1 - n}{s_{EH,p}^2}\right)^{-1}
\]

[18], [19]. \( n \) is the ratio between the ferromagnetic layer thickness and composite layer thickness, defined as \( n = t_m / (t_m + t_p) \) where \( t_m \) and \( t_p \) are the thickness of ferromagnetic and piezoelectric layers; \( l \) is the effective length of the ME composite; \( A \) (= \( A_{ME} + A_p \)) is the section area of the ME composite; and \( \omega \) is the angular frequency and \( V_n \) is the volume of the ferromagnetic layers. Represented in the third equation, is the relation between the mechanical force \( F \), the electric field \( E \) and the electric charge \( Q \) in the piezoelectric layer. The coefficient \( \varepsilon^T \) is the permittivity under a constant strain which is defined by \( \varepsilon^T = \varepsilon^T \left(1 - k_{33,p}^2\right) \) where \( k_{33,p} \) is the elastic coupling coefficient of the piezoelectric layer; and \( V_p \) is the volume of the piezoelectric layers. The last equation gives the elastic relation between the mechanical force \( F \) and the sum of two edge vibration speeds, \( (v_1 + v_2) \), along the length direction.

The simplified coupling equations between the magnetic field, the electric field, the electric charge and the magnetic flux can be derived from (2) for investigation of the modulation performances. This yields

\[
\begin{align*}
\varphi_m \varphi_p C_{EH} E &+ \varphi_m^2 C_{EH} h + \mu^T \varphi_m V_n H - \Psi_l = 0 \\
\left(\varepsilon^T + \varepsilon^T p_{EH}^2 \right) E &+ \varphi_p \varphi_m C_{EH} H - Q_l l = 0
\end{align*}
\]

By applying a magnetic or an electric field wave signal on the composite, the sensitivities (voltage and current detection versus magnetic field excitation, voltage and current detection versus electric field excitation, respectively named \( M/M \), \( M/E \), \( E/M \), \( E/E \)) can be deduced by the derivative of (3) with respect to the excitation type for a low frequency magnetic field \( H \).
The parameters $V_m$ and $V_p$ are the volumes of the ferromagnetic and piezoelectric phase of the ME composite. The first and third equations present the magnetization detected with a coil surrounding the ME composite. The pickup coil converts the magnetization change into an output voltage following Lenz’s law $U(t) = -\frac{\partial \Phi(t)}{\partial t}$, assuming that the output current is null. The second and fourth equations represent the charge detection sensed by the interdigital electrodes of the ME composite. These interdigital electrodes convert the change of electric charges into a current according to the relation $I(t) = \frac{\partial Q(t)}{\partial t}$. In this case, the output voltage is assumed to be null. A charge amplifier is connected to the electrodes to convert the current into an output voltage.

The existence of magnetic domains and their propagation velocity has been predicted in order to explain the magnetization reversal behaviors of ferromagnetic materials [20], [21]. The domain walls can be regarded as magnetic probes for investigating the magnetic behavior of a ferromagnetic material, since they finely change their polarization directions under an external magnetic field. These changes of the magnetic domains can result in net magnetization change in the material. According to Lenz’s law, this can give rise to an electromotive force in a pick-up coil wound around the materials. In the conversion process, a magnetic nonlinear response appears between the applied magnetic field and the induced magnetization. This magnetic nonlinearity is defined by the coherence of two magnetic fields or a magnetic field and a stress for a magnetic flux output. A nonlinear factor $\eta_1$ is defined to relate the strength of the coupling between the magnetic field and the magnetic flux density. This magnetic flux density is given as a function of the magnetic excitation. From this curve, the magnetic permeability can be deduced as a function of the low frequency magnetic field.

For a ferromagnetic material, a change in shape can be explained by sample deformation. The latter produces a mechanical strain (and/or stress) in ferromagnetic materials. If we apply a magnetic field on ferromagnetic materials, a deformation appears as a function of this magnetic field, due to $90^\circ$ domain wall motion. Since the coupling between the applied magnetic field and the induced strain is non-linear, two incoherent magnetic fields can produce a correlated output strain. A nonlinear factor $\eta_1$ can be defined to evaluate this coupling strength. This nonlinear factor can be regarded as either the change of the low frequency magnetic transfer function as a function of the applied excitation or the transfer function for the excitation field as a function of the low frequency magnetic field.

