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Logarithmic Fermi-liquid breakdown in NbFe$_2$

M. Brando, 1, 1 W. J. Duncan, 1 D. Moroni-Klementowicz, 1 C. Albrecht, 1 D. Grüner, 2 R. Ballou, 3 and F. M. Grosche 1, 1

1 Dept. of Physics, Royal Holloway, University of London, Egham TW20 0EX, UK
2 Max-Planck-Institut for Chemical Physics of Solids, D-01187 Dresden, Germany
3 Institut Néel, CNRS & Université Joseph Fourier, BP 166, F-38042 Grenoble Cedex 9, France

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The d-electron low temperature magnet NbFe$_2$ is poised near the threshold of magnetism at ambient pressure, and can be tuned across the associated quantum critical point by adjusting the precise stoichiometry within the Nb$_{1-y}$Fe$_{2+y}$ homogeneity range. Preparing samples close to the critical composition $y = -0.015$ enables the first detailed investigation of the thermodynamic and transport signatures of Fermi liquid breakdown in a pure transition metal compound. In a nearly-critical single crystal ($y = -0.01$), we observe a $T^{3/2}$ power-law dependence of the resistivity $\rho$ on temperature $T$ and a logarithmic temperature dependence of the Sommerfeld coefficient $\gamma = C/T$ of the specific heat capacity, $C$, over nearly two orders of magnitude in temperature, extending down to 0.1 K.

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The standard model of metals, Fermi liquid theory, is expected to break down in clean systems at the low temperature border of magnetism, or magnetic quantum phase transition [1]. A wide range of possibilities exists, however, regarding the precise nature of this breakdown and of the resulting non-Fermi liquid states. Among these, arguably the mildest form of Fermi liquid breakdown involves a logarithmic energy dependence of the real part of the quasiparticle self-energy, while the imaginary part becomes linear in energy. In this logarithmic breakdown [2], the quasiparticle relaxation rate becomes comparable to the quasiparticle energy all the way down to the Fermi level, so that the quasiparticle resonance marginally cannot be resolved even in the low-energy limit. More drastic forms of Fermi liquid breakdown are suggested for those materials on which most of the available evidence for Fermi liquid breakdown near magnetic quantum phase transitions has been collected: in Ce- or Yb-based f-electron metals. In some of these, anomalous temperature dependences of the resistivity and of the heat capacity over extended ranges in temperature, as well as Hall coefficient discontinuities [3-6], have been taken to suggest non-Fermi liquid states in which local moments survive down to very low temperatures. These more extreme scenarios contrast with the “conventional” approach, in which the effects of quantum critical magnetic fluctuations are computed within a band picture of magnetism [7]. Clear-cut experimental evidence for the conventional breakdown scenario, paradoxically still scarce, may be found among the d-electron systems, because for many of these a band picture is much more clearly appropriate than for the inherently more complex f-electron compounds. In particular, the logarithmic Fermi liquid breakdown scenario has long been expected to be realised at the quantum critical point (QCP) of 3D band ferromagnets (fm). The experimental signature of logarithmic Fermi liquid breakdown in such systems are a leading-order logarithmic temperature dependence in $C/T$ and a sub-leading order $T^{5/3}$ contribution to the electrical resistivity [1, 7]. More detailed calculations (e.g. [8, 9]) suggest that the fm qcp may be inherently unstable, either towards first order transitions, or towards long-wavelength modulated structures. Even in these comparatively simple systems a range of phenomena may therefore be expected near the threshold of magnetism.

![Fig. 1](image-url)

**FIG. 1**: By adjusting the precise stoichiometry within a narrow homogeneity range, NbFe$_2$ can be tuned from ferromagnetism (FM) ($y > 0.01$) via an intermediate spin density wave modulated state (SDW) to a quantum critical point (QCP, $y \approx -0.015$). This paper discusses samples A (Fe-rich, $y = 0.015$), B (stoichiometric) and C (Nb-rich single crystal, $y = -0.01$). The precise composition of these nearly-stoichiometric samples has been determined from their lattice constants (from powder x-ray diffraction), which were compared against a scale drawn up by measuring the composition of a large number of samples using wavelength-dispersive x-ray spectroscopy, WDXS (inset).

