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Current understanding of the growth of carbon nanotubes in catalytic chemical vapour deposition

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Abstract

Due to its higher degree of control and its scalability, catalytic chemical vapour deposition is now the prevailing synthesis method of carbon nanotubes. Catalytic chemical vapour deposition implies the catalytic conversion of a gaseous precursor into a solid material at the surface of reactive particles or of a continuous catalyst film acting as a template for the growing material. Significant progress has been made in the field of nanotube synthesis by this method although nanotube samples still generally suffer from a lack of structural control. This illustrates the fact that numerous aspects of the growth mechanism remain ill-understood. The first part of this review is dedicated to a summary of the general background useful for beginners in the field. This background relates to the carbon precursors, the catalyst nanoparticles, their interaction with carbonaceous compounds and their environment. The second part provides an updated review of the influence of the synthesis parameters on the features of nanotube samples: diameters, chirality, metal/semiconductor ratio, length, defect density and catalyst yield. The third part is devoted to important and still open questions, such as the mechanism of nanotube nucleation and the chiral selectivity, and to the hypotheses currently proposed to answer them.

1. Introduction

The last two decades have seen a burst of synthetic nanomaterials stimulated by the prediction of novel properties stemming from their nanoscale dimensions. Among them, carbon nanotubes (CNTs) are particularly attractive nano-objects notably because of the strong influence of their structural features on their electrical and optical properties. However, controlling these structural features soon appeared to be a particularly challenging task. Various synthesis approaches, such as arc discharge and laser ablation, were developed aiming at producing pure and well-controlled CNT samples in large quantity. Due to its
higher degree of control and its scalability, Catalytic Chemical Vapour Deposition (CCVD) is now the standard synthesis method of CNTs. CCVD is at the crossing of two important chemical methods: thin-film growth by Chemical Vapour Deposition (CVD) and chemical conversion by Gas-Solid Heterogeneous Catalysis (GSHC). CCVD consists in the catalytic conversion of a gaseous precursor into a solid material at the surface of catalyst particles or of a continuous catalyst film. Novel aspects specific to CCVD arise from the combination of CVD and GSHC. For instance, the template effect of the catalyst surface on the shape of the growing material is central in CCVD: in the case of catalyst nanoparticles, one-dimensional objects such as CNTs and semiconducting nanowires can be grown; if the catalyst is in the form of a continuous film, two-dimensional materials such as graphene can be prepared. Compared with GSHC, the catalyst in CCVD is not only in contact with the gas phase (and sometimes a support), but presents an additional interface with the growing material. This imposes a supplementary difficulty because both interfaces have to be preserved in order to continuously grow nanotubes/nanowires without disrupting the gaseous precursor supply.

Since the first reports of the catalytic formation of nanotubular carbon filaments in the 1950s [1,2] and 1970s [3-7] and the seminal papers of Sumio Iijima in the early 1990s [8,9], significant progress has been made in terms of synthesis yield, nanotube alignment and sample purity. However, CCVD-grown synthesis of nanotubes still generally suffers from a lack of structural control over the nanotube chirality, the semiconducting/metallic ratio, and the nature and density of defects, highlighting that numerous aspects of the growth mechanism remain ill-understood. The scope of this paper is to present a review of the current understanding of the growth mechanism of CNTs by CCVD. There have been previous reviews in this field [10-16], with different objectives (e.g. chronological description of the evolution of the methods and achievements, focus on simulation works, on the role of the catalyst particles or on a particular type of CCVD such as plasma-enhanced). Compared with
them, the present review primarily focuses on the fundamental aspects of the CNT growth by CCVD. It first aims at summarizing background knowledge derived from neighbouring fields and that is relevant to the understanding of CNT growth by CCVD. The first tutorial part is therefore primarily aimed at beginners in the field. Beginners may also rapidly realize the difficulty arising from the huge number of publications in the field and the variety of studied systems. The second part of this review aims at providing a synthesis of the most relevant works addressing the experimental dependence of CNT features on CCVD conditions. Finally, the third part is devoted to describe important questions that are still open and discuss the hypotheses proposed to account for these experimental dependences and that currently participates to the building of a general growth mechanism of CNTs in CCVD.

2. Background knowledge

The simplest system to grow CNTs by CCVD consists of catalyst nanoparticles brought to high temperature in presence of gaseous carbon-containing molecules. The nanoparticles are commonly made of a transition metal such as Fe, Ni or Co, but other elements and compounds have recently proven to be efficient catalyst as well. In many cases, the catalyst particles are deposited on a support material such as SiO$_2$ or Al$_2$O$_3$. It is apparent from the beginning that the size and shape of the catalyst particle and its interactions with the other components of the system play central roles in CCVD. Generally speaking, it is commonly accepted that CCVD catalyst particles should fulfil the following functions [10-13].

1) Catalyze the dissociation of the gaseous carbon-containing molecules.

2) Allow diffusion of carbon intermediates and their chemical interaction.

3) Provide a nanoscale template for the nucleation and growth of a nanotube.

4) Keep a reactive nanotube rim.
Functions 1 and 2 are also found in heterogeneous catalysis and justify the use of the term catalyst particle, i.e. a particle that helps in rapidly achieving the chemical equilibrium between the carbon-containing molecules and a graphene-type material. Functions 3 and 4 are unique to CCVD catalysts and impose additional or somehow different constraints compared with GSHC catalysts, which justifies the use of the alternative term seed particle.

In this chapter, we aim at providing some background knowledge useful for understanding the catalytic growth of CNTs. This knowledge is mostly derived from chemical vapour deposition, heterogeneous catalysis and metallurgy. The chapter is divided in five parts: i) nature of the most common carbon precursors used for CNT growth and their chemical reactivity, ii) nature of the nanoparticles used to grow CNTs in CCVD and influence of their nanometric size on some of their physical properties, iii) interactions of transition metals with carbon, iv) catalytic activity of transition metals, v) interactions of transition metal nanoparticles with the environment (reactive atmosphere, oxide support).

2.1. Carbon precursors

2.1.1 Chemical nature

A large number of carbon-containing molecules can be used as a carbon source to grow CNTs in CCVD: hydrocarbons (gaseous [17] or liquid [18]), alcohols [19], aromatic compounds [20] or even naturally-occurring carbon resources [20]. Ethylene, acetylene, methane, carbon monoxide and ethanol are presently the most frequent precursors of CNTs in CCVD (Figure 1). It is important to keep in mind that such gaseous carbon precursors not only bear carbon but also other elements such as hydrogen and/or oxygen. These elements are not compulsory since CNTs can be grown from pure carbon [21,22] as commonly achieved in arc discharge and laser ablation syntheses by sublimation of graphite [23]. However, the by-production of hydrogen- and oxygen-bearing molecules such as H$_2$ and H$_2$O may impact the
formation of CNTs. H₂ and H₂O are actually common additives in CCVD with recognized influence on CNT growth as discussed hereafter. Nitrogen- [24], phosphorus- [25] and boron-bearing [26] precursors are known to form substitutionally doped CNTs. However, the influence of oxygen and hydrogen on the defects of CCVD-grown CNTs is still poorly known.

Figure 1. Common carbon precursors of CNTs in CCVD: carbon monoxide, methane, acetylene, ethylene and ethanol from left to right (black: carbon, red: oxygen, white: hydrogen).

2.1.2 Reactivity

Thermodynamic stability is an important feature of a precursor. Figure 2 shows the standard Gibbs energy of formation for different carbon precursors as a function of temperature in the Ellingham approximation (data from [27]). Except for methane, all precursors decompose exothermally. It is seen that methane is more stable than graphite for temperatures lower than 600-700°C. At atmospheric pressure, acetylene, ethylene and ethanol are less stable than graphite at all temperatures while carbon monoxide is more stable than graphite at temperatures higher than about 700°C. It is important to remember that the conversion equilibriums and the inversion temperatures will vary with the partial pressures of the involved gaseous species.

This being said, some general comments can still be drawn. The pyrolysis of methane requires high temperatures to become thermodynamically allowed. Its conversion into higher organic compounds is thermodynamically restricted: experimentally, the main products of methane decomposition are simply carbon and dihydrogen [28]. If coupled with oxygen, methane can form other compounds such as CO₂, CO [28], C₂H₄ and C₂H₆ [29,30]. At the
opposite, the decomposition of acetylene, ethylene and ethanol is thermodynamically allowed at all temperatures and occurs readily provided a sufficient activation. Due to their high Gibbs energies of formation, these latter compounds can self-decompose into carbon, dihydrogen and a large variety of volatile organic compounds and polycyclic aromatic hydrocarbons [31-34]. The disproportionation of CO into carbon and CO$_2$ (i.e. the Boudouard reaction) is the main reaction path in the absence of other reactants (e.g. H$_2$ [35]). The reaction being highly exothermic, the reaction equilibrium shifts toward the reactants when increasing the temperature. Since the number of gaseous molecules decreases in the Boudouard reaction, the equilibrium conversion also increases with increasing pressure.

Figure 2. Gibbs free energies of reaction per mole of carbon for the formation of common metal carbides and carbon feedstocks. “cr” and “g” respectively stand for crystalline and gaseous. Data from [27,36].

The stability of a carbon precursor is also illustrated by the strength of its chemical bonds. Table 1 presents the dissociation energy of the weakest C-H bond of different hydrocarbons.
It is apparent that the strength of the C-H bond decreases with increasing the number of carbon neighbours. A similar trend is observed in the case of a carbon-metal bond as described in §2.3.3.

<table>
<thead>
<tr>
<th>Hydrocarbon</th>
<th>Weakest C-H bond</th>
<th>C-H bond dissociation energy (kJ/mol)</th>
<th>Atomic charge on H</th>
</tr>
</thead>
<tbody>
<tr>
<td>Methane</td>
<td>Primary</td>
<td>440</td>
<td>+0.087</td>
</tr>
<tr>
<td>Ethane</td>
<td>Primary</td>
<td>420</td>
<td>+0.002</td>
</tr>
<tr>
<td>Propane</td>
<td>Secondary</td>
<td>401</td>
<td>-0.051</td>
</tr>
<tr>
<td>Isobutane</td>
<td>Tertiary</td>
<td>390</td>
<td>-0.088</td>
</tr>
</tbody>
</table>

Table 1. Dissociation energies of C-H bonds and charge on H of some light hydrocarbons. From [37].

### 2.2. Catalyst nanoparticles

#### 2.2.1 Chemical nature

Nickel, iron and cobalt are the most common catalysts for CNT growth by CCVD. Over the years, many other elements have been proven suitable. Beside Fe, Ni and Co, MWCNT growth have been reported using nanoparticles of Pd [38], Pt [38], Au [39], Mn [38], W [38], Ti [38], TiC [40], Mg [38], Al [38], In [38], Na [38], K [38] and Cs [38]. These nanoparticles were usually larger than 3 nm. Beside Fe, Ni and Co, SWCNT growth was reported using nanoparticles of other late transition metals (Pd [41], Pt [41], Ru [42]), noble metals (Cu [41,43], Ag [41], Au [41,44]), early transition metals (Mn [45], Cr [46], Mo [47]), elements of the carbon family (diamond [48], Si [49], Ge [49], Sn [46], Pb [46]), lanthanides (Gd [50], Eu [50]) and other mixed compounds (FeSi2 [51], SiC [49,52], SiO2 [53,54], Al2O3 [54], TiO2 [54], Er2O3 [54], ZnO [55]). These nanoparticles were usually less than 3 nm.

Binary mixtures of active catalysts such as Ni, Fe and Co are frequently used and often observed to display a higher activity than individual elements [56]. Non- or weakly active
elements are also frequently mixed as co-catalysts, notably to prevent or control the coarsening of the catalyst. They notably include Mo [57,58] and Mg [59] mixed with Fe or Co.

Considering this wide variety of active elements and compounds, one may wonder which properties are actually required to promote the growth of CNTs. Hereafter are summarized some important physical and chemical properties of the nanoparticles used to grow carbon nanotubes.

### 2.2.2 Vapour pressure and melting point

The physical state of the catalyst during CNT growth (i.e. solid or liquid) is important because it influences several properties of the catalyst such as the solubility of carbon and its diffusion rate. It is still a highly debated issue (see §4.1) whose resolution is complicated by three effects.

First, in the presence of carbon, the melting point can be decreased by up to a few hundred degrees for the elements displaying a eutectic point in their phase diagram with carbon (e.g. Fe, Co, Ni, Pt, Pd, Rh, Ru, Ir, Re). Second, for particles in the range of 1-10 nm, the equilibrium vapour pressure is significantly increased which is usually approximated by the Kelvin or Gibbs-Thomson equation. The equilibrium vapour pressure of a particle of radius $r$ in contact with a vapour phase can be written as:

$$p = p_0 \exp \left( \frac{2\sigma_{sg} V}{kTr} \right)$$

where $p$ and $p_0$ are the equilibrium vapor pressures over curved and flat surfaces, respectively; $\sigma_{sg}$ is the surface tension at the particle-gas interface, $V$ is the volume of an atom in the particle, $k$ is the Boltzmann constant and $T$ is the temperature. The relation reflects the fact that particles with a higher surface/volume ratio are less stable. A practical consequence is that particles tend to evolve toward larger sizes as first described by W. Ostwald (see Ostwald
ripening in §2.5.2.2). In the case of a liquid or solid environment, an analogous equation can be written to express the equilibrium concentration in the outer environment surrounding the nanoparticle. Another consequence is that the melting point of nanoparticles is significantly depressed. The melting point of a nanoparticle in its own liquid can be approximated by:

$$T_m(r) = T_m^{\text{bulk}} \left(1 - \frac{4\sigma_{sl}}{H_f \rho r}\right)$$

where $T_m(r)$ and $T_m^{\text{bulk}}$ are, respectively, the particle and bulk melting points, $\sigma_{sl}$ is the surface tension at the solid-liquid interface, $H_f$ is the bulk latent heat of fusion per volume unit and $\rho$ is the density of the particle. All these effects originate from the large contribution of surface atoms to the total energy of the system. If the nanoparticles are deposited on a substrate, the interaction is therefore also expected to modify their melting point, which is the third effect to consider. As an example, Shibuta et al. [60] calculated that the melting point of a nickel cluster increased by up to 200°C with increasing catalyst–substrate interaction.

2.3. Interaction of carbon with transition metals

2.3.1 Affinity for carbon: carbon solubility and formation of carbides

In general, the ability of transition metals to bond with carbon atoms increases with the number of unfilled d-orbitals. Metals without d-vacancies in their electron configuration, such as Zn or Cu, display a negligible affinity for carbon. Metals with few d-vacancies such as Ni, Fe and Co exhibit a finite carbon solubility. Transition metals with many d-vacancies such as Ti and Mo can form strong chemical bonds with carbon and highly stable carbide compounds. For transition metals, the affinity for carbon therefore increases from the right to the left of the periodic table [61-63]. For example, the solubility of carbon at 700°C (a typical synthesis temperature for CNTs) is below detection limit in Zn, 0.01% at. in Cu, 0.3-0.5% at. in Ni and 1.2% at. in fcc-Co. Elements from Mn to Ti form carbides of increasing stability and
increasing carbon share (Figure 3). Fe is an intermediate case: Fe forms a metastable carbide (Fe₃C), the solubility of carbon is relatively low in α-Fe (~0.1% at. at 700°C) but substantial in γ-Fe (~4% at. at 800°C). The solubility of carbon in metals generally increases with temperature.

Figure 3. Ellingham diagram for carbides of 3d transition metals. Adapted from [36].