The coupling between the magnetic flux and the stress is dominated by the piezomagnetic effect. Unlike magnetostriction, there is a change in sign of the magnetization when an applied external stress changes its direction. The stress induces a magnetization change by producing $90^\circ$ domain wall motion via the piezomagnetic effect. Another magnetization process occurring by $180^\circ$ domain wall motion can be given as a function of the amplitude of the magnetic excitation. These two types of magnetization processes correlate to each other by inducing a coherent output magnetic flux. This coupling can be characterized by a magnetic nonlinear factor $\eta_1$. The relation between the applied stress and the output magnetic flux density can be influenced by a second stress. Thus, a factor $\tau_1$ is defined to describe the piezomagnetic nonlinearity.

Mechanical nonlinearity is based on a change of the flexibility under a stress oscillation. This effect can be characterized by the measurement of the output coupling strength when applying two incoherent stresses on a sample. A nonlinear factor $\kappa_1$ is defined to describe this effect.

The piezoelectric coefficient can change in response to an applied external electric field. This effect is known as the piezoelectric nonlinearity. Therefore, the piezoelectric coefficient, $d_{33,p}$, is a stress dependent parameter. A piezoelectric coefficient, $\psi_1$, is introduced to investigate the correlated charge output under two incoherent stresses. An electric polarization change can result in response to either an electric field or an external stress. These two polarizations correlate to each other before converting to an output electric induction. The nonlinear factor, $\gamma_1$, is defined as the nonlinear relationships between the electric excitation and the low frequency stress.

We notice that all these nonlinear relations can be described by a polynomial equation of the form $y = ax \left(1 + \frac{b}{2} x \right)$ where $y$ can be the strain $S$, the magnetic flux or the electric charge as a function of either the magnetic field $H$ or stress $T$ represented by $x$. $a$ and $b$ are the linear coefficient and relative nonlinear factor, respectively. $x$ can be constituted of a low frequency component $x_f$ and an excitation signal $x_e$. In Table I, we have gathered the nonlinear factors and associated relationships for the different types of operation. A general form of these relations is represented in Fig. 2.

![Fig. 2: Nonlinear relation description rule use.](image.png)

Defining a polynomial function with a linear coefficient and nonlinear terms. The red dot in Fig. 2 (b) corresponds to the highest nonlinear coefficient. Compared to the piezoelectric coupling $\varphi_p$ and the mechanical capacity $C_{meh}$, the magnetoelastic coupling $\varphi_m$ is much more sensitive to an external magnetic field or stress [22], [26]. Therefore, without loss of generality, (4) can be simplified by considering only the dominant terms,
leading to

\[
\begin{align*}
\frac{\partial^2 U}{\partial H_{ex} \partial H} &= \frac{\partial^2 \mu^s}{\partial H_{ex}^2} V_m \\
\frac{\partial^2 I}{\partial H_{ex} \partial H} &= \frac{\partial^2 \varphi_m}{\partial H_{ex}^2} \psi_{EH} \\
\frac{\partial^2 U}{\partial E_{ex} \partial H} &= \frac{\partial^2 \varphi_m}{\partial E_{ex}^2} \psi_{EH} \\
\frac{\partial^2 I}{\partial E_{ex} \partial H} &= \frac{\partial^2 \psi_p}{\partial E_{ex}^2} \psi_{EH}
\end{align*}
\]

By hypothesis, the nonlinearity terms are given by

\[
\frac{\partial^2 \mu^s}{\partial H_{ex}^2} = \nu_1 \mu^s, \quad \frac{\partial \varphi_m}{\partial H_{ex}} = \eta_1 \varphi_m, \quad \frac{\partial \varphi_m}{\partial E_{ex}} = 2\tau_1 \varphi_m \psi_p \text{ and } \frac{\partial \psi_p}{\partial E_{ex}} = \gamma_1 \psi_p.
\]

