Competitive kinetics study of sulfide oxidation by chlorine using sulfite as reference compound

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Graphical abstract

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Abstract

To design and optimize hydrogen sulfide scrubbers working with chlorine, the knowledge of the kinetics of the hydrogen sulfide oxidation is necessary. In this work, the kinetics of the hydrogen sulfide oxidation by sodium hypochlorite was experimentally investigated using a reactor without headspace (100 mL gas-tight syringe) and the competitive kinetics method. The sulfite ion was selected as the reference compound. First, the apparent stoichiometries of sulfite anion and hydrogen sulfide chlorinations were determined performing single-compound experiments. Then, the kinetics of the hydrogen sulfide chlorination was studied in the pH range 6-12 performing simultaneous sulfite and sulfide chlorinations. The results demonstrated that sulfide and sulfite oxidation kinetic rates have the same order of magnitude, which validates the choice of the sulfite anion as the reference compound. Kinetic simulations emphasized that the kinetic rates of the oxidation of both compounds were limited by acid base reactions. The sulfide oxidation in the pH range 6-12 is mainly due to the hydrosulfide (HS-) oxidation by the hypochlorous acid (ClOH) with an associated kinetic constant of $1.2 \times 10^9$ L mol$^{-1}$ s$^{-1}$ at 25°C.

Keywords: Chlorine, sulfide, sulfite, sodium hypochlorite, kinetics, competitive method
1. INTRODUCTION

Hydrogen sulfide (H$_2$S) is a toxic compound involved in emissions from many industries such as waste water treatment or pulp industry (Gostelow et al., 2001; Kangas et al., 1984; Rappert and Müller, 2005). Several processes are currently used to remove H$_2$S: biofiltration, absorption in chlorine solution, absorption in alkanolamine solutions, absorption using the Claus process or catalysts to recover elemental sulfur, etc. (Busca and Chiara, 2003; Kohl and Nielsen, 1997).

Chemical scrubbing, which provides high and reliable efficiencies, is widely used for hydrogen sulfide removal. The process involves mass transfer in an aqueous solution using a gas-liquid contactor. At acid pH, H$_2$S is poorly soluble in water. However, hydrogen sulfide apparent solubility increases with the pH. Indeed, H$_2$S is a weak diacid which dissociates into hydrosulfide (or bisulfide) HS$^-$ ($pK_{a,1} = 7.0$ at 25°C) and sulfide anions as showed by Eqs (1) and (2) (Roustan, 2003):

\[ \begin{align*}
H_2S + H_2O & \xrightleftharpoons[k_1]{k_1} HS^- + H_3O^+ \quad K_{a,1} = k_1/k_1 \\
HS^- + H_2O & \xrightleftharpoons[k_2]{k_2} S^{2-} + H_3O^+ \quad K_{a,2} = k_2/k_2
\end{align*} \]

Authors’ results diverge about the value of $pK_{a,2}$, reported from 12 to 17 (Giggenbach, 1971; Licht et al., 1990; Meyer et al., 1983; Migdisov et al., 2002; Stephens and Cobble, 1971). However, the most recent articles are all concordant and confirm a value around 17. Consequently, S$^{2-}$ can be neglected in most aqueous media. Oxidants are often added to regenerate the scrubbing solution and to enhance mass transfer. The most frequently oxidants used are chlorine (Biard et al., 2010; Biard et al., 2009; Bonnin, 1991; Cadena and
Peter, 1988; Chen et al., 2001), ozone (Kerc and Olmez, 2010) and hydrogen peroxide (Couvert et al., 2006; Féliers et al., 2001).

Proving an excellent efficiency at rather low cost, chlorine is widely used for H₂S chemical scrubbing. Chlorine has attracted significant commercial attention for its wide scope in the fields of bleaching, oxidation, and disinfection. Gaseous chlorine (Cl₂) or sodium hypochlorite (NaOCl) are commonly used for chlorination processes (Deborde and Von Gunten, 2008). Due to the complex chlorine chemistry in water, various species may be present in the solution. Indeed, chlorine gas is hydrolyzed into hypochlorous acid (ClO\text{H}) according to the following reaction (Eq. 3):

\[
\text{Cl}_2 + \text{H}_2\text{O} \ \overset{k_3}{\rightleftharpoons} \ \text{ClOH} + \text{Cl}^- + \text{H}^+ \quad K_3 = \frac{k_3}{k_{-3}}
\] (3)

Wang and Margerum (1994) demonstrated that \(K_3\) is equal to \(5.1 \times 10^{-4}\) L² mol⁻² at 25°C and for a negligible ionic strength (Wang and Margerum, 1994). Hypochlorous acid is a weak acid which dissociates in turn into hypochlorite anions (Eq. 4):

\[
\text{ClO}^- + \text{H}_2\text{O} \ \overset{k_4}{\rightleftharpoons} \ \text{ClO}^- + \text{H}_3\text{O}^+ \quad K_{a,4} = \frac{k_4}{k_{-4}} = K_{a,\text{ClOH}}
\] (4)

Deborde and Von Gunten (2008) reported a value of the acid dissociation constant \(K_{a,4}\) of \(2.9 \times 10^{-8}\) (\(pK_{a,4} = 7.54\)) at 298 K. Consequently, the chlorine speciation depends on several parameters including the pH, the temperature, the chloride concentration and, with a lower importance, the ionic strength. Cl₂, ClO\text{H} and ClO⁻ are called the free chlorine species. Other reactive chlorine species can be formed upon various conditions (Cl₃⁻, Cl₂O, etc.) but their formation are not favored at low chloride concentrations (Doré, 1989). In most chemical conditions applied in water treatment, Cl₂ is negligible in solution for pH > 6.
ClOH is more electrophilic and usually more reactive than ClO⁻ (Deborde and Von Gunten, 2008). The chlorine reactivity with organic or inorganic compounds depends on the chlorine and target compounds speciation; so a great pH dependence of the apparent kinetic rate constants is expected in many cases. The oxidation reactions usually follow a second-order kinetic law with partial first-orders for both the free active chlorine concentration and for the total compound concentration (Deborde and Von Gunten, 2008).

The oxidation of hydrogen sulfide occurs by a complex mechanism which involves many by-products: colloidal sulfur, sulfites, thiosulfates, or sulfates depending on the pH, the temperature and the advancement of the reaction (Bonnin, 1991; Cadena and Peter, 1988; Choppin and Faulkenberry, 1937). Sulfide (oxidation degree -2) is firstly oxidized into sulfur (degree of oxidation 0) which can be further oxidized into thiosulfate (degree of oxidation +2) sulfite (degree of oxidation +4) and sulfate (degree of oxidation +6) depending on the pH and the residual chlorine concentration (Choppin and Faulkenberry, 1937). Sulfite is directly oxidized in sulfate which requires one equivalent of chlorine for one equivalent of sulfite (Fogelmann et al., 1989). Consequently, at least one equivalent of chlorine is required for the production of sulfur as end-product (Eq. 5) whereas 4 equivalents are necessary for the production of sulfate (Eq. 6):

\[
\text{Eq. 5: } \quad \text{Na}_2\text{S} + \text{NaOCl} + \text{H}_2\text{O} \rightarrow \text{S} + \text{NaCl} + 2 \text{NaOH}
\]

\[
\text{Eq. 6: } \quad \text{Na}_2\text{S} + 4 \text{NaOCl} \xrightarrow{\text{complete oxidation}} 4 \text{NaCl} + \text{Na}_2\text{SO}_4
\]