Graphitic carbon will be allowed to form if the carbon concentration overcomes the solubility of carbon in the catalyst particle. For elements that do not form stable carbides (e.g. Cu, Ni, Co, Pb, Sn, Au, Ag, Zn, Cd, Pd, Pt) [64], the critical concentration for the segregation of graphitic carbon is therefore the solubility limit of carbon in the metal. For carbide-forming elements, the carbon concentration must exceed the carbon content of the highest stable carbide (e.g. Mn₃C for Mn, TiC for Ti) for graphitic carbon to form.
A complicating factor is the influence of the particle size on the solid solubility of impurities such as carbon and the stability of mixed compounds (i.e. carbides) [65-67]. The solubility of carbon in nanoparticles is not well established and is still a subject of controversy. Experimentally, there are many reports of increased solubilities inside nanoparticles [66-70], including a giant increase of carbon solubility in Au nanoparticles [71]. A Kelvin-type relation has sometimes been used to explain the experimental observations although this relation actually describes the solubility in the medium around the nanoparticle as already stressed by A. Harutyanyan [13] and not the solubility inside the nanoparticle. Over the last years, thermodynamic models specifically addressing the solid solubility of impurities inside nanoparticles have been devised based on different assumptions: size-dependent entropy [72], regular solution theory [73], quantum confinement of elementary excitations [74], size-dependent melting enthalpy, entropy and atomic interaction energy [75] or linear concentration dependence of the surface energy [76]. In general, these thermodynamic models predict an increase of the solubility of impurities inside nanoparticles of decreasing size. In certain models, however, both solubility increase and decrease are possible depending on the relative binding strengths between atoms in the system. The matter is therefore not well established yet in both the general case and the particular case of carbon dissolution inside metal nanoparticles. Recently, Diarra et al. [77] reported Grand Canonical Monte Carlo simulations to calculate the adsorption isotherms of carbon on nickel nanoparticles of varying size: they found that at a given carbon chemical potential and temperature, smaller nickel nanoparticles dissolve a larger fraction of carbon than larger ones due to the larger carbon solubility in subsurface than in the bulk.

Experimental observations long supported that catalysts having intermediate carbon solubilities (between 0.5 and 1.5 wt.%) and not forming stable carbides were required to promote CNT growth [40] although the reason for that was unclear. The reports of novel
catalysts displaying both low (e.g. Cu) and high (e.g. Ti) affinities for carbon probably should lead to reconsider this conclusion.

2.3.2 Carbon diffusion: bulk, surface and subsurface

The diffusion mode of carbon atoms during CNT growth (bulk versus surface diffusion) has long been and still is a highly debated issue. The solid-state diffusion of impurities (such as carbon) has been studied for many years, notably for metallurgy purposes. Figure 4 shows the solid-state diffusion constants of carbon in various bulk metals and metal carbides as a function of temperature. Despite the absence of a simple rule, some general trends can be given [78].

i) The bulk diffusion of carbon atoms is much faster than that of the atoms of the solid metal host since the former ones diffuse interstitially while the latter ones diffuse substitutionally.

ii) Interstitial diffusion depends on the geometry of the host lattice and is faster in more open structures. For instance, the activation energy for carbon diffusion is 1.53-1.57 eV in close-packed fcc Fe while only 0.83 eV in bcc Fe [79,80].

iii) The higher the melting-point of the host, the smaller the diffusion constant of the solute atoms. For instance, in the case of $\alpha$-Fe, V and Mo that are all bcc metals, but with significantly different melting points, the diffusion constants inversely follow the order of melting points, that is Fe ($T_m$=1808 K) > V ($T_m$=2160 K) > Mo ($T_m$=2890 K).

iv) The diffusion constant depends inversely upon the solid solubility, being least for metals which form a continuous series of compounds (i.e. carbides in the case of carbon diffusion). For instance, in the case of Pd, Ni and $\gamma$-Fe that are all fcc metals with close melting points, the diffusion constants inversely follow the order of carbon affinity, that is Pd > Ni > Fe.
Figure 4. Bulk diffusion constants of carbon in various metals and metal carbides as a function of temperature. The activation energies for bulk diffusion of carbon was measured to be 1.44-1.74 eV in Ni (fcc) [80-83] (at the exception of Massaro et al. [84] who found 0.87 eV in the range 350-700°C), 1.50-1.68 eV in Co (hcp) [80,85], 1.53-1.57 eV in fcc Fe [79,80], 0.83 eV in bcc Fe [79,80], 1.20 eV in V [80,86,87], 1.37 eV in Pd [88,89], 1.44-1.78 eV in Mo [80,90] and 1.58 eV in Zr [91].

Studies on the diffusion of carbon have revealed a strong dependence of the diffusion coefficients on the carbon concentration [78,92,93]. For instance, the activation energy for bulk diffusion of carbon in fcc-Fe decreases from 1.55 eV to 1.24 eV if the amount of dissolved carbon is increased by 6 at. % [94]. In Ni, calculations predict that for carbon concentrations above 50 at. % in the first subsurface layer, the carbon diffusion barrier would decrease from 1.6 eV to below 1.0 eV [82]. This effect is usually explained by the lattice expansion caused by the addition of carbon. It has also been proposed that the repulsion between carbon atoms at close distance could enhance the diffusivity of interstitial carbons [95].

However, for very high carbon contents as encountered in carbides, it is commonly observed that the activation energies for carbon diffusion are much higher than in the
corresponding metals (see Figure 4). This is tentatively explained by the fact that carbon diffusion in carbides is no longer interstitial but mediated by thermal vacancies in the metal and carbon sub-lattices [96]. For instance, the activation barrier is 1.60-1.92 eV in Fe$_3$C [97-99], 3.4 eV in TiC [100], 3.1 eV in VC [101] and 2.9-3.6 eV in Mo$_2$C [102] and 2.6 eV in WC [101]. As a consequence, the bulk diffusion constants of carbon in metal carbides are usually much lower than in the corresponding metals as visible in Figure 4. It is worth noting that the diffusional mobility of the metal atoms in carbides is still several orders lower than that of carbon atoms [103].

Addition of other elements also influences the diffusion rate of carbon. For instance, the diffusion constant of C in fcc-Fe increases with the concentration of Ni and Cu, but decreases in the presence of carbide-forming elements such as Cr, W, Mo and others [92]. Other elements like Si and Co raise or lower the diffusion coefficient of carbon, depending on the temperature and their concentration [92,104]. In agreement with these measurements, calculations predict that the addition of small amounts of Au would reduce the activation barrier from 1.6 eV for pure Ni to 0.07 eV for Ni with 6 at. % of Au [81].

Much less data are available concerning the surface diffusion of carbon. In general, the activation barriers are found to be significantly lower than for bulk diffusion. For instance, calculations on the surface diffusion on Ni(111) and Ni (110) yielded a barrier of 0.4-0.5 eV [105] in good agreement with the experimental value of 0.3 eV measured on a polycrystalline Ni surface [106]. First-principles calculations by Yazyev and Pasquarello [62] on Ni, Pd, Pt, Cu, Ag and Au yielded that bulk diffusion has systematically a higher activation barrier than surface and subsurface diffusions. Surface-to-subsurface diffusion is another interesting case to consider: Xu and Saeys [82] calculated an activation barrier for carbon on Ni(111) of 0.7 eV at low carbon coverages, a value that is intermediate between surface and bulk diffusion.
Like solubility, the diffusion rate of carbon in nanoparticles may be dependent on the particle size. Despite some experimental observations [107], such a possible effect is still insufficiently documented.

2.3.3 Theoretical aspects of carbon structures interactions with metal surfaces

For the CCVD growth of CNTs, a key aspect is the carbon-metal interaction that obviously depends on the nature of the catalyst considered. A large number of papers have been devoted to the theoretical study of this metal carbon interaction, mostly using quantum chemistry (QC) or Density Functional Theory (DFT) based calculations. As usual in such an instance, the general trends are rather robust (e.g. early TMs tend to make too stable carbides, late TMs are better for catalytic purposes) but differences exist in the details. The problem is indeed complex, especially because of the unique ability of carbon to form various structures with different bonding characters. As described hereafter, we can qualitatively consider that the interaction of carbon with a metal surface is stronger for isolated atoms and decreases when C-C bonds with neighboring carbon atoms, corresponding to strong lateral interaction, are formed. The ultimate limit is the formation of a full graphene layer of a flat metal surface that has weak adhesion energy.

The interaction of atomic carbon with different metallic surfaces or bulk metals has been extensively studied. A thorough study of the applicability of DFT for computing key quantities such as the heat of solution of C in Ni is reported by Siegel and Hamilton [108]. A useful reference state is the stability of the ideal C sp² structure such as graphene. Referred to it, and neglecting the energy difference due to the finite diameter of a tube and its curvature, the adsorption or solution energy of a carbon atom directly tells us whether a C atom will prefer binding to the tube or to the metal. The adsorption energy depends on the different
surface sites available on different structures (flat surface with different orientations, steps, clusters …). Interstitial subsurface and bulk sites have been considered, too, as well as carbon dimers. For Ni, Pd, Pt, Cu, Ag and Au [62,82,109-111], the adsorption of a single C atom is less stable than its incorporation in a graphene layer, with energy differences of the order of 1 eV/carbon atom for Ni, Pd, Pt and 2-4 eV/carbon atom for noble metals. Subsurface sites are more favorable than bulk incorporation or adsorption on various surface sites. For Ni and Co hollow (100) semi-octahedral sites are more favorable than compact facets [112,113]. When suitable surface coverage is reached, this leads to the (2x2) P4g “clock” surface reconstruction observed on Ni (100) [114,115]. Complex behavior is also predicted on different facets of Fe, an important catalyst for NT growth. Carbon adsorption on the different facets of bcc Fe has been shown [116-118] to substantially modify their surface energies, thus potentially explaining changes of the nanoparticle shape observed during growth. At low surface coverage, C atoms are separated from each other and their binding on late transition metal surfaces is stronger on open sites than on compact facets. On a bcc Fe (100) facet with a somewhat larger (2/3) surface coverage, carbon chain structures have been experimentally evidenced and found to be strongly interacting with the surface [119,120].

Carbon dimers are found to be the most stable adsorbed species on noble metals, and close to it on Ni [108]. More precisely, acetylene which can be consider as a prototype of carbon dimer is more strongly adsorbed on Ni than on Pd, Pt and Rh (111) surfaces [121] in agreement with the chemisorption model of Nørskov (see 2.4.1). Tight binding calculations, allowing the relaxation of large simulation boxes, indicate, in agreement with experiments, that dimers can be stabilized in subsurface, involving strong local distortions [122].

During nanotube growth, carbon does not interact with a flat surface but rather with a cluster. Attempts have been made [123,124] to take this finite size effect into account, but one rapidly faces difficult challenges. DFT based calculations are better suited to deal with
periodic systems and calculations of interaction energies of carbon with metallic clusters are therefore limited to small cluster sizes, below 100 atoms. In addition, the stability of these small size clusters results from a balance between bulk and surface energies, leading to magic numbers sizes, for which calculations have been done. However, the strong chemisorption of carbon that can modify the surface energy contribution and the presence of a substrate that also strongly interacts with the clusters cast some doubts on the relevance of this approach.

Starting from individual atoms, dimers and chains on the metal surface, the next step is the study of the interaction of caps or tubes with flat surfaces or metal nanoparticles. In this case, carbon atoms have already formed bonds with other neighboring carbons, and, as consequence, the interaction with the metallic surface is weaker. This kind of calculations is in principle more relevant to the experimental nanotube growth situation, but still rely on some assumptions, concerning, in particular, the structure of the metal catalyst, generally taken as pure (no carbon dissolved in) and crystalline. Ding et al. have underlined the importance of a strong carbon metal interaction [125], to sustain a continuous growth by preventing the closure and detachment of the tube: they show that Fe, Co and Ni bind stronger to the tube, and hence perform better than Pd, Cu and Au. Larsson et al. [126] calculated that the adhesion energy between metal clusters and SWCNT caps follows the order Fe~Co>Ni. Depending on the tube chirality, bond strengths are in the (-2.5; -1.5) eV/bond range for the former. In the context of trying to explain chiral selectivity, Reich et al. [127] calculated the interaction of caps with different chiralities on a flat Ni (111) surface, showing small energy differences between them.

Much weaker interaction energies are expected for carbon structures (flakes, flat caps…) lying almost flat on the surface. Fan et al. [128] calculated the adhesion energy and stability of small C flakes on Ni to propose a model for the cap nucleation. Lacovig et al. [129] studied the evolution of the binding energy of carbon flakes on Ir (111) as a function of
the flake size, starting from almost zero (graphene layer) to -1.2 eV / C atom for a C₆ ring, emphasizing the role of the edge atoms contribution in the binding.

When the flakes grow larger, we tend towards a graphene structure that generally interacts weakly with metal surfaces. This pushes DFT calculations to their limits, since Local Density Approximation results in an overestimation of the adhesion energy, while Generalized Gradient Approximations result in near zero adhesion energies. Recent developments try and include non-local corrections to the DFT approximations [130-132]. It may be expected that the adhesion strength of the graphene sheet also depends on the amount of carbon dissolved in the metal particle although this dependence is rarely addressed in the literature.

2.4. Catalytic activity of transition metal nanoparticles

2.4.1 Dissociative adsorption on transition metal surfaces

The role of a catalyst is to accelerate a thermodynamically-allowed chemical process (e.g. the decomposition of carbon-containing molecules) by creating a transition state of lower energy [133]. The corresponding decrease of activation energy depends on the strength of the adsorbate-substrate bond which experimentally reflects in the heat of adsorption. There is a general trend for the heats of adsorption to decrease from the left to the right of the periodic table. For instance, the heat of adsorption of CO on polycrystalline Ti is 6.5 eV, but only 0.9 eV on polycrystalline Cu [133]. This trend can be explained by the chemisorption model developed by Nørskov [134] stipulating that molecules adsorbing on transition metals preferentially interact with the d-states near the Fermi level that give rise to bonding and antibonding levels. The d-electron contribution to the bonding is therefore proportional to (1-f₅) where f₅ is the degree of filling of the d-band.
When a molecule is adsorbed on a metal surface, the activation barrier for its dissociation is lowered. For instance, the activation barrier for the dissociation of acetylene was measured to be 1.4 eV on Ni(111) instead of 5.58 eV for self-decomposition [105]. If the surface bonds are too strong, the reaction intermediates will remain on the surface and block the adsorption of new reactant molecules. Forming adsorbate-substrate bonds of intermediate strength is an important property of a good catalyst. The catalytic activity of transition metals for a given reaction often displays a volcano-shaped pattern across the periodic table [135]. For instance, acetylene and ethylene are observed to be very weakly adsorbed on noble metals such as Au, Ag and Cu [133] while, on other transition metals, the adsorption of unsaturated hydrocarbons is generally strong and dissociative. When one adsorbs an unsaturated hydrocarbon onto a transition-metal surface at low temperature and then heats the surface, the molecule decomposes and leaves the surface covered with partially dehydrogenated fragments (e.g. ethylidyne) or carbon, rather than desorb from the surface. At higher temperatures, polymeric carbon chains with the general formula C\textsubscript{x}H are formed, which eventually results in a graphitic monolayer [133].

It was also demonstrated that dissociative adsorption of hydrocarbons often leads to the population of subsurface sites even in metals having low carbon solubility. For instance, Teschner et al. reported a carbon content of 35 to 45 at % in the three top layers of Pd under alkyne exposure at 350 K while the bulk solubility of carbon in Pd is less than 1 at. % at this temperature. The surface carbide was found to be stable only in the reaction ambient. Interestingly, the degree of subsurface population by carbon was found to strongly influence the catalytic activity and the conversion selectivity [136].

