Large-scale Experimental Validation of a Model for the Kinetics of Ozone and Hydroxyl Radicals with Natural Organic Matter

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ABSTRACT. A unified model for the kinetics of O₃ and •OH with NOM was proposed, calibrated and validated based on large experimental datasets. Single phase batch experiments were done on 11 water samples from 7 resources. Seasonal variations were studied on 3 resources. Effects of reaction time with ozone, ozone dose, pH, temperature, radical scavenger adding, NOM dilution were studied. The experiments represented more than 1200 and 900 concentration measurements, respectively for ozone and *p*CBA (•OH tracer). Mechanistic models were used for ozone self-decomposition and carbonate species kinetics. Results showed that the proposed model is robust and can handle different water characteristics and different experimental conditions: 75% of the experiments were modeled satisfactorily (for ozone and *p*CBA). Following domain of validity was determined: $6 \leq \text{pH} \leq 8$; $1 \text{ meq.L}^{-1} \leq \text{alkalinity} \leq 6 \text{ meq.L}^{-1}$; $0-0.5 \text{ mgC.L}^{-1} \leq \text{TOC} \leq 3.1 \text{ mgC.L}^{-1}$. Only water samples with high organic (TOC > 2.4 mg.L⁻¹) and low inorganic contents (alkalinity < 0.3 meq.L⁻¹) could not be modeled adequately. Seasonal comparisons showed that the quality of the predictions decreases only for *p*CBA when having calibrated the model at another season. The model gave good results when using only 6 single batch experiments for calibration.

KEYWORDS. Ozone Decomposition, Natural Organic Matter, Kinetics, Drinking Water Treatment, Bromate, Model Calibration, Process Simulation; Micropollutants.

HIGHLIGHTS.

- ◆ A reaction mechanism for O₃ and •OH with NOM is proposed, calibrated, and validated
- ◆ More than 2100 concentration measurements were used to validate the model
- ◆ 75% of the experiments were modeled satisfactorily, for O₃ and •OH
- ◆ Validity domain: $6 \leq \text{pH} \leq 8$; $1 \leq \text{alkalinity} \leq 6 \text{ meq.L}^{-1}$; $0-0.5 \leq \text{TOC} \leq 3.1 \text{ mgC.L}^{-1}$
- ◆ The model for ozone is robust against seasonal variations in NOM

ABBREVIATIONS.

A_T: Alkalinity

NOM: Natural Organic Matter

*p*CBA: *Para* ChloroBenzoic Acid

SUVA: Specific UltraViolet Absorbance

TOC: Total Organic Carbon

1. INTRODUCTION

Assisted by modeling tools, management of ozonation processes shall comply with conflicting standards on disinfection and by-products (bromate ions) [1], also taking into account emerging micropollutants. Recently, legal and environmental contexts indeed became more constraining: (i) in many countries, regulations on bromate have dropped to $10 \mu\text{g.L}^{-1}$ [2]; (ii) micropollutants are being increasingly detected in the environment [3].

While the chemistry of ozone is relatively well understood - and hence modeled - in synthetic water; in natural water, however, chemical phenomena are more difficult to study. Particularly, Natural Organic Matter (NOM), generally described as a poorly defined mix of organic substances [4], may react in different ways with ozone and hydroxyl radicals [5]. Also, NOM's composition is influenced by seasonal variations and particulate organic carbon inputs [6]. Finally, quantifying the concentrations of the many ozone-consuming sites in NOM remains difficult, as well as linking reaction kinetics of NOM with measurable physical data [7]. Consequently, there is a need to develop and evaluate unified kinetics models for NOM on the basis of large experimental datasets.

Several studies have already proposed or used models for the kinetics of ozone in natural water, but their results need to be extended, both experimentally and numerically. The simplest approach consists in postulating a pseudo-first order kinetic law for ozone decomposition (see *e.g.* [8] for a review). Some authors consider a two-steps decomposition of ozone, with laws of different orders; for instance, zero-order ("Instantaneous Ozone Demand") followed by first-order decompositions, *e.g.* [9]. When hydroxyl radicals are sought to be modeled, it is of convenience to use the R_{ct} concept [10] in order to recalculate hydroxyl radical concentration based on ozone concentration. This has been done to model: bromate and cryptosporidium fates in a pilot [11]; micropollutants removal in a full-scale wastewater ozonation unit [12]. Values for the R_{ct} are highly dependent on water characteristics and on NOM [13], but a recent study proposed an empirical calculation of the R_{ct} [14]. For more detailed descriptions of the chemistry of ozone, authors use reaction mechanisms. Westerhoff and coworkers [16] focused on the prediction of bromate formation, while Acero and von Gunten [17] focused on the impact of hydrogenocarbonate concentration. Both teams worked with NOM isolates from water samples. Only Bezbarua [15], based on a large experimental dataset, focused on the kinetics of ozone with NOM. A natural pond water sample was fractionated according to the method of Leenheer and Noyes [18] and the kinetics of each fraction was studied. However, predicting simultaneously ozone and hydroxyl radical concentrations remains no easy task [7], and previous studies need to be extended: experimentally, a limited number of water samples were studied; numerically, critical issues on model analysis were rarely discussed: domain of validity (including seasonal variations of NOM), model calibration, model validation.

