Thermodynamic phase diagram of Fe(Se0.5Te0.5) single crystals in fields up to 28 tesla

To cite this version:
Thierry Klein, D. Braithwaite, A. Demuer, W. Knafo, G. Lapertot, et al.. Thermodynamic phase diagram of Fe(Se0.5Te0.5) single crystals in fields up to 28 tesla. Physical Review B: Condensed matter and materials physics, American Physical Society, 2010, 82, pp.184506. <10.1103/PhysRevB.82.184506>. <hal-00957183>

HAL Id: hal-00957183
https://hal.archives-ouvertes.fr/hal-00957183
Submitted on 9 Mar 2014

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L’archive ouverte pluridisciplinaire HAL, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d’enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.
Thermodynamic phase diagram of Fe(Se$_{0.5}$Te$_{0.5}$) single crystals in fields up to 28 tesla

T. Klein,¹,² D. Braithwaite,³ A. Demuer,⁴ W. Knafo,⁵ G. Lapertot,³ C. Marcenat,³ P. Rodière,¹ I. Sheikin,⁴ P. Strobel,¹ A. Sulpine,¹ and P. Toulemonde¹

¹Institut Néel, CNRS, 25 rue des martyrs, 38042 Grenoble, France
²Institut Universitaire de France and Université J. Fourier, Grenoble 1, France
³SPSMS, UMR-E9001, CEA-INAC UJF-Grenoble 1, 17 rue des martyrs, 38054 Grenoble, France
⁴LNCMI, CNRS, 25 Avenue des Martyrs, BP 166, 38420 Grenoble, France
⁵LNCMI, UPR 3228, CNRS-UJF-UPS-INSa, 31400 Toulouse, France

(Received 1 October 2010; published 4 November 2010)

We report on specific heat ($C_p$), transport, Hall probe, and penetration depth measurements performed on Fe(Se$_{0.5}$Te$_{0.5}$) single crystals ($T_c$~14 K). The thermodynamic upper critical field $H_{c2}$ lines have been deduced from $C_p$ measurements up to 28 T for both $H\parallel c$ and $H\parallel ab$, and compared to the lines deduced from transport measurements (up to 55 T in pulsed magnetic fields). We show that this thermodynamic $H_{c2}$ line presents a very strong downward curvature for $T\rightarrow T_c$ which is not visible in transport measurements. This temperature dependence associated to an upward curvature of the field dependence of the Sommerfeld coefficient confirms that $H_{c2}$ is limited by paramagnetic effects. Surprisingly this paramagnetic limit is visible here up to $T/T_c$ ~0.99 (for $H\parallel ab$) which is the consequence of a very small value of the coherence length $\xi_c(0)$~4 Å [and $\xi_{ab}(0)$~15 Å], confirming the strong renormalization of the effective mass (as compared to DMFT calculations) previously observed in ARPES measurements [A. Tamai, A. Y. Ganin, E. Rozbicki, J. Bacsa, W. Meewasana, P. D. C. King, M. Caffio, R. Schaub, S. Margadonna, K. Prassides, M. J. Rosseinsky, and F. Baumberger, Phys. Rev. Lett. 104, 097002 (2010)]. $H_{c1}$ measurements lead to $\lambda_{c1}(0)$~430 ± 50 nm and $\lambda_{c1}(0)$~1600 ± 200 nm and the corresponding anisotropy is approximatively temperature independent (~4), being close to the anisotropy of $H_{c2}$ for $T\rightarrow T_c$. The temperature dependence of both $\lambda(\times T)$ and the electronic contribution to the specific heat confirm the nonconventional coupling mechanism in this system.

DOI: 10.1103/PhysRevB.82.184506

PACS number(s): 74.25.Dw, 74.70.Xa

I. INTRODUCTION

The discovery of superconductivity up to 55 K in iron-based systems¹ has generated tremendous interest. Among those, iron selenide (FeSe$_{1−x}$) [Ref. 2] has been reported to be superconducting with a critical temperature of 8 K at ambient pressure, rising to 34–37 K under 7–15 GPa.³ On the other hand, the substitution of tellurium on the selenium site in Fe$_{1−x}$Te$_x$ (Fe$_{1−x}$Se$_{1−x}$Te$_x$) increases $T_c$ to a maximum on the order of 14–15 K at ambient pressure⁴⁵ (for $x$~0.5). This binary compound is very interesting as it shares the most salient characteristics of iron based systems (square-planar lattice of Fe with tetrahedral coordination) but has the simplest crystallographic structure among Fe-based superconductors (no charge reservoir,⁶ so-called 11-structure). Moreover, even though the end point Fe$_{1−x}$Te [Ref. 7] compound displays antiferromagnetic ordering, a magnetic resonance similar to that observed in other parent compounds [with a (1/2, 1/2) nesting vector connecting the Γ and M points of the Fermi surface] is recovered for intermediate Te contents⁶⁹ suggesting a common mechanism for superconductivity in all iron-based superconductors. However, in contrast to iron pnictides which show only weak to moderate correlations, recent ARPES measurements suggested the existence of very large mass renormalization factors (up to ~20 as compared to DMFT calculations) [Ref. 10] indicating that Fe(Se,Te) is a strongly correlated metal differing significantly from iron pnictides.