2.4.2 Catalytic activity of transition metal carbides

Many metal surfaces will form carbides when exposed to carbon-bearing molecules at high temperatures (see Figure 2 for examples). It is important to judge their catalytic activity
since nanoparticles of carbides (e.g. TiC) or of carbide-forming metals (e.g. Ti, Mn, W, Cr, Mo, Fe) were reported to be active for CNT growth in CCVD (see 2.2.1). Compared with pure metals, carbides generally display lower adsorbate-surface bonds [137-139] and are therefore often considered as having no or weak catalytic activity. Carbides of the group 4-6 metals have been studied for their catalytic activity in oxidation, hydrogenation/dehydrogenation, isomerisation and hydrogenolysis, and in many cases have been found to rival the performance of metals of the Fe-group [140,141]. While refractory carbides do not display high activity for oxidation reactions, they are often as active as transition metals for hydrogenation and dehydrogenation reactions. As a consequence, carbide surfaces are used for catalysis in extreme conditions due to their remarkably high hardness and melting points, as compared to transition metals.

2.4.3 Catalytic activity of oxide surfaces

Nanoparticles of different oxide compounds (e.g. SiO$_2$ [53,54], Al$_2$O$_3$ [54], TiO$_2$ [54], Er$_2$O$_3$ [54], ZnO [55]) have been recently shown to be efficient catalysts of SWCNT growth. In addition, many oxides that are commonly used as catalyst supports in CCVD display catalytic activity. For instance, Yoshihara et al. [142] observed that Al$_2$O$_3$ and TiO$_2$ could catalyze the decomposition of acetylene (but not that of methane). Although heterogeneous catalysis mostly involves metal catalysts, many processes make use of oxides [133,143] such as zeolites (cracking of crude oil), chromium oxide (polyethylene synthesis), vanadium oxide (NO$_x$ reduction), copper oxide, zinc oxide (water-gas shift reaction), and molybdenum oxide (acrylonitrile synthesis). Overall, oxides have lower heats of adsorption than the corresponding metals [144,145], but polar oxide surfaces (e.g. Cr$_2$O$_3$(0001), NiO(111)) display higher adsorption energies than non-polar ones (e.g. MgO(100), NiO(100)) [146]. An oxide catalyst is often referred to as acidic or basic according to the propensity of the metal ions to donate or accept electrons (Lewis acidity) or protons (Brønsted acidity) [133]. In the field of
CNT growth by CCVD, Magrez et al. [147] notably observed that the growth was
dramatically activated when the surface of the support is made basic or when the acidity of
the support is modified from Lewis to Brønsted using water molecules.

2.4.4 Nanometric size effects on catalytic activity

It has long been recognized that the size and the surface structure of the catalyst can
influence the catalytic activity. A catalytic reaction is defined as structure-sensitive if its
conversion rate changes markedly as the size of the catalyst particles is changed. For instance,
while bulk gold has no catalytic activity, Haruta et al. reported that gold nanoparticles can
catalyze the oxidation of carbon monoxide [148]. Using size-controlled gold nanoparticles,
Tsunoyama et al. observed a relationship between the particle size and the catalytic activity
for the oxidation of alcohol, the smaller nanoparticles being more active [149]. This is
correlated by the observations that Pd nanoclusters of decreasing size display larger heats of
adsorption [150].

The reactivity of a metal surface is generally associated to both its geometric features and
its electronic structure. Classically, the structure sensitivity of a catalytic reaction is associated
to a modification of the population of reactive sites (terrace, steps, kinks, surface defects) with
decreasing particle size. For instance, the probability of H₂ dissociation decreases from 0.9 on
a stepped Pt(332) surface to less than 10⁻³ on a defect-free Pt(111) surface [151]. Several
authors reported that reducing the nanoparticle size modifies their electronic structure (i.e.
decrease of the density of states at the Fermi level, modification of the shape and position of
the valence band) [150]. The decrease of the density of states at the Fermi level has
sometimes been proposed to explain size effects in catalysis. In the case of very small
particles of a few tens of atoms, the electronic properties can be dramatically changed
relatively to bulk material due to quantum confinement effects. Meier et al. notably proposed
that the increase in heat of adsorption and the onset of catalytic activity coincide with the metal to non-metal transition that occurs in gold clusters of approximately 3 nm in size [146].

Small catalyst particles are also in closer interaction with their environment and are therefore more sensitive to support effects as detailed below.

2.5. *Interactions of metal nanoparticles with their environment*

2.5.1 *Redox interactions between metal nanoparticles and gas species*

Aging of nickel, cobalt and iron thin films in air results in oxide and hydroxide formation accompanied by a modification of the surface morphology [152,153]. Frequently, catalysts are subjected to an oxidative pre-treatment (i.e. calcination) to remove carbon contaminants or to reduce the surface mobility and the coarsening of catalyst particles.

The propensity of an element to be oxidized or reduced as a function of the gaseous atmosphere is apparent in an Ellingham diagram for oxides (Figure 5). Oxides and hydroxides of iron, cobalt and nickel are generally reduced under hydrogen [154], ammoniac [155] or hydrocarbon [156] atmospheres. It is apparent from Figure 5 that oxides commonly used as supports (SiO$_2$, Al$_2$O$_3$, MgO) are extremely stable and are not expected to be reduced in standard growth conditions. Other oxides such as TiO$_2$, MnO, Cr$_2$O$_3$ and ZnO are also very stable. At some exceptions, the affinity for oxygen among transition metals generally increases from the right to the left of the periodic table, like the affinity for carbon. FeO, for instance, is more difficult to reduce than NiO and CuO. Ellingham diagrams based on bulk thermodynamic values are often useful to predict the stability of oxides at a given temperature and in a given atmosphere.

However, when dealing with nanoparticles, surface and interface effects come into play. The chemical stability of nanoparticles can be modified by the interaction with a support. For
instance, an XPS analysis by J. Lu [157] indicated that under similar reducing conditions, Fe(III) nanoparticles on silicon oxide were substantially reduced to Fe(0), but failed to do so when supported on silicon nitride. The different interactions of metal nanoparticles with oxide substrates are discussed in more detail in the following part.

![Ellingham diagram for oxides](image)

Figure 5. Ellingham diagram for oxides. After [158].

### 2.5.2 Interactions of metal nanoparticles with oxide supports

The chemisorption behaviour of a metal cluster not only depends on its size and surface structure but also on its interaction with the substrate [150]. For example, gold clusters are found to be catalytically active when deposited on Fe₃O₄, FeO or TiO₂ but inactive when
deposited on Al₂O₃ [146,148,150]. *Strong metal-support interactions* (SMSI) is the term commonly used to refer to the reduction of catalytic activity of metal particles on certain supports. SMSI are commonly attributed to two different effects: i) the modification of the electronic structure of the catalyst particle by the oxide support (notably by charge transfer) and ii) the physical encapsulation of the particles by a thin layer of oxide support. Generally speaking, two aspects should be considered when dealing with the interactions of metal nanoparticles with oxide supports: (i) the electronic interaction corresponding to the charge redistribution at the metal-oxide interface and (ii) the chemical interaction corresponding to atom diffusion at the metal-oxide interface [159]. As described hereafter, the difference of electronegativities and the conduction properties of the oxide support strongly influence the phenomena at the metal-oxide interface.

**2.5.2.1 Electronic interaction: charge redistribution**

Contact between a metal particle and an oxide surface results in charge redistribution at the interface [159]. Local charge redistribution occurs within the first few atomic layers at the interface. This local electronic interaction is the dominant effect in the case of insulating oxide supports such as Al₂O₃, MgO and SiO₂ since electrons are strongly localized and the production and diffusion of ionic defects are limited. Local charge redistribution is driven by the difference of electronegativities between the metal and the oxide but is also affected by the surface properties of the oxide (surface stoichiometry, defects and terminations). The electronic interaction affects the catalytic properties of the particles. For instance, Yoon et al. [160] observed that, due to charge transfer, Au₈ clusters are catalytically active when supported on defect-rich MgO(100) surfaces but inert when deposited on a virtually defect-free MgO surface. The modification of the electronic properties and reactivity of the metal particles by the support is only significant for particles smaller than 2 nm [150]. In the case of conducting oxides such as TiO₂, ZrO₂ and ZnO, charge redistribution is long ranged and
driven by the difference of Fermi energies similarly to metal–semiconductor junctions [159]. In this case, the electric fields generated at the interface can significantly enhance the diffusion of ionic defects and promote long-range chemical interactions (see 2.5.2.2 and 2.5.2.3).

**2.5.2.2 Atomic diffusion: wetting, coarsening and encapsulation**

From Bauer’s criterion [161], a thin metal layer deposited on a substrate will preferentially form 3D islands rather than a 2D layer if $\gamma_{\text{metal}} + \gamma_{\text{metal–substrate}} > \gamma_{\text{substrate}}$ where $\gamma_i$ denote surface free energies. Metal oxides generally have lower surface energies than metals which favors the growth of 3D metal islands on oxide surfaces. Conversely, oxidizing metal particles generally leads to a flattening of the particles on the oxide support [162]. The interface term $\gamma_{\text{metal–oxide}}$ has also to be taken into account. Because $\gamma_{\text{metal}}$ and $\gamma_{\text{metal–oxide}}$ are usually difficult to estimate directly, $\gamma_{\text{metal}}$ is usually approximated by the heat of sublimation $\gamma_{\text{metal}}$ which also reflects the strength of metal/metal lateral interactions while $\gamma_{\text{metal–oxide}}$ is approximated by heat of formation of the most stable oxide of the metal since it reflects the strength of the metal-oxide interaction. Figure 6 displays the wetting behavior of different metals on TiO$_2$ as a function of their heat of sublimation and of oxide formation. It is apparent that transition metals with high electronegativity and high cohesion tend to dewet oxide surfaces while the more electropositive and lower cohesion metals tend to wet them [163].
Figure 6. Description of the growth mode of metals on TiO$_2$(110) versus the heat of formation of the most stable metal oxide ($\Delta H^0_{\text{oxide}}$) and the heat of sublimation ($\Delta H^0_{\text{metal}}$), in which $\bullet$ and $\triangle$ represent experimentally observed 3D island and 2D layer growth modes, respectively; and $\times$ represents the positions of metals whose growth modes have not been determined. In Zone I, metal/metal lateral interactions are stronger than metal/TiO$_2$ interfacial interactions so that metals tend to grow in the 3D island mode. In Zone III, metal/metal lateral interactions are weaker than metal/TiO$_2$ interfacial interactions so that metals tend to grow in the 2D layer mode. Zone II is a transition domain where metals show either 3D island or 2D layer growth, depending on secondary factors. From [164].

Surface energies can also be dramatically modified by adsorption of molecular compounds present in the gas phase [165]. In general, adsorbates increase the anisotropy of surface energy between crystal planes, resulting in strong faceting. Encapsulation (or decoration) is another way to minimize surface energy. It involves mass transport from the oxide support onto the surface of the metal particle and results in the covering of the particle by a thin layer of reduced oxide support or even its immersion into the oxide support [159]. It preferentially impacts metals with high surface energy deposited on oxide surfaces of low surface energy. Typical examples are Pt and Pd particles on TiO$_2$ and CeO$_2$ supports. From a kinetic point of view, encapsulation is also favored when the outward diffusion of oxide
cations is promoted by the surface electric field, which is the case when the Fermi energy of the metal is lower than that of the oxide.

If one now considers an ensemble of interacting particles on an oxide support, coarsening (or sintering) is another possibility to minimize the energy of the system [166] [167]. Coarsening of supported metal particles can occur in essentially two ways: either by the diffusion of single metal atoms (or metal-bearing molecules) from small particles to large ones (which is termed Ostwald ripening or interparticle transport), or by the migration and coalescence of whole particles (which is sometimes referred to as Smoluchowski ripening). Ostwald ripening is driven by the fact that vapour pressure varies inversely with particle size (see §2.2.2). It follows that metal atoms escape more quickly from small particles than from larger ones, resulting in a net flow of matter from the former to the latter. The nature of the diffusion process (surface, gas phase) and of the diffusing species (individual atoms, molecular species) can vary from one system to another. In numerous cases, it was found that the presence of oxygen greatly enhanced particle coarsening possibly due to the formation of more mobile metal oxide compounds [168]. The likelihood of particle coarsening by the migration-coalescence mechanism increases with the surface density of particles and their migration coefficients which increase with temperature, but also depend on the diameter, shape and nature of the particles. In practice, the different coarsening modes are characterized by different kinetic laws of the type:

$$\bar{d}^n - \bar{d}_0^n = Kt$$

where $\bar{d}^n$ is the mean diameter after time $t$, $\bar{d}_0^n$ the initial mean diameter, $K$ a temperature-dependent constant and $n$ an integer which is characteristic of the type of coarsening mechanism. Such studies on SiO$_2$-supported Ni particles [169], Al$_2$O$_3$-supported Ni particles [170] and Al$_2$O$_3$-supported Pt particles [171] indicated a change in the predominant
coarsening mechanism from migration-coalescence at low temperatures (i.e. typically less than 700°C) and short times (i.e. typically less than 1h) to Ostwald ripening at higher temperatures and longer times.

### 2.5.2.3 Chemical reactions: redox, alloy formation

Silicon wafers are standard substrates for nanotube growth. However, metals tend to diffuse into silicon and to form metal silicides which have much lower surface reactivity. For instance, for nickel, cobalt or iron deposited on silicon, formation of silicides were observed to occur at temperatures as low as 225°C for nickel [172,173], 450°C for cobalt [174] and 800-850°C for iron [175,176]. The propensity of a given metal to form silicides is apparent in the silicide formation enthalpies as those shown in Figure 7. In first approximation, such bulk thermodynamic data are useful to predict interface reactions. For instance, the Ellingham diagram for oxides in Figure 5 predicts that a silicon substrate tends to reduce the particles of most transition metal oxides deposited on its surface. However, in the case of nanoparticles, it should be kept in mind that the contribution of the surface energy to the total free energy of the system can be dominant.

![Figure 7. Standard enthalpies of formation of some 3d transition metal silicides (from [177]).](image)

This explains why pure silicon supports are rarely used for the growth of CNTs. To circumvent the problem of silicide formation, a diffusion barrier of SiO₂ or Al₂O₃ is
commonly employed. Simmons et al. reported that a 4-nm silicon dioxide layer is the minimum diffusion barrier thickness to prevent iron silicide formation below 900°C [175]. The efficiency of the diffusion barrier depends not only on its thickness and structural quality, but also on the nature of the metal, the processing time and the gas ambient. For instance, silicide formation at metal/SiO₂ interface was reported for many metals after prolonged heating under hydrogen atmosphere (e.g. Ni₅Si formation at Ni/SiO₂ interface [178]). At elevated temperatures, even low reactivity metals (such as Pt, Pd, Rh, Cu and Ni) deposited on SiO₂ and Al₂O₃ can form silicide and aluminide layers [179,180] while highly reactive metals (such as Ti, Zr, Hf) tend to form a thin layer of aluminide or silicide sandwiched between a top layer of metal oxide and the oxide substrate [181,182].

Pauling electronegativity is a good indicator to predict the chemical affinity of transition metals for oxide surfaces. Metals with electronegativity lower than 1.5 tend to form strong chemical bonds with SiO₂ [159]. The more electronegative metals do not reduce a TiO₂ surface whereas the more electropositive metals can reduce one or more TiO₂ layers, thereby forming an interfacial bond that increases their adhesion energy [163]. Mattevi et al. [183] observed that metallic Fe on Al₂O₃ formed Fe(II) and Fe(III) interface states making the interaction of Fe with Al₂O₃ much stronger than with SiO₂ in agreement with the lower electronegativity of Al compared to Si. They proposed that these interface states anchor Fe particles to the oxide surface and limit their coarsening.

