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► To cite this version:

Pierre-Louis Regazzoni, Didier Marot. Investigation of interface erosion rate by Jet Erosion Test and statistical analysis. European Journal of Environmental and Civil Engineering, 2011, 15 (8), pp.1167-1185. 10.3166/EJECE.15.1167-1185 . hal-01006999

HAL Id: hal-01006999

<https://hal.science/hal-01006999>

Submitted on 10 Mar 2018

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Investigation of interface erosion rate by Jet Erosion Test and statistical analysis

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ABSTRACT. Erosion is one of the main causes of instabilities within hydraulic earth structures. Two types of erosion can be distinguished: suffusion and interface erosion. This paper deals with the interface erosion phenomenon and the Jet Erosion Test is used in order to evaluate the erodibility of fine soils. A new energy analysis of the test is developed, relating the total eroded mass to the dissipated fluid energy. A new erosion resistance index is proposed. The erodibility is evaluated for twelve natural soil specimens which are compacted with the Proctor protocol. They represent a large range of erosion sensitivity. A wide dissipated hydraulic energy scale appears and a statistical analysis is carried out which gives a correlation of the erosion resistance index with three physical parameters.

RÉSUMÉ. L'érosion est l'une des principales causes d'instabilités d'ouvrages hydrauliques en terre. Deux types d'érosion peuvent être distingués : la suffusion et l'érosion d'interface. Cet article porte sur l'érosion d'interface et le Jet Erosion Test est utilisé afin d'évaluer la sensibilité à l'érosion de sols fins. Une nouvelle analyse énergétique de l'essai est développée qui relie la masse totale érodée avec l'énergie dissipée par le fluide. Un nouvel indice de résistance à l'érosion est proposé. La sensibilité à l'érosion est évaluée pour douze sols naturels qui sont compactés suivant le protocole Proctor et qui représentent une large gamme de sensibilité à l'érosion. Une large gamme d'énergie est mise en évidence et l'analyse statistique qui est menée permet d'exprimer une corrélation entre l'indice de résistance à l'érosion et trois paramètres physiques.

KEYWORDS: soil erosion, JET, cohesive soils, energy, statistical analysis, water flow, dynamic compaction.

MOTS-CLÉS : érosion, JET, sols cohésifs, énergie, analyse statistique, écoulement, compactage dynamique.

1. Introduction

Internal erosion is one of the main causes of instabilities within hydraulic earth structures such as dams, dikes or levees (Foster *et al.*, 2000). The mechanisms of internal erosion are very complex and involve many parameters, some of which are coupled. In earth structures and their foundations, two types of internal erosion processes can be distinguished: suffusion and interface erosion. Suffusion process concerns only the finer particles which are detached and move inside the soil matrix constituted by the coarse particles. Interface erosion can appear in cracks or concentrated leaks and is then called piping. When the interface erosion appears between two materials having different grain size distributions, it is called contact erosion. However this interface, relatively large compared to the grain scale, can also be located between soil and water. In such case and with a seepage flow which is normal to the interface, process is called backward erosion (Fell and Fry, 2007).

Several testing devices for studying the interface erosion of fine grained soils were proposed by various researchers. These tests apply hydraulic stresses to a soil sample by a variety of methods. In literature, the interpretations of the experiments are based on a linear erosion law stating that the mass rate of erosion, $\dot{m}$, or the volumetric rate of erosion, $\dot{\epsilon}$, is proportional to the excess hydraulic shear stress τ above a threshold value τ_c which represents the minimal hydraulic shear stress needed to initiate erosion. In equation form, the erosion laws are:

$$\dot{m} = k_{d,m} (\tau - \tau_c) \quad [1]$$

$$\dot{\epsilon} = k_d (\tau - \tau_c) \quad [2]$$

with $k_{d,m}$ and k_d : erosion rate coefficients, with $k_{d,m} = k_d \rho_D$ where ρ_D : soil dry density.