In order to shed light on superconductivity in these systems, it is of fundamental importance to obtain a precise determination of both upper and lower critical fields and their anisotropy. Up to now $H_{c2}$ has mainly been deduced from transport measurements¹¹–¹³ and more recently by specific heat up to 14 T.¹⁴ As in other pnictides (see Ref. 15, and references therein), high $H_{c2}(0)$ values have been reported but, in the case of Fe(Se$_{1−x}$Te$_x$), strong deviations from the standard Werthamer-Helfand-Hohenberg model for $H_{c2}(T)$ have been reported. Those deviations have been associated to paramagnetic limitations (so-called Pauli limit).¹¹–¹³ However, in presence of strong thermal fluctuations (see discussion below), the determination of $H_{c2}$ from transport measurement becomes very hazardous and a thorough analysis was hence lacking of an unambiguous determination of $H_{c2}$ from specific-heat measurements.

We show that the $H_{c2}$ lines actually display a very strong downward curvature close to $T_c$ corresponding to $\mu_d dH_{c2}/dT$ values rising up to ~12 T/K for $H\parallel c$ and even ~45 T/K for $H\parallel ab$. This strong curvature, not visible in transport data, shows that $H_{c2}$ remains limited by paramagnetic effects up to temperatures very close to $T_c$ (up to $T/T_c$~0.99 for $H\parallel ab$). The corresponding Pauli field $H_p$ is slightly anisotropic ($H_p^{\parallel ab}/H_p^{\parallel c}$~0.8) whereas the orbital limit [$H_{c2}(0)$] presents a much stronger anisotropy $H_{c2}(0)^{\parallel ab}/H_{c2}(0)^{\parallel c}$~3–4. The huge $\mu_d H_{c2}(0)$ values (~130 ± 20 T for $H\parallel c$ and ~400 ± 50 T for $H\parallel ab$) correspond to very small coherence length values [$\xi(0)$~15 ± 1 Å and $\xi_{ab}(0)$~4 ± 1 Å] confirming the large value of the effective mass previously observed by ARPES (Ref. 10) and hence supporting the presence of strong electronic correlations in this system.

In addition, preliminary $H_{c1}$ measurements led to contradictory results. On the one hand, Yadav et al.¹⁶ reported on
rather high \( H_{c1} \) values \( \sim 100 \) G and \( \sim 400 \) G for \( H \parallel c \) and \( H \parallel ab \), respectively, with \( H_{c1} \) lines showing a clear upward curvature at low temperature. On the other hand, Bendele et al.\textsuperscript{17} obtained much smaller values (\( \sim 20 \) G and \( \sim 45 \) G for \( H \parallel c \) and \( H \parallel ab \), respectively) associated with a clear saturation of the \( H_{c1} (T) \) lines at low temperature. Finally, Kim et al.\textsuperscript{18} reported on strong deviations of the temperature dependence of the superfluid density \( \rho_s \propto 1/\lambda^{7.5} \) from the standard behavior, attributed to a clear signature of multigap superconductivity. We present here detailed first penetration field measurements performed with Hall sensor arrays in a variety of single crystals showing very different aspect ratios. We hence obtained \( \mu_0 H_{c1} (0) = 78 \pm 5 \) G and \( \mu_0 H_{c1}^\text{lab} (0) = 23 \pm 3 \) G. The \( H_{c1} \) lines clearly flatten off at low temperature but do not show the pronounced deep previously obtained in tunnel-diode oscillator (TDO) measurements.\textsuperscript{18} Our TDO measurements however led to a similar deep which is probably due to an overestimation of the absolute \( \Delta \lambda (T) \) value related to spurious edge effects. Finally, we obtained a temperature-independent \( \Gamma_{H_{c1} - H_{c1}^\text{lab}} \) values \( \sim 3.3 \pm 0.5 \) with \( \Gamma_{\lambda} \sim \lambda_{\text{ab}} \sim 4.0 \pm 0.8 \) (see below), being close to the \( \gamma_{H_{c1}} \) value obtained for \( T \to T_c \) (i.e., \( \sim H_{c1}^\text{lab}/H_{c1} \)).

Finally, we confirm that \( \lambda \propto T^2 \) in both crystallographic directions and show that the temperature dependence of \( C_p \) strongly deviates from the standard BCS weak-coupling behavior confirming the nonconventional coupling mechanism of this system. However, the amplitude of the specific heat jump is much larger than those previously reported in other Fe(Se,Te) samples and hence does not follow the \( \Delta C_p \) vs \( T_c \) scaling law reported in iron-based systems.\textsuperscript{19,20}

### II. SAMPLE PREPARATION AND EXPERIMENTS

We present here specific heat, transport, Hall probe, and tunnel diode oscillator (penetration depth) measurements performed in Fe\(_{1+x}(\text{Se}_{0.5}\text{Te}_{0.5})\) single crystals grown by two different techniques. Samples A have been grown using the sealed quartz tube method. The samples were prepared from pure iron and tellurium pieces and selenium shots in a 10:5:0.5 ratio, loaded together in a quartz tube which has been sealed under vacuum. The elements were heated slowly (100 °C/h) at 500 °C for 10 h, then melted at 1000 °C for 20 h, cooled slowly down to 350 °C at 5 °C/h, and finally cooled faster by switching off the furnace. Single crystals were extracted mechanically from the resulting ball, the crystals being easily cleaved perpendicular to their c crystallographic axis. The refined lattice parameters of the Fe\(_{1+x}(\text{Se}_{0.5}\text{Te}_{0.5})\) tetragonal main phase, \( a = 3.7992(7) \) Å and \( c = 6.033(2) \) Å, are in agreement with the literature.\textsuperscript{4,17} The real composition of the crystals checked by x-ray energy-dispersive microanalysis using a scanning electron microscope was found to be Fe\(_{1.052(2)}(\text{Se}_{0.552}\text{Te}_{0.452})\). The temperature dependence of the resistivity shows a metallic behavior at low temperature as expected for this low level \( (\delta = 0.05) \) of interstitial iron.\textsuperscript{21}

Samples of batch B were grown with the Bridgman technique using a double-wall quartz ampoule. The inside tube had a tipped bottom with a 30° angle and an open top. The inside wall of the outer ampoule was carbon coated to achieve the lowest possible oxygen partial pressure during the growth. The Bridgman ampoule was inserted in a three zone gradient furnace (1000°/°/°400°/°700°) and lowered at a speed of 3 mm/h. At the end of the growth, temperature was lowered to room temperature at 5 °C/h. Further characterizations of these crystals have been published elsewhere.\textsuperscript{13} The different single crystals used in this study have been listed in Table I.