The objective of this article is to study and validate a unified model for the kinetics of NOM with ozone and hydroxyl radicals based on a large experimental dataset. Special attention has been given to (i) define the domain of validity of the model (water characteristics, experimental conditions and seasonal variations of NOM); (ii) propose a small number of experiments for model calibration; and (iii) statistically evaluate the model's performance.

Since ozone and hydroxyl radicals are the two main oxidative species of ozonation processes, their concentrations have to be precisely measured and modeled before calculating disinfection, simulating the fate of micropollutants or the formation of bromate ions. The model was first evaluated statistically and its domain of validity determined using all experimental data for calibration. Robustness of the model against seasonal variations of NOM and experimental conditions was then studied and statistically assessed by calibrating the model only with a limited number of experiments.

2. MATERIALS AND METHODS

2.1. Experimental

The single-phase protocol presented in [19] was used in this study (including analyses). A 100 mL gas-tight syringe was used as reactor. Ozonized ultrapure water was injected through a sampling septum; volumes ranged from 3 mL to 5 mL. An oval stirring bar was used to achieve perfect stirring conditions. Throughout the experiment, samples (2 mL to 5 mL) were withdrawn for analysis. Two concentrations were followed during every experiment: ozone and *para* chlorobenzoic acid (*p*CBA, used as hydroxyl radical probe compound as in *e.g.* [20]).

The water samples were chosen in order to cover a wide domain of experimental conditions: pH, alkalinity (A_T) and Total Organic Carbon (TOC). Additionally, various types of natural water were investigated, taken from wells, from three different rivers and from dams or lakes. Each water sample was collected just before the ozonation unit at the corresponding local plant. Moreover, specific water resources were collected at different periods of the year to assess the effect of seasonal changes (Annet-sur-Marne, Meulan and Vitré). Details on the water samples are summarized in table 1.

The same experimental conditions as those presented in [19] were investigated in this study: reaction time with ozone, ozone dose, pH, temperature, presence of radical scavengers (10 mM *tert*-butanol), NOM dilution (for every water sample, the NOM concentration was varied by diluting the water sample with ultra pure water, ozonized and deozonized beforehand). Experiments were done according to three successive designs of experiments: a two-level full-factorial approach tested with {Méry-sur-Oise, Fall} and {Maisons-Laffitte, Winter} was later simplified (see [21]). The difference between low and high experimental temperatures was set at 5.5 °C for the first design of experiments, then increased to circa 15°C. In total, the dataset represented more than 1200 and 900 concentration measurements, respectively for ozone and *p*CBA, see table 1.

Table 1. Main characteristics of the water samples investigated and number of measurements (designs of experiments are separated by double horizontal lines)

Water sample Water origin		pH	A_T	TOC	SUVA	Number of experiments	Number of measurements	
			meq.L ⁻¹	mg C.L ⁻¹	L.mgC ⁻¹ .m ⁻¹		O ₃	<i>p</i> CBA
Méry-sur-Oise, Fall Sand filtered surface water	(Nov. 2008)	7.85	4.55	3.1	1.06	32	224	224
Maisons-Laffitte, Winter Artesian well	(Dec. 2008)	8.15	2.40	<0.5	-	32	224	224
Vitré, Winter Sand filtered dam water	(Feb. 2009)	7.40	1.02	2.0	1.3	14	98	56
Annet-sur-Marne, Winter Sand filtered surface water	(Feb. 2009)	7.40	2.82	1.3	1.43	14	98	56
Meulan, Spring Bank filtered surface water	(Mar. 2009)	7.25	6.24	0.9	2.02	14	98	56
Beaufort, Spring Sand filtered dam water	(Mar. 2009)	6.05	0.12	2.4	1.18	14	98	56
Trondheim, Spring Sand filtered Jontsvatnet Lake water	(Mar. 2009)	7.35	0.32	3.1	0.66	14	98	56
Annet-sur-Marne, Summer	(July 2009)	8.05	4.24	1.6	1.03	10	70	49
Annet-sur-Marne, Fall	(Oct. 2009)	7.70	3.08	1.6	1.23	10	70	49
Meulan, Fall	(Nov. 2009)	7.30	6.02	1.3	1.35	10	70	49
Vitré, Fall	(Nov. 2009)	7.10	1.24	2.3	1.03	10	70	49

2.2. Kinetics Models

2.2.1. Ozone Self-Decomposition

The mechanism used for ozone self-decomposition derives from that presented in [22]. The mechanism used in this study is presented in table 2.