One of these main devices is the Hole Erosion Test apparatus (HET) which was developed by Wan and Fell (2004). HET can be performed on a Proctor mould containing the soil specimen. A 6.35 mm diameter hole is pre-drilled through the centreline-axis to simulate a concentrated leak. A constant hydraulic head is applied to the specimen. The data collected during test are the head losses across the sample and the flow rate. When erosion is produced, the resulting increase of flow rate is used to estimate the increase of the hole diameter and thus to determine the resulting mass rate of erosion.

Thanks to the values of diameter (representing the erosion), with the Wan and Fell (2004)'s method or with the scaling law proposed by Bonelli and Brivois (2008), it is possible to determine the value of the erosion rate coefficient and the value of critical shear stress.

Wan and Fell (2004) proposed a classification of internal erosion risk based on the value of erosion rate index determined from HET results and defined by:

$$I_{HET} = -\log_{10}(k_{d,m}) \quad [3]$$

Wan and Fell described the erosion development by defining six groups, varying from extremely slow to extremely rapid.

Hanson and Cook (2004) developed the submerged Jet Erosion Test (JET). This apparatus is designed to apply a submerged jet on the soil surface and it allows performing in-situ tests. The depth of scour beneath the jet is measured over time and the hydraulic stress on the soil surface decreases as scour occurs. Hanson and Cook assumed that the equilibrium depth is reached when the stress at the interface is equal to the threshold stress. The erosion never stops but the erosion speed is decreasing and the hydraulic shear stress is converging asymptotically to the threshold stress. By fitting scour measurements and time data on an asymptotic function, the equilibrium depth and the corresponding critical stress are deduced. The experimental data are fitted to the calculated scour depth. This yields an estimate of the detachment rate coefficient, k_d .

The soil erodibility classification proposed by Hanson and Simon (2001) is based on both the critical shear stress and the erosion rate coefficient determined from JETs. This classification recognizes five categories from very resistant to very erodible materials.

For the comparison of the two apparatuses, seven natural occurring fine-grained soils, covering a large range of erodibility were tested (Regazzoni *et al.*, 2008). Soils were compacted according to normal Proctor procedure and with an initial water content equal to the optimum water content less one percent. It was shown that by using the commonly used methods, the values of the erosion coefficient are systematically higher with the JET than with the HET and the corresponding mean rate index is systematically smaller with the JET (I_{JET}) than with the HET (I_{HET}). The I_{JET}/I_{HET} ratio varies from 0.32 to 0.84. On average, the HET critical shear stress is about fifty times higher than the JET critical shear stress. Moreover the relative soils classifications yielded by the two erodimeters are not exactly the same (Regazzoni, 2009). Marot *et al.* (2011) proposed an energy analysis and a new erosion resistance index was defined. Using the energy analysis, an identical soil classification was built with the two devices and six categories of soil erodibility were proposed from very resistant to very erodible.

This paper deals with the relationship between surface erosion properties and other soil properties in a large range of erosion sensitivity. The erodibility was evaluated for twelve natural soils. The Jet Erosion Test was used and the results were interpreted by the energy method.

A large range of dissipated hydraulic energy appears, and a statistical analysis was carried out which gives an expression of the erosion resistance index with several physical parameters.

2. Erosion device and energy analysis of tests

2.1. Principle of Jet Erosion Test

Figure 1 presents the principle of the device. The jet test apparatus consists of an adjustable head tank, a jet tube with a nozzle, a point gage and a jet submerged tank which contains the specimen. The point gage is adjusted to close off the nozzle and also to measure the depth of scour below the nozzle.

Figure 1. Principle of Jet Erosion Test

The jet tube is mounted to the submergence tank cover so that the height of the nozzle above the soil surface (distance J_0 on Figure 2) can be adjusted to different heights prior to the start of a test. The jet tube and cover can also be mounted to a heavy-duty field tank for in situ measurements. The jet is typically oriented vertically, but when the test is performed on a slope, it can also be positioned at an angle.