Thus, the ME voltage or current coefficients for the modulation methods are

\[
\begin{align*}
C_{ME,M/M}^{NL} &= \frac{\partial \varphi_m}{\partial H_{ex}} \frac{\partial \psi_p}{\partial H_{ex}} V_m \\
C_{ME,M/E}^{NL} &= \frac{\partial \varphi_m}{\partial H_{ex}} \frac{\partial \psi_p}{\partial E_{ex}} C_{EH} \\
C_{ME,E/M}^{NL} &= \frac{\partial \varphi_m}{\partial E_{ex}} \frac{\partial \psi_p}{\partial E_{ex}} C_{EH} \\
C_{ME,E/E}^{NL} &= \frac{\partial \varphi_m}{\partial E_{ex}} \frac{\partial \psi_p}{\partial E_{ex}} C_{EH}.
\end{align*}
\]

Based on our previous work [6], [23], [24], we assume that the thermal induced internal fluctuations in the ferromagnetic and piezoelectric layers can be considered as the main noise sources. The mechanical loss noise limit is the main noise source for a strain coupled ME composite. An application of Nyquist theorem gives the mechanical noise contribution to the output voltage noise spectral density as:

\[
J_{n,mech}(f) = \frac{\text{Thermal loss factor}}{2\pi f_n C_{EH}} \text{ where the mechanical loss factor is defined by } \tan(\delta_{mech}) = \frac{\tau_1}{\gamma_1}.
\]

The noise transmission can be investigated by supposing that a small low-frequency force is applied on the composite.
By deriving (2) for an excitation field and a small low frequency force, we obtain the transfer functions for the force noise contribution to the sensed current and voltage output as

\[
\frac{\partial^2 U}{\partial H_{ex} \partial F} = \frac{\omega_{ex}}{I} \left( \phi_n \chi_1 + \eta_1^* \right) \phi_n C_{EH}^{mech}
\]

\[
\frac{\partial^2 I}{\partial H_{ex} \partial F} = \frac{\omega_{ex}}{I} \left( \chi_1 + \psi_1 \right) \phi_n \phi_p C_{EH}^{mech}
\]

\[
\frac{\partial^2 U}{\partial E_{ex} \partial F} = \frac{\omega_{ex}}{I} \left( \chi_1 + \tau_1 \right) \phi_n \phi_p C_{EH}^{mech}
\]

\[
\frac{\partial^2 I}{\partial E_{ex} \partial F} = \frac{\omega_{ex}}{I} \left( \chi_1 + \gamma_1 \right) \phi_p C_{EH}^{mech}
\]

Therefore, the output voltage and current noise spectral densities are given by

\[
\begin{align*}
\epsilon_{n_f,M/M} &= \frac{\omega_{ex}}{I} \left( \phi_n \chi_1 + \eta_1^* \right) \phi_n C_{EH}^{mech} H_{ex} f_{n,C_mech} \\
\epsilon_{n_f,M/E} &= \frac{\omega_{ex}}{I} \left( \chi_1 + \tau_1 \right) \phi_n \phi_p C_{EH}^{mech} H_{ex} f_{n,C_mech} \\
\epsilon_{n_f,E/M} &= \frac{\omega_{ex}}{I} \left( \chi_1 + \psi_1 \right) \phi_n \phi_p C_{EH}^{mech} E_{ex} f_{n,C_mech} \\
\epsilon_{n_f,E/E} &= \frac{\omega_{ex}}{I} \left( \chi_1 + \gamma_1 \right) \phi_p C_{EH}^{mech} E_{ex} f_{n,C_mech}
\end{align*}
\]