Table 2. Mechanism for ozone self-decomposition

Type	Reaction	Kinetic constant value (T=293 K)		Reference
Initiation	$O_3 + HO^- \rightarrow HO_2^- + O_2$	$4.10^1 M^{-1}.s^{-1}$		[23]
	$HO_2^- + O_3 \rightarrow \bullet OH + \bullet O_2^- + O_2$	$2.8.10^6 M^{-1}.s^{-1}$		[24]
Propagation	$O_3 + \bullet O_2^- \rightarrow \bullet O_3^- + O_2$	$1.6.10^9 M^{-1}.s^{-1}$		[25]
	$\bullet HO_3 \rightarrow \bullet OH + O_2$	$1.1.10^5 s^{-1}$		[26]
	$\bullet OH + O_3 \rightarrow \bullet HO_2 + O_2$	$9.10^5 M^{-1}.s^{-1}$		[22]
	$\bullet OH + H_2O_2 \rightarrow \bullet HO_2 + H_2O$	$2.7.10^7 M^{-1}.s^{-1}$		[27]
	$\bullet OH + HO_2^- \rightarrow \bullet O_2^- + H_2O$	$7.5.10^9 M^{-1}.s^{-1}$		[27]
Termination	$2\bullet OH \rightarrow H_2O_2$	$5.10^9 M^{-1}.s^{-1}$		[28]
	$\bullet OH + \bullet O_2^- \rightarrow HO^- + O_2$	$10^{10} M^{-1}.s^{-1}$		[28]
	$\bullet OH + \bullet HO_3 \rightarrow H_2O_2 + O_2$	$5.10^9 M^{-1}.s^{-1}$		[29]
	$\bullet HO_3 + \bullet O_2^- \rightarrow HO^- + 2O_2$	$10^{10} M^{-1}.s^{-1}$		[29]
	$2\bullet HO_3 \rightarrow H_2O_2 + 2O_2$	$5.10^9 M^{-1}.s^{-1}$		[29]
Acid-base equilibria		Direct	Reverse	
pK _A = 8.2	$\bullet O_3^- + H^+ \leftrightarrow \bullet HO_3$	$5.2.10^{10} M^{-1}.s^{-1}$	$3.3.10^2 s^{-1}$	[26]
pK _A = 4.8	$\bullet O_2^- + H^+ \leftrightarrow \bullet HO_2$	$2.10^{10} M^{-1}.s^{-1}$	$3.2.10^5 s^{-1}$	[30]
pK _A = 11.6	$HO_2^- + H^+ \leftrightarrow H_2O_2$	$10^{10} M^{-1}.s^{-1}$	$4.2.10^{-2} s^{-1}$	[30]

2.2.2. Influence of Carbonate Species

Most reactions used to model the role played by carbonate species (*i.e.* inorganic carbon) were taken from [16]. Despite the high value of the pK_A of carbonate radicals, the initiation reaction producing a hydrogenocarbonate radical was neglected due to the minor role of the hydrogenocarbonate radical in radical scavenging. The complete mechanism is presented in table 3. The kinetics of the deprotonation reactions were calculated based on the pK_A values and on the kinetics of the protonation reactions.

Table 3. Mechanism for the influence of carbonate species

Type	Reaction	Kinetic constant value (293 K)		Reference
Initiation	$CO_3^{2-} + \bullet OH \rightarrow \bullet CO_3^- + HO^-$	$3.9.10^8 M^{-1}.s^{-1}$		[30]
	$HCO_3^- + \bullet OH \rightarrow \bullet CO_3^- + H_2O$	$5.10^7 M^{-1}.s^{-1}$		[28]
Propagation	$\bullet CO_3^- + HO_2^- \rightarrow CO_3^{2-} + \bullet HO_2$	$5.6.10^7 M^{-1}.s^{-1}$		[16]