Figure 2. Different measurements during Jet Erosion Test

The collected data during the test at specific times include: the depth of scour J measured from a reference level and the head loss between the top of the constant head tank and the top of the submerged tank, ΔH . Data are recorded at intervals chosen by the operator, depending on the erosion rate. Typical intervals range from 15 s to 30 min, with total test times of 2 hours or less (Hanson and Cook, 2004). With these data, it is possible to relate the hydraulic conditions at interface to the erosion rate at a time t .

2.2. Water velocity

With the objective to evaluate the water velocity in the area of the impact, three zones are defined in conformity with Hanson and Cook (2004)'s analysis (see Figure 2). In the zone I (altitude $Z < J_p = 6.2 d_0$, with d_0 : diameter of the jet at the exit), the water velocity on the axis is constant and equal to the initial velocity at the jet origin $u(0, 0)$. In the zone II ($Z > J_p$) and far from the interface ($Z < 0.86 - 0.9 J$, with J : distance between soil-water interface and jet origin), the axial velocity is proportional to the inverse value of the distance between the jet origin and the altitude considered:

$$u(0, Z) = u(0, 0) \frac{J_p}{Z} \quad [4]$$

In the zone near the interface ($J > Z > 0.9 - 0.86 J$), the vertical velocity at a distance r from the jet axe and a distance Z from the jet origin ($u(r, Z)$) decreases to 0 to be converted into radial velocity ($v(r, Z)$). Beltaos and Rajaratnam (1974) conducted tests of impinging circular turbulent jet and they proposed an expression of the vertical velocity on the jet axis:

$$\frac{u(r, Z)}{u(0, Z)} = \exp \left(-0.693 \left(\frac{r}{b_u} \right)^2 \right) \quad [5]$$

where $u(0, Z)$: water velocity at the distance Z from the jet origin on the jet axis in the case of a free jet; b_u : distance from the axis where the water velocity on the axis is divided by two, $b_u = 0.093 (J - J_p)$.

2.3. Energy analysis

Regazzoni (2009) and Marot *et al.* (2011) proposed a method of interpretation based on the energy dissipation between the fluid and the soil. The main issue is to characterize independently the hydraulic loading and the induced erosion; these

characterizations have to be based on measurements and associated with the minimum number of assumptions. The energy equation for the fluid (neglecting the soil phase inside the volume) can be written as:

$$\begin{aligned}\frac{dE}{dt} &= \frac{d}{dt} \iiint_{\text{Mass}} \left(e_{\text{int}} + \frac{u^2}{2} + \vec{g} \cdot \vec{x} \right) dM \\ &= \frac{\partial}{\partial t} \iiint_{\text{Volume}} \left(e_{\text{int}} + \frac{u^2}{2} + \vec{g} \cdot \vec{x} \right) \rho_w dV + \oint_S \left(e_{\text{int}} + \frac{u^2}{2} + \vec{g} \cdot \vec{x} \right) \rho_w (\vec{U} \cdot \vec{n}) dS\end{aligned}\quad [6]$$

where M: fluid mass, V: fluid volume, e_{int} : internal energy, S: interface between fluid and environment, n: normal vector of interface, U: fluid velocity (components: u, v, w), g: gravity, ρ_w : fluid density, x: coordinates.

Total energy is the sum of the mechanical work W and the energy exchange between the system and the environment E_{Ther} :

$$\frac{dE}{dt} = \frac{dE_{\text{Ther}}}{dt} + \frac{dW}{dt} \quad [7]$$

The whole experimental system is placed in a temperature controlled laboratory and it is supplied by the public water system. Thus for test duration, the system can be considered isothermal in time and internal energy is assumed constant. All tests are performed under the same experimental conditions, so the comparison of tests leads to neglect the relative variations of energy exchange between the system and the environment. In consequence the term dE_{Ther} / dt is negligible. As jet test results are analyzed in steady state (assuming during a time step that the water speed evolves slowly), the unsteady term of the kinetic energy is negligible. Finally the Equation [6] becomes:

$$\frac{dW}{dt} = \oint_S \left(\frac{u^2}{2} + \vec{g} \cdot \vec{x} \right) \rho_w (\vec{U} \cdot \vec{n}) dS \quad [8]$$