The equivalent magnetic noise spectral density expressions for the different modulation schemes can be deduced from (6) and (8) in order to evaluate the magnetic detection limits. Taking into account the physical and geometrical parameters of the ME composite, this yields ultimately.
The attenuation and nonlinearity factors, defined in the theoretical part of this paper, can be measured via the amplitude of the modulation signal appearing around the excitation carrier frequency. A general trend of the observed spectrum near the carrier frequency is given in Fig. 3. We noticed that there exists several attenuations in the measurement system as well as in the ME composite itself. These attenuations may result from the demagnetization, the inter-layer mechanical couplings, the electrode contacts, the detection circuit and the excitation (or pick-up) coil loss. The attenuation and nonlinearity factors can be estimated from the spectrum, by measuring the amplitude of the signals located around the excitation carrier frequency and computing with the relevant parameters of the reference and excitation signals (amplitude, frequency, etc.). First, the attenuation factor can be deduced from the ratio $\frac{U_{es}}{U_{es}^0}$, where $U_{es}^0$ is the calculated output voltage amplitude we are expecting for the excitation signal. The second nonlinearity factor is defined as the amplitude ratio of the modulation output signal to the low frequency reference input signal $H$, per excitation output amplitude, written as $\frac{2U_s}{U_{es}H}$. In this ratio, we have multiplied by two in order to standardize the calculations. Thus, the sensitivity model can be constructed by using the coupling parameters, the attenuation factor and the nonlinear factors. The correlation between different detection modes has also been investigated [25]. In these experiments, a strong coherence has been observed between the direct and converse ME modulation modes. However, we did not observe any coherence between the passive and modulation detection methods when they were operated simultaneously. This result confirms that the observed dominant noise source is not due to the passive dielectric loss noise of the sensor.

Table III summarizes the relative nonlinear and attenuation factors for the four modulation modes. The attenuation factors of the magnetic signals for M/M, M/E, E/M and E/E modulations are defined as $Att_{MM}$, $Att_{ME}$, $Att_{EM}$ and $Att_{EE}$, respectively. These factors define the energy losses in the magnetoelectric conversion process as well as the difference between the theoretical and practical environment. Similarly, the corresponding attenuation factors for a mechanical force are given by $Att_{MEM}$, $Att_{MEF}$, $Att_{EFM}$ and $Att_{EEE}$. By assuming that the attenuation depends on the excitation method only, we can show that these relations can be simplified as $Att_{MEM} \approx Att_{ME}$, $Att_{MEF} \approx Att_{ME}$, $Att_{EFM} \approx Att_{EM}$ and $Att_{EEE} \approx Att_{EM}$.

By using the M/M modulation, only the magnetic layers are used for sensing the low frequency magnetic field. The resulting magnetization is sensed along the longitudinal direction. In this excitation method, there are two parameters responding to the applied magnetic field: the magnetic permeability and the magneto-elastic coefficients because the low frequency magnetic field can influence the strain of the sensor. The first effect is due to the 90° domain wall motion and the other results from the 180° domain wall motion in the ferromagnetic layer along the longitudinal direction [26]. For
the magnetization modulation case (M/M), the 180° reversible domain wall motion is the dominant effect for the modulation mechanism. This type of magnetic domain motion does not change the sensor geometry when its magnetic property is induced by an external magnetic field.

The relevant coefficients of the M/M modulation process are illustrated in Table III. An excitation coil (not represented) is connected to a voltage generator to produce a magnetic excitation field corresponding to the applied voltage $U(H_{ex})$ and a pick-up coil recovering the low frequency signals from the magnetization. As detailed in Fig. 3, the output voltage amplitudes $U_{ex}$, $U_1$ and $U_2$ are the responses corresponding to the excitation oscillation, the modulation and the reference signals, respectively. The transfer function and output voltage noise spectral density can be deduced from

$$ T_{R_{MM}} = G_V \times N_m \frac{2 \pi f_{ex}}{\mu \mu_m} \nu_1 \eta_1 \gamma_1 \approx \nu_1 \eta_1 \gamma_1 $$

and

$$ u_{n_{\nu_{1 MM}}} = G_V \times N_m \frac{2 \pi f_{ex}}{l_m} \left( \phi_m \kappa_1 + \eta_1^* \right) \phi_m \gamma_1 \approx \nu_1 \eta_1 \gamma_1 $$

By taking account of the attenuation factor $Att_{MM}$ for the magnetic field transfer function and an attenuation factor $Att_{MEM}$ for the mechanical force.