Termination	$\bullet CO_3^- + H_2O_2 \rightarrow HCO_3^- + \bullet HO_2$	$8.10^5 M^{-1}.s^{-1}$	[28]	
	$\bullet CO_3^- + \bullet O_2^- \rightarrow CO_3^{2-} + O_2$	$4.10^8 M^{-1}.s^{-1}$	[16]	
	$\bullet CO_3^- + \bullet O_3^- \rightarrow CO_3^{2-} + O_3$	$6.10^7 M^{-1}.s^{-1}$	[31]	
	$\bullet CO_3^- + \bullet OH \rightarrow CO_2 + HO_2^-$	$3.10^9 M^{-1}.s^{-1}$	[16]	
Acid-base equilibria		Direct	Reverse	
pK _A = 10.3	$CO_3^{2-} + H^+ \leftrightarrow HCO_3^-$	$5.10^{10} M^{-1}.s^{-1}$	$2.5 s^{-1}$	[32]
pK _A = 9.6	$\bullet CO_3^- + H^+ \leftrightarrow \bullet HCO_3$	$5.10^{10} M^{-1}.s^{-1}$	$1.26.10^1 s^{-1}$	[33]
pK _A = 6.4	$HCO_3^- + H^+ \leftrightarrow H_2CO_3$	$5.10^{10} M^{-1}.s^{-1}$	$2.10^4 s^{-1}$	[32]

2.2.3. Influence of NOM

The model for the kinetics of NOM with ozone and hydroxyl radicals (called “model” in the following) used in this study is detailed in [19] and [21]. Reactive NOM was divided into three fractions (consumers, initiators and promoters) and six species (two for each fraction: an acid and its conjugate base). The reactions of NOM are summarized in table 4. In order to describe the acid character of the NOM fractions, a pK_A was defined for each fraction. The initial concentration and reactivity of each species (NOM^d_a , NOM^d_b , NOM^i_a , NOM^i_b , NOM^p_a and NOM^p_b) had to be calibrated. Because many organic compounds have pH-dependent kinetics in their reactions with ozone (*e.g.* formic and glyoxylic acids [5], phenolic groups [34]...), one of the species of each fraction was considered having a negligible reactivity. Moreover, temperature effects were modeled through the calibration of energies of activation. In the end, 12 model parameters had to be adjusted to fit simulations to experimental data: 3 initial concentrations, 3 kinetic constants, 3 pK_A and 3 energies of activation.

Table 4. Reactions with organic matter

Type (NOM fraction)	Reaction
Direct consumption (consumers)	$NOM^d + O_3 \rightarrow products$
Chain initiation (initiators)	$NOM^i + O_3 \rightarrow \bullet OH + products$
Chain promotion (promoters)	$NOM^p + \bullet OH \rightarrow \bullet O_2^- + products$
Acid-base equilibrium	$NOM^{d,i,p}_a \xrightleftharpoons{K_A^{d,i,p}} NOM^{d,i,p}_b + H^+$

2.3. Modeling Procedure

The concentrations of all chemical species involved in the kinetic models were calculated by solving mass balances. The gas-tight syringe was modeled as a perfectly stirred reactor; accordingly, the mass balance resulted in a large set of non-linear ordinary differential equations. An initial concentration was given to every chemical species; radicals were mostly given a default 10^{-10} μM concentration (detailed values shall be found in [21]).

2.4. Statistical Interpretation of the Results

Goodness-of-fit was measured following the recommendations of [35]: a combination of the value of the objective function O_f (see equation 1) and of the coefficient of determination R^2 was used. Handling experimental data with different orders of magnitude, the values for pCBA concentrations were weighted before calculating R^2 .

$$O_f = \sum_{i=1}^n \left(\frac{Y_{exp,i} - Y_{sim,i}}{Y_{exp,i} \cdot s_{exp,i}} \right)^2 \quad (1)$$

Where:

- n is the number of concentration measurements for a given water sample
- $Y_{exp,i}$ is the i^{th} concentration measurement
- $Y_{sim,i}$ is the i^{th} concentration simulation (issued from the model)
- $s_{exp,i}$ is the experimental standard deviation of the i^{th} concentration measurement

Three groups of experiments were defined:

- *very good* experiments, for which $R^2 > 0.7$ and $O_f < 1.5$;
- *good* experiments, for which $\{R^2 > 0.7 \text{ and } O_f \geq 1.5\}$ or $\{R^2 \leq 0.7 \text{ and } O_f < 1.5\}$;
- *mediocre or bad* experiments, in any other cases.