The mechanical work W is the sum of: work done by pressure, viscous work in the fluid and work by erosion:

$$\frac{dW_{\text{pressure}}}{dt} + \frac{dW_{\text{viscous in fluid}}}{dt} + \frac{dW_{\text{erosion}}}{dt} = \oint_S \left(\frac{u^2}{2} + \vec{g} \cdot \vec{x} \right) \rho_w (\vec{U} \cdot \vec{n}) dS \quad [9]$$

In comparison with free jet, jet in front of a soil-water interface is subjected to a deviation from the centreline. It is assumed that the erosion is mainly associated with this deviation which induces an increase of shear stress and a great variation of pressure.

In front of a wall, Beltaos and Rajaratnam (1974) observed that wall shear stress increases linearly with lateral distance from jet centreline up to a maximum value obtained for $r = 0.14 J$ and then decreases with any further increase in r . Moreover, when r/J ratio increases from 0 to 0.14, wall pressure decreases rapidly reaching 10% of maximum value of stagnation pressure on jet centreline axis. Thus at J depth, erosion energy is assumed to come from the space defined by lateral distance from jet centreline $r \leq 0.14 J$.

With the objective to take into account the variation of vertical velocity with the J altitude and with the distance r from the jet axe considered, Equations [9] and [5] are combined to express the temporal derivative of mechanical work through erosion by:

$$\frac{dW_{erosion}}{dt} = 2\pi \int_0^{0.14J} \frac{u^2}{2} \rho_w (\vec{U} \cdot \vec{n}) r dr = \pi \int_0^{0.14J} \rho_w u^3(0, J) \left(\exp \left(-0.693 \left(\frac{r}{b_u} \right)^2 \right) \right)^3 [10]$$

For convenience, the temporal derivative mechanical work by erosion is named erosion power ($P_{erosion}$).

To classify the soil according to the erosion, an erosion coefficient is proposed:

$$\alpha = \frac{\dot{m}_{dry}}{P_{erosion}} [11]$$

where, $\dot{m}_{dry}$ rate of eroded dry mass.

The energy dissipated by erosion ($E_{erosion}$) is the time integration of the instantaneous erosion power for the test duration. Thus for each test, the erosion energy is computed by trapezoidal rule and the erosion resistance index is built with the erosion energy and the cumulative eroded dry mass (m_{dry}):

$$I_\alpha = -\log \left(\frac{m_{dry}}{E_{erosion}} \right) [12]$$

According to values of erosion resistance index which were determined with both JET and HET devices, Marot *et al.* (2011) proposed six categories of soil erodibility: highly erodible for $I_\alpha < 1$, erodible for $1 \leq I_\alpha < 2$, moderately erodible for $2 \leq I_\alpha < 3$, moderately resistant for $3 \leq I_\alpha < 4$, resistant for $4 \leq I_\alpha < 5$ and highly resistant for $I_\alpha \geq 5$.

3. Experimental investigation

3.1. Soils properties and testing program

Twelve soils were selected (see Table 1), covering a large range of erodibility as determined by previous HET investigations (Regazzoni, 2009). The testing program concerns 8 natural soils, 2 soils were created on the basis of natural soils and 2 soils were created using industrial soil materials. A non plastic soils is considered to have a liquid limit and a plastic limit equal and with a value of about 0. The values of optimal dry density for the normal Proctor compaction are ranging between $1\,378\text{ kg/m}^3$ and $1\,980\text{ kg/m}^3$ for water content between 10% and 24%.