The \( C_p \) measurements have been performed in magnetic fields up to 28 T using both an ac high sensitivity technique and a conventional relaxation technique. For ac measurements, heat was supplied to the sample by a light-emitting diode via an optical fiber and the corresponding temperature oscillations were recorded with a thermocouple (sample A1 and A4). In parallel, the specific heat (sample A5 and B1) were carried out in a miniaturized high-resolution microcalorimeter using the long-relaxation technique. The chip resistance used as both thermometer and heater as well as the thermal conductance of its leads have been carefully calibrated up to 28 T using a capacitance thermometer. Each relaxation provides about 1000 data points over a temperature interval of about 80% above the base temperature which has been varied between 1.8 and 20 K. Data can be recorded during heating and cooling. The merging of the upward and downward relaxation data provides a highly reliable check of the accuracy of this method.

Electrical transport measurements have been performed on sample B1 in static magnetic fields up to 28 T and pulsed magnetic fields up to 55 T and are described in detail elsewhere.\textsuperscript{13} We have also measured the resistivity of sample A5 with a commercial device (PPMS) up to 9 T.

The real part of the ac transmittivity, \( r' \), of samples A1 to A3 has been measured by centering these on a miniature GaAs-based quantum well Hall sensor (of dimension 8 × 8 \( \mu \text{m}^2 \)). The sensor is used to record the time-varying component \( B_{ac} \) of the local magnetic induction as the sample is exposed to an ac field \( \sim 1 \) Oe (\( \omega \sim 210 \) Hz). \( r' \) is then defined as: \( r' = [B_{ac}(T) - B_{ac}(4.2 \text{ K})]/[B_{ac}(T) - B_{ac}(4.2 \text{ K})] \). The remanent local dc field \( B_{rem}(H_d) \) in the sample has been measured after applying a magnetic field \( H_d \) and sweeping the field back to zero. In the Meissner state, no

<table>
<thead>
<tr>
<th>Sample</th>
<th>( d ) (( \mu \text{m} ))</th>
<th>( w ) (( \mu \text{m} ))</th>
<th>( l ) (( \mu \text{m} ))</th>
<th>Measured by</th>
</tr>
</thead>
<tbody>
<tr>
<td>A1</td>
<td>50</td>
<td>180</td>
<td>220</td>
<td>ac-( C_p ), HP, TDO</td>
</tr>
<tr>
<td>A2</td>
<td>60</td>
<td>300</td>
<td>750</td>
<td>HP</td>
</tr>
<tr>
<td>A3</td>
<td>65</td>
<td>400</td>
<td>600</td>
<td>HP</td>
</tr>
<tr>
<td>A3′</td>
<td>40</td>
<td>400</td>
<td>300</td>
<td>HP</td>
</tr>
<tr>
<td>A3″</td>
<td>40</td>
<td>100</td>
<td>100</td>
<td>HP</td>
</tr>
<tr>
<td>A4</td>
<td>( m \sim 50 \mu \text{g} )</td>
<td></td>
<td></td>
<td>ac-( C_p )</td>
</tr>
<tr>
<td>A5</td>
<td>( m \sim 1.1 \text{ mg} )</td>
<td></td>
<td></td>
<td>dc-( C_p ) R</td>
</tr>
<tr>
<td>B1</td>
<td>( m \sim 0.7 \mu \text{g} )</td>
<td></td>
<td></td>
<td>dc-( C_p ) R</td>
</tr>
</tbody>
</table>
vortices penetrate the sample and \( B_{\text{ren}} \) remains equal to zero up to \( H_o = H_f \) (the first penetration field). A finite remanent field is then obtained for field amplitudes larger than \( H_f \) as vortices remain pinned in the sample.

Finally, the London magnetic penetration depth in the Meissner state, \( \lambda \), has been measured on the same samples with a LC oscillating circuit (14 MHz) driven by a TDO. The samples have been glued at the bottom of a sapphire rod which were introduced in a coil of inductance \( L \). The variation in the penetration depth induce a change in \( L \) and hence a shift of the resonant frequency \( \delta f(T) = f(T) - f(T_{\text{min}}) \). \( \delta f(T) \), renormalized to the frequency shift corresponding to the extraction of the sample from the coil \( \Delta f_0 \) is then equal to the magnetic susceptibility. At low temperatures (typically for \( T \leq 12 \) K), \( \lambda \approx d \) (\( d \) being the lowest dimension of the sample, here the thickness), and we have \( \frac{\delta f(T)}{\Delta f_0} \approx \frac{1}{\lambda} \), where \( \lambda \) is an effective penetration depth depending on the field orientation and \( \tilde{R} \) an effective dimension of the sample. When the magnetic field is applied along the \( c \) axis, only the in-plane supercurrents are probed and \( \lambda = \lambda_{ab} \), whereas \( \lambda = \lambda_{ab} + \frac{1}{\lambda_c} \) for \( H \parallel ab \) (\( w \) being the width of the sample). The effective dimension \( \tilde{R} \) is calculated following Ref. 22.