The boundary of 0.7 for R^2 was determined qualitatively. The value of 1.5 for O_f was determined statistically. 1.5 is the approximate median value of an empirical cumulative distribution function built with 5000 acceptable (*i.e.* equal to experimental values $\pm$ experimental error) data sets of simulated concentrations created randomly [21].

3. RESULTS

In order to evaluate the model and determine its domain of validity, all the experiments of each water sample were used for model calibration. We show in figures 1 to 5 how the model is able to take into account experimental condition changes: reaction time with ozone, ozone dose, pH, temperature, radical formation potential (with or without radical scavengers) and NOM dilution. Different water samples have been systematically chosen in order to give the best overview of the model's abilities. The global experimental uncertainties, determined with experiment replicates done with Méry-sur-Oise, Fall} and {Maisons-Laffitte, Winter} water samples are following: $\pm 0.1 \text{ mg.L}^{-1}$ for ozone and $\pm 4 \mu\text{g.L}^{-1}$ for pCBA.

Figure 1. Experimental and simulated concentration profiles, {Maisons-Laffitte, Winter} water: $A_T=2.4 \text{ meq.L}^{-1}$; natural $\text{pH}=8.15$; $T=13.5^\circ\text{C}$; no radical scavenger adding; $\text{TOC}<0.5 \text{ mg.L}^{-1}$; left: small ozone dose= 1.9 mg.L^{-1} , right: large ozone dose= 2.6 mg.L^{-1}

Figure 2. Experimental and simulated concentration profiles, {Meulan, Spring} water: $A_T=6.24 \text{ meq.L}^{-1}$; small ozone dose $\approx 1.9 \text{ mg.L}^{-1}$; $T=20^\circ\text{C}$; no radical scavenger adding; $\text{TOC}=0.9 \text{ mg.L}^{-1}$; left: $\text{pH}=7.25$, right: $\text{pH}=6.25$

Figure 3. Experimental and simulated concentration profiles, {Annet-sur-Marne, Fall} water: $A_T=3.08 \text{ meq.L}^{-1}$; small ozone dose $\approx 1.5 \text{ mg.L}^{-1}$; $\text{pH}=7.7$; no radical scavenger adding; $\text{TOC}=1.6 \text{ mg.L}^{-1}$; left: $T=23^\circ\text{C}$, right: $T=5^\circ\text{C}$

Figure 4. Experimental and simulated concentration profiles, {Méry-sur-Oise, Fall} water: $A_T=4.55 \text{ meq.L}^{-1}$; small ozone dose $\approx 1.9 \text{ mg.L}^{-1}$; natural $\text{pH}=7.85$; $T=19^\circ\text{C}$; $\text{TOC}=3.1 \text{ mg.L}^{-1}$; left: no radical scavenger, right: 10 mM *tert*-butanol adding

Figure 5. Experimental and simulated concentration profiles, {Vitré, Winter} water: $A_T=1.02 \text{ meq.L}^{-1}$; small ozone dose $\approx 1.5 \text{ mg.L}^{-1}$; lowered pH=6.4; $T=20^\circ\text{C}$; 10 mM *tert*-butanol adding; left: TOC=2 mg.L^{-1} , right: TOC=1 mg.L^{-1} (reached by dilution with ultra pure water, ozonated and deozonated beforehand)

Another illustration of the goodness-of-fit is given in figures 6 and 7 through the comparisons between experimental and simulated concentrations, for ozone and *p*CBA respectively ({Annet-sur-Marne, Summer} water sample). The complete set of experiments on {Annet-sur-Marne, Summer} water sample is presented in these figures, which represent the same 10 experiments. As it can be globally seen on figures 1 to 7, *p*CBA concentrations are more difficult to model than ozone concentrations. Note on figures 6 and 7 the relative position of the 90th percentile lines with regards to the experimental uncertainty. The modeling results obtained with {Annet-sur-Marne, Summer} water sample can be considered as average, with 2 experiments ranked *very good*, 5 experiments ranked *good* and 3 ranked *mediocre*.

Figure 6. Comparison of experimental and simulated concentration measurements for ozone, {Annet-sur-Marne, Summer} water sample, 10 experiments

Figure 7. Comparison of experimental and simulated concentration measurements for *p*CBA, {Annet-sur-Marne, Summer} water sample, 10 experiments

3.2. Testing the Model: Summary of Results

All the experiments were ranked according to the definitions of the quality groups used with the goodness-of-fit measures. The results are gathered in figure 8. Globally, 64% (7 out of 11) of the water samples have more than two thirds of their experiments which are considered as *good* or *very good*; 64% of the water samples have more than a third of their experiments which are considered as *very good*. The modeling results were not satisfactory for two water samples: Beaufort, Spring and Trondheim, Spring. For these water samples however, the *very good* experiments still represented around 25%.