Finally, metal thin films on silica/alumina can also form surface silicates/aluminates when heat-treated [184-189]. In presence of oxygen, a mixed oxide interlayer of NiAl₂O₄ can form by interdiffusion between Ni and Al₂O₃ [190]. A Mössbauer study by Oshima et al. [191] showed that a quarter of α-Fe deposited on SiO₂/Si changed to Fe₂SiO₄ when heat-treated at 840°C for 10 min under an hydrogen/argon/water atmosphere. Upon ethylene exposure at high temperature, Fe₂SiO₄ was observed to be predominantly carbonized into Fe₃C. At least
for cobalt, silicate formation is activated by water vapor [192,193] and was observed to occur at temperatures as low as 220°C [192]. In Fischer-Tropsch synthesis, silicate formation during catalyst ageing is a major cause of catalyst deactivation [193]. Following silicate formation, the catalytic activity can be partially recovered by a reducing treatment. For instance, cobalt silicates and aluminates can be partially reconverted into cobalt using hydrogen, but this requires higher reduction temperatures (~700-900°C) than Co₃O₄ and CoO (~300-400°C under H₂). Accordingly, Li et al. [184] reported that following a high-temperature reduction treatment, surface cobalt silicates can form well-dispersed Co nanoparticles highly efficient for SWCNT growth.

2.6. **Summary**

CNTs can be grown using a large variety of carbon sources and catalyst nanoparticles. When going from the right to the left of the periodic table, transition metals display a stronger affinity for carbon as explained by the d-band model of Nørskov. This results in higher carbon solubility, higher propensity to form stable carbides and higher adsorption energy. Because a good catalyst forms adsorbate-substrate bonds of intermediate strength, the catalytic activity of transition metals for a given reaction generally displays a volcano-shaped pattern across the periodic table. Compared to the corresponding metals, metal carbides and metal oxides generally have lower but non negligible catalytic activities for hydrocarbon dissociation. The thermodynamic stability of gaseous precursors and solid compounds at a given temperature and in a given environment can be estimated by using Ellingham diagrams.

Bulk diffusion of carbon through metals proceeds interstitially, making it much faster than the bulk diffusion of metal atoms but still slower than the surface diffusion of carbon on the metal. Bulk diffusion of carbon through metal carbides is always slower than through the corresponding metals. Qualitatively, the interaction of carbon atoms with a metallic surface is
stronger for isolated atoms and decreases with the number of C-C bonds formed with neighboring carbon atoms. The ultimate limit is the formation of a full graphene layer of a flat metal surface which has weak adhesion energy.

Due to the large number of interfacial atoms, nanoparticles have size-dependent properties that can significantly differ from their bulk counterparts: increased vapor pressure, depressed melting point, modified carbon solubility, increased catalytic activity, and increased sensitivity to the environment.

The reactivity of supported metal nanoparticles is strongly influenced by the electronic and chemical interactions with the oxide support. For insulating oxides, the electronic interaction is localized at the interface and driven by the difference of electronegativities. For conducting oxides, charge redistribution is long range and driven by the difference of Fermi energies. For insulating oxide supports such as Al₂O₃, MgO and SiO₂, chemical reactions (redox, alloy formation) are confined at the interface and are notably driven by the differences of electronegativity between metals. For conducting oxides such as TiO₂, ZrO₂ and ZnO, the spatial extent of the interfacial reaction can be strongly increased by the electric field created at the metal/oxide interface.

Since metal oxides generally have lower surface energy than metals, the growth of 3D metal islands is favored on oxide supports. The more electronegative transition metals tend to dewet oxide surfaces while the more electropositive metals tend to wet them. The oxidation of metal particles generally leads to a flattening of the particles. Particles can coarsen by Oswald ripening or migration-coalescence, which are both dependent on the particle sizes, the nature of the support and of the gas phase. Experimentally, the different coarsening mechanisms can be differentiated by their kinetic behaviors. Metal particles can also get encapsulated by a thin support oxide layer, a phenomenon which preferentially impacts metals with high surface energy deposited on oxide surfaces of low surface energy.
3. Synthesis-structure relationship in carbon nanotubes grown by catalytic chemical vapour deposition

The structural features of carbon nanotubes grown by CCVD strongly depend on the experimental conditions which include the preparation and pre-treatment of the catalyst and the synthesis conditions (Figure 8). This part aims at summarizing the synthesis-structure relationship in CNTs grown by CCVD as reported in the current literature. Considering the huge amount of articles published in the field since the mid-90s, an exhaustive summary is a nearly impossible task, and probably a useless one considering the diversity of experimental systems. Instead, this summary focuses on the most significant studies with respect to a particular experimental dependence. For each structural feature, the experimental dependence is summarized trying to highlight the most influential parameters and the dominant trends.

Figure 8. Input parameters and output features of carbon nanotube growth by CCVD

3.1. Nanotube outer diameter

A correlation between the size of the catalyst particles used in CCVD and the diameter of the resulting nanotubes is often observed. For instance, Cheung et al. [194] reported that iron nanoparticles of average diameters $d_{\text{NP}}$ of 3, 9, and 13 nm produced multi-wall carbon nanotubes with average diameters $d_{\text{NT}}$ of 3, 7, and 12 nm, respectively, which corresponds to a ratio $d_{\text{NT}}/d_{\text{NP}}$ close to 1. Schäffel et al. [195] obtained a similar ratio $d_{\text{NT}}/d_{\text{NP}}$ using iron
particles of 3 to 18 nm. Chen et al. [196] reported that the diameter distribution of SWCNTs was correlated with the size of the used SiO$_2$ particles with a ratio $d_{NT}/d_{NP} \sim 0.8$-0.9.

Such correlations based on the initial and overall size distribution of catalyst particles raise the concern of certain particles being inactive for CNT growth. An improved approach is based on the direct observation of particle-tube connections by post-growth HRTEM analyses. In the case of Fe particles of 1.3-2.0 nm, Nasibulin et al. [197] measured a consistent $d_{NT}/d_{NP}$ ratio of $\sim 0.6$-0.7 within a given batch. Using a similar approach, Hiraoka et al. [198] measured a $d_{NT}/d_{NP}$ ratio of ca. 0.3-0.5 in the case of Fe particles of 2-3 nm and Zhang et al. a $d_{NT}/d_{NP}$ ratio close to 1 in the case of Fe particles of 1-3 nm [199]. In the case of Co particles of 1-10 nm, Fiawoo et al. [200] actually observed that two configurations of nanotube-nanoparticle junctions coexisted: a perpendicular configuration corresponding to $d_{NT}/d_{NP}$ ratio lower than 0.75 and a tangential configuration for $d_{NT}/d_{NP}$ ratio higher than 0.75. Interestingly, they observed that the perpendicular configuration is dominant at short synthesis times (typically less than 2 min) and the tangential one at longer times.

The direct observation of CNT growth by in situ TEM [201-207] is probably the best approach to address the question of the size relationship between a nanotube and its catalyst particle. A first result of in situ TEM studies is that active particles are rarely spherical during CNT growth: a dynamic reshaping of the particle occurs, at least in the case of the standard Fe, Co and Ni catalysts. In many cases (in particular for MWCNT growth on large particles), the catalyst particle displays a pear-like shape, the top of which top fits the inner diameter of the tube and bottom fits the outer one (Figure 9). To date, all in situ TEM observations on MWCNTs showed a direct correlation between the nanotube outer diameter and the largest diameter of the catalyst particle. In the case of SWCNTs, this conclusion has to be somehow tempered by the small number of in situ TEM observations. In the case of SWCNT growth on a Ni particle, growth simulations performed by W. Zhu et al. [208] support that the $d_{NT}/d_{NP}$
ratio must be lower than 0.8-0.9 to prevent the nanotube rim to spontaneously close and to support continued growth.

![figure9](image)

**Figure 9.** In situ ETEM observation of the growth of a four-wall CNT from a fluctuating catalyst nanoparticle of (Fe,Mo)$_{23}$C$_6$-type structure. From [205].

Based on the observed relationship between the nanotube outer diameter and the particle size, controlling the size distribution of catalyst particles is the most standard way to tune the nanotube diameter distribution. This is commonly achieved by controlling the thickness of the deposited catalyst [209,210], its coarsening [154,211] or its evaporation [212-215] during the thermal pre-treatment preceding the growth. However, the observations of Fiawoo *et al.* [200] of two coexisting configurations of nanotube-particle junctions and the *in situ* observations that catalyst particles rapidly rearrange during the growth and adopt an equilibrium shape by interaction with the growing nanotube [201-207] suggest that parameters other than the particle size influence the size relationship between the particle and the nanotube. Growth parameters such as the growth temperature and the carbon precursor supply notably influence the final CNT diameter distribution.
In general, increasing the growth temperature is reported to shift the CNT diameter distribution toward larger diameters [216-221]. By analogy with the influence of the thermal pretreatment, such results are often explained by an increased catalyst coarsening when increasing the growth temperature [217]. Yet, a study of Yao et al. [222] showed an opposite effect of temperature at the level of individual SWCNTs. Following the same nanotube, Yao et al. found that changing the temperature during growth resulted in a change of the nanotube diameter even though the catalyst particle remained the same: the SWCNT diameter increased when decreasing the growth temperature and inversely. A similar trend was reported by Mahjouri-Samani et al. [223]. Yao et al. [224] found that the diameter change was highly related to the initial nanotube diameter and that the range of variation mediated by the temperature was limited. As an example, for an initial nanotube diameter of 1.6 nm, the maximum diameter variation was found to be 0.4 nm.

The dependence of the diameter distribution on the carbon supply is the subject of even more controversy. Lu et al. [225] initially reported that small-diameter SWCNTs are preferentially grown at low carbon feeding rates even when highly polydisperse nanoparticles are used as catalyst. Tanioku et al. [218] and Geohegan et al. [226] also reported that the proportion of small-diameter SWCNTs increased as the feedstock pressure or flux were reduced. At the opposite, Saito et al. [227] and Wang et al. [228] reported that increasing the flow rate of ethylene or the pressure of carbon monoxide resulted in SWCNTs of smaller diameter. At least in the case of nickel, Picher et al. [229] found that the diameter dependence varied with the studied range of precursor supply and that, for each growth temperature, there was an optimal precursor pressure for the growth of small-diameter SWCNTs.

Gaseous additives can also influence the diameter distribution of SWCNT samples. For instance, Tian et al. reported that the mean diameters of SWCNTs grown from CO can be
shifted from 1.2 to 1.9 nm by increasing the CO$_2$ concentration [230]. They attributed this effect to the selective etching of small-diameter tubes by CO$_2$.

### 3.2. Nanotube inner diameter

In 1983, Gary Tibbetts [231] studied a sample of tubular carbon filaments grown by CCVD and reported a linear relationship between the inner and outer diameters of the filaments. For the sample studied by Tibbetts, the proportionality coefficient $d/i/o$ was $\sim$0.6. More recently, a statistical analysis by Chiodarelli *et al.* [232] of MWCNT samples grown in different CVD conditions also yielded a linear trend between the average number of walls $N_{\text{Walls}}$ and the average outer diameter $d/o$ of each MWCNT sample: $N_{\text{Walls}} \approx d/o$(nm) - 2, which corresponds to $d/i/o \sim 0.3-0.4$. This explains why adjusting the size of the catalyst particles (or the catalyst thickness) is among the most popular methods to tune the outer diameter and hence the walls number of CNTs. As an example, using catalyst nanoparticles of controlled sizes, Schäffel *et al.* [195] and Chiang *et al.* [233] showed that increased catalyst sizes lead to increased wall numbers. Zhao *et al.* [210] reported that CNTs of larger outer diameters and larger wall numbers were obtained by increasing the catalyst thickness. Yamada *et al.* [234] even showed that high selectivity for double-walled CNTs could be achieved by precisely controlling the thickness of the catalyst film. However, the statistical analysis of Chiodarelli *et al.* [232] yields a quite large standard deviation $\sigma_N$ which increases with the average outer diameter: $\sigma_N \approx 0.17 d/o$. This suggests that the inner diameter is not only related to the outer diameter, but is also influenced by other growth parameters.

The precursor supply notably influences the inner diameter. Sharma *et al.* [235] observed that the number of walls decreased at lower precursor supply. Zhang *et al.* [236] reported that low ethylene supply leads to CNTs with small diameters and few walls and that selective synthesis of single- and double-walled CNTs could be achieved by tuning the flow
rates. These results suggest that a decreased carbon concentration of the catalyst particle (i.e. lower carbon chemical potential) leads to a decreased number of walls, as can be deduced from the model originally proposed by Tibbetts [231]. In situ TEM observations during CNT growth of Gamalski et al. [206] showed that, in certain cases, the number of walls of a nanotube could decrease during its growth. In the experiments of Gamalski et al., the thinning of the wall finally led to the detachment of the nanotube from the catalyst particle and the nucleation of another CNT displaying the same behaviour. Similarly, studying the growth of MWCNTs displaying periodic fluctuation of their inner diameter and periodic inclusion of catalyst material, Jourdain et al. [237] found that the size evolution of the carbon units along the MWCNT could be quantitatively accounted for by periodic fluctuations of the carbon concentration of the catalyst particle. Together, these results support that the inner diameter is influenced by the instantaneous carbon concentration of the catalyst particle which depends on both the carbon supply and consumption.

Concerning the temperature dependence of the inner diameter, there is no general agreement in the literature. For instance, Mudimela et al. [238] reported larger wall numbers (and larger outer diameters) with increasing growth temperature, while Sharma et al. [235] reported that both the number of walls and the outer diameter decreased with increasing temperature. The lack of agreement on the temperature dependence of nanotube structural features is a quite general trend; this maybe explained by the variety of catalyst systems and growth conditions experimentally studied and by the large number of thermally-activated processes involved at the different CCVD stages.

Additives were also reported to influence the nanotube inner diameter. Adding sulphur to the catalyst particles has been reported by several authors to reduce the inner diameter and increase the wall number [239-241]. For instance, Ci et al. [240,241] reported that the addition of sulphur favoured the formation of DWCNTs with small inner diameters at the
expense of SWCNTs. At the opposite, Pan et al. [242] reported an enlargement of the inner diameter of CNTs by adding boric acid (HBO₃) to the catalyst.

3.3. Nanotube chiral angle

Many authors reported a higher occurrence of high-chiral-angle CNTs (i.e. near-armchair) in nanotube samples [243-250]. The fact that both indirect (i.e. photoluminescence excitation) and direct methods (i.e. electron diffraction) of structural determination led to the same result strengthens this conclusion. In more detail, all authors agree on the higher occurrence of near-armchairs among relatively small-diameter CNTs (i.e. diameter ca. less than 3 nm). However, Hirahara et al. [248] observed that this preferential occurrence disappeared for CNTs larger than 3 nm while Arenal et al. [250] reported a preferential occurrence of near-armchairs even for few-walled CNTs of diameters between 3 and 8 nm.

Beyond this general trend, highly-selective synthesis of SWCNTs of high chiral angles were reported using specific catalyst systems such as Co-MCM41 [251], CoSO₄/SiO₂ [252], Co–Mo [253,254], Fe-Ru [255], Fe-Co [245], Fe-Cu [256] or Al-Cu-Fe [257] (Figure 10). He et al. [256] notably reported the predominant growth of (6,5) SWCNTs using Fe-Cu nanoparticles at low synthesis temperature. Using NiₓFeₓ catalyst nanoparticles of controlled sizes, Chiang and Sankaran showed that the chirality distribution could be influenced at constant particle size by varying the Ni/Fe ratio of the particles [56]. Lolli et al. [258] reported that changing the catalyst support from SiO₂ to MgO resulted in nanotubes with comparable diameters but different chiral angles.