### III. UPPER CRITICAL FIELD

Figure 1 displays typical ac measurements for both \( H \parallel c \) and \( H \parallel ab \) (sample A4). As shown, a well-defined specific-heat jump is obtained at \( T_c \) for \( H = 0 \) (\( \sim 20\% \) of the total \( C_p \)) and this peak progressively shifts toward lower temperature as the magnetic field is increased (here up to \( 28 \) T). The \( H_{c2} \) line has been deduced from the midpoint of the \( C_p/T \) anomaly after subtraction of a smooth polynomial background from the raw data. As shown in Fig. 2(A), the corresponding \( H_{c2} \) lines present a very strong downward curvature for \( T \rightarrow T_c \), which was not revealed by previous transport measurements [the same behavior is observed in all measured samples, see, for instance, Figs. 2(B) and 3(A) for a comparison between samples A4 and B1]. Note that a very similar curvature has been reported very recently from \( C_p \) measurements up to 14 T.14

Such a curvature is a strong indication for paramagnetic effects and we have hence fitted the experimental data using a weak-coupling BCS clean limit model including both orbital and Pauli limitations.23 This model only requires two fitting parameters (plus \( T_c \)): the initial slope \( dH_{c2}/dT \big|_{T=T_c} \) and the zero-temperature Pauli limit \( H_p \). The results are shown in Fig. 3(A) for sample A4 and B1. As shown, very good fits can be obtained in both samples using very similar fitting parameters: \( \mu_0 dH_{c2}/dT \big|_{T=T_c} \sim 38 \pm 3 \) T/K and \( \sim 13 \pm 2 \) T/K for \( H \parallel ab \) and \( H \parallel c \), respectively, and \( \mu_0 H_p \sim 45 \pm 2 \) T and \( \sim 54 \pm 4 \) T/K for \( H \parallel ab \) and \( H \parallel c \), respectively.

As previously observed in layered systems (see Ref. 24 and discussion in Ref. 25) \( H_{c2}^{ab} \) is actually very close to a \((1 - T/T_c)^{1/2} \) law. Strikingly, this simple behavior is valid up to \( T/T_c \sim 0.99 \) in our system [see Fig. 3(B)]. Such a dependence can be directly inferred from a Ginzburg-Landau (GL) expansion which leads to 25

\[
\left( \frac{H}{H_p} \right)^2 + \frac{H}{H_o} = 1 - \frac{T}{T_c}
\]

(1)

(\( H_p \) is the orbital field) i.e., \( H_{c2} \sim H_p(1 - T_{c})^{0.5} \) for \( H \gg H_p^2/H_o \). A fit to Eq. (1) [solid line in Fig. 3(B)] leads to \( \mu_0 H_p^{ab} \sim 65 \) T and \( \mu_0 H_p^{c} \sim 75 \) T, \( \mu_0 H_o^{ab} \sim 650 \) T, and \( \mu_0 H_o^{c} \sim 170 \) T (sample A4).20 We hence have \( \mu_0 H_p^{ab}/H_o \sim 6 \) T for \( H \parallel ab \), field which is reached for \( T/T_c \sim 0.99 \). Fe(Se,Te) is thus a rare example of superconductor for which the upper critical field is dominated by paramagnetic effects on almost the totality of the phase diagram (for \( H \parallel ab \)). A shown in Fig. 3(B), a linear dependence is recovered very close to \( T_c \) with \( \mu_0 dH_o^{ab}/dT \sim 45 \) T/K and \( \mu_0 dH_o^{c}/dT \sim 60 \) T/K.

---

**FIG. 1.** ac specific-heat measurements \( C_p/T^2 \) as a function of \( T \) of a Fe(Se,Te) single crystal (sample A4) for \( \mu_0 H=0, 8, 12, 16, 20, 24 \), and 28 T (from right to left) for (a) \( H \parallel ab \) and (b) \( H \parallel c \). The data have been renormalized taking \( C_p(T=20 \text{ K})=3.8 \text{ J/mol K} \). The \( H_{c2} \) line is deduced from the midpoint of the specific-heat jump after subtraction of a smooth polynomial background. (c) Specific heat from relaxation data (\( H \parallel c \)) for the indicated magnetic fields (sample A5). Inset: temperature dependence of the electronic contribution to the specific heat \( C_e = C_p - \beta T^2 - \delta T^2 \) (solid symbols), where the phonon contribution \( (\beta T^2 + \delta T^2) \) has been subtracted from the normal-state data [see thin line in Fig. 1(C)]. The BCS behavior for \( 2\delta/k T_c = 3.5 \) (solid line) and \( 2\delta/k T_c = 5 \) (dotted line) are displayed for comparison.
FIG. 2. (Color online) (a) $H$-$T$ phase diagram (batch A) in both $H_{ab}$ (open symbols) and $H_{c}$ (closed symbols) displaying the $H_{c2}$ line deduced from specific-heat measurements (see Fig. 1) (squares), the field corresponding to the onset of the diamagnetic screening (circles) as well as the fields corresponding to zero resistance (downward triangles) and $R/R_{N}$=0.5 (upward triangle, $R_{N}$ being the normal-state resistance). (b) Same as in (a) for sample B1. The transport data are taken from Ref. 13. See Fig. 3 for a direct comparison between the $H_{c2}$ lines in each batch.