The equivalent magnetic noise spectral density corresponding to the mechanical noise limit can be expressed by the ratio between the output voltage noise and the transfer function $b_{n_{\nu_{1 MM}}} = \frac{u_{n_{\nu_{1 MM}}}}{T_{R_{MM}}}$. The nonlinear term $\nu_1$ can be calculated by $\nu_1 = H_2 / H = \frac{2 U_2}{U_{ex} H}$ with the measured parameters ($G_V = 1$). A low frequency magnetic field was then applied to investigate such a magnetization modulation for several injection amplitudes. From the measurements, there was a gap of several orders of magnitude between the measurement and the theoretical calculations. We believe that the noise produced by the measurement system is the dominant noise source, exceeding the intrinsic mechanical sensor noise contribution. Thus, the performance of the magnetization modulation can be improved by optimizing the excitation and detection system.

Because of the symmetrical behavior of the magnetic and electric layers in strain-coupled ME composites, the direct and converse ME modulations are theoretically equivalent in sensitivities for low frequency magnetic fields according to previous calculations. The magnetoelastic coupling factor is influenced by the external low frequency magnetic field, via the magnetostrictive coefficient $d_{11,M}$. Also, the mechanical impedance of the composites varies as a function of the external magnetic field resulting from the mechanical stress. However, this effect is not regarded as the dominant one above that of the magnetic-field-induced magnetoelectric impedance change. We notice that the linear transfer function for each modulation mode was measured at first since the parametric modulation is based on the detection of its change. The linear relation and the latter are required to evaluate the relative non-linearity factors.

For the M/E modulation, the magnetic excitation was achieved via the same custom-built modulation coil that was used above for the M/M mode. In this case, the coil was used to apply a relatively high frequency excitation magnetic field along the sensor length. Thus, the magnetic domains rotate and line-up with the external magnetic excitation. In particular, the magnetoelastic domain wall motion changes the deformation of the sensor via Joule and inverse piezomagnetic effects. For sub-resonant excitation frequencies, the Joule effect was dominant with regards to the magnetic induced deformations. This can then be used for the passive detection mode of the ME laminate under a bias magnetic field. This field can shift the working point into a dynamical linear regime. However, at the resonant excitation frequency of the ME composite, the magnetoelastic domains are forced to move synchronously with the external applied magnetic field. Thus, the inverse piezomagnetic effect becomes the dominant effect. Therefore,
a direct ME modulation can then be achieved at its first harmonic frequency without any magnetic bias. In the piezoelectric layer, the induced electric charges are collected across a pair of interdigital electrodes. Kapton films with high resistivity, low electric dissipation loss factor and good thermo/hydro-stability were bonded to the piezoelectric layers.

<table>
<thead>
<tr>
<th>Modulation Mode</th>
<th>Sensitivity</th>
<th>Equivalent magnetic noise</th>
</tr>
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<tbody>
<tr>
<td>M/M</td>
<td><img src="image" alt="Graph" /></td>
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<tr>
<td>M/E</td>
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</tbody>
</table>

Red circles, black points, triangles are the near carrier resonance measurement values, the predicted values (cf. theoretical equations) and the demodulated values, respectively.
to protect these fragile layers from mechanical cracks as well as to incorporate the interdigital electrodes. These electrodes were connected to a classical charge amplifier [27], [28] with a resistance of $R_1 (= 10 \, \text{G} \Omega)$ and a capacitance of $C_1 (= 100 \, \text{pF})$. The basic relation between the input charge $Q_{ex}$ and output voltage $U_{ex}$ is given by $U_{ex} = Q_{ex} / C_1$. With the objective of developing a technique for quantitative measurements of the attenuation, an attenuation factor $Att_{ME}$

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<tr>
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<td><img src="image4" alt="Graph" /></td>
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<td><strong>E/E</strong></td>
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</tbody>
</table>

