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Combining Face Averageness and Symmetry for 3D-based Gender Classification

Baiqiang Xia, Boulbaba Ben Amor, Hassen Drira, Mohamed Daoudi, and Lahoucine Ballihi.

Abstract

Although human face averageness and symmetry are valuable clues in social perception (such as attractiveness, masculinity/femininity, healthy/sick, etc.), in the literature of facial attribute recognition, little consideration has been given to them. In this work, we propose to study the morphological differences between male and female faces by analyzing the averageness and symmetry of their 3D shapes. In particular, we address the following questions: (i) is there any relationship between gender and face averageness/symmetry? and (ii) if this relationship exists, which specific areas on the face are involved? To this end, we propose first to capture densely both the face shape averageness (AVE) and symmetry (SYM) using our Dense Scalar Field (DSF), which denotes the shooting directions of geodesics between facial shapes. Then, we explore such representations by using classical machine learning techniques, the Feature Selection (FS) methods and Random Forest (RF) classification algorithm. Experiments conducted on the FRGCv2 dataset show a significant relationship exists between gender and facial averageness/symmetry when achieving a classification rate of 93.7% on the 466 earliest scans of subjects (mainly neutral) and 92.4% on the whole

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FRGCv2 dataset (including facial expressions).

Keywords:

3D Face, Gender Classification, Face averageness, Face symmetry, Dense Scalar Field, Feature selection, Random Forest.

1 1. Introduction

Human gender perception is an extremely reliable and fast cognitive pro-2 cess since the face presents a clear sexual dimorphism [1]. In human face 3 analysis using machines [3], automatic gender classification is an active re-4 search area. Developed solutions could be useful in human computer in-5 teraction (intelligent user interface, video games, etc.), visual surveillance, 6 collecting demographic statistics for marketing (audience or consumer pro-7 portion analysis, etc.), and security industry (access control, etc.). Research 8 on automatic gender classification using facial images goes back to the beging ning of the 1990s. Since then, significant progress has been reported in the 10 literature [4, 5, 6, 7, 8]. Fundamentally, proposed techniques differ in (i) the 11 format of facial data (2D still images, 2D videos or 3D scans); (ii) the choice 12 of facial representation, ranging from simple raw 2D pixels or 3D cloud of 13 points to more complex features, such as Haar-like, LBP and AAM in 2D, 14 and shape index, wavelets and facial curves in 3D; and (iii) the classifiers, 15 for instance Neural Networks, SVM, and Boosting methods [4]. 16

17 1.1. Related work on 3D-based gender classification

Statistically, the male and the female faces present different morphological
characteristics in geometrical features, such as in the hairline, the forehead,
the eyebrows, the eyes, the cheeks, the nose, the mouth, the chin, the jaw, the

neck, the skin and the beard regions [13]. Usually, the female brow tends to be 21 more arched than that of the male (which is more horizontal), the noses and 22 chins in male faces are more prominent than those in female faces [27], and 23 men have a more acute nasolabial angle than women [26]. The 3D face scans, 24 which capture the spatial structure of the facial surfaces, allow to capture 25 these differences between male and female faces more easily compared to 2D 26 texture images. Thus, the goal of 3D-based gender classification is to develop 27 a fast and automatic approach which yields high classification performance 28 compared to the 2D-based approaches. 29

In [9], Liu et al. analyze the relationship between facial asymmetry and 30 gender. They impose a 2D grid on each 3D face to represent the face with 31 3D grid points. With the selected symmetry plane, which equally separates 32 the face into right and left halves, the distance difference between each point 33 and its corresponding reflected point is calculated as height differences (HD). 34 In addition, the angle difference between their normal vectors is calculated 35 as orientation differences (OD). The approach based on HD-face achieves 36 91.16% and the approach based on OD-face achieves 96.22%. However, these 37 performances are reported on a private dataset of 111 full 3D neutral face 38 models of 111 subjects, and 3D face manual landmarks are needed. 39

In [12], *Lu et al.* use Support Vector Machine (SVM) to classify ethnicity (Asian and Non-Asian) and gender (Male and Female). A merging of two frontal 3D face databases (UND and MSU databases) is used for the experiments. The best gender classification results using 10-fold cross-validation reported is 91%. However, this approach is based on six landmarks (inside and outside corners of the eyes, the nose tip, and the chin point) manually ⁴⁶ labeled. Moreover, the results are obtained only on neutral faces.

In [15], Wu et al. use 2.5D facial surface normals recovered with Shape From Shading (SFS) from intensity images for gender classification. The best average gender recognition rate reported is 93.6% with both shape and texture considered. However, seven manual landmarks are needed and a small dataset of neutral scans has been used to perform the experiments.

In [16], Hu et al. propose a fusion-based gender classification method 52 from 3D frontal faces. Each 3D face shape is separated into four face regions 53 using face landmarks. With the extracted features from each region, the 54 classification is done using SVM on a subset of the UND dataset and another 55 database captured by themselves. Results show that the upper region of 56 the face contains the highest amount of discriminating gender information. 57 Fusion is applied to the results of four face regions and the best result reported 58 is 94.3%. Their experiments only involve neutral faces. In this study, no 59 attention is given to facial expressions. 60

In [3], Toderici et al. employ MDS (Multi-Dimensional Scaling) and 61 wavelets on 3D face meshes for gender classification. They use the 4007 62 3D scans of the 466 subjects from the FRGCv2 dataset for gender classifi-63 cation. Experiments are carried out subject-independently with no common 64 subject used in the testing stage of 10-fold cross validation. With polynomial 65 kernel SVM, they achieve 93% gender classification rate with the unsuper-66 vised MDS approach, and 94% classification rate with the wavelets-based 67 approach. Both approaches significantly outperform the kNN and kernel-68 kNN approaches. 69