$\sim$ 12 T/K, in good agreement with a values deduced from the BCS fitting procedure.\textsuperscript{27}

Those extremely high $H_{c}$ values are related to very small values of the coherence lengths $\xi_{ab,\parallel} = \frac{\phi_{0}}{2\pi \mu_{0} H_{c}} \sim 15 \pm 1$ Å and $\xi_{ab,\perp} = \xi_{ab} \times (H_{c2}^{ab}/H_{c}^{ab}) \sim 4 \pm 1$ Å which confirm the very strong renormalization of the Fermi velocity observed in ARPES measurements\textsuperscript{10} (see also theoretical calculations in Ref. 28). Indeed, one gets $v_{F,ab} = \pi \Delta \xi_{ab}/\hbar \sim 1.4 \times 10^{4}$ m/s [\(\Delta\) being the superconducting gap $\sim 2$ meV (Refs. 29 and 30)] i.e., $\nu_{v,ab} \sim 0.09$ eV Å in perfect agreement with ARPES data which also led to $\nu_{v,ab}$

FIG. 3. (Color online) (a) Comparison between the $H_{c2}(T)$ values deduced from specific-heat measurements in sample A4 (blue squares) and sample B1 (red circles) for both $H_{ab}$ (closed symbols) and $H_{c}$ (open symbols) and theoretical values for clean weakly coupled BCS superconductors including both orbital and Pauli limitations (solid lines). (b) $H_{c2}$ vs $(1-t)$ (sample A4) in a log-log scale ($t=T/T_{c}$) showing that the linear dependence of the $H_{c2}$ line rapidly crosses to a $\sim(1-t)^{3}$ dependence. The solid lines are fits to Eq. (1) (see text for details). The linear slopes close to $T_{c}$ ($\sim 45$ and $\sim 12$ T/K) extrapolate to very high orbital limits. On the contrary the irreversibility line (blue circles) displays the $(1-t)^{2}$ dependence characteristic of vortex melting.

$\sim 0.09$ eV Å for the $\alpha_{3}$ hole pocket centered on the $\Gamma$ point (note that the $H_{c2}$ line will be dominated by the band having the larger critical field, i.e., the lower Fermi velocity). Our measurements do hence confirm the strong correlation effects previously suggested by ARPES measurements.\textsuperscript{10}

An estimate of the paramagnetic field in the weak-coupling limit is given by the Clogston-Chandrasekhar for-
However, as pointed above, the onset of diamagnetism actually differs slightly from the onset of the diamagnetic response (see below and Ref. 13) confirming that the large apparent anisotropy of g deduced from those measurements is an artifact, probably related to the anisotropy of flux dynamics (see discussion on the irreversibility line below). The anisotropy of the upper critical field is then strongly temperature-dependent rising from $H_{c1}/H_{c2} \sim 0.8$ for $T = 0$, reflecting the small anisotropy of the g factor, to $H_{c1}/H_{c2} \sim 0.8$ for $H = 3.5–4$ close to $T_c$, reflecting the anisotropy of the coherence lengths (see Fig. 7).

IV. IRREVERSIBILITY LINE

The small $\xi$ values associated to large $\lambda$ values, $\lambda_{ab}(0) \sim 430$ nm (see below and Ref. 17) lead to strong fluctuation effects hindering any direct determination of $H_{c2}$ from either transport or susceptibility measurements. These fluctuations can be quantified by the Ginzburg number $G_i = (k_B \xi_i / \xi_0 \xi_c)^2 / 8$, where $\xi_0 = (\Phi_0 / 4 \pi \lambda_{ab})^{1/2}$ is the line tension of the vortex matter. One hence obtains $\xi_0 \xi_c \sim 40$ K (as a comparison $\xi_0 \xi_c \sim 200$ K in cuprates) and $G_i = 10^{-2}$ which is very similar to the value obtained in YBa$_2$CuO$_{2+\delta}$. In YBa$_2$Cu$_{2−x}$Fe$_x$O$_{6−\delta}$ (so-called 1111-phase, see Ref. 32, and references therein) clearly showing that thermal fluctuations are very strong in this system.

To emphasize this point, we have reported in Fig. 2, the temperatures corresponding to both $R = 0$ and $R/R_0 = 0.5$ deduced from transport measurements up to 9 T for sample A4 (see also Fig. 4) and even up to 50 T for sample B1 (see Ref. 13) ($R_0$ being the normal state resistance). As shown, none of those lines present the strong downward curvature obtained in $C_p$ measurements. On the contrary, the $R/R_0 = 0$ lines vary almost linearly with $T$ with $d\mu_B H/dT \sim 11$ T/K and $5$ T/K for $H_{ab}$ and $H_{bc}$, respectively, in agreement with previous measurements. However, as pointed above, these lines do not correspond to any thermodynamic criterion and discussions of the corresponding lines should hence be taken with great caution. Moreover whereas the midpoint of the specific heat coincides with the $R = 0$ temperature for $H = 0$ in sample A4, this midpoint rather lies close to the $R/R_0 = 0.5$ point in sample B1 clearly showing that neither of those two transport criteria can be associated with the $H_{c2}$ line.

Similarly, as previously observed in high-temperature cuprates and 1111-pnictides, the onset of the diamagnetic response ($T_H = 0$) also lies well below the $H_{c2}$ line [see Figs. 2(A) and 4]. Indeed, this onset is related to the irreversibility line above which the system is unable to screen the applied ac field due to the free motion of vortices. This irreversibility line is then expected to lie close to the $R = 0$ line. As shown in Fig. 4 the onset of diamagnetism actually differs slightly from the onset of resistivity. This difference is much probably related to different voltage-current criteria (the magnetic screening corresponds to much smaller electric fields but requires higher currents) but both lines present the positive curvature characteristic of the onset of irreversible processes. Note that, as expected for vortex melting (for a review see Ref. 33), the irreversibility line (here defined as the onset of $T_r'$) varies as: $\mu_B H \propto (1 - T/T_c)^\alpha$ with $\alpha = 2$ [see Fig. 3(B)]. A similar curvature has also been reported by Bendele et al. for the irreversibility field deduced from magnetization measurements.