Table 1. *Classification and properties of soils tested*

Soil reference in paper	USCS classification	Atterberg limits		Normal Proctor state	
		Liquid limit (%)	Plasticity index (%)	Optimum dry density (kg/m^3)	Optimum water content w_{opt} (%)
P2	ML	21	4	1860	12
P3	CL	31	15	1900	13
TE	CL-ML	29	4	1703	16
MF	CL	47	34	1815	14
TF	CH	55	40	1708	17
MP	CH-CL	54	31	1679	17
BC	CH	69	44	1378	24
L	ML	Non plastic		1670	19
Mix 0	CL	44	23	1619	21
Mix 1	CL	34	11	1650	20
K50 S50	CL	30	13	1780	15
K20 S80	ML	Non plastic		1980	10

Notes: USCS = Unified Soil Classification System.

Figure 3 shows that the soils are covering a large part of the Atterberg limits diagram.

The grain size distribution of each soil is described by four fractions: clay fraction F_{clay} (mass fraction in percentage of soil particles finer than $2\text{ }\mu\text{m}$), silt

fraction F_{silt} (mass fraction in percentage of soil particles between 2 μm and 74 μm), fine sand fraction F_{fs} (mass fraction of soil particles between 74 μm and 425 μm) and coarse sand fraction F_{cs} (mass fraction of soil particles coarser than 425 μm). The values of each fraction are given on Table 2.

Figure 3. *Casagrande diagram of soils tested*

Table 2. *Values of grain size distribution*

Soil reference in paper	Clay fraction ($d < 2\mu\text{m}$) (%)	Silt fraction ($2\mu\text{m} < d < 74\mu\text{m}$) (%)	Fine sand fraction ($74\mu\text{m} < d < 425\mu\text{m}$) (%)	Coarse sand fraction ($d > 425\mu\text{m}$) (%)
P2	13.0	47.0	21.2	18.8
P3	26.0	47.0	14.3	12.7
TE	10.9	76.6	9.4	3.1
MF	33.0	41.9	21.7	3.4
TF	42.3	51.4	5.5	0.8
MP	40.0	51.8	5.0	3.2
BC	65.9	30.5	1.8	1.8
L	6.8	92.2	0.7	0.3
Mix 0	40.2	57.3	1.5	1.1
Mix 1	21.8	76.6	0.5	1.1
K50 S50	17.9	53.1	28.8	0.2
K20 S80	12.1	35.8	51.9	0.3

The preparation of the specimen is made according to the following procedures. First the natural soils are prepared, it means: a drying at 65°C, the crushing and sieving with a #4 A.S.T.M. sieve. For all tested soils, water is added and blended to target optimum water content less 1% (in conformity with procedure defined by USBR, 1987). The soil is let 36h (at least) in a plastic bag. The compaction is made in three layers of 25 blows with a normal Proctor rammer. The specimen is let in a plastic bag for 12 hours before test performed by jet device.

3.2. Results of testing

Thirty eight tests were performed and the test duration was ranging from 1 740 s to 6 300 s. Figure 4, plots the erosion power (maximum values between 0.04 W and 1.25 W) in function of the scour depth (maximum values between 0.02 m and 0.11 m). Based on this chart, a classification of erodibility of specimens can not be precisely established because the kinetic of the scour development is not taken into account and this characteristic can be very different for two tests. For example, during test TF-2, scour depth reaches 0.03 m in 75 min with associated erosion power $P_{\text{erosion}} = 0.11$ W, whereas only 2 min is sufficient to obtain the same order of magnitude for test TF-4.

Figure 4. Erosion power in function of scour depth

Figure 5. Energy in function of eroded dry mass

With the objective to consider the kinetic of erosion development, Figure 5 shows the energy dissipated by fluid flow in function of the cumulative eroded dry mass. The value of expended energy was between 29 J to 23 729 J and cumulative eroded dry mass varied between 0.106 kg and 1.685 kg.

As shown on Table 3, obtained values of erosion resistance index I_{α} are between 1.42 and 5.22. This great range of values may be due to the great variability of tested soils.

According to the values of I_{α} index and Marot *et al.* (2011)'s classification: L soil is erodible, MF, TE, Mix1 and K20 S80 are moderately erodible, TF, P3 and P2 appear moderately erodible to moderately resistant, MP and K50 S50 are moderately resistant. Relatively to the others soils, the great variability of Mix0 and BC does not allow to classify them precisely. It is shown that for Mix0 soil, water content discrepancy of 4% is sufficient to induce a variation of soil erodibility from highly resistant to erodible. With a water content discrepancy of 3%, BC can vary between moderately resistant to erodible.