A number of magnetic transition metal compounds have been investigated in the search for logarithmic Fermi liquid breakdown, including MnSi [10], ZrZn$_2$ [11, 12],
Ni$_3$Al [13] and Fe [14]. High pressure has been used in these cases to approach the fm qcp. Non-Fermi liquid forms have indeed been observed in transport properties, such as a distinctive $T^{5/3}$ power-law resistivity in MnSi over three orders of magnitude in temperature and, very recently, a striking linear-in-$T$ contribution to the thermal resistivity in ambient-pressure ZrZn$_2$ [15]. However, the technical constraints intrinsic to high pressure experiments have so far hindered multi-probe investigations. Alloying offers an alternative approach to the fm qcp [16], but the dopant concentration must be minimal. Otherwise, disorder-induced scattering may smear or completely remove phase transitions, or lead to diffusive transport, and site disorder or inhomogeneity may cause cluster or even spin-glass formation, all of which complicate the theoretical description and obscure the objective of the study.

Balanced on the threshold of magnetism at ambient pressure, the hexagonal C14 Laves phase compound NbFe$_2$ provides a new perspective to this long-standing problem. Stoichiometric NbFe$_2$ has been reported as a rare example of low-temperature spin-density-wave (SDW) order ([17], [18]). The SDW state grows out of low-ordered moment fm order, which can be induced by slight Fe-excess (Fig. 1). Slight Nb-excess, on the other hand, suppresses the SDW ordering temperature, and a qcp ($T_N \to 0$) is approached close to $\approx$ Nb$_{0.95}$Fe$_{1.985}$. Here, we report the first detailed study of a slightly niobium-rich single crystal of NbFe$_2$, which is very close to a magnetic qcp at ambient pressure. We find that the resistivity follows a $T^{3/2}$ power-law temperature dependence between 0.1 K and 10 K and that the heat capacity varies logarithmically with temperature between 0.1 K and 4 K. These results represent the first demonstration of the key experimental signatures of logarithmic Fermi liquid breakdown in a pure transition metal compound.

We present data from an iron-rich polycrystal (sample A, Nb$_{0.985}$Fe$_{2.015}$), a stoichiometric polycrystal (sample B, NbFe$_2$) and a niobium-rich single crystal (sample C, Nb$_{1.01}$Fe$_{1.99}$). The polycrystals have been prepared by melting together the elements (99.95% Nb, 4N vacuum-re-melted iron) in an argon atmosphere using radio-frequency induction heating on a water-cooled copper boat, immediately followed by a short (1-3 hour) anneal near 1000 $^\circ$C. Similarly, the single crystal has been obtained using a Czochralski method from an induction-heated melt in an argon atmosphere. Measurements of the resistivity, heat capacity, magnetisation and magnetic susceptibility down to 1.8 K have been carried out in a 9 T Physical Properties Measurement System (Quantum Design). High-resolution measurements of the resistivity at temperatures down to 50 mK were obtained in an adiabatic demagnetisation refrigerator (Cambridge Magnetic Refrigeration) by a standard 4-terminal AC technique. The low temperature heat capacity was determined in the same refrigerator by a relaxation-time technique.

Slightly Fe-rich NbFe$_2$ represents the point of departure of our investigation (Fig. 2). At 1.5% excess iron, we observe (i) Curie-Weiss behaviour in the inverse susceptibility down to $T_m \approx 32$ K, (ii) a kink in $\rho(T)$ at a slightly lower temperature $T_{\rho} \approx 25$ K and (iii) fm hysteretic loops in the lowest-temperature $M-H$ isotherms. Whereas the low-$T$ state clearly appears ferromagnetic, no ordered moment is observed between $T_m$ and $T_{\rho}$. This suggests that the transition at $T_m$ may be into a non-fm ordered state and that the transition to fm order happens only at a lower temperature $T_c \approx T_{\rho} < T_m$.