Few studies focus on hydrogen sulfide chlorination due to the high kinetic rates observed, the complex chemistry of these species and the difficulty to analyze sulfur compounds properly. The kinetics of the H₂S oxidation in alkaline solutions has been investigated by Bonnin (1991) through reactive absorption. Using a gas-liquid contactor and
an excess of sodium hypochlorite in solution, Bonnin determined an apparent kinetic constant of $1.8 \times 10^8$ L mol$^{-1}$ s$^{-1}$ between pH 9 and 11 and confirmed that the kinetics is very fast. This determination did not take both chlorine and sulfide speciations into account. Moreover, Biard et al. (2010) demonstrated that Bonnin used a wrong assumption when he neglected the gas-phase resistance to simplify the absorption rate. In 2010, considering the results of field chemical scrubbing experiments, Biard et al. assessed that the apparent kinetic constant at alkaline pH below 10.5 could reasonably range between $10^6$ and $10^9$ L mol$^{-1}$ s$^{-1}$. Deborde and Von Gunten (2008) proposed a kinetic constant for the specific reaction of HS$^-\,$ with ClOH very close to that of sulfite ions in the range $10^8$-$10^9$ L mol$^{-1}$ s$^{-1}$. This determination was based on the HS$^-\,$ nucleophilicity assuming a chlorine electrophilic attack similar to those previously described for halides or other anionic inorganic compounds ($\mathrm{SO}_3^{2-}$, I$^-$, Br$^-$, Cl$^-$, and CN$^-\,$). The specific kinetic constants of H$_2$S reactions with ClO$^-$ ($k = 6.75 \times 10^6$ L mol$^{-1}$ s$^{-1}$) and ClOH ($k = 1.62 \times 10^5$ L mol$^{-1}$ s$^{-1}$) have been studied by reactive absorption in a gas-liquid contactor (Vilmain et al., 2014). The surprising larger value found with ClO$^-\,$ was justified by a two steps mechanism (acid base reaction between H$_2$S and ClO$^-\,$ followed by direct oxidation between ClOH + HS$^-\,$). Therefore, these kinetic constants are apparent and probably overestimate the true values. To satisfactorily design and understand chemical scrubbers applied to H$_2$S treatment, a good knowledge of the kinetics and mechanism of oxidation is necessary. Due to the absence of accurate kinetic data, the scrubbers’ design is largely based on the feedback from existing plants more than on a precise demonstration. The goal of this study is then to extend the study of Vilmain et al. (2014) through the determination of the kinetic constant between HS$^-\,$ and ClOH/ClO$^-\,$ and to be able to calculate the kinetic rate of hydrogen sulfide chlorination in a rather large pH range at T = 298 K. The competitive kinetics method has
been selected. This method has been successfully applied to determine large kinetic constants, especially in the ozonation field (Beltrán, 2004; Biard et al., 2011; Hoigne and Bader, 1983) and is based on the comparison of the consumptions by free chlorine of the target compounds (H$_2$S) and a reference compound whose kinetic constant is known. The sulfite anion SO$_3^{2-}$ was selected as the reference compound since its kinetic rate should be close to sulfide kinetic rate in a rather large pH range considering that their nucleophilicities (i.e. their kinetic constants) are similar (Deborde and Von Gunten, 2008). Moreover, the sulfite oxidation mechanism is very simple since 1 equivalent of chlorine is consumed to oxidize directly 1 equivalent of sulfite into sulfate and its oxidation kinetics has been deeply investigated at T = 298 K (Fogelman et al., 1989).
2. MATERIALS AND METHODS

2.1. Experimental method

The competitive kinetics method was applied to determine the H$_2$S chlorination kinetics using the sulfite anion SO$_3^{2-}$ as the reference compound. The chlorination of both pure compounds (sulfite and sulfide) was carried out previously to find out the apparent stoichiometries for each compound depending on the initial concentrations. Both chlorinations were performed in a 100 mL gas-tight syringe (Hamilton) whose needle was replaced by a septum allowing to quickly withdraw and inject samples. A stir bar was placed in the syringe for the subsequent mixing. As mentioned by Biard et al. (2011), this kind of reactor is headspace free to avoid H$_2$S volatilization as well as oxygen dissolution which can consume sulfite anions. Moreover, its volume varies when sampling due to the plunger course which enables to keep a constant pressure inside the reactor.

Fig. 1: Presentation of the experimental method.

A schematic representation of the protocol is illustrated in Fig. 1. All solutions were prepared using Ultra Pure Water (UPW) prepared by reverse osmosis using an Elga lab purification unit (resistivity > 18 MΩ cm). UPW was deoxygenated by N$_2$ (99.999% with maximum 2 ppmv of residual O$_2$, provided by Air Liquide) bubbling. To avoid SO$_3^{2-}$ oxidation by O$_2$, the sulfite solution was prepared directly in the reactor by adding sodium sulfite. Then 100 mL of UPW was added to dissolve it. 90 mL of this solution were drained to keep only 10 mL. Then, 3mL of a sulfide solution, a buffer solution and UPW until 98.4 mL were added with gas-tight glass syringes (SGE, Australia). Reaction solutions were buffered for experiments at pH 6, 7, 7.5 and 8. For pHs 9-12, the initial pH was set by adding NaOH. The
syringe was held horizontally in a thermostatic bath regulated at 25 °C ± 0.2. After 20 min, 1 mL of chlorine solution was injected in the reactor using a gas-tight syringe (from SGE). Then, after 2 min of stirring (assuming oxidation is achieved) and complete chlorine consumption, 0.6 mL of ethanol (99% purity) was injected in the reactor to stabilize the sulfite ions in the aqueous solution before analyses (de Carvalho and Schwedt, 2000).

We note that sulfite and sulfide can react together to form thiosulfate. This reaction is slow and does not happen during the short time between the mixture preparation and the chlorine injection.

2.2. Analytical methods

The pH was controlled directly after each experiment by a pH-meter type Eutech Instruments Cyberscan 510 (±0.01 pH unit tolerance) equipped with a Fisher Scientific probe. The pH variation due to chlorine addition was found negligible in all cases. The sulfite anions were analyzed using ion chromatography (§ 2.2.2). Since HS⁻ and SO₃²⁻ have the same retention time, H₂S was previously stripped from a sample of the solution set at neutral pH by N₂ bubbling.

2.2.1. Hydrogen sulfide analysis

The methylene blue spectrophotometric method has been evaluated and recommended by various researchers for sulfide quantification (Fogo and Popowsky, 1949; Reese et al., 2011). N,N-Dimethyl-1,4-phenylenediamine (DMPD) reacts with hydrogen sulfide to form a compound which changes into blue leucomethylene. This compound, oxidized under acidic conditions in the presence of an oxidant (usually Fe(III)), forms methylene blue. This method was used in combination with the standard addition method for a higher accuracy of H₂S measurement. The limit of quantification and detection are
approximately 0.3 ppm and 0.1 ppm. Statistic methods validated the repeatability, reproducibility and the reliability of the method.

2.2.2. Determination of the sulfite and sulfate anions’ concentrations by ionic chromatography

Dionex-DX 120 Ion Chromatography, equipped with IonPac® AG 18 (4 mm × 50 mm) guard column and AS18 analytical column (4 mm × 250 mm), was used for SO$_3^{2-}$ quantification. Filtered samples (syringe filter with prefiter Minisart from Sartorius, membrane: cellulose acetate; threshold: 0.45 µm) were injected (250 µL samples). KOH eluent (flow rate of 1.06 mL min$^{-1}$) was degassed by vacuum and produced electrochemically in-line. Ramped eluent concentration was used with 10 mmol L$^{-1}$ (0-10 min), 10-45 mmol L$^{-1}$ (10-25 min) and 45 mmol L$^{-1}$ (25-35 min). Data acquisition was performed by Chromeleon software. The resolution between sulfate and sulfite peaks was equal to 1.6.

Sulfite is easily oxidizable and is particularly unstable in the presence of oxygen. This oxidation was prevented before the reaction step by preparing the sulfite solution in the 100 mL syringe with deoxygenated water. Only a small amount of O$_2$ can dissolve in the solution during the sample preparation prior to ionic chromatography. Therefore, ethanol was selected to stabilize the sulfite anions immediately after the reaction (de Carvalho and Schwedt, 2000). Using non-deoxygenated UPW, the sulfite anion concentration decreases quickly (38.0% of recovery after 350 min) whereas using deoxygenated UPW in the syringe enabled this phenomenon to be limited. An ethanol concentration of 0.1 mol L$^{-1}$ is necessary to achieve a negligible sulfite consumption (99.4% of recovery after 350 min).
2.2.3. Chlorine analysis

Chlorine was measured after sampling using the iodometric method. 5 mL of glacial acetic acid and 1 g of potassium iodide was added to the sample. Thereafter, the sample was titrated with 0.1 M or 0.001 M sodium thiosulfate (Normadose® VWR).

2.3. Reagents

All chemical products had an analytical grade. Sodium sulfide nonahydrate, sodium sulfite, sodium thiosulfate, sodium hypochlorite, potassium hydrogen phthalate, potassium sulfate, acetic acid, absolute ethanol and acetone were purchased from Acros Organics (Belgium). Sodium hydroxide was purchased from Fischer Scientific, potassium iodate from Labogros, potassium dihydrogen phosphate from Panreac Quimica, and tris-(hydroxymethyl)aminomethane from Merck. Hydrochloric acid was obtained from Prolabo. Hydrochloric acid (0.01, 0.1, 1 M) was prepared using Analar Normapur® solutions. The hydrogen sulfide solutions were prepared daily by serial dilutions.