Table 3. *Results of jet tests*

Sample	Water content at compaction (%)	Initial dry mass (kg)	Eroded dry mass (kg)	Energy (J)	Erosion resistance index I_{α}	Classification^a
P2-1	17	1.650	0.194	380	3.29	Mod. resistant
P2-2	13	1.775	0.106	372	3.54	Mod. resistant
P2-3	15	1.701	0.638	478	2.87	Mod. erodible
P2-4	16	1.691	0.635	352	2.74	Mod. erodible
P2-5	13	1.774	0.135	736	3.74	Mod. resistant
P2-6	12	1.730	1.378	234	2.23	Mod. erodible
P3-1	12	1.742	1.365	1477	3.03	Mod. resistant
P3-2	12	1.730	1.624	1475	2.96	Mod. erodible
TE-1	16	1.609	0.224	102	2.66	Mod. erodible
TE-2	17	1.611	0.401	123	2.49	Mod. erodible
TE-3	16	1.609	0.356	61	2.23	Mod. erodible
TE-4	16	1.607	0.974	139	2.15	Mod. erodible
MF-1	14	1.682	0.550	118	2.33	Mod. erodible
MF-2	15	1.685	0.451	58	2.11	Mod. erodible
MF-3	14	1.688	0.594	150	2.40	Mod. erodible
MF-4	15	1.662	0.462	58	2.10	Mod. erodible
MF-5	15	1.683	0.312	51	2.21	Mod. erodible
MF-6	15	1.689	0.197	46	2.37	Mod. erodible
MF-7	14	1.682	0.755	171	2.36	Mod. erodible
TF-1	17	1.571	0.380	268	2.85	Mod. erodible
TF-2	18	1.498	0.407	437	3.03	Mod. resistant
TF-3	17	1.518	0.506	403	2.90	Mod. erodible
TF-4	18	1.427	0.941	201	2.33	Mod. erodible
MP-1	18	1.564	0.134	352	3.42	Mod. resistant
MP-2	17	1.590	0.636	649	3.01	Mod. resistant
MP-3	18	1.512	0.752	1077	3.16	Mod. resistant
MP-4	19	1.567	0.714	773	3.03	Mod. resistant
BC-1	26	1.263	0.629	844	3.13	Mod. resistant

Sample	Water content at compaction (%)	Initial dry mass (kg)	Eroded dry mass (kg)	Energy (J)	Erosion resistance index I_α	Classification ^a
BC-2	23	1.306	1.242	119	1.98	Erodible
L-1	19	1.583	1.562	55	1.55	Erodible
L-2	19	1.579	1.093	29	1.42	Erodible
Mix 0- 1	19	1.528	1.027	61	1.77	Erodible
Mix 0- 2	23	1.541	0.144	23729	5.22	High. resistant
Mix 1- 1	20	1.564	1.543	168	2.04	Mod. erodible
Mix 1- 2	22	1.540	1.206	621	2.71	Mod. erodible
K50 S50-1	14	1.678	1.470	3262	3.35	Mod. resistant
K50 S50-2	16	1.679	0.647	2805	3.64	Mod. resistant
K20 S80	10	1.861	1.685	465	2.44	Mod. erodible

^a Classification according Marot *et al.* (2011) soil erodibility system.

4. Estimation of erosion resistance index from other soil properties

4.1. Systematic approach and existing correlation

It is useful to estimate soil erodibility by physical parameters that may be easily measured. Analyse of correlation coefficient for each relation between physical parameter and erosion resistance index I_α shows that no physical parameter allows estimating I_α index. This lack of correlation may be due to the great variability of tested soils.