Optimized gaseous feed are usually required to achieve SWCNT synthesis with high chiral selectivity. Lolli et al. reported that increasing the synthesis temperature resulted in an increase in nanotube diameter without a change in the chiral angle while varying the composition of the gaseous feed modified the (n,m) distribution [258]. Wang et al. confirmed
the influence of the gaseous feed by reporting that high-chiral-angle SWCNTs were preferentially obtained at high pressure of CO [228] (or under vacuumed ethanol or methanol [254]. Similarly, M. He et al. [259,260] found that using CO instead of CH₄ as carbon precursor led much smaller diameter SWCNTs with a higher occurrence of large chiral angles. Ghorannevis et al. [261] reported that an appropriate hydrogen concentration was the critical factor in achieving a narrow chirality distribution of (6,5) tubes when using a gold catalyst in plasma-enhanced CVD. Despite this general trend, there is no satisfying explanation for it.

Figure 10. Contour plots of normalized photoluminescence emission intensities under various excitations for the Fe-Ru SWNTs grown at various temperatures. From [255].

Additional factors were reported to affect the chirality distribution. For instance, Koziol et al. [262] observed that the addition of a nitrogen-containing compound in the hydrocarbon feedstock leads to the growth of large MWCNTs in which all the walls are either of the armchair or zigzag structure. Recently, the same authors showed that nitrogen interacted with the catalyst in the form of ammonia, causing a restructuring of the catalyst
surface and stabilizing the iron catalyst in its Fe₃C carbide phase [263]. Such a restructured catalyst is proposed to be at the origin of the epitaxial growth of MWCNT with only armchair and zigzag walls. The growth support may also be influential: using monocrystal sapphire as growth substrate, Ishigami et al. [219] reported the preferential growth of near-zigzag tubes on the A-plane and of near-armchair tubes on the R-plane.

3.4. Metallic / semiconducting nanotube ratio

Structurally, two-thirds of SWCNTs are semiconducting and one-third is metallic. In the absence of selectivity, a nanotube sample would be expected to present such proportions. Actually, there are several reports of synthesis conditions yielding SWCNT samples enriched in semiconducting or metallic tubes.

Several examples of semiconductor-enriched SWCNT samples were notably reported using plasma-enhanced CVD (PECVD). Based on electrical measurements, Y. Li et al. reported a percentage of semiconducting tubes of 89%. Later, they found that higher percentages of semiconducting SWCNTs are especially obtained when the growth parameters are adjusted to produce SWCNTs of small diameters, i.e. of the order of 1.1 nm [264]. Electrical measurements preformed by Mizutani et al. [265] confirmed that most CNTs grown by PECVD display a semiconducting behaviour. However, their Raman characterization also revealed several radial breathing modes corresponding to metallic SWCNTs. Scanning gate microscopy measurements suggested that the semiconducting behaviour observed for CNTs fabricated by PECVD process may actually result from the opening of a band gap due to defects caused by irradiation damage during the PECVD growth. Also using Raman spectroscopic assessments, L. Qu et al. [266] found at the opposite that arrays of SWCNTs grown by PECVD combined with fast heating, contained ≈96% of semiconducting tubes.
These results support a higher reactivity of metallic SWCNTs in plasma conditions leading to a modification of their electrical properties or even to their selective removal.

Other examples of selective removal of metallic tubes in reactive environments can be found in the literature. Hong et al. [267] found that applying a UV irradiation during the CVD growth of SWCNTs on quartz increased the proportion of semiconducting tubes up to 95% (as assessed by Raman and electrical measurements). Similarly, Yu et al. [268] reported that introducing a small amount of oxygen during the CVD synthesis of SWCNTs by the floating catalyst method led to the selective removal of metallic SWCNTs (based on Raman characterization). Parker et al. [269] found that the semiconducting SWCNT percentage peaked at 85% using isopropanol as carbon source while 2-butanol and methane yielded 70% and 32% of semiconducting SWCNTs, respectively. Using different alcohols as carbon precursors, Wang et al. [270] observed that the proportion of semiconducting tubes grown from an Fe–Co/MgO catalyst increased when decreasing the ratio of carbon atoms to oxygen atoms in the precursor composition. Similarly, L. Ding et al. [271] observed that increasing the proportion of methanol in the ethanol precursor increases the proportion of semiconducting tubes grown on quartz. Both groups proposed a selective etching of metallic tubes by hydroxyl radicals to explain the semiconductor enrichment. However, Che et al. [272] reported that isopropanol yielded a much higher fraction of semiconducting tubes (up to 97%) than ethanol suggesting that a too high amount of water may be detrimental to semiconducting tubes. Recently, W. Zhou et al. confirmed the higher chemical reactivity of metallic tubes to water etching and detailed rules for choosing the appropriate water concentration for selectively removing metallic tubes during CCVD [273].

Harutyunyan et al. [274] also reported that the M/SC ratio was highly sensitive to the composition of the atmosphere used during the annealing stage preceding the introduction of the carbon source and notably to the presence of water: the presence of water in Ar ambient
favoured the growth of semiconducting tubes whereas the same amount of water in He ambient promoted the growth of metallic tubes. Using an optimized atmosphere, these authors could increase the proportion of metallic tubes up to 91%, as shown by both Raman and electrical measurements.

Finally, the nature of the catalyst was also reported to affect the M/SC ratio. Using Ni-Fe catalyst particles of controlled size and composition, Chiang et al. [275] showed that the semiconducting content (assessed by optical absorption and Raman spectroscopy) significantly changed with the Ni-Fe ratio and could reach 90% for Ni_{0.27}Fe_{0.73} nanoparticles of 2.0 nm mean diameter. Using europium oxide (Eu$_2$O$_3$) catalyst particles, Qian et al. [276] found that 80% of the as-grown SWCNTs were semiconducting based on Raman measurements.

### 3.5. Defect density and carbonaceous impurities

Several methods exist to quantify the defect density of CNTs, including microscopic observations (HR-TEM [277], STM [278]) and electrochemical labelling [279]. Most usually, the crystalline quality of CNT samples is assessed by Raman spectroscopy which provides a rapid and statistical assessment of the defect density based on the intensity ratio of the defect-induced D-band to the graphitic G-band [280-285]. A difficulty of this approach is the potential contribution of carbonaceous impurities to the D-band, even though these contributions can often be distinguished by their positions and linewidths [286-293] or by their deposition kinetics [294]. For instance, Yasuda et al. [294] performed Raman measurements of the G/D ratio at different synthesis times showing that the level of carbonaceous impurities solely depends on the cumulated time of exposure to the carbon source (i.e. ethylene).
Figure 11. (a) Time evolution of the calculated weights of SWCNTs (red line), carbonaceous impurities (black line), and forest (blue line and squares). (b) Time evolution of the absolute purity in SWCNT. From [294].

By analogy with standard crystal growth, the crystalline quality of CNTs is expected to increase with decreasing supply and increasing mobility of the elementary building blocks. Qualitatively, in situ TEM observations of Sharma et al. [235] confirm that straight nanotubes tend to form at high temperatures and low precursor pressures while bent and defective nanotubes form at low temperatures and high precursor pressures. More quantitatively, the Raman measurements of the D/G ratio reported by Picher et al. indicate that the defect density of CNT sample follows a power law with precursor pressure [295].

The dependence of D/G on the growth temperature as reported in the literature is more complex. Studying CNT samples grown at increasing temperatures, Vinten et al. [296], Kwok et al. [297] and Picher et al. [295] observed three different regimes: with increasing growth temperatures: D/G first exponentially decreases, then decreases less markedly for an
intermediate range of temperatures and finally increases strongly. Concerning the high temperature regime, Kwok et al. [297] and Picher et al. [295] observed that the increase of D/G was proportional to the growth duration which they both attributed to the deposition of pyrolytic carbon activated at high temperatures in agreement with the conclusions of Yasuda et al. based on coupled TEM-Raman studies [294] and of Feng et al. based on coupled TEM-thermal analyses [298]. Concerning the observation of two different regimes at low and intermediate temperatures, different explanations have been proposed (e.g. predominance of non-SWCNT carbon impurities at low temperature, change of the catalyst state) but there is still no agreement in the literature.

Certain molecular species were also reported to act as defect-promoters. Noda et al. notably reported that the addition of water to ethylene degrades the quality of CCVD-grown SWCNTs [299]. Similarly, Gao et al. [279] found that using an oxygen-containing precursor such as ethanol yielded a higher linear density of defects than using methane. Using a nitrogen-containing additive (acetonitrile), Thurakitseree et al. [300] showed that the density of defects by nitrogen incorporation into the sp² carbon network could reach one atomic percent.

A remaining question is the influence of the catalyst on the defect density of CNTs. Theoretical works [301] support that the catalyst may strongly influence the processes of defect creation and annealing, but dedicated experimental studies are still missing.

3.6. Proportion of catalyst particles active for nanotube growth

After growth, it is commonly observed that many catalyst particles did not yield nanotubes. Different denominations are used in the literature for the ratio of the number of synthesized nanotubes by the number of catalyst particles, such as “catalyst activity” or “synthesis yield”. To avoid confusion with other features of the catalyst or of the synthesis
process, we will use here the term proportion of active particles (PAP). The PAP is best evaluated when using well separated catalyst particles deposited on a support. For instance, using individual Ni particles of 4.7±1.5 nm in different growth conditions, Paillet et al. [302,303] measured PAP ranging between 0.5% and 20%. Using spatially ordered Fe particles of 1.7±0.6 nm, Ishida et al. [304] measured similarly low PAP of ~10%. Y. Li et al. [305] led post-growth HRTEM observations to understand the low PAP obtained with discrete Fe particles of 1-2 nm and 3-5 nm. They observed that inactive particles yield only single spherical graphitic shells around them and that smaller nanoparticles (<1.8 nm) tend to be more active in producing SWCNTs with appreciable lengths. In agreement with the observations of the group of J. Liu that particle activity for nanotube growth was strongly size-dependent [225], Li et al. proposed that the disparity in particle size was the likely cause to the low PAP. The encapsulation of inactive particles by a graphitic shell is commonly observed during post-growth HRTEM analyses (Figure 12) and often invoked to explain the inactivity [306]. Rümmeli et al. [307] proposed that the nucleation of a carbon cap proceeds by precipitation of carbon from a supersaturated catalyst particle. They suggested that the biggest particles displaying a too large volume to surface area ratio would therefore be encapsulated by the precipitating carbon. Using the same argument and based on the observation that the ratio of the number of encapsulating graphitic layers, \( N_L \), to the particle diameter, \( D_p \), is typically 0.2-0.3 nm\(^{-1}\), Ding et al. [308] even suggested that encapsulating layers were formed by precipitation of carbon from a carbide particle of composition \( M_3C \) (e.g. Fe\(_3\)C). Experimentally remains the question of whether these encapsulating shells were formed during the exposure to the carbon precursor (therefore causing the inactivity) or at a later stage (e.g. during cooling). In situ TEM observations frequently reveal inactive particles larger or smaller than some active neighbours [206] but, up to now, the origin of their inactive could not be directly assessed.
When considering a possible encapsulation of the catalyst particle by carbon, the exact nature of the carbonaceous material has to be considered since their reactivity can greatly vary with their composition (e.g. H or O contents) and structural disorder. For instance, Davis et al. [309] showed that the dissociation of ethylene on a Pt(111) surface leads to the formation of a carbonaceous overlayer containing a large fraction of hydrogen. With increasing time, increasing temperature or decreasing hydrogen partial pressure, the hydrogen concentration of the overlayer decreases, finally leading to a graphitic layer that is irreversibly adsorbed and displays no catalytic activity [310]. In the case of propylene conversion on Mo at 600°C, Wu et al. [311] also confirmed the slow transformation of an easily removed hydrogen-rich overlayer into an inactive and irreversibly adsorbed graphitic layer. In the case of nanotube growth, Schünemann et al. [312] observed that the carbonaceous layer deposited by pyrolytic decomposition of cyclo-hexane did not prevent the growth of CNTs, but acted indeed as a carbon source. Interestingly, after monitoring the growth of an individual tubule by \textit{in situ} field emission imaging, Marchand et al. [313] found that increasing the temperature by a few tens of degrees reactivated the nanotube growth. This observation suggests that at low temperatures, deactivation is mainly caused by the encapsulation of the catalyst particle by a disordered carbonaceous layer whose structure is temperature-dependent.

Figure 12. Nickel particles encapsulated by a thick (a) or single-layer (b) graphitic observed after nanotube growth together with active catalyst particles. From [306].
Accordingly, preventing the particle encapsulation and reducing the catalyst coarsening are the two main ways used in the literature to grow high-density CNT samples. The vertically aligned CNT (VACNT) forests prepared by the so-called “super-growth” reported by Futaba et al. [314] are among the best examples of high-density samples. Using iron on alumina as catalyst and a controlled addition of water vapour to the ethylene precursor, they obtained PAP of up to 84% [315]. Later, they showed that other oxygen-containing compounds such as CO₂, ethanol or acetone, also act as growth enhancers [316]. They concluded that a controlled amount of oxygen supplied by the growth enhancer activates the catalysts by cleaning off the carbon coating that deactivates them. In another example of high-density growth, the growth of aligned CNT arrays on quartz, Zhou et al. [317] reported that the nucleation efficiency can be enhanced by a factor 3-4 by performing multiple cycles of growth separated by a short argon exposure. A similar observation was reported by Bin Wu et al. [318]. Based on the observation of nanotube etching with increasing the number of cycles, they postulated that oxygen-containing functions (e.g. –OH) reacted with the most reactive forms of carbon (amorphous carbon, small-diameter SWCNTs). Using Fe/Al₂O₃ catalysts presenting a gradient of iron thickness, Hasegawa et al. [319] evidenced that millimetre-tall VACNT forests can be grown without addition of water if the carbon precursor supply is set below a certain limit in order to retain an active catalyst; water only extends the catalyst lifetime when an excess precursor supply is used. They also found water addition to widen the window of catalyst thickness for VACNT growth toward higher thicknesses and to suppress nanotube growth from the smallest catalyst particles [299].

The carbon etching effect of oxygen-bearing enhancers may not be the only reason for the high nucleation yield of the super-growth. Zhu et al. [320] and Noda et al. [321] reported that replacing Al₂O₃ support beneath the Fe catalyst by SiO₂ decreases the nanotube yield by nearly two orders of magnitude under the same growth conditions. Studying Fe catalysts
supported on different types of alumina, Amama et al. [322] observed that SWCNT forest growth was strongly dependent on the type of alumina. Highest nanotube yields were obtained using alumina of high porosity (e.g. sputtered Al₂O₃) which was correlated with low Ostwald ripening rates and mild subsurface diffusion rates. Burt et al. [323] also observed that the VACNT yield was strongly dependent on the grain size of the sputtered alumina layer. From Noda et al., using cobalt as catalyst instead of iron had little effect, but using nickel instead of iron reduced the CNT forest height by 2-3 orders of magnitude [321]. These results highlight the importance of the catalyst and the support for growing high-density CNT samples. Mattevi et al. [183] proposed that interaction of Fe on Al₂O₃ is much stronger than that on SiO₂, and restricts Fe surface mobility. The resulting much narrower Fe catalyst particle size distribution on Al₂O₃ would lead to a higher CNT nucleation density. This is in line with the report of Esconjauregui et al. [324] that plasma-assisted thermal pretreatment of catalyst films of Ni, Co or Fe on TiN greatly facilitates the direct growth of high-density arrays of CNTs by promoting a stronger catalyst-support interaction and hence stabilizes smaller catalyst particles with a higher number density. Amama et al. [325] reported that the addition of water contributed to reduce the migration of iron catalysts on alumina and proposed that the formation of hydroxyl groups at the surface of alumina by water was at the origin of the reduced surface diffusivity of catalyst atoms. At the opposite, Hasegawa et al. observed no influence of water addition to the rate of catalyst coarsening inferred from the evolution of the average CNT diameter from the top to the bottom of CNT forests [319]. After exploring a large range of growth condition, Hasegawa and Noda [326] concluded that both a moderate carbon supply and a suppressed catalyst restructuring are key requirements in order to grow dense millimetre-tall SWCNT forests. As a consequence of those, they observed that the optimal growth domain for high-density SWCNT growth followed a diagonal in the temperature-carbon supply diagram [326].
3.7. Nanotube length

Experimentally, the elongation rate (or growth rate) of nanotubes is observed to decrease with time until complete termination of the growth (Figure 13). In Figure 13, one can observe that nanotube kinetics is characterized by an initial growth rate and a lifetime corresponding to the saturation of the nanotube length. This general behavior was observed at the level of individual nanotubes [235,306,313], of thin nanotube carpets [327,328] and of thick nanotube forests [329-332]. The final length of a nanotube depends not only on the nature of the growth limiting step but also on the nature of the deactivation process(es) limiting the lifetime. Obviously, the nature of the rate-limiting step and of the dominating deactivation process may vary with the experimental conditions. Hereafter, we describe the parameter dependence of the growth rate and lifetime and discuss the particular case of the kite growth method which produces the longest nanotubes to date.