The black solid and dashed lines are the measurement and predicted responses (based on the model and results given in Table I), respectively.
was defined. This factor can be experimentally confirmed by
the calculated and measured carrier output amplitudes for the
M/E modulation. Moreover, the number of inter-digital
electrodes, $N_p$, should also be considered for calculations. This
number determines the efficiency of the charge detection by
the piezoelectric layer. The nonlinear factor for the magnetic
field can be defined by the ratio of equivalent side-band input
magnetic field to the low frequency magnetic field. This can be
further deduced as a formula of the sideband output signal
amplitude $U_2$, the output carrier amplitude $U_{ex}$ and the
reference magnetic field. Thus, the magnetic nonlinearity
factor was defined as $\eta = \frac{H_2}{H_{ex}} = \frac{2U_2}{U_{ex}H}$, as summarized in

Table III. Considering the number of inter-digital fingers $N_p$
of the electrodes, the attenuation and nonlinear factors, the
transfer function for the low frequency magnetic field and the
output voltage noise density can be given as

$$T_{M/E} = \frac{N_p}{\mu_0 l_p} \eta \phi_0 \phi_p \left( \frac{C^H}{H_{ex} \eta} \right)_{Att_{ME}}$$

and

$$u_{u,f-M/E} = \frac{N_p}{l_p k_1} \left( \kappa + \psi \right) \phi_0 \phi_p \left( \frac{C^H}{H_{ex} f_{a - c_{mech}} \eta} \right)_{Att_{ME}}$$

which induces an attenuation factor $Att_{ME}$ for the magnetic
field transfer function and an attenuation factor $Att_{ME}$ for the
mechanical force.

These attenuation factors define the uncertainty for the
transmission of a low frequency force. The equivalent
magnetic noise spectral density can then similarly be expressed
by the ratio between the output voltage noise and the transfer
function as $h_{u-M/E} = \frac{u_{u,f-M/E}}{T_{M/E}}$. By applying a low reference
field, the sensitivity and noise was investigated as a function of
the amplitude of the excitation field. Table IV shows the
transfer functions, the output voltage noise spectral densities and
the equivalent magnetic noise densities for this low frequency
reference. However, a noise increase can be noticed in Table IV
for higher excitation field. The ratio of the ME
hysteresis loss energy to the total energy determines the noise
level at a given excitation frequency. We believe that the
increase of this ratio results from an excess noise increase.
Table V shows the transfer functions, the output voltage noise
spectral densities and the equivalent magnetic noise densities
as a function of frequency for the low frequency magnetic
reference, after the demodulation process. The transfer
function is nearly constant over the measurement bandwidth
from 0.1 Hz to 100 Hz. We notice that the predicted
mechanical limit is a constant from the dashed lines in
Table V. However, for stronger excitation amplitudes, the
measured noise curves are higher than the predicted ones. This
is due to the growth of the mechanical hysteresis loss. Thus, it
is necessary to choose the optimal excitation amplitude so that
the intrinsic noise of the composite can be discerned from the
noise contribution of the detection electronics.

Presented in Table II is the experimental configuration for
the converse ME modulation or so-called E/M modulation. A
pair of Helmholtz coils generates a reference low frequency
magnetic field along the longitudinal sensing direction of the
ME composite. A voltage generator was then used to produce
an excitation field across the interdigital electrodes in the in-
plane, longitudinal direction. A voltage amplifier with a gain
of $Gv (= 35)$ was used to amplify the low frequency field from
an $N_m$ turns home-made coil. The output voltage corresponding to the low frequency field, the excitation carrier and
the modulation signal are defined respectively as $U_1$, $U_{ex}$
and $U_2$. The transfer function and the output voltage noise
spectral density can be calculated by

$$T_{E/M} = Gv \times N_m \frac{2\pi f_{ex}}{\mu_0 f_m} (2\phi_0 \psi_1) \phi_p \phi_p \left( \frac{C^H}{H_{ex} f_{a - c_{mech}} \eta} \right)_{Att_{EM}}$$

(14)

and

$$u_{u,f-E/M} = Gv \times N_m \frac{2\pi f_{ex}}{f_m} (\kappa + \psi_1) \phi_p \phi_p \left( \frac{C^H}{f_{a - c_{mech}} \eta} \right)_{Att_{EM}}$$

(15)

where an attenuation factor $Att_{EM}$ for the magnetic field
transfer function and an attenuation factor $Att_{EM}$ for the
mechanical force are both induced.