In [17], Ballihi et al. extract facial curves (26 level curves and 40 radial

⁷⁰

curves) from 3D faces for gender classification. The features are extracted 71 from lengths of geodesics between facial curves from a given face to the Male 72 and Female templates computed using the Karcher Mean Algorithm. The 73 Adaboost algorithm is then used to select salient facial curves. They obtained 74 a classification rate of 84.12% with the nearest neighbor classifier when using 75 the 466 earliest scans of the FRGCv2 dataset as the testing set. They also 76 performed a standard 10-fold cross-validation for the 466 earliest scans of 77 FRGCv2, and obtain 86.05% with Adaboost. 78

Compared to [17], in the current paper, we represent mathematically fa-79 cial bilateral symmetry and averageness for gender classification using Dense 80 Scalar Fields. The DSFs denoting the shooting directions for geodesics be-81 tween facial shapes, are both novel and interesting. We view this representa-82 tion for gender classification as the main contribution of this paper. The set 83 of facial deformations is a nonlinear space while the set of Dense Scalar Field 84 (DSF) is a vector space. The only remaining challenge is the large dimen-85 sionality of DSF, which is handled using a feature-selection-based dimension 86 reduction, followed by a Random Forest classifier. In terms of experimental 87 performances, the present approach have achieved higher classification rates 88 compared to [17]. In summary, the novelty of this paper is in represent-89 ing bilateral symmetry and face averageness using DSF and its successful 90 application to the gender classification problem. 91

⁹² 1.2. Methodology and contributions

From the above analysis, existing works on 3D-based gender classification are based on local or global *low-level* feature extraction (see table 2 for a complete summary) followed by classical classification methods. To the best of our knowledge, no work has been done considering *high-level* cues, such as face averageness and bilateral face symmetry, except the study in [9] which investigates the relationship between facial symmetry and gender. Using sparse measures of height differences (HD), and orientation differences (OD) on a defined grid imposed on full 3D face models, their process requires manual landmarks on the face and the experiments are performed on a small dataset. The main contributions of this work are as follows :

- We introduce two *high-level* features, face averageness (AVE) and bilateral face symmetry (SYM), for 3D-based gender classification. These primary facial perception features are rarely considered in the literature of facial attribute recognition.
- We provide an interesting mathematical tool, named *Dense Scalar Field* (DSF) [18], to capture densely and quantitatively the averageness/symmetry differences on the face surface. The DSFs grounding on Riemanniann shape analysis are capable to densely capture the shape differences in 3D faces (such as averageness/symmetry differences).
- We propose a fully-automatic gender classification without any human interaction. We achieve competitive results compared to the approaches in the state-of-the-art on a challenging dataset, FRGCv2. Also, we provide a comprehensive study of the robustness of the proposed approach against age, ethnicity and expression variations.
- An overview of the proposed approach is shown in Figure 1. Firstly, during the first step an algorithm commonly used for facial scans preprocessing is applied. Its includes hole filling, facial part cropping and 3D mesh smoothing



Figure 1: Flow chart of the proposed gender classification approach. There are various pipelines for gender classification. Namely, the pipelines are, (1) the symmetry DSF features (SYM-Original), (2) the selected features of symmetry DSF features (SYM-Selection), (3) the averageness DSF features (AVE-Original), (4) the selected features of averageness DSF features (AVE-Selection), (5) the fusion of symmetry and averageness DSF features by concatenation (FUS-Original), and (6) the selected features of the fusion of symmetry and averageness DSF features of symmetry and averageness DSF features (FUS-Selection).

applied to each scan, together with nose tip detection and pose normaliza-120 tion, as proposed in [17] or [12]. We denote the preprocessed face as S. The 121 plane which equally separates the preprocessed face S into right and left 122 halves is picked up as the middle plane. This plane $P(t, \overrightarrow{n_h})$ passes through 123 the detected nose tip t and has a horizontal normal $\overrightarrow{n_h}$ from the frontal view. 124 Secondly, a DSF extraction step goes after the preprocessing. Here, the pre-125 processed face S is approximated by a collection of radial curves defined over 126 the facial region and stemming from the nose tip. Then, the Dense Scalar 127 *Field* (DSF) features are computed, pair-wisely, to capture the shape dif-128

ferences (averagenesss/symmetry differences) between corresponding radial 129 curves on each indexed point. Thus, we obtain two DSFs for each scan, an 130 averageness DSF and a symmetry DSF. A fusion descriptor is then obtained 13 for each scan by concatenating its averageness DSF and symmetry DSF. 132 Thirdly, after DSF extraction, we investigate the two following classification 133 pipelines. In the first pipeline, Random Forest classifier is applied directly 134 on the obtained feature vectors - averageness DSFs, symmetry DSFs and 135 fusion DSFs. In the second pipeline, we first apply a supervised feature se-136 lection (FS) algorithm on the averageness, symmetry and their fusion DSFs, 13 then the Random Forest (RF) classifier is applied on the selected features for 138 gender classification. 139

This work relates closely to the work previously published in [17], in terms 140 of face representation by an indexed collection of radial curves, which is one 14: of the first steps of our approach's pipeline. However, while this face param-142 eterization is in common, the feature extraction step is completely different. 143 Indeed, in [17], the features are extracted from *lengths of geodesics* be-144 tween facial curves from a given face to the Male and Female templates. In 145 contrast, this work considers the *shooting vectors on the geodesics* be-146 tween facial curves to capture shape differences. The DSFs are computed to 147 describe densely the Symmetry and Averageness of a given face. This allows 148 to compute densely and and locally the facial features on each point of the 149 face. 150

The rest of the paper is organized as follows: in section 2, we highlight our methodology for extracting features that contain 3D facial averageness/symmetry difference; in section 3, we detail the classifier, the feature selection method, and the fusion method for gender classification; experimental results and discussions are presented in section 4 while section 5 concludes
the work.