Figure 8. Distribution of the quality of the simulations, all datasets

4. DISCUSSION

4.1. Domain of Validity of the Model

Results showed that the model is robust and can handle different water characteristics and different experimental conditions. The model is able to take into account all experimental condition changes (reaction time with ozone, ozone dose, pH, temperature, radical scavenger adding and NOM dilution). Moreover, modeling results are satisfactory for 75% of the experiments.

4.1.1. Water Quality Characteristics

The quality of the model predictions is contrasted for two water samples out of eleven: {Beaufort, Spring} and {Trondheim, Spring}. In both cases, ozone concentrations are well predicted while *p*CBA concentrations are modeled poorly (underprediction). Both samples have high organic content, and at the same time, low inorganic content. The water samples from {Vitré, Winter and Fall}, for which more than a third of the experiments were classified as mediocre or bad in figure 8, have also a large organic/inorganic ratio, to a smaller extent however.

One possible explanation for this limitation lies in a hypothesis of the model. Apart from consumers, initiators and promoters, authors generally consider radical scavengers when defining reactive NOM fractions [5]. In this study however, following the conclusions of [36], scavenger-acting species were regarded as negligible compared to carbonate species. This hypothesis may not hold anymore for water samples such as {Beaufort, Spring} and {Trondheim, Spring}. Therefore, test simulations were run with a model including a radical-scavenging fraction of NOM. The model was tested with {Trondheim, Spring} water, but the results were only slightly improved. Given the gap observed between the

experimental and simulated points (especially for long reaction times with ozone), it is likely that the stoichiometry (1:1) of the scavenging reaction has to be changed.

Finally, a wide range of water characteristics has been experimentally studied and modeled. If we consider three global indicators for water quality: pH, A_T and TOC, experiments have been done at low, medium and high values for the three indicators – including almost all $3^3 = 27$ possible combinations. Considering all the water samples modeled satisfactorily, the following domain of validity can be determined:

- $6 \leq \text{pH} \leq 8$;
- $1 \text{ meq.L}^{-1} \leq A_T \leq 6 \text{ meq.L}^{-1}$;
- $0\text{-}0.5 \text{ mgC.L}^{-1} \leq \text{TOC} \leq 3.1 \text{ mgC.L}^{-1}$.

4.1.2. Experimental Conditions

By reviewing the results obtained with the first and the second designs of experiments (discarding the results from {Beaufort, Spring} and {Trondheim, Spring}), a ranking of the best simulated experiments was established. It was found that some experiments were systematically well predicted while others less accurately.

The best predictions were obtained under following experimental conditions:

- Scavenger adding;
- Scavenger adding with simultaneous pH drop, temperature drop or NOM dilution;
- large ozone dose with simultaneous pH drop;
- large ozone dose with simultaneous NOM dilution.

Less accurate predictions were obtained for the following experimental conditions:

- large ozone dose;
- simultaneous temperature and pH drops;
- NOM dilution with simultaneous pH drop.

Experiments for which radical scavengers had been added were very well predicted whatever the other experimental conditions (pH drop, temperature drop, NOM dilution). This reflects the fact that predicting concentrations is simple for ozone compared to hydroxyl radicals. Predicting the impact of a change in initial ozone concentration is more difficult with the model as ozone and $p\text{CBA}$ concentrations were respectively slightly overpredicted and underpredicted when ozone dose was increased. This mismatch was reduced when pH was lowered or when NOM was diluted. An explanation relates to the assumption made for calculating the initial hydroxyl radical concentration. Based on typical reported values for the R_{ct} in natural water ([13]; [37]), the initial hydroxyl radical concentration was calculated according to: $[\cdot\text{OH}]_0 = 10^{-8} \cdot [\text{O}_3]_0$. The same R_{ct} value of 10^{-8} was used to simulate all experimental conditions. It has however been reported that R_{ct} changes with pH, temperature and NOM properties [13], but also more recently with ozone dose [38]. Predicting the impact of simultaneous drops in temperature and pH was also found to be difficult. It is likely that simultaneous temperature and pH drops would have been better modeled if temperature dependence for pK_{As} would have been taken into account.