V. LOWER CRITICAL FIELD

The first penetration field has been measured on a series of Fe(Se$_{0.5}$,Te$_{0.5}$) samples with very different aspect ratios...
(see Table I). To avoid spurious effects associated to strong pinning preventing the vortex diffusion to the center of the sample, \( H_f \) has also been measured on several locations of the same sample. The inset of Fig. 5 displays typical examples on sample A3’ (two positions) and A3”. In samples with rectangular cross sections, flux lines partially penetrate into the sample through the sharp corners even for \( H_u < H_f \) but remain “pinned” at the sample equator. The magnetization at \( H_u = H_f \) is then larger than \( H_{c1} \) and the standard “elliptical” correction for \( H_{c1} \) \( \neq H_u \) (\( -N \) where \( N \) is the demagnetization factor) cannot be used anymore. Following Ref. 35, in presence of geometrical barriers, \( H_f \) is related to \( H_{c1} \) through

\[
H_{c1} \approx \frac{H_f}{\tanh(\sqrt{\alpha d/w})},
\]

where \( \alpha \) varies from 0.36 in strips to 0.67 in disks, \( d \) and \( w \) being the thickness and width of the sample, respectively. To reduce the uncertainty associated with the \( \alpha \) value as well as the \( d/w \) ratio in real samples of irregular shape, five different samples with different aspect ratios have been measured (see Table I). Sample A3’ has been cut out of sample A3 and finally A3” out of A3’ in order to directly check the influence of the aspect ratio on \( H_f \). The corresponding \( H_f \) values are reported in the inset of Fig. 7 together with the theoretical predictions from Eq. (2) taking \( \mu_0 H_{c1}^f = 78 \) G (the predictions for a an standard elliptical correction are also displayed for comparison).

The lower critical fields \( (\mu_0 H_{c1}^f, \mu_0 H_{c1}^{ab}) \) are then related to the penetration depth \( (\lambda_c, \lambda_{ab}) \) through

\[
\mu_0 H_{c1}^f = \frac{\Phi_0}{4\pi \lambda_c} \left[ \ln(\kappa) + c(\kappa) \right],
\]

\[
\mu_0 H_{c1}^{ab} = \frac{\Phi_0}{4\pi \lambda_{ab}} \left[ \ln(\kappa') + c(\kappa') \right],
\]

where \( \kappa = \lambda_{ab}/\xi_{ab}, \kappa' = \lambda_c/\xi_c \) and \( c(\kappa) \) is a \( \kappa \)-dependent function tending toward ~0.5 for large \( \kappa \) values. Taking \( \mu_0 H_{c1}^f = 78 G \) one gets \( \lambda_{ab}(0) \sim 430 \pm 50 \) nm, which is in fair agreement with muons relaxation data.\(^{31,36}\) This very large \( \lambda \) value confirms the general trend previously inferred in iron pnictides (see, for instance, Ref. 17, and references therein) pointing toward a linear increase of \( T_u \) vs \( 1/\lambda_{ab}^2 \) as initially proposed in cuprates by Uemura et al.\(^{37}\) For \( H_{c1}^{ab} \), no correction was introduced (flat samples) and one hence obtains \( \mu_0 H_{c1}^{ab} = \mu_0 H_{c1}^f = 23 \pm 3 G \) leading to \( \lambda_c \sim 1600 \pm 200 \) nm (taking \( \mu_0 H_{c1}^{ab} = 0.7 \times \mu_0 H_{c1}^f \sim 460 T \)).

As shown in Fig. 5, \( H_{c1}(T) \) clearly shows a saturation at low temperature. As a comparison we have reported on Fig. 5 the temperature dependence of the superfluid density deduced from muons relaxation data\(^{36}\) and \( \rho_S(T) \) measurements.\(^{18}\) Both \( H_{c1} \) and \( \rho_S(T) \) curves are similar but do not reproduce the important shoulder at 5 K of the superfluid density. This shoulder has been interpreted as a clear signature of multigap superconductivity and as a failure of the clean limit s-wave (including s±) pairing.\(^{18}\) Our measurements do not support this interpretation.

In order to shed light on this discrepancy, we have performed TDO measurements on each of the samples of Table I. As described in Sec. II, \( \lambda_c \) and \( \lambda_{ab} \) were deduced from the effective penetration depth \( \tilde{\lambda} \) measured for both \( H \parallel ab \) and \( H \parallel c \). As shown in Fig. 6 (sample A3”), both \( \Delta \lambda_{ab} \) and \( \Delta \lambda_c \) are proportional to \( T^* \) with \( n \) close to 2, in good agreement with previous measurements for \( H \parallel c \) (Ref. 18) (the same temperature dependence has been obtained for all samples). The TDO data then require the introduction of the value of \( \lambda_{ab}(0) \) to convert the \( \Delta\lambda(T) \) data into \( \rho_S(T) / \rho_S^{TDO}(0) = 1/[1 + \Delta \lambda_{ab}(T)/\lambda_{ab}(0)]^2 \). Introducing \( \lambda_{ab}(0) \sim 430 \) nm and taking \( R \sim 14 \mu m \) (from Ref. 22), \( \rho_S(T) \) shows a change of curvature around 5 K, very similar to the one previously reported in Ref. 18 (see inset of Fig. 6). A similar discrepancy has already been observed in MgCNi\(_3\) and interpreted as a reduction in the critical temperature at the surface of the sample due to a modification of the carbon stoichiometry.\(^{38}\) However, such an explanation is not expected to hold here as single crystals were extracted mechanically from the bulk.