Based on a parametric study on 98 sets of test data, Wan and Fell (2004) proposed a correlation between erosion rate index determined by HET and nine physical parameters which was expressed for fine grained soils by:

$$I_{HET} = -10.200 + 0.010 \rho_d - 0.042 \frac{\rho_d}{\rho_{d \text{ opt}}} + 0.100 w + 0.010 \Delta w_R - 0.006 \text{ Fines} + 0.042 \text{ Clay} - 0.090 w_L + 0.110 I_p + 0.440 \text{ Pin Hole} \quad [13]$$

where ρ_d : dry density of the soil in kg/m^3 , $\rho_d/\rho_{d \text{ opt}}$: percentage compaction in percent, w : water content at compaction in percent, Fines: mass fraction of fine particles in percent ($d \leq 0.075 \text{ mm}$), Clay: mass fraction of clay in percent ($d \leq 0.005 \text{ mm}$), w_L : liquid limit in percent, I_p : plasticity index in percent, PinHole: pin hole test classification (between 1 (D1) and 6 (ND1)), and Δw_R : water content ratio in percent expressed by:

$$\Delta w_R = \frac{w - w_{\text{opt}}}{w_{\text{opt}}} \quad [14]$$

where w_{opt} : water content at Proctor optimum.

The coefficient for the correlation [13] was 0.73.

According to the value of pin hole test classification and the value of its associated coefficient in Equation [13], this term contributes significantly to the correlation. This contribution may be due to the physical principle of pin hole test which is similar to the HET.

For the 38 sets of test data performed by the authors, a research of predictive equation was realized by the mean of Xlstat software. Without the contribution of pin hole test value a new predictive equation for the erosion resistance index is proposed:

$$I_\alpha = -6.020 + 0.012 \rho_d - 0.164 \frac{\rho_d}{\rho_{d \text{ opt}}} + 0.307 w - 0.009 \Delta w_R - 0.013 \text{ Fines} - 0.010 F_{\text{clay}} + 0.065 w_L - 0.029 I_p \quad [15]$$

The obtained correlation coefficient (R^2) is 0.64, for a sample size $N = 38$.

Five terms contribute to Equation [13] and Equation [15] with the same sign (constant, ρ_d , $\rho_d/\rho_{d \text{ opt}}$, w , Fines) but others parameters contribute with opposite sign to the correlations. Because of the coupling between several parameters, it is difficult to evaluate the contribution of each parameter and to reduce the number of parameters.

It can be noted that in predictive Equations [13] and [15] contribution of soil density appears two times but the influence of saturation ratio is not taken into account. That may be a reason of the weakness of correlation coefficient in spite of size of eight or nine parameters.

4.2. Reduction of physical parameters number by statistical analysis

4.2.1. Definition of used parameters

The used parameters for the statistical analysis try to represent the soil in several characteristics. The first characteristic considers the grain size distribution. The size curve distribution is introduced by considering the clay fraction of the soil F_{clay} , the silts fraction F_{silt} , the fine sand fraction F_{fs} and the coarse sand fraction F_{cs} . The characterization is completed by the Atterberg limits on the soil fraction below 425 μm . With the objective to take into account presence of fluid phases in soil, the water content, w , and the saturation ratio S_r (in percent) are considered. To describe the soil structure, the compaction, c , and the dry densities are considered:

$$c = \frac{\rho_d}{\rho_s} \quad [16]$$

where ρ_d : dry density of the soil; ρ_s : solid density.

To represent the interaction between clay and water, the clay water content is introduced:

$$W_{\text{clay}} = \frac{w}{F_{\text{clay}}} \quad [17]$$

Two parameters linking the Atterberg limits to the clay water content are defined:

$$\Delta w_L = w_L - W_{\text{clay}} \quad [18]$$

$$\Delta w_P = W_{\text{clay}} - w_P \quad [19]$$

where w_L : liquid limit and w_P : plastic limit.

With the objective to represent the soil water exchange, the surface exchange S_d is defined by:

$$S_d = 6 \sum \frac{1}{d_{50, Xi}} p_i c \quad [20]$$

where $d_{50, Xi}$: average diameter of the considered fraction. For clay fraction, we consider 2 μm , for sand and silt fractions, average diameter is computed with grain size distribution. p_i : percentage in composition of the considered fraction.