Buffer solutions were prepared by dissolving appropriate amounts of three chemical products in Ultra Pure Water: potassium hydrogen phthalate, potassium dihydrogen phosphate and (hydroxymethyl)aminomethane completed with HCl or NaOH.
3. RESULTS AND DISCUSSION

3.1. Chlorination of the pure compounds: determination of the apparent stoichiometries

The apparent stoichiometric coefficients, \( \delta \) and \( \gamma \), of the reactions between sulfite and sulfide anions with chlorine at 25°C were determined through the chlorination of each pure compound:

\[
\text{Na}_2\text{S} + \delta \text{NaOCl} \rightarrow \text{products} \tag{7}
\]

\[
\text{Na}_2\text{SO}_3 + \gamma \text{NaOCl} \rightarrow \text{products} \tag{8}
\]

\( \delta \) and \( \gamma \) were calculated from the \( \text{Na}_2\text{S} \) and \( \text{NaOCl} \) consumptions by chlorine:

\[
\delta = \frac{[\text{NaOCl}]_{t=0} - [\text{NaOCl}]_{\text{final}}}{[\text{Na}_2\text{S}]_{t=0} - [\text{Na}_2\text{S}]_{\text{final}}} \tag{9}
\]

\[
\gamma = \frac{[\text{NaOCl}]_{t=0} - [\text{NaOCl}]_{\text{final}}}{[\text{Na}_2\text{SO}_3]_{t=0} - [\text{Na}_2\text{SO}_3]_{\text{final}}} \tag{10}
\]

\( \delta \) and \( \gamma \) were determined for different pH and different ratio of the initial reagents' concentrations, \( R_{\text{sulfide}} \) and \( R_{\text{sulfite}} \), defined as:

\[
R_{\text{sulfide}} = \frac{[\text{Na}_2\text{S}]_{t=0}}{[\text{NaOCl}]_{t=0}} \tag{11}
\]

\[
R_{\text{sulfite}} = \frac{[\text{Na}_2\text{SO}_3]_{t=0}}{[\text{NaOCl}]_{t=0}} \tag{12}
\]

In the one hand, in excess of oxidant (low \( R_{\text{sulfide}} \)), the oxidation was almost complete and around 4 equivalents of chlorine were consumed for 1 equivalent of sulfide whatever the pH in agreement with the reaction 5 (Fig. 2). Sulfate was the end-product of
the oxidation (Choppin and Faulkenberry, 1937) which was confirmed by the detection of sulfate anions by ionic chromatography. In the other hand, when sulfide was in sufficient excess ($Ra_{sulfide} > 3$), the oxidation was restricted to the parent compound. One equivalent of chlorine was consumed for one equivalent of sulfide ($\delta = 1$) improving the selectivity of the reaction. Indeed, in this case, the end-product should be only sulfur which is in agreement with the literature (Choppin and Faulkenberry, 1937). Moreover, no sulfite and sulfate anions were detected by ionic chromatography. Consequently, to ensure no sulfite anions produced during sulfide anion oxidation and no interaction during mixture experiments, $Ra_{sulfide}$ must be larger than approximately 3. The pH seems to have a slight effect only when the initial chlorine concentration was larger than the sulfide anion concentration.

Otherwise, since sulfite anions is directly oxidized into sulfate anions, which cannot be further oxidized by chlorine (Fogelmann et al., 1989), one equivalent of chlorine was consumed for one equivalent of sulfite ($\gamma = 1$), whatever the value of $Ra_{sulfite}$ applied (Fig. 2). The rather large dispersion of the points around 1 is due to the quite low sulfite anion analytical methods precision (sulfite instability in solution). This low precision has no influence in the competitive kinetics method results analysis (section 3.2).

**3.2 Chlorination of sulfide/sulfite anion mixtures: determination of the relative apparent kinetic constant**

Chlorination of the sulfide/sulfite mixture was performed between pH 6 and 12. Each experiment was triplicated with $Ra_{sulfite} \approx 1.5$ and $Ra_{sulfide} \approx 2.7$. These ratios were optimal to accurately measure the sulfite and sulfide consumptions and to optimize the sulfide oxidation selectivity. Chlorine was the limiting reagent and was not detected at the end of each experiment.
Since the consumptions of the three species were measured, the mass balance could be checked. According to Eqs 9 and 10:

$$\left[\text{NaOCl}\right]_{t=0} - \left[\text{NaOCl}\right]_{\text{final}} = \delta \left[\left[\text{Na}_2\text{S}\right]_{t=0} - \left[\text{Na}_2\text{S}\right]_{\text{final}}\right] + \gamma \left[\left[\text{Na}_2\text{SO}_3\right]_{t=0} - \left[\text{Na}_2\text{SO}_3\right]_{\text{final}}\right]$$  \hspace{1cm} (13)

**Figure 3: Sulfite and sulfide consumptions ($\Delta[i]$) during competitive kinetics trials.**

The oxidation removal efficiencies of sulfite and sulfide were in the range 10-25% and were significantly measurable. Figure 3 presents a histogram of the average consumed concentrations ($\Delta[i]$) of hydrogen sulfide and sulfite for each pH studied. The mass balance was well respected by taking $\gamma$ and $\delta = 1$, except at pH 10 at which a lower sulfide and/or sulfite consumption was measured.

Assuming that partial orders are equal to 1 (Deborde and von Gunten, 2008), the ratio of the kinetic constants $k_{\text{relative}}$, can be written as (Beltrán, 2004; Biard et al., 2011):

$$k_{\text{relative,1}} = \frac{k_{\text{app sulfite}}}{k_{\text{app sulfide}}} = \frac{\delta}{\gamma} \left(\frac{\ln \left[\text{Na}_2\text{S}\right]_{t=0}}{\left[\text{Na}_2\text{S}\right]_{\text{final}}} - \frac{\ln \left[\text{Na}_2\text{SO}_3\right]_{t=0}}{\left[\text{Na}_2\text{SO}_3\right]_{\text{final}}}\right)$$  \hspace{1cm} (14)

Equation 14 can be used by knowing just the concentrations of the two target compounds (i.e. the initial oxidant concentration is not required). In this study, the oxidant concentration was also measured, enabling to calculate $k_{\text{relative}}$ by two additional equations deduced from the mass balance equation (Biard et al., 2011):

$$k_{\text{relative,2}} = \frac{k_{\text{app sulfite}}}{k_{\text{app sulfide}}} = \frac{\delta}{\gamma} \left(\frac{\ln \left[\text{Na}_2\text{S}\right]_{t=0}}{\left[\text{Na}_2\text{S}\right]_{\text{final}}} - \frac{\ln \left[\text{Na}_2\text{SO}_3\right]_{t=0}}{\left[\text{Na}_2\text{SO}_3\right]_{\text{final}}}\right)$$  \hspace{1cm} (15)
\[
\begin{align*}
276 & \quad k_{\text{relative},3} = \frac{k_{\text{sulfide}}}{k_{\text{sulfite}}^{\text{app}}} = -\frac{\delta}{\gamma} \left( \frac{[\text{Na}_2S]_{t=0} - [\text{NaOCl}]_{t=0} + [\text{Na}_2\text{SO}_3]_{t=0} - [\text{Na}_2\text{SO}_4]_{\text{final}}}{\ln \left( \frac{[\text{Na}_2\text{SO}_3]_{t=0}}{[\text{Na}_2\text{SO}_4]_{\text{final}}} \right)} \right) \\
\end{align*}
\]

\( k_{\text{relative}} \) obtained with the three methods and the average value at constant temperature (25±0.2 °C) is shown in Fig. 4. Except at pH = 10, the values of \( k_{\text{relative}} \) found were close whatever the equation used since the mass balance was well respected. At pH = 10, a stronger dispersion was observed but the average value was consistent with the value obtained by Eq. 14 like the other values of pH. Consequently, the average value of \( k_{\text{relative}} \) is reliable. Depending on the pH, \( k_{\text{relative}} \) is in the range 1-2 confirming that sulfite and sulfide oxidation kinetic rate are close, even at pH close to the neutrality, at which acidic species (\( \text{H}_2\text{S}, \text{HSO}_3^- \)) are present and can bias this observation. Indeed, according to Deborde and Von Gunten (2008), \( \text{HS}^- \) and \( \text{SO}_3^{2-} \) oxidation kinetic rates are expected to be similar but no data are available for \( \text{H}_2\text{S} \) and \( \text{HSO}_3^- \) ones. The trend of Fig. 4 remains complicated to justify since many chemical reactions are \textit{a priori} involved. The next section focuses on sulfite oxidation kinetic rate analysis prior to sulfide kinetic rate determination.

\textit{Figure 4: Effect of pH on the } \( k_{\text{relative}} \) \textit{values determined with equations 14-16 and the average value of } \( k_{\text{relative}} \). \textit{The error bars represent the standard deviations.}