![Figure 13. Time evolution of the thickness of a forest of VACNT measured by in situ optical absorbance for different partial pressures of carbon precursor (ethanol). T=825°C. From [331].](image-url)
3.7.1 Growth rate

Growing carbon filaments from acetylene at low temperatures (350-600°C), Baker et al. measured growth activation energies that were remarkably correlated with the activation energy for solid-state carbon diffusion through the corresponding bulk metals [6,333,334]. This supported that, in these conditions, bulk diffusion through a solid-state catalyst particle was the rate-determining step. A similar correlation was noted by other authors [335-337] usually when using low temperatures (400-600°C) and relatively reactive carbon sources (e.g. acetylene, propylene, butadiene).

However, many authors did not observe this correlation in their experimental conditions. Using acetylene in microwave plasma-assisted CVD, Bartsch et al. [337] measured an activation energy of 1.4–1.6 eV (in agreement with values for carbon diffusion in solid-state metals) for the formation of bamboo-like CNTs at 800-900°C but an activation energy of 0.3–0.6 eV for the growth of MWCNTs at 900-1100°C. They inferred that bulk diffusion was the rate-determining step in both cases, but through a solid or a liquid particle depending on the temperature range. Other authors reported high activation energies of the order of 2-2.8 eV at low temperatures [327,330,338,339] which may be compatible with gas-phase conversion of the carbon or bulk diffusion of carbon through carbide metals, but not with bulk diffusion through pure metals (see 2.3.2).

In contradiction with the hypothesis that growth kinetics is simply determined by the diffusion rate of carbon, the growth activation energy is often reported to be influenced by the reactivity of the gas phase. For instance, using plasma-assisted growth from acetylene at 150-500°C, Hofmann et al. [105] reported activation energies of 0.23–0.4 eV much lower than the value of 1.2 eV that Ducati et al. measured for thermal growth [340] or the value of 1.5 eV measured by Baker et al.. They concluded that the rate-limiting step in plasma-assisted conditions was the surface diffusion of carbon on the catalyst particle and that precursor
decomposition was the limiting step in purely thermal conditions. Meshot et al. [341] also showed that the growth activation energy was dependent on the pre-treatment of the gas mixture and increased from 1.02 to 1.88 eV when increasing the preheating temperature of the gas mixture from 980 to 1120°C.

In addition, the growth rate is often reported to increase with increasing precursor pressure. The reaction orders were reported to be close to unity by most authors [298,327,331,338,342] except by Wirth et al. [332] who measured a reaction order of 0.6 for low-pressure acetylene growth on Fe/Al₂O₃. Noteworthy, several authors reported that above a critical precursor pressure, the growth rate is independent of the precursor pressure [298,327,331] which was interpreted by Picher et al. [327] and Feng et al. [298] as the transition from a kinetic regime controlled by gas diffusion to a surface-controlled regime.

Many growth models predict that the nanotube growth rate will either increase [343,344] or decrease [330] with diminishing size of the catalyst particle. For instance, the model proposed by Puretzky et al. [330] stipulates that the larger diameter nanotubes should grow faster than the smaller diameter ones due to their higher surface area to circumference ratio. They later refined this model by including a size-dependent activation energy for feedstock dissociation to account for the experimental bell-like distribution of nanotube diameters [226]. Experimentally, however, there is no general agreement on the variation of the nanotube growth rate with the particle size or nanotube diameter. Growing arrays of aligned MWCNT by PECVD, Huang et al. [345] observed that the CNT growth rate was diminished when reducing the catalyst thickness from 35 nm to 10 nm. A similar observation was reported by Lee et al. [346] using a lower range of catalyst thicknesses (0.7-10 nm). Using a gradient of catalyst thickness, Zhang et al. [33] reported that the growth rate increased with increasing catalyst thicknesses, while Hasegawa et al. [347] found that the initial growth rate of thick CNT forests was rather constant for catalyst thicknesses of 0.4-3.0
nm. Contrary to Zhang et al., Patole et al. [348] observed that the CNT growth rate increased when decreasing the catalyst thickness from 3.0 to 0.5 nm. They also noted that the growth rate decreased with time as $t^{1/2}$, which supported that the rate was controlled by the diffusion through a barrier of increasing thickness (i.e. CNT or amorphous carbon mat) rather than by a catalyst size-related effect. This illustrates the difficulty to use CNT arrays to address this question because of the possible combination with other effects: diffusion through the stack, competitive/synergetic effects between neighbouring particles [349,350]. In this context, it is worth mentioning the in situ study of CNT length by aerosol size classification of Chiang et al. [351] who reported that reducing the catalyst size from 2.6 nm to 2.2 nm increased the CNT growth rate by a factor 3.

Since the nature of the catalyst strongly affects the physical and chemical properties of the particles, it may significantly influence the CNT growth rate. For instance, growth simulations performed by Page et al. [352] predict that the growth rate on Ni particles would be 69% larger than on Fe particles due to a faster integration of carbon chains into the nanotube. However, experimental comparisons of CNT growth rates for different natures of catalyst are quite few. Comparing the efficiency of Ni, Co and Fe catalyst films in the same PECVD conditions, Huang et al. [345] found that Ni yielded the highest growth rate, largest diameter and thickest wall, whereas Co results in the lowest growth rate, smallest diameter and thinnest wall. The CNT growth rates with SiO$_2$ [353] and Al$_2$O$_3$ [354] nanoparticles are usually of the order of 10 nm/s, which is much lower than with standard iron-group catalysts. Motta et al. [355] also reported that the presence of sulphur facilitates the formation of nanotubes. They found that sulphur forms a layer on the surface of the catalyst particles which may play a role in encouraging nanotube growth by surface diffusion.

Other factors may influence the nanotube growth kinetics. For instance, Louchev proposed a kinetic model where the growth rate is controlled by the surface diffusion of
carbon atoms over the surfaces of the carbon nanotube and of the underlying support [356]. This is in tune with the proposition of Magrez et al. [147] that the support contributes to the conversion and supply of carbon-containing intermediates to the nanotube root. Quantitative assessments of these effects on the growth kinetics of CNTs are however still missing.

### 3.7.2 Lifetime

Several authors reported on the temperature dependence of the lifetime. Studying the growth kinetics of thin CNT carpets on silica-supported catalysts as a function of temperature, Picher et al. [327] found that the evolution of the lifetime was inversely correlated with that of the initial growth rate: the lifetime first decreases with increasing temperature until a critical temperature above which it increases with temperature. However, they observed that the correlation ceased at too high temperature or too low precursor pressure [156]. Studying the growth of CNT forest from ethylene at 600-700°C, Bronikowski [339] found that the lifetime decreases with increasing temperature with an apparent activation energy of 3.4 eV for an alumina underlayer and 2.1 eV for a silica underlayer. Studying the growth kinetics of thick CNT forests at higher temperatures (650-1000°C), Vinten et al. [296] also observed that the lifetime generally decreased with increasing temperature. In addition, they identified a critical temperature above which the initial growth rate started to plateau and the lifetime decreased even more abruptly. Monitoring the mass uptake of a Fe-Mo/Al₂O₃ catalyst during CNT growth, Feng et al. [298] observed that, with increasing temperature, the catalyst lifetime first slightly decreased, then increased and finally declined.

Several studies also showed the dependence of the lifetime on the gas phase. Using ethylene as carbon source and an Fe/Al₂O₃ catalyst, Futaba et al [329] reported that the lifetime tended to decrease with increasing precursor supply. Using other types of catalysts (Ni/SiO₂, Fe-Mo/Al₂O₃) and carbon sources (acetylene, ethanol), Feng et al. [298] and Picher et al. [327] also found that the lifetime generally decreases with increasing precursor pressure.
When applying a separate preheating of the process gas for the growth of CNT forests, [341], Meshot et al. observed that the lifetime strongly varied with the preheating temperature and peaked for a certain value. As already highlighted, Futaba et al. showed that the addition of water at an appropriate concentration could increase the growth lifetime [329]. Using ultrapure process gases free of oxygen and water contaminations, In et al. [338] found that the lifetime was significantly lower with purified gases than with unpurified ones, but was strikingly insensitive to variations in ethylene or hydrogen pressures. Generally speaking, these results support that different deactivation processes are at play during nanotube growth and that the predominance of each depends on the growth conditions.

Finally, in the case of thick base-grown CNT forests, the diffusion of gaseous species through the growing mat of CNTs may become limiting. Observing that the growth rate decreases with time as $t^{1/2}$, Zhu et al. attributed the decrease to the growing diffusion resistance of the mat to gaseous species [357]. Based on diffusion modeling, Xiang et al.[358] argued that this explanation could only hold for highly dense millimetre-tall SWNT arrays, but not for other types of CNT samples.

### 3.7.3 Ultralong carbon nanotubes obtained by kite growth

To understand the processes controlling the nanotube length, it may be useful to learn from the syntheses yielding the longest CNTs. At the time of writing, the longest reported nanotubes were obtained by kite growth, a particular mode of CCVD growth where one extremity of the CNT floats in the gas phase while the other one remains attached to the support [359,360]. Such CNTs can reach lengths of 4-20 cm [361]. Their growth rates extrapolated from the synthesis duration and the CNT length can reach 10-90 $\mu$m/s [361]. Ethanol, carbon monoxide and methane are the main carbon sources used for the growth of such ultralong CNTs by kite growth. It is worth noting that the addition of an appropriate amount of water to methane [361] or ethanol [362,363] significantly enhances the growth rate.
of such ultralong CNTs. The nature of the catalyst is varied: Co, Cu, Fe, Fe-Mo. The growth temperatures are relatively high (850-1000°C) compared to standard CCVD conditions. In kite growth, ultralong CNTs are believed to grow by the tip-growth mechanism, i.e. with the catalyst particle attached at the floating end of the nanotube. This supports that substrate-related deactivation processes are major causes of nanotube length limitation.

### 3.8. Summary

The structural features of carbon nanotubes grown by CCVD strongly depend on the support-catalyst system and on the synthesis conditions. From in situ TEM observations, the catalyst particle undergoes a dynamic reshaping to accommodate the growing carbon structure. In many cases, the reshaping leads to a pear-shaped catalyst particle. In first approach, the outer diameter of the nanotube is observed to correlate with the lateral dimension of the catalyst particle. However, for a given particle, the nanotube diameter is also found to vary with the growth temperature although the operating mechanism is still unclear. Carbon supply strongly influences the overall nanotube diameter distribution, but the reported trends are often contradictory, which suggests that its influence is strongly dependent on the growth conditions and of the studied systems. The nanotube inner diameter is often found proportional to the outer diameter with a proportionality coefficient which varies with the growth conditions. Consequently, adjusting the size of the catalyst particles is a common way to obtain CNTs of controlled wall numbers. Other parameters are also found influential. A decreased carbon supply generally reduces the number of walls, as expected from the initial model of Tibbetts for a reduced carbon chemical potential. The temperature dependence of the inner diameter is still unclear and gives rise to contradictory reports. The addition of sulphur is reported to reduce the inner diameter of CNTs.
Concerning the chiral angle, a higher occurrence of near-armchair CNTs in as-grown samples is frequently reported. Obtaining such chirality-enriched samples usually requires special (often binary) catalyst systems, low synthesis temperatures and optimized gaseous feeds. The origin of this chiral selectivity is the subject of an intense debate and of different hypotheses as detailed in §4.4. The addition of nitrogen and certain crystal substrates were also reported to promote the growth of specific chiralities. The growths of semiconducting- or metallic-enriched samples were reported by several groups. Most preferential growths of semiconducting SWCNTs can be attributed to a higher sensitivity of metallic SWCNTs to reactive environments (plasma, UV irradiation, oxygen-containing atmosphere) leading to a modification of their electrical properties or to their selective removal. The growth of samples highly enriched in metallic SWCNTs was also reported by an optimization of the annealing of the catalyst under a water-containing helium atmosphere. At the time of writing, this preferential growth of metallic SWCNTs remains is not explained.

The defect density of CNT samples is most commonly assessed by Raman measurements of the D band. However, these measurements can also be influenced by the presence of defective carbonaceous by-products (e.g. pyrolytic carbon). In first approximation, the resultant defect density of CNTs simply increases with increasing carbon supply and decreasing synthesis temperature as expected from classical crystal growth theory. In-depth studies actually showed different regimes of defect integration or of by-product formation when varying the growth temperature. Different hypotheses were proposed to explain the occurrence of these different regimes (e.g. change of state of the catalyst, reaction with contaminants, formation of defective carbon by-products), but the matter is still not closed. The use of oxygen- or nitrogen-containing precursors and the addition of water were shown to increase the defect density of CCVD-grown CNTs. In most CCVD syntheses, the percentage of particles yielding a nanotube is low (typically less than 10%). Particle inactivity is usually
attributed to the stochastic nature of nanotube nucleation or to its dependence on the particle size. Water and diverse oxygen-containing precursors were found to increase the percentage of active particles and to promote the growth of highly dense CNT forests. Their effect is usually attributed to the prevention of particle encapsulation by cleaning off carbon species at the surface of the particle. Fe/Al₂O₃ used with ethylene and water traces is a popular catalyst for growing high-density CNT forests whose efficiency is attributed to both the etching effect of water and the low coarsening of iron particles on alumina.

For given conditions, the final length of a nanotube depends on the growth limiting step, on the main deactivation process, and on their respective parameter dependences. Growth activation energies are commonly used to infer the nature of the limiting step. However, the reported values (0.2-3 eV) greatly vary from one catalyst system to another and with the growth conditions. The good correlation between the values measured by Baker (0.7-1.5 eV) and the values corresponding to bulk diffusion through solid metals supported this latter stage to be limiting. Other groups measured lower values (0.2-0.6 eV), which led them to assign the limiting step to surface diffusion or to bulk diffusion through a liquid particle. Higher values (1.5-3 eV) were also reported which were usually attributed to the surface or gas-phase conversion of carbon precursors. This latter proposition is additionally supported by the dependence of the activation energies on the gas phase reactivity (plasma activation, preheating, precursor pressure). From these reports, it is reasonable to conclude that the nature of the limiting step depends on the nature of the catalyst and the growth conditions although what actually fixes the limiting step is still not rationalized. The growth lifetime generally decreases with increasing precursor supply. This can be counteracted by a controlled addition of an appropriate oxygen-containing additive such as water. In a large range of precursor pressure and temperature, the lifetime is observed to be inversely correlated with growth rate. These results support that carbon encapsulation is a major cause of catalyst deactivation.
However, the complex temperature dependence of the lifetime supports that other deactivation processes, such as catalyst coarsening, may be at play, especially at high temperature and low carbon supply. It is apparent that the same phenomena (catalyst coarsening, particle encapsulation) are invoked for both the growth deactivation and the catalyst inactivity, supporting that, in many cases, particles inactivity may be considered as early deactivation. It is worth mentioning that the longest tubes to date, which were grown by kite growth, were obtained using both catalyst particles detached from the support (i.e. tip growth) and a controlled addition of water.