The equivalent magnetic noise spectral density can be
expressed by the ratio between the output voltage noise and
and the transfer function as $h_{u-E/M} = \frac{u_{u,f-E/M}}{T_{E/M}}$. The nonlinear
term $2\phi_p \psi_1$ for the E/M modulation can be calculated by

$$2\phi_p \psi_1 = \frac{H_2}{E_{ex}} = \frac{2U_2}{U_{ex} H}$$

with measured parameters. By using a

2 Hz reference field, the sensitivity and noise were
investigated as a function of the excitation amplitude of the
carrier. Shown in Table IV are the transfer functions, the
output voltage noise spectral densities and the equivalent
magnetic noise spectral densities as a function of amplitude for
a low frequency reference. The values of the transfer functions
are linearly proportional to the amplitude of the excitation
fields. Clearly, the noise contribution from the detection
electronics dominates the total output noise level for low
amplitude excitation signals. However, the loss energy
increased faster than the stored one. This results an increase of
the loss factor for stronger excitations. Table V shows the
transfer functions, the output voltage noise spectral densities and
the equivalent magnetic noise densities as a function of frequency
of the reference field for the E/M modulation. Similarly to the direct ME modulation, a low-pass filter
of 781 Hz serves in the demodulation process for the
synchronism detection.

Table II also illustrates the setup configuration of the
magneto-capacitance modulation for sensing low frequency
magnetic fields. Unlike the direct and converse ME
modulations, the frequency of the magnetostriction was readily
doubled in the ME composite. This is because of the
reversibility of the magnetic domain wall motion for zero
biased magnetic oscillations at low frequencies. The
modulation process occurs in the piezoelectric layers. As known, there exists a part of the electric domain that can be changed by the mechanical strain or stress, which can be regarded as the origin of the stress-dielectric effect. The magnetic field induced electric capacity change, for the case of a magnetoelectric thin film composite, should be thoroughly treated as a strain (stress) induced dielectric effect, as there is no direct response of the electrical capacitance to the external magnetic fields in the ME composite. Thus, the magnetoelastic coupling is important for this detection mode since the variance of the dielectric coefficient is principally influenced by the state of stress resulting in the ferromagnetic phase. A magnetic bias can be applied to the ferromagnetic layer by shifting the working point, so that the magnetic induced strain can be maximized. In our experiments, a magnetic bias was chosen for investigating the sensitivity and noise behavior for magneto-capacitance modulation [29], [30]. This magnetic bias was applied to eliminate the frequency doubling of the reference signal and to enhance the sensitivity. The same charge amplifier as in the M/E modulation was used to amplify the low frequency signal from the generated charges with a resistance and a capacity in parallel. A voltage generator was connected onto the positive input for generating the excitation electric field \( E_{ex} \) across the attached inter-digital electrodes by applying an oscillation voltage \( U(E_{ex}) \). The amplitudes of the output signals were \( U_{ex}, U_2 \) and \( U_1 \) corresponding to the excitation, modulation and reference signals, respectively. The transfer function and the output voltage noise spectral density can then be given by

\[
T_{E/E} = \frac{N_p}{\mu_0 C_1} \gamma_1 \mu_0 C_1 E_{ex} At_{EE} = \frac{C U_{ex}}{\mu_0 C_1} At_{EE} \tag{16}
\]

and

\[
\gamma_1 = \frac{E_2}{U_{ex} H} \frac{2U_2}{U_{ex} H}
\]