\subsection*{3.3 Sulfite oxidation kinetics}

The sulfite anion is a basic species in equilibrium with the hydrogen sulfite (\( \text{HSO}_3^- \)). The apparent pK\(_a\) value is included in the range 6.91-7.2 at 298 K, depending on the hydrogen sulfite concentration since \( \text{HSO}_3^- \) exists in two tautomeric forms (Rhee and Dasgupta, 1985). At low sulfite concentration (< 10\(^{-4}\) L mol\(^{-1}\) s\(^{-1}\)), pK\(_{a,5}\) = 6.91. \( \text{H}_2\text{SO}_3 \) (\( \text{H}_2\text{O} + \text{SO}_3 \)) is present only at very acidic pH and is neglected in this discussion. The oxidation mechanism of the sulfite anion with chlorine involves \textit{a priori} several acid-base (Reactions 17...
to 21) and oxidation reactions (Reactions 22 to 24) synthesized Table 1. The potential reaction between ClO$^-$ and HSO$_3^-$ has not been considered since it involves a weak base and a weak acid whose coexistence in solution is unlikely. Moreover, the kinetic rate of this reaction should be low since ClO$^-$ and HSO$_3^-$ are respectively poorer electrophile and nucleophile than ClOH and SO$_3^{2-}$ (Fogelman et al., 1989). Fogelman et al. determined the kinetic constants of reactions 22 and 23 using the stopped-flow method at 298 K (Fogelman et al., 1989). Even if hypochlorous acid (ClOH) does not predominate at pH > 7.54, since $k_{23}$ $>>$ $k_{22}$, sulfite anion is more oxidized by ClOH than ClO$^-$ for pH < 12-12.1. Their study was conducted at pH > 9.5, at which reaction 24 which involves two acids is unexpected and unfortunately $k_{24}$ is unknown. For the rest of the discussion, this reaction was neglected since HSO$_3^-$ should be less reactive than SO$_3^{2-}$ and the study was mainly conducted in the pH range (> 6.91-7.2) at which SO$_3^{2-}$ is predominant. This assumption will be confirmed in the section 3.2.5. Kinetic constants of bimolecular proton transfer reactions (Eqs 17 to 21) are not precisely known. According to Eigen (1964), the orders of magnitude of the kinetic constants for recombination of a base with H$^+$ (reverse reactions 18 and 20) and of an acid with HO$^-$ (Reactions 17 and 19) are respectively typically $10^{10}$-$10^{11}$ and $10^{9}$-$10^{11}$ L mol$^{-1}$ s$^{-1}$ (Eigen, 1964). The ratio of them for a given acid/base couple is between 2 and 3 in many cases. Fogelman et al. used with a good agreement a value of $k_{17} = 3 \times 10^9$ L mol$^{-1}$ s$^{-1}$ in their simulations (Fogelman et al., 1989). Taking this into consideration, $k_{17}$, $k_{18}$, $k_{19}$ and $k_{20}$ are respectively set to the values presented in Table 1. The rather large value of $k_{20}$ has been chosen equal to $k_{30}$ by analogy (H$_2$S dissociation, Table 5). Considering that $pK_{a,4}$-$pK_{a,5}$ $\approx$ 0.5, $k_{21}$ can be set to $3 \times 10^8$ L mol$^{-1}$ s$^{-1}$ according to Eigen (1964).

In a batch reactor, at constant temperature and volume, the kinetic law of total sulfite consumption can be written:
\[
\frac{d[SO_3^{2-}]}{dt} = \frac{d[SO_3^{2-}]}{dt} - \frac{d[HSO_3^{-}]}{dt} = \frac{d[ClO^{-}]}{dt} - \frac{d[ClOH]}{dt}
\]  
(25)

\[
\frac{d[SO_3^{2-}]}{dt} = k_{22} [SO_3^{2-}] [ClO^{-}] + k_{23} [SO_3^{2-}] [ClOH]
\]  
(26)

The kinetic rate of this reaction was expected to decrease with the pH since the hypochlorous acid concentration decreased. The temptation is high to consider that both acid/base couples are in equilibrium to introduce the total sulfite and hypochlorite concentrations and the pK_a values:

\[
\frac{d[SO_3^{2-}]}{dt} = k_{app}^{sulfite} \times [SO_3^{2-}] [ClO^{-}]_T
\]  
with
\[
k_{app}^{sulfite} = \frac{k_{23}}{(1+10^{\Delta pH-k_{a,SO}})(1+10^{\Delta pH-k_{a,ClOH}})}
\]  
(27)

With this assumption, at a constant pH, the kinetics is second-order with a calculated apparent kinetic constant \(k_{app}^{sulfite}\) (whose evolution versus the pH is represented in Fig. 5). The subscripts “cal” means that \(k_{app}\) has been calculated through Eq 27. Then, the chlorine and the sulfite concentration-time profiles can be determined by Eq. 28, which is the classical solution of the differential equation for a second-order kinetics in a batch reactor:

\[
T = k_{app}^{sulfite} \times t \quad \text{with} \quad T = \frac{1}{[ClO^{-}]_{T,0} - [SO_3^{2-}]_{T,0}} \ln \frac{[SO_3^{2-}]_{T,0}}{[ClO^{-}]_{T,0}}
\]  
(28)

Fig. 5: Effect of pH on \(k_{app,cal}\) for sulfite and sulfide oxidations. \(k_{app,cal}\) was calculated with Eq. 27 and 38 whereas \(k_{app,sim}\) was calculated through the numerical simulations (using the conditions of Table 2). The blue and green areas delimit zones where \(k_{app}\) for respectively sulfite and sulfide should be located for a wide range of experimental conditions.
Equation 27 implies that proton transfer reactions (reactions 17 to 21) are instantaneous compared to oxidation reactions to maintain sulfite and chlorine species equilibrium over all times. This assumption can be controversial, especially at pH close to the neutrality, where the kinetic rate is maximal. To assess it, the concentration-time profile of each species involved in reactions 17 to 23 has been determined using the software COPASI developed by the Virginia Bioinformatics Institute (USA) and the universities of Heidelberg (Germany) and Manchester (UK). This open-source software is dedicated to the numerical resolution of differential equations systems found in biological and chemical kinetics.

Examples of concentration-time and reaction rate-time profiles returned by COPASI are presented in appendix. An analytical solution is not possible, especially since steady-state approximations (Bodenstein) are not possible. HO⁻ and H⁺ concentrations have been fixed to their initial values since a buffer is added to maintain a constant pH (except at pH ≥ 9 at which it is not necessary). Different operating conditions (pH, total sulfite and chlorine concentrations) have been applied to assess their influence. For each simulation, the time course is discretized into 500 intervals until a degree of advancement of 90% is reached (t₉₀ is the corresponding time). The term T (Eq. 28) can be calculated during the data post processing. Then a linear regression model using the time series data is applied (using the “Linest” function of Excel®):

- to check if the kinetic rate is second-order (using appropriated statistic criteria such as the determination coefficient R² and the F-test value);
- if so, to determine the apparent 2nd order kinetic constants (called k_{app, sim}) from the slope;
- to compare k_{app, sim} and k_{app, cal}. 

Tables 2, 3 and 4 synthesize the results to assess respectively the influence of the pH (at the chlorine and sulfite initial concentrations used in the section 3.2.2), the order of magnitude of the initial concentrations and the initial concentrations ratio (Tables 3 and 4 simulations were performed at pH 8 since it is the pH which presents the largest discrepancy between $k_{app,cal}$ and $k_{app,sim}$). Except for a few limited cases (Simulations #11 and #15), the reaction was predicted to follow second-order kinetics. At pH lower than 10, $k_{app,sim}$ was always lower than $k_{app,cal}$ (Table 2), which emphasizes that the kinetic rate was limited by proton transfer reactions. Fig A.2 clearly highlights that the ClOH consumption rate by reaction 23 was larger than its reformation rate due to reactions 17, 18 and 21. Even if ClOH and ClO$^-$ were in equilibrium at the beginning of the simulation, the ratio [ClOH]/[ClO$^-$] decreased with time whereas the pH stayed constant. Consequently, using Eq. 27 can lead to severe overestimations of the kinetic rate and by the way bias the results of the competitive study. For example, with the initial conditions of simulation #4, the time necessary to achieve a degree of advancement of 90 % using $k_{app,cal}$ was 0.46 ms, whereas the time simulated was 0.98 ms. This observation is particularly true for pH ranging between 7 and 9 where the kinetic rate is maximal. When the pH exceeds 10, the oxidation kinetic rate decreased and the ClOH consumption was more easily compensated, which enabled to maintain more easily the species equilibrium. In this case, the apparent kinetic constant calculated by Equation 27 was exact and the reaction time necessary to consume 90% of the limiting reagent (chlorine) increased beyond 1 s.

Even if the kinetic rate of the reaction increases with the initial concentrations ($t_{90}$ decreases), the value of $k_{app,sim}$ decreases (Table 3). Indeed, with larger initial concentrations, the HSO$_3^-$/SO$_3^{2-}$ equilibrium is more difficult to maintain since the kinetic rate is larger. By the way, $k_{app,sim}$ tends towards $k_{app,cal}$ when the initial concentration decreases. When sulfite...
is the limiting reagent (simulation #13), sulfite equilibrium is more difficult to maintain. The apparent kinetic constant is rather poorly influenced by the initial concentrations ratio (Table 4) except when chlorine is added in great excess. In this case, the kinetic rate is pseudo first-order, the chlorine species stay obviously at the equilibrium and the simulated apparent kinetic constant tends towards the calculated one.

Table 2

Table 3

Table 4
3.4 Sulfide oxidation kinetics

Table 5

As for the sulfite anions, the sulfide oxidation (Table 5) a priori involves several acid-base reactions (17, 18 and 29 to 31) and pure oxidation reactions (32 to 34). Only the first oxidation step which leads to elemental sulfur was considered since the initial concentrations ratio ($R_a^{sulfide}$) was carefully selected. Moreover, in the pH range studied (6-12), $S^{2-}$ can be neglected. Based on these assumptions, the kinetic law of total sulfide consumption can be written:

$$\frac{d[H_2S]_T}{dt} = \frac{d[H_2S]}{dt} - \frac{d[HS^-]}{dt} = \frac{d[ClO^-]}{dt} - \frac{d[ClOH]}{dt}$$

(36)

$$\frac{d[H_2S]_T}{dt} = k_{32}[H_2S][ClO^-] + k_{33}[H_2S][ClOH] + k_{34}[HS^-][ClO^-] + k_{35}[HS^-][ClOH]$$

(37)

If chlorine and sulfide species are in equilibrium with their respective conjugated species, then:

$$\frac{d[H_2S]_T}{dt} = k_{app,calc}[H_2S][ClO^-]$$

(38)

With $k_{app,calc} = \frac{k_{32}}{\left(1 + 10^{pK_{app,calc}} \right) \left(1 + 10^{pH - pK_{app,calc}} \right) \left(1 + 10^{pH - pK_{app,calc}} \right)} + \frac{k_{33}}{\left(1 + 10^{pK_{app,calc}} \right) \left(1 + 10^{pH - pK_{app,calc}} \right) \left(1 + 10^{pH - pK_{app,calc}} \right)} + \frac{k_{34}}{\left(1 + 10^{pK_{app,calc}} \right) \left(1 + 10^{pH - pK_{app,calc}} \right) \left(1 + 10^{pH - pK_{app,calc}} \right)} + \frac{k_{35}}{\left(1 + 10^{pK_{app,calc}} \right) \left(1 + 10^{pH - pK_{app,calc}} \right) \left(1 + 10^{pH - pK_{app,calc}} \right)}$

(39)

For the sulfite oxidation, $k_{app,calc}$ and $k_{app,sim}$ are equal only for pH 11 and 12 (Table 2).