It is important to note that the temperature dependence of the superfluid density is very sensitive to the absolute value of \( \Delta \lambda \) and, although very similar to the one reported by Kim et al.,\(^{18}\) the amplitude of \( \Delta \lambda_{ab}/T^2 \sim 40 \) \( A/\sqrt{K} \) observed in our samples is much larger than the one reported recently by Sarafin et al.\(^{14}\) \((-10 \sim A/\sqrt{K})\). Similar discrepancies in the absolute amplitude of \( \Delta \lambda \) have also been reported in other pnictides\(^{39}\) and have been attributed to complications from rough edges which may lead to an overestimation of \( \Delta \lambda \). Dividing the absolute \( \Delta \lambda_{ab} \) by a factor ~5 (i.e., taking \( R \)
FIG. 6. Temperature dependence of $\lambda_{ab}$ (solid symbols) and $\lambda_c$ (open symbols) deduced from the frequency shift in TDO measurements (sample A3, Table I). Inset: temperature dependence of the superfluid density $\rho_S^{\text{TDO}}(T)/\rho_S^{\text{TDO}}(0)=1/(1+\Delta\lambda_{ab}(T)/\lambda_{ab}(0))^2$ taking $\lambda_{ab}(0)=430$ nm and $R=14$ $\mu$m (solid symbols) [i.e., following Ref. 22, see corresponding $\Delta\lambda_{ab}(T)$ values on the main panel] or $R=70$ $\mu$m (open symbols). The average $H_{c1}(T)/H_{c1}(0)$ curve (see Fig. 5) is displayed as the thick solid line.

$=70$ $\mu$m for $H||c$ instead of 14 $\mu$m) actually leads to a very good agreement between TDO and $H_{c1}$ data (see Fig. 6) hence indicating that this value has probably been overestimated due to an underestimation of the effective dimension $R$ in presence of rough edges.

Very similar temperature dependences of $H_{c1}$ were obtained in both directions (see Fig. 5) leading to a (almost) temperature-independent anisotropy of $H_{c1}$: $\Gamma_{H_{c1}} \sim 3.4 \pm 0.5$ and hence $\Gamma_{H_{c1}}=\lambda_c/\lambda_{ab}=(H_{c1}^c/H_{c1}^{ab}) \times [(\ln(k_F^c)+c(k_F^c))/(\ln(k_F^{ab})+c(k_F^{ab}))]^{-1} \sim 1.2 \pm 0.8$ (see Fig. 7). This value is hence very close to the one obtained for $H_{c2}$ close to $T_c$, as $\Gamma_{H_{c2}}(T\rightarrow T_c) \sim \xi_{ab}/\xi_c$ (see Fig. 7). Similarly, very similar temperature dependences have been obtained for $\Delta\lambda_c$ and $\Delta\lambda_{ab}$ (with $\Delta\lambda_c \sim 5 \times \Delta\lambda_{ab}$ up to $T \sim T_c$) again suggesting a weak temperature dependence of this anisotropy. Finally, this value is also close to the one obtained for the irreversibility field deduced from the onset of diamagnetic screening.

VI. FINAL DISCUSSION

The value of the normal state Sommerfeld coefficient ($\gamma_0$) in Fe(Se$_{0.5}$Te$_{0.5}$) compounds remains debated as values ranging from $\sim 23$ mJ/mol K$^2$ (Ref. 40) to $\sim 39$ mJ/mol K$^2$ (Ref. 4) have been obtained. For nonsuperconducting samples, it has even been shown recently$^{31}$ that $\gamma_0$ rises rapidly for $x<0.1$ reaching $\sim 55$ mJ/mol K$^2$ for $0.1 \leq x \leq 0.3$. Even though our maximum field (28 T) is too low to fully destroy superconductivity down to 0 K hence hindering any precise determination of $\gamma_0$, it is worth noting that a $\gamma_0$ value on the order of $\sim 39$ mJ/mol K$^2$ is incompatible with the entropy conservation rule in our sample. A reasonable fit to the data [solid line in Fig. 1(C)] assuming $C_p/T = \gamma_0 + \beta T^2 + \delta T^4$ for $20 > T > 12$ K and $\mu_B H=28$ T leads to $\gamma_0=23 \pm 3$ mJ/mol K$^2$ in good agreement with the value obtained by Tsurkan et al.$^{30}$ This $\gamma_0$ value is also in fair agreement with the one deduced from ARPES measurements ($\sim 30$ mJ/mol K$^2$ (Ref. 10)).

Similarly, the Debye temperature ($\Theta_D \sim 143$ K) is in reasonable agreement with the one previously reported in both Fe(Se$_{0.57}$Te$_{0.43}$) ($\Theta_D \sim 174$ K (Ref. 4)) and Fe$_{1.05}$Te ($\Theta_D \sim 141$ K (Ref. 42)).

The electronic contribution to the specific heat ($C_p/T = C_{p,e}/T - \beta T^2 - \delta T^4$) is then displayed in the inset of Fig. 1 together with the theoretical prediction for a single-gap BCS superconductor in the weak-coupling limit (i.e., taking $2\Delta/k_B T_c \sim 3.5$, thin solid line). As shown, this standard behavior largely overestimates the experimental data at low temperature suggesting the presence of a much larger gap. A reasonable agreement to the data is obtained assuming $2\Delta/k_B T_c \sim 5$ (dotted line). However, even though some indication for the presence of a large gap were obtained by fitting either $\mu$SR (Ref. 36) or optical conductivity$^{33}$ data, the corresponding gap value ($\sim 3$ meV) is much larger than the value obtained by spectroscopy ($\sim 1.8$–2 meV (Refs. 29 and 30)). Moreover those former measurements also suggest the presence of a much smaller gap which is not present in our specific-heat measurements.