¹⁵⁷ 2. Feature Extraction Methodology

As mentioned earlier, after the preprocessing, the next step of our approach is to extract densely the averageness and symmetry features from faces. Both of them are based on a Riemannian shape analysis of 3D face.

¹⁶¹ 2.1. Background on Dense Scalar Field Computation

The idea to capture locally and densely face asymmetry and its average-162 ness is to represent facial surface S by a set of parameterized radial curves 163 emanating from the nose tip t. Such an approximation can be seen as a so-164 lution to facial surface parameterization which approximates the local shape 165 information. Then, a Dense Scalar Field (DSF), based on pairwise shape 166 comparison of corresponding curves, is computed along these radial curves 16 on each point. A similar framework has been used in [18] for 4D face ex-168 pression recognition by quantifying deformations across 3D face sequences 169 followed by a classification technique. More formally, a parametrized curve 170 on the face, $\beta : I \to \mathbb{R}^3$, where I = [0, 1], is represented mathematically 17 using the square-root velocity function [19], denoted by q(t), according to: 172 $q(t) = \frac{\dot{\beta}(t)}{\sqrt{\|\dot{\beta}(t)\|}}$. This specific parameterization has the advantage of capturing 173 the shape of the curve and providing simple calculus [19]. 174

Let us define the space of such functions: $C = \{q : I \to \mathbb{R}^3, ||q|| = 1\} \subset \mathbb{L}^2(I, \mathbb{R}^3)$, where $||\cdot||$ implies the \mathbb{L}^2 norm. With the \mathbb{L}^2 metric on its tangent spaces, C becomes a Riemannian manifold. Given two curves q_1 and q_2 , let ψ denote a path on the manifold \mathcal{C} between q_1 and q_2 , $\dot{\psi} \in T_{\psi}(\mathcal{C})$ is a tangent vector field along the path $\psi \in \mathcal{C}$. In our case, as the elements of \mathcal{C} have a unit \mathbb{L}^2 norm, \mathcal{C} is a hypersphere of the Hilbert space $\mathbb{L}^2(I, \mathbb{R}^3)$. The geodesic path ψ^* between any two points $q_1, q_2 \in \mathcal{C}$ is simply given by the minor arc of great circle connecting them on this hypersphere, $\psi^* : [0, 1] \to \mathcal{C}$, given by:

$$\psi^*(\tau) = \frac{1}{\sin(\theta)} \left(\sin((1-\tau)\theta)q_1 + \sin(\theta\tau)q_2 \right)$$
(1)

and $\theta = d_{\mathcal{C}}(q_1, q_2) = \cos^{-1}(\langle q_1, q_2 \rangle)$. We point out that $\sin(\theta) = 0$ if the distance between the two curves is null, in other words $q_1 = q_2$. In this case, for each τ , $\psi^*(\tau) = q_1 = q_2$. The tangent vector field along this geodesic $\dot{\psi}^*: [0, 1] \to T_{\psi}(\mathcal{C})$ is given by (2):

$$\dot{\psi}^* = \frac{d\psi^*}{d\tau} = \frac{-\theta}{\sin(\theta)} \left(\cos((1-\tau)\theta)q_1 - \cos(\theta\tau)q_2\right)$$
(2)

Knowing that on a geodesic, the covariant derivative of its tangent vector field is equal to 0, $\dot{\psi}^*$ is parallel along the geodesic ψ^* and we shall represent it with $\dot{\psi}^*|_{\tau=0}$. This vector $\dot{\psi}^*|_{\tau=0}$ represents the initial velocity of the geodesic path connecting q_1 to q_2 and called also the shooting vector for this geodesic. Accordingly, (2) becomes:

$$\dot{\psi}^*|_{\tau=0} = \frac{\theta}{\sin(\theta)} \left(q_2 - \cos(\theta) q_1 \right) \tag{3}$$

with $\theta \neq 0$. Thus, $\dot{\psi}^*|_{\tau=0}$ is sufficient to represent this vector field; the remaining vectors can be obtained by parallel transport of $\dot{\psi}^*|_{\tau=0}$ along the geodesic ψ^* . with the magnitude of $\dot{\psi}_{\alpha}^*$ at each point, located in curve β_{α}^S with index k, we build a *Dense Scalar Field* (DSF) on the facial surface S, $V_{\alpha}^{k} = |\dot{\psi}_{\alpha}^{*}|_{(\tau=0)}(k)|$. This *Dense Scalar Field* quantifies the shape difference between corresponding curves on each indexed point.