Consequently, $k_{relative}$ should be used to study the sulfide oxidation only at these pH. $k_{app,exp}$ for the sulfite oxidation can be extrapolated from $k_{relative}$ (Eqs 14-16) and $k_{sulfite,app,calc}$ (Eq. 27):

$$k_{app,exp} = k_{relative} \times k_{sulfite,app,calc}$$

(39)
At these pHs, it is quite obvious that reactions 32 and 34 are unlikely. Then, $k_{33}$ and $k_{35}$ can be determined by numerical resolution trying to minimize the following least square objective function:

$$\text{Min}(F_i \text{ at pH }= 11 + F_i \text{ at pH }= 12) \quad \text{With } F_i = \left( \frac{k_{\text{app,exp}} - k_{\text{app,cal}}}{k_{\text{app,exp}}} \right)^2$$

An excellent agreement is obtained with $k_{35} = 1.2 \times 10^9$ L mol$^{-1}$ s$^{-1}$ when the value of $k_{33}$ can be set between 0 and $10^4$ L mol$^{-1}$ s$^{-1}$ with a very restricted influence (Table 6). In Table 6, $R_{33}$ represents the following ratio:

$$R_{33} = \frac{k_{33}}{1 + 10^{pH-pK_{33}}} \cdot \frac{k_{\text{app,cal}}}{1 + 10^{pH-pK_{\text{app,cal}}}}$$

It confirms the order of magnitude proposed by Deborde and von Gunten (2008) but invalidated, as expected, the value determined by Bonnin (1991). The very weak sensitivity of the model to $k_{33}$ emphasizes that reaction 33 (sulfide oxidation by hypochlorite anion) is unlikely or very limited, at least at pH ≤ 12, even if the ClOH concentration is low at basic pH. Consequently, the value of $k_{33}$ cannot be determined with a sufficient confidence degree. It justifies why $k_{\text{relative}}$ is larger than 1 at pH 11 but lower than 1 at pH 12. Indeed, at pH 12, sulfite is oxidized simultaneously by ClO- and ClOH.

Using the same methodology than for sulfite (section 3.2.3), it is possible to determine $k_{\text{app,sim}}$ for sulfide and to try to compare it to $k_{\text{app,cal}}$ (Table 7 and Fig. 5). The same main conclusions apply for both compounds. The sulfide oxidation is limited by acid-base reactions (17, 18, 29-31) at pH lower than 10, especially when pH ranges between 6 and 9. Therefore, it confirms that it was pertinent to use only the results obtained at pH 11 and 12 to determine $k_{35}$ by numerical resolution. The simulation at pH 6 (simulation #16) demonstrates that reactions 32 and 34 can be neglected whatever the pH. Indeed, the
reaction rate of reaction 32 does not exceed 2% of the reaction rate of reaction 35 (obtained through simulations) when reaction 34 is absolutely negligible.

Table 6

Table 7

3.5 Discussion

$k_{35}$ was calculated using $k_{\text{relative}}$ at pH 11 and 12. When the pH ranges between 6 and 11, the experimental value of $k_{\text{relative}}$ follows a very special trend. Using the values of $k_{\text{app,cal}}$ (Eqs 27 and 38) and $k_{\text{app,sim}}$ (Tables 2 and 7), $k_{\text{relative}}$ can be recalculated twice and compared to the experimental value ($k_{\text{relative,exp}}$):

$$k_{\text{relative,cal}} = \frac{k_{\text{app,cal}}}{k_{\text{sulfide}} k_{\text{app,cal}}}$$  \hspace{1cm} (42)

$$k_{\text{relative,sim}} = \frac{k_{\text{app,sim}}}{k_{\text{sulfide}} k_{\text{app,sim}}}$$  \hspace{1cm} (43)

Figure 6: Comparison between the experimental $k_{\text{relative}}$ values and the calculated and simulated ones.

On the one hand, the value of $k_{\text{relative,cal}}$ is totally in disagreement with $k_{\text{relative,exp}}$ (Fig. 6). This result was expected since $k_{\text{app,cal}}$ is determined assuming that acid-base species stays at the equilibrium, which is not valid at pH lower than 10. On the other hand, the value of $k_{\text{relative,sim}}$ follows the same trend than $k_{\text{relative}}$ at basic pH which is probably not a coincidence. The agreement remains imperfect but one has to consider that $k_{\text{relative}}$ suffers from experimental uncertainties whereas $k_{\text{app,sim}}$ is calculated with estimated values of the kinetic constants of numerous acid-base reactions. Moreover, there is a potential uncertainty concerning $pK_{a,5}$.

Table 8
Before going further, several questions need to be discussed and assumptions have to be confirmed:

- \( k_{\text{relative,sim}} \) and \( k_{\text{relative,exp}} \) present an interesting correlation. However, the values of \( k_{\text{app,sim}} \) are determined with estimated values of the different acid-base reactions (17-21 and 29-31). What is the sensitivity of the values of \( k_{\text{app,sim}} \) to these estimated kinetic constants? To answer to this question, \( k_{\text{app,sim}} \) for sulfite and sulfide have been recalculated at pH 6 with underestimated and overestimated values of the kinetic constants (Table 8). On the one hand, the results demonstrate that \( k_{\text{app,sim}} \) is not so sensitive to these values (especially for sulfide). At least, it does not change the conclusions of the numerical resolutions. The most influential kinetic constants are those of reactions 21 and 31. On the other hand, the influence on \( k_{\text{relative,sim}} \) is rather important (\( k_{\text{relative,sim}} = 1.81 \) and 1.26 respectively using simulations 24+26 and 25+27) and can justify the disagreement observed at this pH between \( k_{\text{relative,exp}} \) and \( k_{\text{relative,sim}} \).

- The potential reactions between ClOH and ClO\(^-\) and S\(^2-\) were neglected; this hypothesis required to be discussed more deeply. A possible influence of these two reactions is expected only at very basic pH. Concerning the reaction between ClOH and S\(^2-\), their respective predominance domains are far apart. By the way, assuming a probably overestimated kinetic constant of \( 5 \times 10^9 \) L mol\(^{-1}\) s\(^{-1}\), \( k_{\text{app,cal}} \) at pH 12 goes from \( 4.2 \times 10^{-4} \) to \( 4.4 \times 10^{-4} \) L mol\(^{-1}\) s\(^{-1}\) which confirms that this reaction can be neglected at pH lower than 12. The potential reaction between S\(^2-\) and ClO\(^-\) involves species whose coexistence domains are concomitant. However, it would imply a collision between two weak bases whose one of them carries two negative charges and consequently which requires exceeding an important electrostatic repulsion force. With a probably overestimated value of the kinetic constants of \( 5 \times 10^5 \) L mol\(^{-1}\) s\(^{-1}\) (maximal order of magnitude encountered between
ClO\(^-\) and any species), \(k_{app,cal}\) goes from \(4.2 \times 10^4\) to \(5.0 \times 10^4\) L mol\(^{-1}\) s\(^{-1}\) at pH 12. It confirms that the reaction between ClO\(^-\) and S\(^2-\) is unlikely at least at pH lower than 12. Moreover, a low \(pK_a\) has been considered in this calculation (13.78 according to Stephens and Cobble (1971)) even if the most recent studies seem to confirm that this value is up to 17 at 298K (Migdisov et al., 2002).

- Reaction 24 was neglected between pH=6 and pH=12. This assumption must be demonstrated. It involves two weak acids with compatible predominance domains. Simulation #1 (pH=6) performed with this additional reaction provides the following results:

\[ f \ k = 10^7 \text{ L mol}^{-1} \text{ s}^{-1}, \text{ the kinetic rate due to this reaction remains lower than 10\% compared to the kinetic rate of the reaction between ClOH and SO}_3^{2-}. \]

\[ f \ k = 10^8 \text{ L mol}^{-1} \text{ s}^{-1}, \text{ the kinetic rate due to this reaction exceeds the kinetic rate of the reaction between ClOH and SO}_3^{2-}. \text{ However, this order of magnitude remains unexpected regarding the value between SO}_3^{2-} \text{ and ClOH and considering that HSO}_3^- \text{ is less electrophilic. Moreover, in this case, a huge drop of } k_{relative} \text{ in Fig. 6 would have been observed at pH 6. Therefore, we can assume that the potential reaction between HSO}_3^- \text{ and ClOH can be neglected at pH larger than 6-7.} \]
CONCLUSIONS

Finding a reliable chemical oxidation method requires the knowledge of the reaction kinetics. The objective of this research was to assess the kinetics of sulfide oxidation by chlorine in a wide pH range (6-12). There are few reliable studies of this reaction studied in the literature, mainly because the large observed kinetic rates makes such studies difficult. The competitive kinetics method using sulfite as the reference compound has been selected. Speciations of chlorine, sulfite and sulfide is rather complex since it involves several acidic or basic compounds.