4.2.2. Principle of statistical analysis

Multivariate analysis allows the full set of variables related to the measurements to be reduced to a subset representing the principal components assuming a linear correlation between the variables. Each parameter is represented in a factor space, and the geometrical representation associates a vector to each parameter. The scalar product of two associated vectors is equal to the correlation coefficient of the two parameters. An automatic classification is used to define all variables according to the most useful factors. Figure 6 shows the variables in two first factor planes.

Figure 6. Variables representation in: (a) factor plane 1-2; (b) factor plane 3-4

Thus in each plan, two variables are in linear relationship when their positions are near the unit circle, and very close to each other or diametrically opposite (for example on Figure 5a: variables ρ_d , c and w or Δw_L , Δw_P and w_{clay}). Two variables are independent when their representations are in quadrature (for example: variables F_{clay} and $\log(S_d)$ on Figure 6a, F_{cs} and I_α on Figure 6b).

4.2.3. Results of statistical analysis

Now, we are eliminating the variables which are correlated, or seem meaningless by their redundancy information with other variables.

By leading a new multivariate analysis, three parameters are kept and the correlation with erosion resistance index is:

$$I_\alpha = -0.97 + 0.47 \Delta w_L - 0.36 c + 5.41 S_r \quad [21]$$

The obtained correlation coefficient (R^2) between the prediction and the measurement is 0.35 with $N = 38$. By observing the distribution of the error (cf. Figure 7), it appears that the problematic soils are represented by MF, Mix 0,

Mix 1. These soils are dispersive (Regazzoni, 2009), therefore we take into account the dispersive property of the soils.

Figure 7. *Erosion resistance index, measured values vs predicted values*

A new correlation is defined for non-dispersive soils:

$$I_{\alpha} = -2.31 + 0.69 \Delta w_L + 1.41 c + 6.07 S_r \quad (R^2 = 0.59, N = 27) \quad [22]$$

For the dispersive soils the expression of estimated value of I_{α} is:

$$I_{\alpha} = -1.36 + 8.69 \Delta w_L + 2.68 c + 2.08 S_r \quad (R^2 = 0.81, N = 11) \quad [23]$$

By distinguishing between dispersive and non-dispersive soils, we identify the main parameters for a soil analysis in relation to the surface erosion phenomenon. These main physical parameters which take into account the influence of each phase (solid, water and gas) and the influence of soil plasticity are: compaction, saturation ratio and difference between clay water content and liquid limit.

5. Conclusion

A Jet Erosion Test device is used in order to characterize the sensitivity to erosion of twelve fine soils which cover a large part of the Atterberg limits diagram.

The tested samples are compacted with the standard Proctor procedure at optimum water content less 1%. Study of energy exchanges between fluid and soil leads to propose a new analysis of Jet Erosion Test and a new erosion resistance index is defined. In contrast to the precedent models based on stress, the energy model leads to a same classification of soil surface erodibility for two types of apparatus: Jet Erosion Test and Hole Erosion Test (Marot *et al.*, 2011).

Several physical parameters are determined and a statistical analysis is performed in order to identify the main parameters for a correlation with erosion resistance index.

By distinguishing the dispersive behaviour from non-dispersive behaviour, the multivariate statistical analysis leads to an expression of the erosion resistance index as a function of three physical parameters: compaction, saturation ratio and difference between clay water content and liquid limit. These parameters take into account the influence of each phase and the influence of soil plasticity. Thus, this method allows reducing the number of variables for the description of the erosion sensitivity.

It is shown that for Mix 0 soil, water content discrepancy of 4% is sufficient to induce a variation of soil erodibility from highly resistant to erodible. Thus the use of predictive equation for real structure needs to take into account the soil heterogeneities and the composition of pore and eroding fluid.

Acknowledgement

The authors wish to acknowledge Electricité de France (EDF-CIH) for the funding of the work and for their advice.

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