4. Open questions and current hypotheses

This part addresses a few selected questions that are considered as important in the field of nanotube growth and are the subjects of intense investigations. These questions directly impact on the experimental dependence of the nanotube features described in the preceding chapter. For each question, the associated hypotheses are described together with the pros and cons from experimental results and in silico simulations.

4.1. State of the particle

4.1.1 Physical state

The physical state of the particle (liquid or solid) is a subject of controversy. As described in §2.2.2, the melting point of a metal particle can be significantly lowered by the size effects or the incorporation of carbon atoms or increased by interaction with the substrate. Simulations performed by Diarra et al. [364] show that, at the standard temperatures of CNT growth and in the absence of carbon, nickel nanoparticles down to 147 atoms (~1 nm) are solid. However, they observed that the incorporation of carbon tend to amorphize or melt the outer layer of the nanoparticle, eventually leading to a complete melting for smaller nanoparticles and large carbon fractions (i.e. larger than 10% at.).
In the 70s, Baker [5,6,365] proposed that the growth of carbon filaments proceeded via the vapour-liquid-solid (VLS) model developed by Wagner and Ellis for the growth of silicon whiskers [366]. In the original VLS model of Wagner and Ellis, the role of the particle is to form a liquid alloy droplet which acts as a preferred site for deposition from the vapour; once the liquid particle is supersaturated, the filament starts growing by precipitation of silicon atoms from the droplet. There are therefore two main and different hypotheses in the VLS model of Wagner and Ellis: i) the particle is liquid and ii) reactant atoms diffuse through the bulk of the particle. Actually, the proposition of Baker et al found massive support because the growth activation energies they measured were in excellent agreement with the values corresponding to the bulk diffusion of carbon through the corresponding metals. The results of Baker not only supported that bulk diffusion was a required step, but also that it was the rate determining step of carbon filament growth. However, it is often forgotten that the activation energies measured by Baker were in excellent agreement with those of bulk diffusion through the metals in the solid state and not in the liquid state. The results of Baker therefore provided a strong support for the second hypothesis of the VLS model (the bulk diffusion hypothesis), but were in contradiction with its first hypothesis (the liquid particle hypothesis). The use of the VLS term by opposition to a model where the particle would be solid is therefore often misleading. Preferably, one should specify which hypothesis of the VLS model one considers.

Experimentally, the rounded and elongated shapes of nickel catalyst particles observed after nanotube growth led Kukovitsky et al [367] to conclude that the particles were liquid during the growth process. However, in situ TEM observations by Helveg et al. [201] and other groups [202-205] demonstrated that, although highly deformable, nickel and iron catalyst particles remained crystalline during CNT growth. It is worth mentioning that, to date, all in situ TEM observations of crystalline particles correspond to rather large particles.
(typically larger than 4 nm). Experimentally, the physical state of transition metal catalyst particles of a few nanometres that are active for SWCNT growth is still an open question.

If one considers the current list of active catalysts for SWCNT growth (see §2.2.1), the melting temperature of the bulk phase ranges from 327°C (Pb) to 3550°C (diamond) for individual elements and up to 2830°C (SiC) for mixed compounds. Even by taking into account the influence of the particle size, carbon content and support, one must conclude that at standard growth temperatures (600°C-1000°C), some catalyst particles are probably liquid (e.g. Pb) while other ones are solid (e.g. diamond). For instance, the quantum-based molecular dynamics simulations reported by Page et al. [368] support that, during CNT growth, the surface of SiO₂ nanoparticles is converted to an amorphous SiC layer while the core of the SiO₂ nanoparticle remains oxygen-rich and solid. From all these results, one must conclude that both liquid and solid particles can support the growth of a CNT. However, the physical state would modify several properties of the particle that influence the efficiency and features of CNT nucleation, growth or deactivation (i.e. carbon solubility and diffusivity, deformability). For a given element, a solid or liquid state may be preferred to assist the growth of CNTs.

4.1.2 Chemical state

The chemical state of transition metal particles during CNT growth is also a controversial subject, especially in the case of iron. Essentially, the question is how much carburized is the metal particle during the growth: is it still metallic or carbidic? Is carbon dissolved in the bulk, only in subsurface sites, or does it remain at the surface of the particle? Obviously, one may expect from the content of §2.3 that the answer varies with the considered metal, its carbon affinity and its propensity to form carbides.
Esconjauregui et al. [38] performed in situ X-Ray diffraction (XRD) studies of CNT growth from a large range of elements as catalyst. They observed that all transition metal particles undergo carburization during the induction phase. At the onset of CNT growth, higher transition metal carbides such as Ni3C tended to decompose while lower transition metal carbides, such as WC, remained stable during CNT growth. Other metal carbides, such as Mo2C, were found stable but inactive for CNT growth. They also reported that MWCNTs could be grown by using pre-carburized Ni3C particles as catalyst. The in situ TEM studies reported by Lin et al. [306] confirmed that Ni particles of 1-10 nm remain metallic during CNT growth and do not transform into Ni3C carbide. [369] In situ XPS studies of Wirth et al. also showed that Ni, Co and Fe catalyst particles are in the metallic state during CNT growth.

The case of iron requires special attention. As can be seen in Figure 3, the stability of Fe3C at the considered temperatures is close to that of graphite. Therefore, one should expect the stability of Fe3C to strongly depend on the experimental conditions (i.e. temperature and carbon activity of the gas phase). Hofmann et al. observed the presence of additional carbide peaks in XPS in the case of iron, but not in the case of nickel and cobalt catalysts [370]. In line with the results of Esconjauregui et al, Emmenegger et al [371] reported in situ XRD data showing that, when exposed to C2H2, Fe2O3 was progressively converted into Fe3C which decomposed after 20-30 min into Fe and graphite, this process coinciding with the onset of CNT growth. This result supports that Fe is in the metallic state during CNT growth and in the carbidic state before CNT nucleation. In contrast with these results, in situ TEM observations [21,204,372] and XRD measurements [373] of different groups showed that CNTs nucleate and grow from Fe3C particles. To complete this description, it is also worth mentioning the post-growth analysis by TEM reported by Z. He et al. [374]. These authors observed that, in the same sample, both Fe and Fe3C particles could be found at nanotube ends. Interestingly, the ratio of Fe and Fe3C particles was found to vary with the synthesis.
temperature, Fe$_3$C particles being more abundant at low temperature. In addition, CNTs connected to Fe$_3$C particle were all bamboo-like and were much shorter than the CNTs connected to Fe particles. Similarly, *in situ* TEM and XRD data from Wirth *et al.* [375] showed that both metallic Fe and carbidic Fe$_3$C can be the active catalyst phase. Interestingly, they found that the nature of the main catalyst phase strongly depended on the α/γ-Fe proportion following catalyst reduction: they observed that metallic Fe was the main active catalyst phase for γ-rich catalyst mixtures while Fe$_3$C was the main catalyst phase in the case of α-rich catalyst mixtures, which could be accounted for by considering the metastable Fe-C phase diagram.

4.2. Reaction intermediates

A still open question concerns the nature of the reaction intermediates incorporated at the nanotube edge. This is important since the nature of the intermediates affects the mechanism of carbon incorporation in the nanotube and, hence, the growth rate, the defect density and the chiral selectivity. Simulations reported by Wang *et al.* [376] notably predict that changes of chirality would be more frequent in the case of the addition of carbon adatoms than in the case of carbon dimers.

Many studies were devoted to study the dissociation mechanism of carbon precursor molecules on a metal surface. Studying the dissociation of C$_2$H$_2$ on Fe(001) by first-principles calculations, Lee *et al.* [377] observed C-C bond breaking, leading to the formation of CH fragments. Molecular dynamics simulations performed by Vasenkov *et al.* [378] also supported a C-C bond scission of C$_2$H$_2$, but highlighted that surface contamination by oxygen could impede the dissociation. Experimentally, Moors *et al.* [122] studied the surface products of acetylene decomposition on a nickel nanocrystal using field-assisted desorption coupled with mass spectrometry. They found that, for short reaction times (t<10ms), the carbon
spectrum is dominated by C\textsubscript{1} species, demonstrating rapid C-C bond scission during acetylene decomposition. Only at longer reaction times (t>10ms) were higher C\textsubscript{n} carbon oligomers (n=2-4) observed to form from C\textsubscript{1}. Using C\textsuperscript{13}\textsubscript{-}marked ethanol as carbon source, Maruyama \textit{et al.} [379] demonstrated that a smaller amount of site-1 carbon atom (\textit{i.e.} next to OH) was incorporated into the CNTs, also supporting a prior scission of C-C bond in ethanol. Studying ethanol dissociation on Rh(111) by X-ray photoelectron spectroscopy and temperature-programmed desorption, Vesselli \textit{et al.} [380] confirmed that C-C bond cleavage is the preferential dissociation channel, while C-O bond scission was not observed.

Other works support that chains of a few carbon atoms may be the intermediates of carbon incorporation in the CNT. For instance, growth simulations performed by Irle \textit{et al.} [381] support that carbon incorporation proceeds via carbon chains that are covalently attached to the nanotube edge. The image of an octopus on a rock was used by the Irle group to popularize this hypothesis. Simulations of nanotube nucleation and growth by Amara \textit{et al.} [200,382] and Neyts \textit{et al.} [383] also support that both processes proceed via carbon chains. Additional support was provided by the calculations of graphene nucleation and growth on a Cu(111) surface (Wesep \textit{et al.} [384]) showing that the formation of carbon chains of 3–13 atoms was preferred compared to two-dimensional compact islands of equal sizes. Experimentally, the afore mentioned study of Moors \textit{et al.} [122] support a rapid aggregation of C\textsubscript{1} into carbon oligomers of 2-4 units. Studying graphene growth on Ru by low-energy electron microscopy, Loginova \textit{et al.} [385] found that graphene growth essentially occurs through addition of carbon clusters of about five atoms. Obviously, if the \textit{octopus hypothesis} can account for SWCNT and graphene growth, it does not seem applicable in the case of the inner walls of MWCNTs.

Some reports support the possibility of a direct polymerization of carbon precursors, such as alkynes and benzene, without C-C bond scission. When monitoring the decomposition
products of benzene by mass spectrometry during the CCVD growth of MWCNTs, Tian et al [20] surprisingly observed no possible hydrocarbon species derived from benzene. Concluding that the carbon-hydrogen bonds of benzene were dissociated but not the carbon-carbon bonds, they proposed that CNT growth proceeded by direct integration of six-membered rings. Their conclusion was supported by density functional theory calculations [386] showing the formation of biphenyl from two benzene molecules on a Ni(111) surface. The calculations indicated that the C-H bond of benzene could be selectively dissociated while the C-C bond was still retained. Observing that the growth kinetics of CNT forests were characteristic of heterogeneous chain reactions, Eres et al. [387] proposed that acetylene could self-assemble without C-C bond dissociation into larger carbon structures such as chains and nanotubes. Using different alkyne additives for the growth of MWCNT forests in a cold-wall reactor, Plata et al. [388] observed that multiple alkynes reacted with ethylene to accelerate MWCNT growth, suggesting a polymerization-like formation mechanism without full dissociation of the carbon precursors into C₁ or C₂ units.

4.3. **Mechanism of nanotube nucleation and growth**

Numerous works have been devoted to understand the requirements for nucleating a nanotube. *In situ* TEM studies have now unambiguously demonstrated that nanotube growth in CCVD is initiated by the formation of a carbon cap at the surface of the particle. These results validated the yarmulke hypothesis originally proposed by Hongjie Dai et al [389]. The experimental conditions favoring a high density of nucleation have already been described in §3.6. Here, we will describe the different theoretical approaches that have been reported to rationalize the nucleation process.
4.3.1 Thermodynamic models

Analytical models based on thermodynamic arguments are an interesting first approach to identify the processes at play during nucleation and evaluate their respective contributions. Kuznetsov et al. [390] considered the probability of formation of a carbon nucleus at the surface of a metal/carbon particle and the corresponding critical radius. They hypothesized that the carbon nucleus has the form of a flat saucer whose edges are bent in order to bond to the metal surface. The change in Gibbs free energy for the formation of the nucleus includes four contributions: the free energy of precipitation of the carbon atoms from the particle, the free energy associated with the surfaces of the nucleus, the free energy associated with the nucleus edges and the strain energy arising from bending the graphene layer. The model predicts that the critical radius of nucleus formation decreases with increasing temperature, increasing saturation of the metal-carbon solution and decreasing specific edge free energy. The authors observed a good agreement between this critical diameter and the average diameter of CNTs formed by different methods as a function of the catalyst nature and synthesis temperature. Dijon et al. [391] used a similar approach to compare the probability of two models of nanotube nucleation leading to either base-growth or tip-growth as a function of the particle size and oxidation state of the catalyst.

The model developed by Kanzow et al. [392] addressed the thermodynamic conditions for a graphene sheet at the surface of a liquid metal/carbon particle to bend and form a fullerene-like cap. From the model, the formation of a cap will be preferred if the available thermal energy exceeds the work of adhesion at the graphene/particle interface and the strain energy associated with the cap formation: the work of adhesion depends on the metal and decreases with the carbon content while the strain energy per unit area decreases with increasing the size of the graphene sheet. Although simple, the model could also reproduce the general dependence of the nanotube diameter distribution on the catalyst type and the
temperature observed in arc discharge and laser ablation. More recently, Schebarchov et al. [393] developed a model based on a flexible graphitic cap with its free edge constrained to the surface of a rigid spherical particle. They considered that the cap will lift if the curvature energy penalty in the collapsed state exceeds the work of adhesion. Their model provided a prediction of the catalyst-to-nanotube diameter ratio in good agreement with experimental observations for nickel and iron catalysts. However, a model based on a rigid catalyst particle may appear as too unrealistic with regard to the large particle deformability observed during in situ TEM observations.

4.3.2 Computer simulations

Such macroscopic models provide useful insights, but they generally lack reliable input data and their applicability at the nanoscale and the building hypotheses can often be questioned. For instance, all models consider a rigid particle which is contrary to most recent experimental observations. Contrary to thermodynamic models that consider idealized objects such as perfect cap structures on a spherical nanoparticle, but lack of reliable energy parameters, computer simulation approaches start, or should start, from a validated interatomic energy model and try and find conditions to nucleate a cap and/or grow a tube, that quite often incorporate a large number of defects. As described in §2.3.3, different atomic interaction models for metal and carbon have been proposed, ranging from simple empirical models to more sophisticated and more demanding in computer resources ab initio calculations. The computer simulation methods used are generally “brute force” Molecular Dynamics (MD) or Monte Carlo (MC) methods. In the former, atoms are generally added randomly close to the nanoparticle surface, while the latter enables more sophisticated approaches controlling carbon chemical potential, via Grand Canonical Monte Carlo (GCMC) simulations [382] or using force biased method to accelerate the relaxation and favor a healing of defective structures [383]. Such a naive approach is probably correct for simulating
the heterogeneous nucleation of a cap on a metal nanoparticle, but the question of whether the driving forces leading to the formation of a cap (e.g. carbon density in the vapor phase in the case of MD or the carbon chemical potential in GCMC) are realistic should be raised. In the case of homogeneous nucleation, specific techniques have been devised to evaluate the nucleation barriers [394,395]. In the present instance, too short time scales and exceedingly large driving forces often lead to carbon structures that are highly disordered. There is however a lot to be gained from atomistic computer simulation since the nanotube nucleation is very difficult to study by any other experimental technique.