The results enable to determine the kinetic constant of the reaction between the hydrosulfide anion (HS⁻) and the hypochlorous acid (ClOH): $k_{35} = 1.2 \times 10^9 \text{ L mol}^{-1} \text{ s}^{-1}$ at 298 K.

This reaction is prevalent in the pH range 6-12 even if ClO⁻ is predominant over ClOH at pH > 7.54. The potential reactions between the hypochlorous acid and the conjugated acid (H₂S) and base (S²⁻) are unlikely. Moreover, the reaction between the hypochlorite anion (ClO⁻) and HS⁻ was confirmed as negligible. However, we cannot confirm that the reaction between ClOH and S²⁻ is unlikely at pH > 12.

Numerical simulations focused on both sulfite and sulfide oxidations demonstrated that oxidation rates are limited by the various acid base reactions whose kinetic rates are not sufficient to maintain the acid base pairs equilibria. Consequently, in the range pH=6-10, the true kinetic rate should be lower than the kinetic rate determined assuming that acid and base equilibriums are maintained during the oxidation.

The results of these simulations enable to correlate the result of the competitive method. Additionally to sulfide kinetics investigation, the results allowed to affirm that the potential reaction between HSO₃⁻ and ClOH is unlikely at least at pH > 6.
Study of the chlorination process at pH lower than 6 is even more complicated since,
depending on the total chloride concentration, Cl₂ can be found in solution which excludes
the possibility of working at such pH in chemical scrubbing to avoid Cl₂ desorption in the
treated gas.

In future, the influence of the sulfide oxidation kinetic rates in chemical scrubbing will
be assessed to develop a tool for scrubbers design as well as to understand deeper the
mechanism involved.
References


Appendix: concentration-time and reaction rate-time profiles

examples with the Software COPASI

Fig A.1: Concentration profile versus time for simulation 1 obtained with Copasi (Virginia Bioinformatics Institute (USA) and the universities of Heidelberg (Germany) and Manchester (UK)).
Fig A.2: Reaction rate profile versus time for simulation 1 obtained with Copasi (Virginia Bioinformatics Institute (USA) and the universities of Heidelberg (Germany) and Manchester (UK)). Negative fluxes are permitted for reversible reactions when the reverse reaction rate is larger than the forward one. Only the most significant reactions (17, 17, 19, 21, 23) have been represented for clarity.

Figs A.1 and A.2 were obtained using the simulation #4 conditions (pH = 8, see Table 2) which simulates the initial concentrations used with the competitive kinetics method.
Aim of the study

Unknown kinetics

Oxidant: chlorine (ClOH/ClO−)

Target: Sulfide (H₂S/HS−)

Reference: Sulfite (SO₃−)

Pure-compound oxidation

Apparent stoichiometry

Mixture oxidation

Sulfide oxidation kinetics determination

Pure-compound oxidation

Apparent stoichiometry

Known kinetics
Sulfide chlorination kinetics was studied using the competitive method

Sulfite was selected as the reference compound

The sulfide oxidation in the pH range 6-12 is mainly due to HS\(^{-}\) oxidation by ClOH

Kinetic constants between ClOH and HS\(^{-}\) is evaluated at 1.2×10\(^9\) L mol\(^{-1}\) s\(^{-1}\)

Numerical resolutions are performed to check the reliability
Figure 1

Sulfites
Magnetic stirring bar

Ultra pure water degassed

Residual chlorine analysis
Hydrogen sulfide analysis
Sulfite ions analysis at pH=7

Addition of chlorine and ethanol
Placed in a thermostated bath at 25 °C
Figure 2
Figure 3
Figure 4

![Graph showing the relationship between pH and relative rate constants. The graph plots pH on the x-axis ranging from 6 to 13 and relative rate constants on the y-axis ranging from 0.00 to 4.00. There are four distinct sets of data points, each represented by a different marker: red diamonds, blue diamonds, green triangles, and black squares. Each set includes error bars, indicating variability. The black line is a sigmoidal curve that connects the data points, suggesting a non-linear relationship between pH and relative rate constants.]
Figure 5
Table 1: Reactions involved in the sulfite oxidation mechanism. $K_\text{i}$ (equilibrium constants) and $k_\text{i}$ (kinetic constants) are reported at 298 K.

<table>
<thead>
<tr>
<th>Reaction</th>
<th>Eq (i)</th>
<th>$K_\text{i}$</th>
<th>$k_\text{i}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>ClOH + HO$^-$ $\xrightarrow{k_{17}}$ ClO$^- + H_2O$</td>
<td>(17) $10^{\Delta pK_w-pK_a,4} = 2.88 \times 10^6$</td>
<td>$k_{17} = 3 \times 10^7 \text{ L mol}^{-1} \text{ s}^{-1}$</td>
<td>$k_{17} = 1.0 \times 10^4 \text{ s}^{-1}$</td>
</tr>
<tr>
<td>ClOH $\xrightarrow{k_{18}}$ ClO$^- + H^+$</td>
<td>(18) $10^{\Delta pK_a,4} = 2.88 \times 10^8$</td>
<td>$k_{18} = 288 \text{ s}^{-1}$</td>
<td>$k_{18} = 10^{10} \text{ L mol}^{-1} \text{ s}^{-1}$</td>
</tr>
<tr>
<td>HSO$<em>3^-$ + HO$^-$ $\xrightarrow{k</em>{19}}$ SO$_3^{2-} + H_2O$</td>
<td>(19) $10^{\Delta pK_w-pK_a,5} = 1.23 \times 10^7$</td>
<td>$k_{19} = 2.5 \times 10^{10} \text{ L mol}^{-1} \text{ s}^{-1}$</td>
<td>$k_{19} = 2.3 \times 10^3 \text{ s}^{-1}$</td>
</tr>
<tr>
<td>HSO$<em>3^-$ $\xrightarrow{k</em>{20}}$ SO$_3^{2-} + H^+$</td>
<td>(20) $10^{\Delta pK_a,5} = 1.23 \times 10^7$</td>
<td>$k_{20} = 9.2 \times 10^3 \text{ s}^{-1}$</td>
<td>$b_{k_{20}} = 7.5 \times 10^{10} \text{ L mol}^{-1} \text{ s}^{-1}$</td>
</tr>
<tr>
<td>ClOH + SO$<em>3^{2-} \xrightarrow{k</em>{21}}$ ClO$^- + HSO$_3^-$</td>
<td>(21) $10^{\Delta pK_a,5 - pK_a,4} = 0.23$</td>
<td>$k_{21} = 3 \times 10^9 \text{ L mol}^{-1} \text{ s}^{-1}$</td>
<td>$k_{21} = 1.28 \times 10^9 \text{ L mol}^{-1} \text{ s}^{-1}$</td>
</tr>
<tr>
<td>ClO$^- + SO_3^{2-} \xrightarrow{k_{22}}$ SO$_4^{2-} + Cl^-$</td>
<td>(22) $K_{22} = 2.3 \times 10^4 \text{ L mol}^{-1} \text{ s}^{-1}$</td>
<td></td>
<td></td>
</tr>
<tr>
<td>ClOH + SO$<em>3^{2-} \xrightarrow{k</em>{23}}$ SO$_4^{2-} + Cl^- + H^+$</td>
<td>(23) $K_{23} = 7.6 \times 10^8 \text{ L mol}^{-1} \text{ s}^{-1}$</td>
<td>Assumed to be negligible at pH &gt; 6-7</td>
<td></td>
</tr>
<tr>
<td>ClOH + HSO$<em>3^-$ $\xrightarrow{k</em>{24}}$ SO$_4^{2-} + Cl^- + 2H^+$</td>
<td>(24)</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

---

1 $K_w$ is the water dissociation constant = $10^{-14}$ at 298 K.
2 (Eigen, 1964)
3 (Fogelman et al., 1988)
Table 2: Simulation results with $[\text{SO}_3^{2-}]_{T,0} = 5.0 \times 10^{-5} \text{ mol L}^{-1}$ and $[\text{ClO}^-]_{T,0} = 3.0 \times 10^{-5} \text{ mol L}^{-1}$ and various pH. The F-test value is determined with 500 degree of liberty.