where an attenuation factor \( At_{EE} \) for the magnetic field transfer function and an attenuation factor \( At_{EE} \) for the mechanical force are both induced. The equivalent magnetic noise spectral density can be expressed by the ratio between the output voltage noise and the transfer function \( b_{n_{EE}} = \frac{u_{n_{EE}}}{T_{E/E}} \). The nonlinear term \( \gamma_1 \) for the magneto-capacitance modulation was calculated by

\[
\gamma_1 = \frac{E_2}{U_{ex} H}
\]

using measured parameters, where \( E_2 \) is the equivalent electric field for the modulation signal. A low frequency magnetic field was applied on the ME composite to investigate the transfer functions and noise behavior by varying the amplitude of the excitation as shown in Table IV. A gap of several orders of magnitude can be seen in the equivalent magnetic noise spectral density of the corresponding figure in Table V. Therefore, we can conclude that thermal-mechanical fluctuations are not the dominant noise source for the magneto-capacitance modulation, presently. Table V again shows the transfer function, the output voltage noise spectral density and the equivalent magnetic noise spectral density as a function of frequency for the low frequency signals. In general, the sensitivity was dominated by the magneto-elastic coupling and the stress induced piezoelectric coefficient. The investigations of the sensitivity, output voltage noise and the equivalent magnetic noise spectral densities as a function of frequency are given in Table V. A gap between the measured and theoretical curves was also observed as a function of frequency.

| TABLE VI | TRANSFER FUNCTION, OUTPUT VOLTAGE NOISE AND EQUIVALENT MAGNETIC NOISE SYNTHESIS |
|-----------------|-----------------|-----------------|-----------------|-----------------|
|                | M/M             | M/E             | E/M             | E/E             |
| Magnetic transfer function (V/T) | Predicted* | 365 | 66.700 | 1.1 10^6 | 288 |
|                  | Measured       | 267 | 75.000 | 0.66 10^6 | 319 |
| Output voltage noise spectral density (µV/√Hz) | Predicted* | 0.08 | 7.8 | 11.3 | 8.97 10^-3 |
|                  | Measured       | 6.5 | 7 | 42.2 | 1.64 |
| Equivalent magnetic noise spectral density (pT/√Hz) | Predicted* | 220 | 114 | 10 | 3.3 |
|                  | Measured       | 22.600 | 89 | 68.2 | 5.290 |
| Power consumption (mW) | High (~100) | High (~100) | Low (~10) | Low (~10) |
| Magnetic bias for best sensitivity | Unclear | \( \approx 0 \) | \( \approx 0 \) | \( H_{dE} \) |
| Vibration sensitivity | Medium | Weak | Weak | Strong |
| Stability in time | Weak | Strong | Strong | Weak |
The origin of this excess noise is from the detection system. This is experimentally and theoretically confirmed in [31]. The transfer capacity, output voltage noise and equivalent magnetic noise levels are presented in Table VI. Here, the noise sources and noise amplification from the detection electronics were considered as the dominant contributions to the equivalent magnetic noise. To summarize, the used parameters and their definitions are given in the Table VII.

### IV. Conclusion

In summary, the dynamic sensitivity and noise floor of a long type, sandwich-like, push-pull-structured magnetostrictive-piezoelectric composite has been theoretical evaluated and measured. The theoretical model was based on an equivalent circuit model, which was extended to nonlinear modulation techniques. In addition, thermally induced mechanical fluctuations and their contribution to the total
performance of magnetic field sensing has been investigated. The modeling results were adapted to the measured ones. Equivalent magnetic noise levels were measured using either magnetic or electric field excitations with a charge amplifier or a pick-up coil detection system as required by the corresponding modulation methods. Presently, the direct (M/E) and converse magnetoelectric (E/M) modulations are expected to be the intrinsic mechanical loss under a frequency excitation field. Further research will focus on the mechanical noise sources for the magnetization modulation (M/M) and the magneto-capacitance (E/E) modulation. For the other two methods, the sensor sensitivities should be enhanced in order to attain the intrinsic sensor noise. To this end, the noise from the detection process should be further reduced in the future research.

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REFERENCES