Reducing the Fe-excess lowers the magnetic transition temperature and changes the nature of the ordered state. Our findings confirm the reported interpretation that stoichiometric NbFe$_2$ forms a magnetically ordered, but not ferromagnetic, low temperature state (Fig. 3). We note that this state is characterised by a very high magnetic susceptibility $\gamma \sim 0.02$, which corresponds to a Stoner enhancement factor $\chi/\chi_0 \approx 180$, where $\chi_0 \approx 10^{-4}$ is the bare band structure susceptibility estimated from the calculated density of states $g(E_F) \approx 40$(Ry f.u. spin)$^{-1}$ [19]. The enhancement of the specific heat capacity Sommerfeld coefficient $\gamma = C/T \approx 45$ mJ/molK$^2$, with respect to its band structure value $\gamma_0 \approx 15$ mJ/molK$^2$, by contrast, is about 3, leaving a Wilson ratio $R_W = \chi/\gamma \tilde{n} \approx 60$, which suggests extreme proximity to ferromagnetism. We suspect that the so far unidentified magnetic order in NbFe$_2$ is a long-wavelength modulated

![FIG. 2](image_url): Magnetic properties of slightly iron-rich NbFe$_2$ (sample A). The inverse susceptibility follows a Curie-Weiss behaviour from 100 K down to $T_m \approx 32$ K, with fluctuating moment $\sim 1.0 \mu_B$/atom. Low temperature ferromagnetism is inferred from Arrot plot isotherms (upper left inset), which exhibit typical hysteretic behaviour with a remanent magnetisation $\sim 0.04 \mu_B$/atom. The $T$-dependence of the resistivity $\rho$ (lower right inset) exhibits a kink (arrow) just below $T_m$. Both above and below this kink $\rho(T)$ follows a $T^{5/3}$ power-law form.
state, possibly helical. The ordering wave-vector $Q$ may be estimated as $\sim 0.05 \text{ Å}^{-1}$, by inserting the measured $\chi_{Q=0} \simeq 0.02$ at $T_m$ into the dispersion $\chi_q^{-1} \simeq |q| |q - Q|^2$ with a typical $c \simeq 2.4 \cdot 10^{4} \text{ Å}^2$ (value determined for ZrZn$_2$ by neutron scattering). The very small magnetisation $M \simeq 0.02 \mu_B$/atom at just above the critical field leads us to expect, then, a weakly modulated structure with a wave-length of about 130 Å.

If the iron content in NbFe$_2$ is reduced beyond stoichiometry, our own results as well as literature data [17, 18] show that $T_m$ decreases, giving rise to a qcp at a composition close to Nb$_{0.01}$Fe$_{0.99}$. We have investigated the vicinity of this qcp in a slightly niobium-rich single crystal (Nb$_{0.01}$Fe$_{0.99}$), which despite its off-stoichiometric composition, has the highest residual resistance ratio (RRR $\simeq 18$) of all the samples presented.