<table>
<thead>
<tr>
<th>pH</th>
<th>Simulation number</th>
<th>$\text{SO}_3^{2-}/\text{HSO}_3^-$ equilibrium</th>
<th>$\text{ClO}^-/\text{ClOH}$ equilibrium</th>
<th>$t_90$ (s)</th>
<th>2$^{nd}$ order</th>
<th>$k_{app,sim}$ (L mol$^{-1}$ s$^{-1}$)</th>
<th>$R^2$</th>
<th>F-test value</th>
<th>$k_{app,sim}/k_{app,cal}$ (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td>6</td>
<td>1</td>
<td>70% of the time</td>
<td>Always</td>
<td>9.90×10$^{-4}$</td>
<td>Yes</td>
<td>7.56×10$^7$</td>
<td>1.000</td>
<td>1.42×10$^6$</td>
<td>93.4</td>
</tr>
<tr>
<td>7</td>
<td>2</td>
<td>40% of the time</td>
<td>No</td>
<td>2.72×10$^{-4}$</td>
<td>Yes</td>
<td>2.79×10$^8$</td>
<td>1.000</td>
<td>2.03×10$^7$</td>
<td>85.9</td>
</tr>
<tr>
<td>7.5</td>
<td>3</td>
<td>30% of the time</td>
<td>No</td>
<td>4.14×10$^{-4}$</td>
<td>Yes</td>
<td>1.76×10$^8$</td>
<td>0.999</td>
<td>3.53×10$^5$</td>
<td>55.8</td>
</tr>
<tr>
<td>8</td>
<td>4</td>
<td>35% of the time</td>
<td>No</td>
<td>9.82×10$^{-4}$</td>
<td>Yes</td>
<td>7.58×10$^7$</td>
<td>0.999</td>
<td>4.09×10$^5$</td>
<td>41.9</td>
</tr>
<tr>
<td>9</td>
<td>5</td>
<td>Always</td>
<td>No</td>
<td>4.68×10$^{-3}$</td>
<td>Yes</td>
<td>1.65×10$^7$</td>
<td>0.999</td>
<td>7.30×10$^5$</td>
<td>65.1</td>
</tr>
<tr>
<td>10</td>
<td>6</td>
<td>Always</td>
<td>No</td>
<td>3.10×10$^{-2}$</td>
<td>Yes</td>
<td>2.47×10$^6$</td>
<td>1.000</td>
<td>1.44×10$^7$</td>
<td>93.4</td>
</tr>
<tr>
<td>11</td>
<td>7</td>
<td>Always</td>
<td>Mainly</td>
<td>2.69×10$^{-1}$</td>
<td>Yes</td>
<td>2.84×10$^5$</td>
<td>1.000</td>
<td>1.32×10$^9$</td>
<td>99.3</td>
</tr>
<tr>
<td>12</td>
<td>8</td>
<td>Always</td>
<td>Always</td>
<td>1.55</td>
<td>Yes</td>
<td>4.93×10$^4$</td>
<td>1.000</td>
<td>3.69×10$^{11}$</td>
<td>100.0</td>
</tr>
</tbody>
</table>
Table 3: Simulation results at pH = 8 and various chlorine and sulfite concentrations keeping a constant ratio. The F-test value is determined with 500 degree of liberty.

<table>
<thead>
<tr>
<th>[SO$<em>3^{2-}$]$</em>{T,0}$ (mol L$^{-1}$)</th>
<th>5.0×10$^{-6}$</th>
<th>5.0×10$^{-5}$</th>
<th>5.0×10$^{-4}$</th>
<th>5.0×10$^{-3}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>[ClO$^-$]$_{T,0}$ (mol L$^{-1}$)</td>
<td>3.0×10$^{-6}$</td>
<td>3.0×10$^{-5}$</td>
<td>3.0×10$^{-4}$</td>
<td>3.0×10$^{-3}$</td>
</tr>
<tr>
<td>Simulation number</td>
<td>9</td>
<td>4</td>
<td>10</td>
<td>11</td>
</tr>
<tr>
<td>SO$_3^{2-}$/HSO$_3^-$ equilibrium</td>
<td>Always</td>
<td>35% of the time</td>
<td>No</td>
<td>No</td>
</tr>
<tr>
<td>ClO$^-$/ClOH equilibrium</td>
<td>No</td>
<td>No</td>
<td>No</td>
<td>No</td>
</tr>
<tr>
<td>$t_{90}$ (s)</td>
<td>5.48×10$^{-3}$</td>
<td>9.82×10$^{-4}$</td>
<td>2.66×10$^{-4}$</td>
<td>1.75×10$^{-4}$</td>
</tr>
<tr>
<td>2$^{nd}$ order</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Almost</td>
</tr>
<tr>
<td>$k_{app,sim}$ (L mol$^{-1}$ s$^{-1}$)</td>
<td>1.38×10$^{8}$</td>
<td>7.58×10$^{7}$</td>
<td>2.7×10$^{7}$</td>
<td>3.96×10$^{6}$</td>
</tr>
<tr>
<td>$R^2$</td>
<td>1.000</td>
<td>0.999</td>
<td>0.980</td>
<td>0.950</td>
</tr>
<tr>
<td>F-test value</td>
<td>1.69×10$^{6}$</td>
<td>4.09×10$^{5}$</td>
<td>3.02×10$^{4}$</td>
<td>1.17×10$^{4}$</td>
</tr>
<tr>
<td>$k_{app,sim}/k_{app,cal}$ (%)</td>
<td>76.3</td>
<td>41.9</td>
<td>14.9</td>
<td>2.2</td>
</tr>
</tbody>
</table>
Table 4: Simulation results at pH = 8 and various chlorine and sulfite concentrations. The F-test value is determined with 500 degree of liberty.

<table>
<thead>
<tr>
<th>[SO$<em>3^{2-}$]$</em>{T,0}$ (mol L$^{-1}$)</th>
<th>5.0×10$^{-5}$</th>
<th>5.0×10$^{-5}$</th>
<th>3.0×10$^{-5}$</th>
<th>5.0×10$^{-3}$</th>
<th>5.0×10$^{-5}$</th>
</tr>
</thead>
<tbody>
<tr>
<td>[ClO$^{-}$]$_{T,0}$ (mol L$^{-1}$)</td>
<td>3.0×10$^{-5}$</td>
<td>5.0×10$^{-5}$</td>
<td>5.0×10$^{-5}$</td>
<td>3.0×10$^{-5}$</td>
<td>3.0×10$^{-3}$</td>
</tr>
<tr>
<td>Simulation number</td>
<td>4</td>
<td>12</td>
<td>13</td>
<td>14</td>
<td>15</td>
</tr>
<tr>
<td>SO$_3^{2-}$/HSO$_3^{-}$ equilibrium</td>
<td>35% of the time</td>
<td>40% of the time</td>
<td>Almost never</td>
<td>Always</td>
<td>almost never</td>
</tr>
<tr>
<td>ClO$^{-}$/ClOH equilibrium</td>
<td>No</td>
<td>No</td>
<td>No</td>
<td>No</td>
<td>Always</td>
</tr>
<tr>
<td>$t_{50}$ (s)</td>
<td>9.82×10$^{-4}$</td>
<td>1.90×10$^{-3}$</td>
<td>7.52×10$^{-4}$</td>
<td>6.68×10$^{-6}$</td>
<td>4.46×10$^{-6}$</td>
</tr>
<tr>
<td>2$^{nd}$ order</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Yes</td>
<td>Almost</td>
</tr>
<tr>
<td>$k_{app,sim}$ (L mol$^{-1}$ s$^{-1}$)</td>
<td>7.58×10$^7$</td>
<td>9.50×10$^7$</td>
<td>9.76×10$^7$</td>
<td>6.61×10$^7$</td>
<td>1.73×10$^8$</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.999</td>
<td>0.975</td>
<td>0.993</td>
<td>0.985</td>
<td>0.949</td>
</tr>
<tr>
<td>F-test value</td>
<td>4.09×10$^5$</td>
<td>6.57×10$^4$</td>
<td>1.22×10$^5$</td>
<td>7.05×10$^6$</td>
<td>2.51×10$^7$</td>
</tr>
<tr>
<td>$k_{app,sim}/k_{app,cal}$ (%)</td>
<td>41.9</td>
<td>52.5</td>
<td>53.9</td>
<td>36.5</td>
<td>95.8</td>
</tr>
</tbody>
</table>
Table 5: Reactions involved in the sulfide oxidation mechanism. $K_i$ (equilibrium constants) and $k_i$ (kinetic constants) are reported at 298 K. S can be further oxidized. We consider it as negligible since we used $Ra_{sulfide}$ such as elemental sulfur oxidation would remain marginal.