199 2.2. Face symmetry description

The idea of the face symmetry description is to capture the bilateral 200 symmetry difference in the face by DSF. Symmetry difference is defined as 201 the deformation from a face point to its corresponding symmetrical point 202 on the other side of face. In practice, symmetry DSF is calculated on each 203 indexed point of the corresponding symmetrical curves in the preprocessed 204 face **S**. Let β_{α} denote the radial curve that makes an angle α with the 20 middle plane $P_{\mathbf{S}}(t, \overrightarrow{n_h})$ from the frontal view of \mathbf{S} , and $\beta_{2\pi-\alpha}$ denotes the 206 corresponding symmetrical curve that makes an angle $(2\pi - \alpha)$ with $P_{\mathbf{S}}(t, \overrightarrow{n_h})$. 20 The tangent vector field $\dot{\psi_{\alpha}}^*$ that captures the deformation from β_{α} to $\beta_{2\pi-\alpha}$ 208 is then calculated. With the magnitude of $\dot{\psi_{\alpha}}^{*}$ at each point, located in the 209 curve β_{α} with index k, we build a symmetry Dense Scalar Field (symmetry 210 DSF) on the facial surface. 21

This Dense Scalar Field quantifies the shape difference between corre-212 sponding symmetrical curves on each point of the preprocessed face S. Some 213 examples illustrating this symmetry descriptor are shown in Figure 2. For 214 each subject, face in column (a) shows the 2D intensity image; column (b) 215 illustrates the preprocessed 3D face surface S; column (c) illustrates the the 216 3D face S with extracted curves; column (d) shows the symmetry degree as 217 a color-map of the DSF mapped on S. The color bar is shown in the up-218 right corner. The hot colors mean the minimum difference (i.e. maximum 219 symmetry) and cold colors signify the maximum difference (i.e. minimum 220



Figure 2: Illustrations of the symmetry DSFs on faces. (a) 2D intensity image; (b) preprocessed 3D face S; (c) 3D face S with extracted curves; (d) color-map of symmetry DSF mapped on S with three poses. While the cold colors reflect lower symmetrical regions, the warm colors represent higher symmetrical parts of the face.

symmetry). The hotter the color, the higher is magnitude of the bilateral symmetry. In this work, the symmetry DSFs are generated with 200 radial curves extracted from each face and 100 indexed points on each curve. Thus, the size of each DSF is 20000. The average time consumed for extracting all 200 curves for each face is 1.048 seconds, and for generating the bilateral symmetry descriptor (symmetry DSF) on all the 200 \times 100 points of each face is 0.058 seconds. The average preprocessing time consumed for each



Figure 3: The averageness face template is defined as the middle point of the geodesic path between two representative faces randomly taken from the male and female classes in the FRGCv2 dataset.

scan is 0.116 seconds. The total computation time (including preprocessing)
for each scan is less than 1.25 seconds. All our programs are developed in
C++ and executed on Intel Core i5 CPU 2.53 GHZ with 4Go of RAM.

231 2.3. Face averageness description

As mentioned earlier, generally, male faces have more prominent features (forehead, eyebrows, nose, mouth, etc.) in comparison with female faces. Here, our aim is to capture the morphologcial sexual differences between male and female faces by comparing their shape differences to a defined face template. We assume that such differences change with the face gender. Thanks to DSF, presented in subsection 2.1, we are able to capture densely such shape differences as long as a face template is defined.

As shown in Figure 3, the face template is defined as the middle point of the geodesic path which connects a male face (*ID: 02463d548; Age: 48; White*) to a female face (*ID: 04200d74; Age: 21; White*) taken from the FRGCv2 dataset. With the two faces represented by collections of radial curves, we compute pair-wisely the geodesic path between corresponding curves using equation (1). By interpolation, we have the middle point of the geodesic which we take as the face template T.

For a preprocessed face \boldsymbol{S} , let $\beta_{\alpha}^{\boldsymbol{S}}$ denote the radial curve that makes 246 an angle α with the middle plane $P_{\mathbf{S}}(t, \overrightarrow{n_h})$ from the frontal view of \mathbf{S} , and 247 β_{α}^{T} denotes the curve that makes the same angle α with $P_{T}(t, \overrightarrow{n_{h}})$ in the 248 averageness face template \boldsymbol{T} . The tangent vector field $\dot{\psi}_{\alpha}^{*}$ that represents the 249 projection of the deformation between the given face and the template face, 250 in the tangent space associated with the template face, is then calculated on 25 each point. Similar to the symmetry descriptor, with the magnitude of $\dot{\psi}_{\alpha}^{*}$ at 252 each point, located in curve β_{α}^{S} with index k, we build an averageness Dense 253 Scalar Field (averageness DSF) on the facial surface, $V_{\alpha}^{k} = |\dot{\psi}_{\alpha}^{*}|_{(\tau=0)}(k)|$. This 254 Dense Scalar Field quantifies the shape difference between corresponding 255 curves of S and T on each indexed point. 256

Figure 4 shows this averageness descriptor. For each subject, the face in 25 column (a) shows the 2D intensity image; column (b) illustrates the prepro-258 cessed 3D face surface S; column (c) shows the 3D face S with extracted 259 curves; column (d) shows color-map of the Averageness DSF mapped on S260 with three poses. The hot colors mean the minimum difference (i.e. maxi-261 mum averageness) and cold colors signify the maximum difference (i.e. min-262 imum averageness). The hotter the color, the higher is the magnitude of the 263 averageness. 264

²⁶⁵ 3. Gender classification

In this work, face averageness and symmetry are different types of information in the 3D facial shapes. Each of them provides a perspective (maybe



Figure 4: Illustrations of the averageness DSFs on faces. (a) 2D intensity image; (b) preprocessed 3D face surface S; (c) the 3D face S with extracted curves; (d) color-map of the Averageness DSF mapped on S with three poses. While the cold colors reflect lower averageness, the warm colors represent higher averageness on the face.

correlated perspectives) in face perception. Thus, we first study individually their relationship with gender, then we combine them to find out if it enhances the gender classification results, which means that they contribute to gender classification in different ways. In practice, we use an *early fusion method* which consist in concatenating the *averageness DSF* and *symmetry DSF* features of each scan, to form the *fusion DSF* description. Then, we explore the performance of the Random Forest algorithm with the *avera*- *geness DSF*, the *symmetry DSF* and the *fusion DSF* in different scenarios, in combination of Feature Selection methods. It has been demonstrated by *Perez et al.* in [29], that different types of information (such as gray scale intensity, range image and LBP texture) contributes to face based gender classification differently, and the fusion of multi-information yields a better classification performance.