Some evidence for nodes (or for deep gap minima) in Fe(Se$_{0.5}$Te$_{0.5}$) has been suggested by fourfold oscillations in the low-temperature specific heat for $H||c$.$^{44}$ However, despite the high resolution of our ac technique and the very good quality of our samples (the specific heat jump at $T_c$ is slightly larger than in Ref. 44) we did not observe these
oscillations in our samples [i.e., $\Delta C_p/(\Delta H/\Theta) < 10^{-2}$]. Nodes are also expected to show up in the field dependence of the Sommerfeld coefficient $[\gamma(H)]$ which is then expected to vary as $H^p$ with $\gamma < 1$ (as $\alpha = 0.5$ for the so-called Volovik effect for $d$-wave pairing with line nodes whereas $\alpha = 1$ for classical single-gap BCS systems). We have hence extrapolated the $C_p(T)/T$ data to zero using either a BCS formula (see discussion above, $C_p/T - \gamma(H) \propto \exp[-(\Delta H)/kT]$ in our temperature range) or a phenomenological second-order polynomial fit. Both procedure led to a concave curvature for $\gamma(H)$ with $\alpha \approx 1.5 \pm 0.3$ for $H||c$ and $\alpha \approx 2.2 \pm 0.6$ for $H|ab|$. This concave behavior can be attributed to the effect of Pauli paramagnetism on the vortex cores\(^{45}\) (see Refs. 46 and 47 for experimental data in heavy fermions) hence clearly supporting the importance of these effects in Fe$_2$(Se$\delta$(Te$_{1-x}$)$_x$).

Finally note that the temperature dependence of the superfluid density can be fitted by either a parabolic or a linear dependence on $T$ in our experiments which is clearly lower than the experimental value $\rho_0 = 0.5$ for the so-called Vоловик effect in iron pnictides for which $\rho_0 = 0.5$ for the so-called Vоловик effect in iron pnictides. Hence we hence extrapolate the $\rho_{0}(T)$ curve as $\rho_{0}(T) = 0.5$ (see Refs. 46 and 47 for experimental data in heavy fermions) hence clearly supporting the importance of these effects in Fe$_2$(Se$\delta$(Te$_{1-x}$)$_x$).

VII. CONCLUSION

In summary, (i) precise determinations of the $H_{c2}$ lines from $C_p$ measurements led to a very strong downward curvature, similar to that observed in layered systems.

(ii) The temperature dependence of the upper critical field and the field dependence of the Sommerfeld coefficient both indicate that $H_{c2}$ is limited by strong paramagnetic effects with $\mu_0H_{c2} \sim 45 \pm 2$ T and $\sim 54 \pm 4$ T for $H|ab$ and $H||c$, respectively.

(iii) The very small value of the coherence length $\xi_{ab}(0) \sim 15 \AA$ confirms the strong renormalization of the effective mass (compared to DMFT calculations) previously observed in ARPES measurements\(^{10}\) and associated strong electron correlation effects. $\gamma$ is estimated to $\sim 23 \pm 3$ mJ/mol K$^2$ in fair agreement with the ARPES value.

(iv) The anisotropy of the orbital critical field is estimated to be on the order of 4 hence leading to a $\xi_{ab}(0)$ value smaller than the $c$ lattice parameter.

(v) Neither the temperature dependence of $\lambda$ nor that of the electronic contribution to the specific heat follow the weak-coupling BCS model (an BCS dependence with $\Delta/kT \sim 5$ remains possible) but no evidence for nodes in the gap is obtained from the field dependence of the Sommerfeld coefficient. We did not observe the fourfold oscillations of the low-temperature specific heat previously obtained by Zeng et al.\(^{44}\)

(vi) The amplitude of the specific-heat jump $\Delta C_p/T_c \sim 40 \pm 5$ mJ/mol K$^2$ is much larger than that previously observed in Fe$_2$(Se$\delta$(Te$_{1-x}$)$_x$) and does not follow the $\Delta C_p/T_c^2$ inferred in iron pnictides. Similarly neither the slope of the $H_{c2}$ line nor the absolute value of $\Delta\lambda(T)$ obey the scaling laws previously proposed for iron pnictides.\(^{48,49}\)

(vii) $\lambda_{ab}(0) = 430 \pm 50$ nm and $\lambda_{c}(0) = 1600 \pm 200$ nm, confirming the very small superfluid density previously observed in iron pnictides. The corresponding anisotropy is almost temperature independent with $\Gamma_{\lambda} \sim T_{c2}(T-T_{c}) \sim \gamma_{\xi}$.

(viii) These large $\lambda$ values associated to small $\xi$ values lead to a very small condensation energy $\epsilon_0 \xi^2 \sim 40$ K and hence to large fluctuation effects hindering any determination of $H_{c2}$ from either transport or susceptibility measurements. A detailed analysis of the influence of these fluctuations on the specific-heat anomaly will be presented elsewhere.

(ix) The strong upward curvature of the irreversibility line (defined as the onset of diamagnetic screening): $H_{irr} \sim (1 - T/T_{c})^2$ strongly suggests the existence of a vortex liquid in this system.

ACKNOWLEDGMENTS

This work has been supported by the French National Research Agency, Grant No. ANR-09-Blanc-0211 SupraTerrafer and ANR “DELICE,” and by the Euromagnet II grant via the EU under Contract No. RII-CT-2004-506239. T.K. is most obliged to V. Mosser of ITRON, Montrouge, and M. Konczykowski from the Laboratoire des Solides Irradiés, Palaiseau for the development of the Hall sensors used in this study. We thank J.-P. Brison for the software used to fit the $H_{c2}$ data.