<table>
<thead>
<tr>
<th>Reaction</th>
<th>Eq (i)</th>
<th>$K_i$</th>
<th>$k_i$</th>
</tr>
</thead>
<tbody>
<tr>
<td>$H_2S + HO^- \xrightarrow{k_{29}} HS^- + H_2O$</td>
<td>$10^{pK_w - pK_{a,1}} = 10^{7.0}$</td>
<td>$k_{29} = 2.5 \times 10^7$ L mol$^-1$ s$^-1$</td>
<td>$k_{29} = 2500$ s$^-1$</td>
</tr>
<tr>
<td>$H_2S \xrightarrow{k_{30}} HS^- + H^+$</td>
<td>$10^{pK_{a,1}} = 10^{7.0}$</td>
<td>$k_{30} = 7500$ s$^-1$</td>
<td>$k_{30} = 7.5 \times 10^{10}$ L mol$^-1$ s$^-1$</td>
</tr>
<tr>
<td>$ClO^{-} + HS^- \xrightarrow{k_{31}} ClO^+ + H_2S$</td>
<td>$10^{pK_{a,1} - pK_{a,4}} = 0.29$</td>
<td>$k_{31} = 3 \times 10^9$ L mol$^-1$ s$^-1$</td>
<td>$k_{31} = 1.04 \times 10^9$ L mol$^-1$ s$^-1$</td>
</tr>
<tr>
<td>$ClO^{-} + H_2S \xrightarrow{k_{32}} S + H_2O + Cl^-$</td>
<td></td>
<td>$k_{32} = 6.75 \times 10^6$ L mol$^-1$ s$^-1$</td>
<td></td>
</tr>
<tr>
<td>$ClO^{-} + HS^- \xrightarrow{k_{33}} S + HO^- + Cl^-$</td>
<td></td>
<td>$k_{33}$</td>
<td></td>
</tr>
<tr>
<td>$ClOH + H_2S \xrightarrow{k_{34}} S + H_3O^+ + Cl^-$</td>
<td></td>
<td>$k_{34} = 1.62 \times 10^8$ L mol$^-1$ s$^-1$</td>
<td></td>
</tr>
<tr>
<td>$ClOH + HS^- \xrightarrow{k_{35}} S + H_2O + Cl^-$</td>
<td></td>
<td>$k_{35}$ expected close to $10^9$ L mol$^-1$ s$^-1$</td>
<td></td>
</tr>
</tbody>
</table>

1 (Eigen, 1964)  2 (Vilmain et al., 2014)
Table 6: Numerical resolution results for $k_{33}$ value determination.

<table>
<thead>
<tr>
<th>pH</th>
<th>11</th>
<th>12</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>$k_{\text{relative}}$</td>
<td>1.55</td>
</tr>
<tr>
<td></td>
<td>$k_{\text{app,exp}}$ (L mol$^{-1}$ s$^{-1}$)</td>
<td>$4.4 \times 10^5$</td>
</tr>
<tr>
<td>$k_{33}$ value (L mol$^{-1}$ s$^{-1}$)</td>
<td>0</td>
<td>$10^4$</td>
</tr>
<tr>
<td>$k_{33}$ value (L mol$^{-1}$ s$^{-1}$)</td>
<td>$1.23 \times 10^9$</td>
<td>$1.05 \times 10^9$</td>
</tr>
<tr>
<td>$k_{\text{app,cal}}$ (L mol$^{-1}$ s$^{-1}$)</td>
<td>$4.2 \times 10^5$</td>
<td>$3.7 \times 10^5$</td>
</tr>
<tr>
<td>$F_i$ (%)</td>
<td>0.23</td>
<td>2.51</td>
</tr>
<tr>
<td>Error (%)</td>
<td>5</td>
<td>16</td>
</tr>
<tr>
<td>$k_{33}/k_{\text{app,cal}}$ (%)</td>
<td>0</td>
<td>2.7</td>
</tr>
</tbody>
</table>
Table 7: Simulation results with \([H_2S]_{T,0} = 10.0 \times 10^{-5} \text{ mol L}^{-1}\) and \([ClO]_{T,0} = 3.0 \times 10^{-5} \text{ mol L}^{-1}\) and various pH. The F-test value is determined with 500 degree of liberty

<table>
<thead>
<tr>
<th>pH</th>
<th>Simulation number</th>
<th>SO(_3^{2-})/HSO(_3^-) eq.</th>
<th>ClO(^-)/ClOH eq.</th>
<th>(t_{90}) (s)</th>
<th>(2^{nd}) order</th>
<th>(k_{app,sim}) (L mol(^{-1}) s(^{-1}))</th>
<th>(R^2)</th>
<th>F-test value</th>
<th>(k_{app,sim}/k_{app,cal}) (%)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>6</td>
<td>16</td>
<td>80% of the time</td>
<td>2.99E×10(^{-4})</td>
<td>Yes</td>
<td>9.49×10(^{7})</td>
<td>0.999</td>
<td>4.92E+05</td>
<td>88.0</td>
</tr>
<tr>
<td></td>
<td>7</td>
<td>17</td>
<td>Almost no</td>
<td>7.68×10(^{-5})</td>
<td>Yes</td>
<td>3.64×10(^{8})</td>
<td>1.000</td>
<td>1.49×10(^{6})</td>
<td>76.9</td>
</tr>
<tr>
<td></td>
<td>7.5</td>
<td>18</td>
<td>30% of the time</td>
<td>1.30×10(^{-4})</td>
<td>Yes</td>
<td>2.02×10(^{8})</td>
<td>0.993</td>
<td>7.25×10(^{4})</td>
<td>41.6</td>
</tr>
<tr>
<td></td>
<td>8</td>
<td>19</td>
<td>Almost no</td>
<td>3.65×10(^{-4})</td>
<td>Yes</td>
<td>7.30×10(^{7})</td>
<td>0.999</td>
<td>4.77×10(^{5})</td>
<td>25.6</td>
</tr>
<tr>
<td></td>
<td>9</td>
<td>20</td>
<td>Almost no</td>
<td>1.92×10(^{-3})</td>
<td>Yes</td>
<td>1.48×10(^{7})</td>
<td>1.000</td>
<td>1.89×10(^{6})</td>
<td>36.6</td>
</tr>
<tr>
<td></td>
<td>10</td>
<td>21</td>
<td>Always</td>
<td>8.82×10(^{-3})</td>
<td>Yes</td>
<td>3.24×10(^{6})</td>
<td>1.000</td>
<td>7.91×10(^{6})</td>
<td>77.1</td>
</tr>
<tr>
<td></td>
<td>11</td>
<td>22</td>
<td>Always</td>
<td>6.93×10(^{-2})</td>
<td>Yes</td>
<td>4.09×10(^{5})</td>
<td>1.000</td>
<td>2.62×10(^{8})</td>
<td>97.1</td>
</tr>
<tr>
<td></td>
<td>12</td>
<td>23</td>
<td>Always</td>
<td>6.75×10(^{-1})</td>
<td>Yes</td>
<td>4.22×10(^{4})</td>
<td>1.000</td>
<td>3.43×10(^{10})</td>
<td>100</td>
</tr>
</tbody>
</table>
Table 8: Simulation results with underestimated and overestimated kinetic constants of acid-base reactions. The operating conditions are those of simulations #1 and #16.

<table>
<thead>
<tr>
<th>Simulation number</th>
<th>24 ($k_i$ underestimations for sulfite)</th>
<th>25 ($k_i$ overestimations for sulfite)</th>
<th>26 ($k_i$ underestimations for sulfide)</th>
<th>27 ($k_i$ overestimations for sulfide)</th>
</tr>
</thead>
<tbody>
<tr>
<td>k$_i$ values (L mol$^{-1}$ s$^{-1}$)</td>
<td>k$_{17}$ = $10^9$</td>
<td>k$_{17}$ = $10^{10}$</td>
<td>k$_{17}$ = $10^9$</td>
<td>k$_{17}$ = $10^{10}$</td>
</tr>
<tr>
<td></td>
<td>k$_{18}$ = $3\times10^9$</td>
<td>k$_{18}$ = $5\times10^{10}$</td>
<td>k$_{18}$ = $3\times10^9$</td>
<td>k$_{18}$ = $5\times10^{10}$</td>
</tr>
<tr>
<td></td>
<td>k$_{19}$ = $5\times10^9$</td>
<td>k$_{19}$ = $2.5\times10^{10}$</td>
<td>k$_{19}$ = $5\times10^9$</td>
<td>k$_{19}$ = $2.5\times10^{10}$</td>
</tr>
<tr>
<td></td>
<td>k$_{20}$ = $10^{10}$</td>
<td>k$_{20}$ = $7.5\times10^{10}$</td>
<td>k$_{20}$ = $7.5\times10^{10}$</td>
<td>k$_{20}$ = $7.5\times10^{10}$</td>
</tr>
<tr>
<td></td>
<td>k$_{21}$ = $10^8$</td>
<td>k$_{21}$ = $10^9$</td>
<td>k$_{21}$ = $10^8$</td>
<td>k$_{21}$ = $10^9$</td>
</tr>
<tr>
<td>$k_{app, sim}$ (L mol$^{-1}$ s$^{-1}$)</td>
<td>$5.17\times10^7$</td>
<td>$7.58\times10^7$</td>
<td>$9.35\times10^7$</td>
<td>$9.53\times10^7$</td>
</tr>
<tr>
<td>$t_{90}$ (s)</td>
<td>$1.47\times10^{-3}$</td>
<td>$1.00\times10^{-3}$</td>
<td>$3.00\times10^{-4}$</td>
<td>$2.99\times10^{-4}$</td>
</tr>
<tr>
<td>$k_{app, sim}/k_{app, cal}$ (%)</td>
<td>63.9</td>
<td>93.7</td>
<td>86.7</td>
<td>88.28</td>
</tr>
<tr>
<td>$R^2$</td>
<td>0.991</td>
<td>1.000</td>
<td>0.999</td>
<td>0.999</td>
</tr>
</tbody>
</table>