281 3.1. Feature Selection

The size of the features is another important characteristic of the ap-282 proach. As pointed out by Bekios-Calfa et al. in [28], in limited computa-283 tional resource contexts, such as the mobiles, the development of resource-284 limited algorithms is important for applications of computer vision and pat-285 tern recognition. In their work, they make use of LDA techniques to reduce 286 feature size. In our work, we use feature selection methods to select a much 28 smaller set of the features to reduce the computational cost. Compared with 288 LDA techniques, feature selection methods do not tranferm the meaning and 289 values of feature, thus they allow to track back to the corresponding point 290 on the face. 29

Feature subset selection is the process of identifying and removing as 292 much irrelevant and redundant information as possible [22]. It is a central 293 problem in machine learning. The earliest approaches for feature selection 294 were *the filter* methods. These algorithms use heuristics based on general 295 characteristics of the data to evaluate the merit of feature subsets. Another 296 school of approaches argues that the bias of a particular induction algorithm 297 should be taken into account when selecting features. This method, called 298 the wrapper [23], uses an induction algorithm along with a statistical re-299

sampling technique such as cross-validation to estimate the final accuracy of 300 feature subsets. The filter methods operate independently of any learning 30 algorithm. The undesirable features are filtered out of the data before the 302 learning begins. They are generally much faster than wrapper methods, es-303 pecially on data of high dimensionality. Since the averageness, symmetry and 304 fusion DSFs are really dense and possibly redundant after DSF extraction, we 305 use a feature selection procedure on the DSFs to get rid of the irrelevant and 306 redundant features. For the merits of filter methods, we chose a filter, named 30 Correlation-based-Feature-Selection (CFS) [22]. It is an algorithm that cou-308 ples the evaluation formula based on an appropriate correlation measure and 309 a heuristic search strategy. The central hypothesis of CFS is that good fea-310 ture sets should contain features that are highly correlated with the class, 311 yet uncorrelated with each other. The feature evaluation formula (Pearsons 312 correlation coefficient), based on ideas from test theory, provides an opera-313 tional definition of this hypothesis. Within CFS, we try two heuristic search 314 strategies, the Best-First search strategy and the Greedy-Step-Wise search 315 strategy. The Best-First search strategy [24] is an AI search strategy that al-316 lows back-tracking along the search path. It moves through the search space 317 by greedy hill-climbing augmented with a back-tracking facility. When the 318 path being explored becomes non-improving, the Best-First search will back-319 track to a more promising previous subset and continue the search from there. 320 The stopping criterion is the number of consecutive non-improving nodes (5) 32 in our experiments) that result in no improvement. For Greedy-Step-Wise, it 322 performs a greedy forward or backward search through the space of attribute 323 subsets. It stops when the addition/deletion of any remaining attributes 324



³²⁵ results in a decrease in evaluation.

Figure 5: Feature selection. (a) selected points of symmetry DSF in the face; (b) color-map of original symmetry DSF; (c) selected points of averageness DSF in the face; (d) color-map of original averageness DSF; (e) selected points of both averageness DSF and symmetry DSF in face.

After Feature selection, we retain 301 salient points for averageness DSF, 326 271 salient points for symmetry DSF, and 365 salient points for the fusion. 327 The feature selection procedure significantly reduces the size and complexity 328 of original DSF description. Figure 5 shows the selected features of aver-329 ageness DSF and symmetry DSF in faces. Column (a) maps the selected 330 features of symmetry DSF in the face; Column (b) shows the color-map of 331 original symmetry DSF on the face; Column (c) maps the selected points 332 of averageness DSF in the face; Column (d) shows the original averageness 333 DSF on the face; Column (e) maps the selected points of both averageness 334 DSF and symmetry DSF in the face. For both averageness DSF and sym-335

metry DSF, we observe dense distribution of salient points around the nose
and eyes regions. More salient points exist in forehead regions in averageness DSF, and more salient points exist in cheek regions in symmetry DSF.
These observations show that averageness DSF and symmetry DSF share
both similarities and differences. In other words, they are complementary in
face description.

342 3.2. Gender classification based on Random Forest

Face-based gender classification is a binary classification problem which 343 estimates the gender c of a given test face into Male or Female $\mathbf{c} \in \{Male, Female\}$. 344 We carry out gender classification experiments with the well-known machine 345 learning algorithm, Random Forest. Random Forest is an ensemble learning 346 method that grows many classification trees $t \in \{t_1, .., t_T\}$ [25]. To classify a 34 new face from an input vector (DSF-based feature vector $v = V_{\alpha}^{k}$), each tree 348 gives a classification result and the forest chooses the classification having 349 the most votes. In the growing of each tree, firstly, N instances are sampled 350 randomly with replacement from the original data, to make the training set. 35 Then, if each instance comprises of M input variables, a constant number m352 (m < < M) is specified. At each node of the tree, m variables are randomly 353 selected out of the M and the best split on these m variables is used to split 354 the node. The process goes on until the tree grows to the largest possible 355 extent, without pruning. 356

The performance of the forest depends on the correlation between any two trees, and the strength of each individual tree. The forest error rate increases when the correlation decreases, or the strength increases. Reducing m reduces both the correlation and the strength. Increasing it increases both. Thus, an optimal m is needed for the trade-off between the correlation and the strength. In Random Forest, the optimal value of m is found by using the oob-error rate (out-of-bag-error rate). It is reported that face classification by Random Forest achieves a lower error rate than some popular classifiers, including SVM [20]. As far as we know, there is no reported work in the literature of face-based gender classification using Random Forest.