4.1.3. Seasonal Variations of NOM

As the kinetics of ozone with NOM may be altered by seasonal variations of the water quality, the seasonal stability of the model has to be determined. This has been done by exploring the robustness of the model calibration: the values of the parameters found with {Annet-sur-Marne, Winter} water sample were used to simulate the experiments done with {Annet-sur-Marne, Summer} and {Annet-sur-Marne, Fall} water samples; the values of the parameters found with {Meulan, Spring} and {Vitré, Winter} water samples were used to respectively simulate the experiments done with {Meulan, Fall} and {Vitré, Fall} water samples. The results are presented in figure 9 and can be compared with the results obtained previously on {Annet-sur-Marne, Summer and Fall}; {Meulan, Fall} and {Vitré, Fall} water samples.

Figure 9. Distribution of the quality of the simulations done when calibrating the model at another season (sample names followed by “V” for “validation”), comparison with a calibration for each water sample

Results show that the quality of the predictions decreases when having calibrated the model at another season. This remark applies however differently to ozone and to *p*CBA. As illustration, we give in figure 10 the comparison of experimental and simulated concentrations for ozone and *p*CBA for all the water samples from Annet-sur-Marne, using the model calibrated only on the basis of the experimental results obtained with {Annet-sur-Marne, Winter}. On one hand, despite scattering of the points, predictions for ozone concentrations are relatively reliable and the model is found to be stable throughout the year. On the other hand, predictions for *p*CBA are much less accurate, even if the linearity between experimental and simulated data remains high ($R^2=0.86$ for {Annet-sur-Marne, Summer}; $R^2=0.84$ for {Annet-sur-Marne, Fall}). Note in particular the progressive drift of the results for *p*CBA concentrations. A similar trend was observed with the water samples from Vitré, and to a smaller extent, with the water samples from Meulan.

Figure 10. Comparisons of experimental and simulated concentration measurements for Annet-sur-Marne water samples. Model calibration based on {Annet-sur-Marne, Winter} results. Left: ozone; right: *p*CBA.

4.2. Reducing the Data Needed for Calibration: Validation of the Model

From a practical perspective, doing 10 to 32 experiments to calibrate the proposed model is feasible, still cumbersome and expensive. From a modeling perspective, if all the experimental data are used for calibration, there is no guarantee that the model is able to extrapolate to different experimental conditions.

A methodology, proposed in [21], combines experimental and numerical approaches (i) to reduce the experimental dataset needed for calibrating the model; (ii) and to reduce the number of parameters optimized together. On one hand, the most influent experimental conditions are determined by multiple linear regression analysis; by considering only these influent conditions, the number of calibration experiments is reduced. On the other hand, the most influent model parameters on the objective function are determined by sensitivity analysis; by sequencing the calibration of the parameters according to their sensitivities, the size of the mathematical problem is reduced.

The results of the multiple linear analysis performed on five water samples ({Méry-sur-Oise, Fall}; {Maisons-Laffitte, Winter}; {Annet-sur-Marne, Winter}; {Meulan, Spring} and {Vitré, Winter}) show that:

- Experimental ozone concentration is mostly sensitive to pH and temperature drops;
- Experimental *p*CBA concentration is mostly sensitive to the adding of radical scavengers.

The results of the sensitivity analysis show that:

- NOM fractions which mainly modify the concentration profiles for ozone and *p*CBA, are the initiating and consuming fractions;
- Promoting fraction plays a smaller role.

Based on these results, a reduced set of experiments was defined for calibration purposes. Six experiments were selected and used to calibrate the model (see [21]). The remaining experiments were used for validation. We present in figure 11 the results obtained with this reduced calibration procedure. Comparing with previous results (figure 8), it can be concluded that the reduced calibration procedure gives modeling results almost as good as those obtained with much more experimental data.:

- The number of experiments to do at laboratory to calibrate the model can be reduced. Doing the six experiments used in the reduced calibration procedure represents 2 days of lab work;
- The model was validated *a posteriori*, given that 70% of the experiments could be predicted satisfactorily by extrapolation (80%, when using all the experiments for calibration).

Figure 11. Distribution of the quality of the simulations for 6 water samples, full-dataset validation based on reduced-dataset calibration

4.3. Comparison to Other Modeling Studies

4.3.1. Amount of Data

Most authors who have modeled the kinetics of ozone with NOM focused on other aspects of the ozonation process: bromate formation ([39]; [11]), impact of inorganic carbon [17], fate of micropollutants ([40]; [41]), pathogen inactivation [11]. Consequently, little amounts of data can be found in these studies on the kinetics of ozone with NOM.