Not all models give the same carbon solubility in the metal nanoparticle, nor has this solubility been systematically evaluated, but when carbon solubility is non-vanishing, a general trend is that the cap nucleation takes place once the nanoparticle is saturated with carbon [382,396]. The very small Fe clusters used in DFT [397] or tight-binding DFT [398] calculations do not allow such an analysis. In many models [382,396,399], carbon chains appear on the surface before a cap is formed. Although no direct experimental evidence has been produced, the presence of carbon chains during the nucleation and growth has been suggested by Eres et al. [387] and by Loginova et al. [385] in the case of graphene. The length of the observed carbon chains depends on the model and the precise nucleation and growth conditions and lead to more or less disordered structures. Quite interestingly, Neyts et al. [400] observed that the almost defect-less carbon nucleus formed could change its chirality in the early stages of the growth, thus discarding a possible determination of the tube chirality at the nucleation stage (Figure 14).
Figure 14. Coupled Monte Carlo / molecular dynamics study of the nucleation of a nanotube cap on a Ni nanoparticle. The local chirality of the cap appears to be changing at this stage of the nucleation process. After [400].

Once a cap is formed, it has to detach from the nanoparticle in order to avoid the encapsulation of the catalyst. Different explanations have been proposed to explain the cap detachment and lift-off. By systematically varying temperature and work of adhesion of the graphitic cap on the nanoparticle, Ribas et al. [401] could identify conditions leading either to a successful growth or to nanoparticle encapsulation. To explain the formation and lift-off of carbon domes observed by in-situ TEM during the formation of a multiwall nanotube on an Au doped Ni catalyst, Pigos et al. [402] identified two critical factors: the surface energy of the nanoparticle (that can be modified by chemisorbed carbon species) and the faceting of the nanoparticle. More recently, Diarra et al. [364] showed that the wetting properties of carbon sp² walls on a Ni nanoparticle strongly depend on the fraction of carbon dissolved, and demonstrated that the cap lift-off takes place when the carbon concentration in the catalyst is within a critical window.

Computer simulation modeling of the nucleation and growth of carbon nanotubes has made significant progress by incorporating more efficient and realistic atomic interaction models, and by using more sophisticated computer simulation techniques and algorithms. The
next challenge is a full understanding of the mechanisms leading to chiral selectivity that is discussed in the next paragraph.

4.4. **Chiral selectivity**

Chiral selectivity is an important issue in nanotube research due to the large number of applications requiring nanotubes with controlled electrical and optical properties. A higher proportion of high-chiral-angle CNTs (i.e. near-armchair) in nanotube samples is commonly reported as was already detailed in §3.3. The origin of this higher occurrence is still a matter of questioning. In the following, we review the theoretical works that have been devoted to this question and the hypotheses that have been proposed to explain the chiral selectivity of nanotube growth.

4.4.1 **Nucleation selectivity**

A first possibility is that chiral selectivity could be set at the nucleation stage. This hypothesis relies on the fact that the structure of a cap uniquely determines the chirality of the nanotube that will grow from it: in the absence of defects, the nanotube structure is an amplification of the edge structure of the cap. There is a statistical or entropic aspect to this question, i.e. how many different cap configurations exist for a given (n,m) tube. Brinkman et al. [403] established a census of the nanotube caps compatible with all tubes up to a diameter of 3 nm. Considering either general caps or isolated-pentagon caps, they found that the number of compatible caps increases quasi-exponentially when increasing the nanotube diameter. Reich et al. [404] performed a detailed study of the geometry, structure, and energetics of nanotube caps. They observed that tubes with diameters smaller than 6.8 Å have only caps that violate the isolated pentagon rule. The caps with isolated pentagons were found to have an average formation energy of 0.29 eV/atom while a pair of adjacent pentagons required a formation energy of 1.5 eV. This much larger formation energy justifies the
isolated pentagon rule and would explain the quasi-absence of SWCNTs of diameters less than 7 Å in nanotube samples. The (5,5) nanotube is the smallest diameter tube that has a cap obeying the isolated pentagon rule (a half C\textsubscript{60}). The other tubes with only one cap fulfilling the isolated pentagon rule are (9,0), (9,1), (8,2), and (6,5). Therefore, these results cannot account for the higher abundance of (6,5) and high-chiral angle SWCNT in many samples. This statistical approach is interesting in the first place, but all cap sizes are not equally probable since caps progressively grow in size and are constrained by the catalyst particle. In addition, considering that pentagons are randomly formed neglects the chemistry of formation of carbon cycles and the influence of the catalyst surface.

Reich et al [405] performed \textit{ab initio} calculations of the stability of different caps on a flat Ni surface. The results showed that certain caps are preferentially stabilized on a Ni(111) surface due to lattice matching with the catalyst surface. However, the energy differences were small (of the order of the thermal energy) and considering a flat and rigid catalyst surface now appears far from the experimentally encountered situation. The energy of graphene edges were calculated by Liu et al. [406] who found that the energy of an arbitrary graphene edge was significantly dependent on the orientation (from armchair to zigzag) and on the chemical functionnalization of the edge (\textit{i.e.} –H or –Ni). They proposed that this difference of edge energies may influence the chiral selectivity at the nucleation stage. At the opposite, Zhu et al. [208] calculated the formation energies of (10,0) and (5,5) SWCNT caps sitting on a Ni\textsubscript{55} cluster and found the energy difference to be too small to expect a preferential nucleation of caps corresponding to either high or low chiral angles SWCNTs.

Most of these simulations were performed starting from pure Ni or Co catalysts but, in some cases, carbide particles may be more relevant. For instance, Koziol et al. [262] reported the preferential growth of achiral CNTs (zigzag and armchair) when nitrogen was added during the growth. They observed that the catalyst particles are iron carbide and are
preferentially oriented with the [010] direction parallel to the nanotube axis and, more precisely, to either the [100] or [210] graphene direction [407]. Their studies support that the role of nitrogen is to stabilize iron carbide catalyst particles which act as epitaxial template for the selective nucleation of achiral CNTs.

### 4.4.2 Growth-rate selectivity

A second possibility is that the growth rate of nanotubes is chirality-dependent. Corresponding models assume that carbon integration, the last stage of the growth mechanism, is the rate-determining step and that its rate depends on the nanotube chirality. Experimentally, this is supported by several observations of higher reactivity of armchair edges compared to zigzag edges in the case of graphene [408-410]. Shu et al. [411] calculated that connecting a Cu atom to an armchair site lowers the barrier of incorporating carbon atoms onto graphene edge from 2.5 eV to 0.8 eV, which would result in a much faster growth of armchair edges compared to zigzag edges. In the case of SWCNTs, Rao et al. reported in situ Raman measurements of the growth rates of individual index-identified tubes [412] showing a positive correlation between the nanotube growth rate and its chiral angle.

On the theoretical side, several works were devoted to the question of chirality-dependent kinetics. Zhao et al. [413] found that the energy of the frontier orbitals for (5,5) and (6,6) armchair carbon nanotubes bonded to Ni atoms exhibits a periodic behavior when increasing the number of carbon atoms in the nanotube. In contrast, the energy of the frontier orbitals of the (6,5) tube was found constant as the number of C atoms increases. They proposed that the energetic smoothness of carbon addition in (6,5) SWCNT may account for its experimentally high occurrence. Wang et al. [414] simulated the growth of armchair (5,5), chiral (6,5), and zigzag (9,0) nanotubes on a relaxed Ni55 cluster and studied the reactivity caused by charge transfer between the metal particle and the tube. They notably found that the edge of a (6,5) tube presents one particularly reactive site which could explain the preferential
growth of chiral (6,5) nanotubes over armchair (5,5) and zigzag (9,0) nanotubes. Gomez-Gualdrón et al. studied the energetics of frontier orbitals for different caps connected to a 9-atom Co cluster during C₂ addition [415]. The LUMO orbital expected to participate in the C₂ addition reaction was found to be located in a more favorable part of the cap rim for near-armchair than for near-zigzag caps. They concluded that the carbon atoms in the near-armchair caps may have a better predisposition for continuation of the nanotube growth when the growth proceeds by C₂ addition.

Also considering carbon addition to either armchair or zigzag nanotube edges connected to metal steps, Ding et al. [416] calculated that the addition of carbon to an armchair site has essentially no barrier while for a zigzag edge, the barrier energy is of the order of 1.1-1.5 eV. Building on that, they proposed that the lengthening rate of a nanotube is proportional to the linear density of armchair sites (kinks) at the nanotube edge, which is approximately proportional to the chiral angle of the tube (Figure 15). Dumlich and Reich [417] theoretically considered the geometric constraints for the addition of C₂ dimers to armchair kinks at the edge of a nanotube. Observing that nanotube growth basically proceeds via the conversion of dangling bonds from armchair (a) to zigzag (z) and vice versa, they concluded that all armchair kinks are not equivalent and that a nanotube edge actually contains three types of armchair kinks (•) for C₂ addition: aa•aa, aa•z and z•z. In the case of a low energy difference between zigzag and armchair dangling bonds, the growth rate is proportional to the density of armchair kinks, that is a conclusion similar to Ding et al. In the case of a much larger energy for zigzag dangling bonds than for armchair ones, the model predicts that (n, n/2) chiral tubes would be kinetically favoured.
A third possibility is that the resistance of a growing tube regarding growth termination or chiral change depends on its chiral structure. Actually, environmental TEM observations frequently show the introduction of defects and the creation of kinks during CNT growth [207]. Changes of chirality along as-grown CNTs were experimentally observed [418]. Yao et al. [222] showed that chiral changes could be induced by slight modifications of the growth conditions (i.e. temperature. Recently, Kim et al. [419] simulated the dynamics of SWCNT chirality during growth and observed that improper defect healing could lead to changes in the tube chirality. In this respect, zigzag SWCNTs were found significantly inferior in maintaining their chirality compared to armchair SWCNTs. Besides defect integration, a major cause of growth termination or of chirality change is the coarsening of the catalyst particles. Using first principles calculations, Börjesson et al. [420] studied the influence of the nanotube chirality on the Ostwald ripening of the attached particle. They found that the Ostwald ripening of metal particles attached to CNTs not only depends on the particle size, but also on the nanotube chirality. Particles attached to armchair and zigzag nanotubes of similar diameters were found to have different propensity to ripening. For both
hypotheses (defect integration and catalyst coarsening), experimental studies of the chiral
dependence are presently missing.

4.5. Summary

Concerning the state of the particle, in situ TEM studies show that catalyst particles of
iron, nickel and cobalt are highly deformable, but still crystalline during growth. These
observations were made on rather large particles (typically larger than 4 nm), which leaves
open the question of the physical state in the case of smaller nanoparticles. Considering the
range of elements active for CNT growth, certain particles are likely to be liquid (e.g. Pb) and
other ones solid (e.g. diamond) in the standard conditions of nanotube growth. Having an
either liquid or solid particle does not appear to be a requirement for growing a CNT, although the nanotube and growth features are likely to be modified. From in situ studies
(TEM, XPS, XRD), nickel and cobalt particles are usually in a metallic state during nanotube
growth while iron particles may either display a metallic or carbide structure.

The nature of the reaction intermediates (adatoms, dimers, chains, undissociated
precursors) is still unsettled. Different in situ studies revealed the presence of C\textsubscript{1} species at
short synthesis times. At longer times, the conversion of carbon adatoms into higher C\textsubscript{n}
oligomers (n=2-5) is reported both experimentally and in silico. In the case of alkynes and
aromatic precursors, the hypothesis of a direct polymerization without C-C bond scission has
been proposed by certain groups to account for the abnormal kinetic behavior.

Concerning the mechanism of nanotube nucleation, the formation of a carbon cap at
the surface of the particle (the yarmulke hypothesis) has now been validated by in situ TEM
observations. Thermodynamic models support a strong influence of the carbon concentration,
metal-carbon interaction and temperature on the formation of a carbon nucleus of critical size.
Numerical simulations also confirm that surface carbon formation takes place once the
nanoparticle is saturated with carbon. They highlight the critical importance of the carbon cap-metal surface adhesion in the process of cap lift-off and its dependence on the fraction of carbon dissolved in the particle.

To explain the chiral selectivity experimentally observed, three general hypotheses are considered: chiral-selective nucleation, chiral-dependent growth rate and chiral-dependent lifetime. The selective nucleation hypothesis is now somehow abandoned due to the small differences of formation energies calculated for caps of different chiralities. Growth-rate selectivity is currently preferred based on calculations showing a large difference of barrier energies for carbon integration at armchair and zigzag sites and on experimental measurements of the growth rate of individual SWCNTs of different chiral angles. The lifetime selectivity assuming a chiral-dependent propensity for growth termination or chiral change has found some support from simulation works, but is still to be experimentally validated.

Beside those questions, many other questions remain that could not be addressed in detail in this review either due to the limited space or to the limited number of reported studies. One may notably mention the mechanism leading to either base- or tip-growth, the influence of the substrate on the growth kinetics or the mechanisms of defect integration. The interested reader can also refer to the list of open questions established after each edition of the Guadalupe Workshop on the Nucleation and Growth Mechanisms of Single Wall Carbon Nanotubes\(^1\).

5. Conclusion

As apparent from this review, the growth mechanism of CNTs in CCVD is complex and still the subject of intense investigations. Its understanding is noticeably complicated by

the variety of experimental systems in terms of catalyst, support, carbon precursor and growth conditions. Too different systems often lead to too different observations to allow unification and rationalization. In addition, the studied systems are still frequently insufficiently controlled and characterized. Learning from other fields of research such as heterogeneous catalysis or molecular biology, one may identify two successful approaches to work out complex mechanisms: the study of model systems and the development of numerical simulations. As evidenced in this review, numerical simulations have already been extremely beneficial for orienting experimental works and improving our understanding of CNT growth mechanism. With increasing calculating capacities, simulation will probably become an essential prediction tool for the phenomena that are still too difficult to study experimentally. On the experimental side, the field would probably benefit from the establishment and study of model systems, as was successfully demonstrated in the field of heterogeneous catalysis with the study of model surfaces and metal clusters. Fe/Al₂O₃ used with ethylene as carbon source and water as additive is an example of such a model system which has self-established due to its high nanotube yield. Other model systems having characteristic features important for fundamental studies such as catalyst clusters of uniform size, no or negligible catalyst coarsening, known limiting step or known dissociation products, would also be highly desirable. Novel types of experiments may also help improving our understanding of the role of the catalyst nanoparticles in CCVD. For instance, the recent discovery that SWCNT seeds can be elongated by vapour-phase epitaxy without the need of a catalyst nanoparticle [421] will probably shine light on the exact role of the nanoparticle at each stage (precursor decomposition, cap nucleation, nanotube amplification) of the CCVD process.

In conclusion, we now have a qualitatively good description of many phenomena acting during CNT growth, but quantitative relations are often lacking (e.g. quantitative parameter dependences of the defect density, growth rate, number of walls, outer and inner
diameters). More quantitative models would be extremely helpful for orienting experimental works and facilitating the analysis of experimental data. Growth kinetics or chiral selectivity are good examples of the valuable contribution of quantitative models to the rationalization of experimental data and to the orientation of experimental studies. For the future, we would clearly need more quantitative models that can be experimentally tested if we wish to build a more accurate and predictive theory of nanotube growth. Establish and study model systems and develop more quantitative and predictive theoretical tools should be particularly important goals for the young and creative minds entering the field. As apparent from this review, many exciting challenges are still awaiting them.

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