367 4. Experiments

The FRGCv2 database was collected by researchers from the University 368 of Notre Dame [21] and contains 4007 3D face scans of 466 subjects with 369 differences in gender, ethnicity, age and expression. For gender, there are 370 1848 scans of 203 female subjects and 2159 scans of 265 male subjects. The 37 ages of subjects range from 18 to 70, with 92.5% in the 18 - 30 age group. 372 When considering ethnicity, there are 2554 scans of 319 White subjects, 373 1121 scans of 99 Asian subjects, 78 scans of 12 Asian-southern subjects, 16 374 scans of 1 Asian and Middle-east subject, 28 scans of 6 Black-or-African 375 American subjects, 113 scans of 13 Hispanic subjects, and 97 scans of 16 376 subjects subjects whose ethnicity are unknown. About 60% of the faces have 377 a neutral expression, and the others show expressions of disgust, happiness, 378 sadness and surprise. All the scans in FRGCv2 are near-frontal. With this 379 dataset, we conducted two experiments. The first one is to examine the 380 robustness of our approach to age and ethnicity variations. It uses the 466 38: earliest scan of each subject in FRGCv2, of which more than 93% are neutral-382 frontal. The second one extends to examine the robustness of our approach 383 to variations of expression. It considers all the 4007 scans in FRGCv2, about 384

³⁸⁵ 40% of which are expressive faces. For these experiments, the results are ³⁸⁶ generated in a subject-independent fashion, using a 10-fold cross-validation ³⁸⁷ setup.

388 4.1. Data preprocessing

The 3D face models present some imperfections, such as the holes (caused 389 by the absorption of the laser in the dark areas like eyebrows and eyes and 390 by the self-occlusions), the hair, and the spikes (caused by acquisition noise). 39: Thus, a preprocessing step is needed to limit their influence. Firstly, through 392 boundary detection, link-up and triangulation, holes are filled in each scan. 393 Secondly, since the scans in FRGCv2 are all near-frontal, the nose tip is de-394 tected with a simple algorithm. The nose tip is detected by analyzing the 395 peak point of the face scan in the depth direction. Then, the mesh is cropped 396 with a sphere centered at the nose tip to discard the hair and the neck re-39 gions. Finally, a smoothing filter is used to distribute evenly the 3D vertices 398 which capture the original 3D shape. We next perform the well-known Iter-399 ative Closest Point (ICP) algorithm to normalize the poses of the obtained 400 meshes according to a reference mesh (frontal). The symmetry plane is then 40 picked up as the plane that has as origin the nose tip and has an horizontal 402 normal. In practice, the preprocessing step is performed automatically on 403 the whole FRGCv2 dataset without any manual intervention. We obtained 404 4005 well preprocessed scans after preprocessing. The failed two scans (with 405 scan id 04629d148 and 04815d208) were resulted from wrong nose tip detec-406 tion. Considering the ratio of failure is rather tiny (2/4007 < 0.0005), we omit 407 the influence of the two failed scans for the results generation. 408



Figure 6: The reported results of the proposed methods¹ using Random Forest with different number of trees.

409 4.2. Robustness to variations of age and ethnicity

Among the 466 earliest scans, 431 scans are neutral-frontal and 35 are 410 expressive-frontal. In our 10-fold cross validation setup, the 466 scans are 411 randomly partitioned into 10 folds with each fold containing 46 - 47 scans. 412 In each round, 9 of the 10 folds are used for training while the remaining 413 fold is used for testing. The average recognition rate and standard devia-414 tion for 10 rounds then give a statistically significant performance measure. 415 The relationship between the gender classification result and the number of 416 trees used in the Random Forest is depicted in Figure 6(a). It demonstrates 417 that a significant relationship exists between gender and facial averageness 418 and facial symmetry considered separately. We note also that both the fu-419 sion and the feature selection improve the gender classification results. In 420 fact, the fusion descriptor outperforms individual averageness and symmetry 421 descriptor. This implies that facial averageness and symmetry relate to gen-422 der in different ways. At the same time, results after the feature selection 423 always override the results without feature selection. This means that the 424 original averageness DSF and symmetry DSF contain redundant information. 425 Gender-related features are distributed unequally in the facial regions. The 426 best gender classification rate is 93.78%, achieved by 80-Tree Random Forest 427 with the fusion descriptor after feature selection. This result is detailed in 428 the confusion matrix in Table 1. The recognition rate for females (92.02%) is 429

¹Methods as described in Figure 1 : (1) the symmetry DSF features (SYM-Original), (2) the selected features of symmetry DSF features (SYM-Selection), (3) the averageness DSF features (AVE-Original), (4) the selected features of averageness DSF features (AVE-Selection), (5) the fusion of symmetry and averageness DSF features by concatenation (FUS-Original), and (6) the selected features of the fusion of symmetry and averageness DSF features (FUS-Selection).

slightly lower than for male ones (95.44%). It is probably due to the fact that
more male faces were used for training. We also performed a 10-fold 100repetition experiment with Random Forest under the same setting, which
resulted at an average classification rate of 92.84% with a standard deviation
of 3.58%.

 Table 1: Confusion matrix of RF-based classification.

| % | Female | Male | | | | |
|--|--------|-------|--|--|--|--|
| Female | 91.63 | 8.37 | | | | |
| Male | 4.56 | 95.44 | | | | |
| $\hline Recognition Rate = 93.78 \pm 4.29\%$ | | | | | | |



Figure 7: DSFs on faces with different Age.