Studies focusing on the kinetics of ozone with NOM proposed to link the reactivity of natural water to that of NOM isolates. Therefore, those studies ([15]; [16]) focused on a single water source which was then thoroughly studied. In particular, Bezbarua [15] tested a model over a very large experimental dataset. However, the experiments were done with radical scavenger adding ($0.5\text{--}4 \cdot 10^{-4}$ M *tert*-butanol), whereas 45% the experiments of this study were done without *tert*-butanol adding. In addition, no study has, to our knowledge, compared the modeling of ozone and *p*CBA decompositions on water samples from different resources. The impact of seasonal variations of NOM on the modeling of the kinetics of ozone and hydroxyl radicals with NOM remains unpublished.

4.3.2. Values of the Parameters

Numerical tests gave evidence of the non-unicity of the solutions found for the values of the parameters [21]; we shall therefore not discuss in detail the values of the model parameters. It is likely that a high number of combinations for parameter values may lead to similar modeling results. Therefore, conclusions among modeling studies cannot be directly established and physicochemical conclusions should not be drawn. A similar remark was made for biological models (ASMs) [42]. The values of the parameters of the model can be found for each water sample in [21].

Figure 12. Distribution of the values of the model parameters (among the 11 water samples): pK_{AS} , kinetic constant rates, energies of activation, initial concentrations of the different NOM fractions

The values taken by the model parameters are globally consistent with common kinetic values reported for comparable reactions, as suggested by the boxplots of the pK_{AS} , kinetic constant rates, energies of activation and initial concentrations represented in figure 12. It is also interesting to note that, contrary to pK_A values, which are quite similarly distributed over the NOM fractions, kinetic constant rates and initial concentrations tend to be more dependent on the type of NOM fraction considered: constant rates for initiation tend to be evenly distributed among the 11 water samples and are generally below $100 \text{ M}^{-1} \cdot \text{s}^{-1}$, whereas for consumers they mostly range from $10^4 \text{ M}^{-1} \cdot \text{s}^{-1}$ to $10^6 \text{ M}^{-1} \cdot \text{s}^{-1}$ and for promoters from $10^7 \text{ M}^{-1} \cdot \text{s}^{-1}$ to $10^9 \text{ M}^{-1} \cdot \text{s}^{-1}$. Two initial concentrations for promoters were found higher than 1 mg C.L^{-1} , suggesting that only general conclusions should be drawn from comparisons among parameter values. These high values can be explained by the non-unicity of the solutions found and by the less important sensitivity of the model outputs towards the promoting fraction.

5. CONCLUSION

The proposed model is able to adequately reproduce changes in reaction time with ozone, ozone dose, pH, temperature, radical scavenger adding (*tert*-butanol), and NOM dilution (75% of the experiments were modeled satisfactorily). This model was validated on a very large experimental dataset comprising more than 1200 and 900 concentration measurements for ozone and *p*CBA, respectively (11 water samples from 7 water resources). Generally, ozone concentrations were better modeled than *p*CBA concentrations. Considering all the water samples modeled satisfactorily, the following domain of validity can be determined:

- $6 \leq \text{pH} \leq 8$;
- $1 \text{ meq.L}^{-1} \leq A_T \leq 6 \text{ meq.L}^{-1}$;
- $0\text{-}0.5 \text{ mgC.L}^{-1} \leq \text{TOC} \leq 3.1 \text{ mgC.L}^{-1}$.

Seasonal comparisons showed that the quality of the predictions decreases when having calibrated the model at another season. This remark applies however differently to ozone and to *p*CBA: predictions for ozone concentrations are reliable throughout the year, whereas predictions for *p*CBA are progressively drifted.

The experimental dataset for calibration could be reduced to 6 experiments, out of 32, without excessive loss in quality over the whole validity domain. For a group of five water samples, this alternate calibration procedure gave good results: 70 % of the experiments were modeled satisfactorily; when using all the experiments for calibration, 80 % of the experiments were modeled satisfactorily.

In order to broaden the results of this study, following modeling and experimental prospects can be formulated:

- It was not possible to adequately simulate waters with high TOC/A_T ratios, most likely because of the necessity for such matrices to consider a model for radical scavenging by NOM. First trials have been unsuccessful in incorporating NOM scavenging. Future work shall deal with this issue;
- A procedure to systematically minimize the number of experiments to be considered for calibration purposes may be developed. So far, six experiments have been chosen for a simplified calibration. Was this choice optimal? Could the number of experiments considered for calibration be further reduced?

The proposed model, together with a mechanistic model for the formation of bromate, has been implemented successfully at full-scale on an industrial ozonation unit [43]. Results showed that such an approach is sound and may be used for decision-support tools, in particular to address the trade-off between disinfection and by-product formation.

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