The $H - T$ map of the susceptibility of this single crystal (Fig. 4) suggests magnetic order below $T_m \simeq 2.8$ K and a very small critical field $\mu_0 H_c \simeq 0.2$ T. Transition-metal compounds are governed by band energy scales which are orders of magnitude larger than those of narrow-band f-electron compounds. Rescaling temperature by the ratio of the Sommerfeld coefficients brings $T_m$ to a similar relative magnitude as, for example, in VbRh$_2$Si$_2$. Despite its residual, weak low temperature order the resistance of the single crystal follows a $T^{3/2}$ power law down to $T < 0.1$ K, and its heat capacity divided by temperature, $C/T$, increases logarithmically without any indication of a cross-over to conventional Fermi-liquid behaviour (Fig. 5). We have observed qualitatively similar behaviour in a number of single crystals of similar composition, but note that the precise value of the resistivity power-law exponent varies between 3/2 and 5/3. By contrast, in stoichiometric samples of NbFe$_2$ ($T_N \simeq 10$ K) $\rho(T)$ recovers a $T^2$ form below 0.6 K, and $C/T$ saturates for $T < 1$ K (inset of lower panel, Fig. 5) at values far below those observed in the single crystal. The precise form of $\rho(T)$ may depend on stoichiometry and sample orientation. The key result, however, anomalous forms for both the resistivity and the heat capacity, which are characteristic of logarithmic Fermi-liquid breakdown, is robust.

Our findings raise questions as to (i) why $\rho$ and $C/T$ appear unperturbed by the onset of magnetic order, (ii) the role of disorder, and (iii) the nature of magnetic order in Nb$_{0.01}$Fe$_{0.99}$. Firstly, the ordered moment below $T_m$ ($<0.02 \mu_B$) represents a tiny fraction of the fluctuating moment: magnetic order is then expected to have only a minor effect on the magnetic fluctuation spectrum and hence on the low-T properties (cf. small $C$ anomaly at $T_N \simeq 10$ K even in stoichiometric sample, inset of Fig. 5). Secondly, although a $T^{3/2}$ form for $\rho(T)$ has also been observed in spin-glasses (e.g. [21]), (i) in spin glasses this form for $\rho(T)$ is only seen below the freezing temperature, whereas here it also holds above $T_m$, (ii) the dynamic range of the anomalous resistivity is far larger in the pure compounds measured here than in reported spin glass measurements and (iii) the measured $C/T$ is completely inconsistent with that found in spin glasses. Finally, while the observed form for $\rho(T)$ cannot decide unambiguously between fn and SDW quantum criticality, the measured $C/T$ is consistent with predictions for a fn qcp. Naively, one would expect only a sub-leading $\sqrt{T}$.
FIG. 5: Quantum criticality in single-crystal Nb$_{1.01}$Fe$_{1.99}$ (sample C). Upper panel: $\rho(T)$ follows a power-law form with exponent significantly less than the Fermi-liquid value 2 over a wide range in $T$, down to 0.1 K. A detailed analysis involving piece-wise three-parameter fitting of the data (inset, horizontal bars indicate $T$-range, vertical bars indicate precision of exponent estimate) confirms that the power-law exponent locks into a stable value close to $3/2$ over nearly two decades of $T$-dependence, which increases the already high electronic contribution to $C/T$ at 4K by about 30% on cooling to 0.1 K.

correction to the Fermi-liquid form for the heat capacity close to a SDW qcp, but the situation is less clear, if the SDW ordering wavevector $Q$ is very small. Our bulk measurements as well as theory work [8, 9] suggest a small wavevector SDW state ($Q \sim 0.05\text{Å}^{-1}$) for stoichiometric NbFe$_2$. Quantitative calculations will be needed to clarify whether a small-$Q$ SDW qcp explains the observed experimental signatures, while renewed neutron studies are planned to identify the small-moment ordered state of NbFe$_2$.

Among the pure transition metal compounds – a class of materials believed to be well understood and yet full of surprising twists and discoveries – these findings represent the first clear indication of a logarithmic break-down of the Fermi liquid state, as expected at a 3D fm qcp. NbFe$_2$ may be sufficiently close to ferromagnetism for its critical behaviour to fall into this category. It presents a unique opportunity for multi-probe studies of band-magnet quantum criticality at ambient pressure.

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* New address: Max-Planck-Institut for Chemical Physics of Solids, D-01187 Dresden, Germany.
† New address: Cavendish Laboratory, Cambridge CB3 0HE, UK.