Figure 8: DSFs on faces with different Ethnicity.

Figure 7 illustrates the color-maps of symmetry DSF and averageness 435 DSF on female faces with age differences and Figure 8 illustrates the color-436 maps of symmetry DSF and averageness DSF on male faces with differences 437 in ethnicity. The information related to age, ethnicity and identity of scans 438 are presented in the 2D images in the upper row of each figure. Based on 439 the middle rows of Figure 7 and Figure 8, we can observe that the bilateral 440 symmetry of both genders convey a visually symmetrical pattern, where the 441 color-map of left-face is globally in symmetry with the right-face, although 442 subtle local asymmetry exists. Low-level deformations (red color) are usually 443 located near the middle plane and high-level deformations (yellow and green 444 colors) happen more frequently in further areas. The asymmetry, in female 445 faces, change obviously more smoothly than in male faces. On the other 446

hand, with the lower rows of Figure 7 and Figure 8, we observe that female faces exhibit more deformations in mouth, nose and eye regions to deform from the averageness face template. More subtly, in cheek and forehead regions, the color is more consistent in male faces. All of these observations above stay relatively consistent with changes of age and ethnicity. We believe that these common patterns contribute to the robustness of our approach to variations of age and ethnicity to some extent.



Figure 9: Gender classification results of different age group (the blue bars show the average recognition rate of each age group, and the red line shows the number of scans in this age group).

As it is well known that face perception is strongly affected by age [30], we provide Figure 9 to analyze gender classification performance for different age groups. In this figure, the blue bars show the average recognition rate for each age group, and the red line shows the number of scans in the same age group. We could confirm that gender classification is strongly influenced by the age. Generally, although the gender classification results decrease from above 90% to about 80% when increasing the age, all these results are near or ⁴⁶¹ above 80%. That is to say the performance of our approach stays relatively
⁴⁶² high with age variation. Moreover, due to unbalanced age distribution of
⁴⁶³ scans in FRGCv2 dataset, we see the number of scans decreased significantly
⁴⁶⁴ when the age is increased. We assume that this is also a reason for the
⁴⁶⁵ decrease of the gender classification results.



Figure 10: Gender classification results of different ethnicity group (the blue bars show the average recognition rate of each age group, and the red line shows the number of scans in this ethnic group).

Figure 10 analyzes the relationship between the obtained classification rate when varying the ethnicity. Here, the whole FRGCv2 dataset is separated into Asian and Non-Asian groups. We can see that the gender classification rates, shown by the blue bars, stay above 90% when varying the ethnicity. The classification rate of Non-Asian group is 3 - 4 percent higher than that of the Asian group. This is probably due to a more sufficient training step has been involved with Non-Asian group, since it contains more than two times of the number of the scans of the Asian group, as shown in thefigure by the red line.

475 4.3. Robustness to expression variations

In this experiment, with all the preprocessed scans of FRGCv2, we first 476 performed the DSF extraction for averageness, symmetry and fusion descrip-477 tors, and then did the 10-fold subject-independent cross-validation with Ran-478 dom Forest. For each round, the scans of 46 subjects are randomly selected 479 for testing, and the scans of the remaining subjects are dedicated to the 480 training. For all the 10 rounds of experiments, no common subjects are used 481 in training/testing. The relationship between the classification result and 482 the number of trees used in Random Forest is shown in Figure 6(b). We note 483 again that both fusion and feature selection improve the results. The best 484 result achieved with the fusion and feature selection is $92.46\% \pm 4.79$ with 485 100-Tree Random Forest. We argue this result by the fact that the majority 486 of the selected features are located on the facial areas which are less affected 487 by the expressions in particular the nose, the eyebrows, and the forehead as 488 illustrated in Figure 5. Considering the FRGCv2 dataset is a challenging 489 dataset which contains as many as 4007 scans with various changes in age, 490 ethnicity and expression, we claim even more confident that a significant re-491 lationship exists between gender and 3D facial averageness/symmetry, and 492 our method is effective and robust to ethnicity and expression variations. 493



Figure 11: DSFs on faces with different expressions.

Figure 11 shows color-maps of DSFs generated for a subject with differ-494 ent expressions. Similar to the observations in Figure 7 and Figure 8, we 495 perceive again in the middle row of Figure 11 that the symmetry deforma-496 tions on both sides of the face are globally in symmetry, although tiny local 497 asymmetry exists in areas like eye corners and lips. Low-level deformations 498 (red) always locate near the middle plane and high-level deformations (yel-499 low and green) occur more frequently in farther areas. With the lower rows 500 of Figure 7 and Figure 11, we observe again that female faces require more 501 deformation in mouth, nose and eye regions to deform from the averageness 502 face template. In cheek and forehead regions, the color is more consistent in 503 male faces. All these visible patterns do not change significantly with expres-504 sion variations. We assume that these patterns contribute to the robustness 505

of our approach to expression changes. Figure 6(c) shows the best gender recognition results (shown as bars) and their standard deviation (shown as black lines) in our experiment. It shows that the gender recognition rate increases with both fusion and feature selection, and the performances of all the approaches change little between the 466 earliest scans protocol and the whole FRGCv2 dataset protocol. It means our approach is even relatively robust to the size of the training set.



Figure 12: Gender classification results of different expression group (the blue bars show the average recognition rate of each age group, and the red line shows the number of scans in this expression group).

Again, in Figure 12, we illustrate the effects of expression variations on the proposed approach. We separated the FRGCv2 dataset into Open-mouth and Closed-mouth groups. Despite the fact of the unbalanced number of training scans in Open-mouth and Closed-mouth groups, as shown by the red line, the results shown by the blue bars in the figure are all above 90%, and the results between these two groups are comparable with each other.

519 4.4. Comparison with state of the art

Table 2 gives a comparison of this work with previous studies in 3D-based 520 gender classification. With differences in the dataset, landmarking, exper-521 iment settings and so on, it is difficult to compare and rank these works 522 simply according to the result values. Compared with our work, works in [9], 523 [14], [15] are based on relatively smaller dataset which leave doubts about the 524 statistical significance of their performances on larger and more challenging 525 datasets. Works in [9], [12], [14], [15] require manual landmarking, thus they 526 are not fully-automatic. Works in [9], [14], [15], [16] use different experi-52 mental settings other than the most prevailing 10-fold cross-validation. Our 528 work addressed gender classification in a fully automatic way without man-529 ual landmarking. Experimented on a large dataset, FRGCv2, which contains 530 challenging variations in expression, age and ethnicity, and reached competi-53 tive results with literature. The nearest works to ours are done by *Ballihi et* 532 al. in [17] and Toderici et al. in [3]. With the 466 Earliest scans of FRGCv2 533 and standard 10-fold cross-validation, Ballihi et al. achieved 86.05% classifi-534 cation rate, while we achieved a much higher result of 93.78% by combining 535 facial shape averageness and bilateral asymmetry. In [3], Toderici et al. also 536 performed automatic 10-fold cross-validation on the FRGCv2 dataset in a 537 subject-independent fashion. In general, we have achieved comparable re-538 sults than them. They achieve about 1% higher gender classification rate 539 than us. While we achieve a lower standard deviation which signifies better 540 stability of the algorithm than theirs². 54

²During the work, we found 8 scans of a subject (id 04662, female indeed) had been mislabeled as male in the FRGCv2 metadata. We corrected them before the experiments.

| Reference | Dataset | Auto | Features | Classifiers | Experiment | Results | Shape/ |
|-----------------|------------------|------|---------------|--------------|-----------------|-----------------------|---------|
| | | | | | settings | | Texture |
| Ballihi et | 466 earli- | Yes | facial curves | A daboost | 10-fold cross- | 86.05% | Shape |
| al. $[17]$ | $est\ scans\ of$ | | | | validation | | |
| | FRGCv2 | | | | | | |
| Toderici | All scans of | Yes | Wavelets | Polynomial- | 10-fold cross- | Male : $94 \pm 5\%$ | Shape |
| et al. [3] | FRGCv2 | | | SVM | validation | Female : $93 \pm 4\%$ | - |
| Hu et al. | 729 UND | Yes | Curvature | RBF-SVM | 5-fold cross- | 94.03% | Shape |
| [16] | scans and | | based shape | | validation | | - |
| 2 5 | 216 private | | index | | | | |
| | scans | | | | | | |
| Han et al. | 61 3D scans | No | Geometry | RBF-SVM | 5-fold cross- | $82.56 \pm 0.92\%$ | Shape |
| [14] | $in \ GavabDB$ | | Features | | validation | | - |
| Wu et al. | Needle maps | No | PGA features | Posterior | 200 train/60 | $93.6 \pm 4\%$ | Shape+ |
| [15] | of 260 sub- | | • | Probability | test, 6 repeti- | | Texture |
| | jects from | | | | tions | | |
| | UND | | | | | | |
| $Lu \ et \ al.$ | 1240 scans | No | Grid element | Posterior | 10-fold cross- | $91 \pm 3\%$ | Shape + |
| [12] | from UND | | values | Probability | validation | | Texture |
| | and MSU | | | | | | |
| Liu et al. | 111 full 3D | No | Variance Ra- | linear clas- | half train/ | $HD:91.16 \pm 3.15\%$ | Shape |
| [9] | scans of 111 | | tio in HD and | sifier | half test, 100 | $OD:96.22 \pm 2.30\%$ | |
| | subjects | | OD faces | | repetitions | | |
| Our | 466 earli- | Yes | AVE+SYM | Random | 10-fold cross- | $93.78 \pm 4.29\%$ | Shape |
| $work^1$ | est $scans$ of | | DSFs | Forest | validation | | _ |
| | FRGCv2 | | | | | | |
| Our | $All\ scans\ of$ | Yes | AVE+SYM | Random | 10-fold cross- | $92.46 \pm 3.58\%$ | Shape |
| $work^2$ | FRGCv2 | | DSFs | Forest | validation | | |

Table 2: Comparison of our approach to earlier studies.

542 5. Conclusion

In this paper, we have proposed a fully automatic approach based on 3D 543 facial averageness/symmetry differences for gender classification. We have 544 proposed to use our Dense Scalar Fields grounding on Riemannian Geom-545 etry to capture densely facial averageness and its bilateral symmetry. The 546 remaining challenge is the large dimensionality of the DSFs, which is handled 54 using a feature-selection-based dimension reduction, followed by a Random 548 Forest classifier. Despite the wide range of age, ethnicity and facial ex-549 pressions, our method achieves a gender classification result of $93.78\% \pm$ 550 4.29% with 466 earliest scans of subjects, and 92.46% \pm 3.58 on the whole 551

FRGCv2 dataset. We have also demonstrated that a significant relationship exists between the gender and these two high-level cues in face perception, the face averageness and symmetry. Our approach is competitive with stateof-the-art approaches. One of the limitations of the proposed approach is the dependence on near-frontal pose of faces to compute the symmetry and the averageness DSFs.

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