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Experimental assessment of dry stone retaining wall stability on a rigid foundation

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Abstract

Dry stone masonry retaining walls are present in the majority of mountainous areas all around the world, but the technique is marginal today in developed countries. The emergence of the concept of sustainable development calls for renewed use of this technique, both for the repair of existing retaining walls and the building of new ones. The objective of this research was to seek the knowledge necessary to ensure the stability of these structures, using experimental investigations in the laboratory and in situ. From this work, a model has been developed for calculating the stability of dry stone retaining walls. After laboratory testing to quantify the interface friction, the data obtained were used in a model based on the equilibrium of the forces at failure. The model considers the possibility of the internal failure of the wall, taking into account the irregularity of the geometry of the stones and of their arrangement, using a parameter determined by in situ experiments. Full-size on-site experiments on 5 walls (2 and 4 m high), loaded using hydrostatic pressure, are presented. These allowed quantification of the parameters of the model, and its validation for two types of material. These tests also determined the limits of monolithic behaviour of the masonry, thus defining failure and enabling the fulfilment of practical engineering requirements.

Keywords: Dry stone masonry retaining walls

1. Introduction

Dry stone masonry is a vernacular construction method found in various forms, in many areas all around the world. The system of construction consists in the laying out of the stones without using mortar, and calls for skilled masons. They must be able to make decisions about which stone to use and where to place it, while complying with the essential rules of dry stone masonry. The walls were generally built using materials directly available on or close to the site, which explains the great diversity of the existing works and their integration into the landscape. These walls often sat on the rock substratum, as the presence of stones on the surface, used in the construction, results from the rock existing at shallow depth.

Dry stone walling in European countries is considered to contribute to landscapes and cultures, and to make an important economic contribution to existing craft, agriculture and tourism

industries. Considering sustainable development objectives, dry stone has many advantages, especially if the stones are obtained from local quarries or are found in situ [10]. It thus seems legitimate to rehabilitate this ancestral technique, but this requires the establishment of scientific knowledge of the specific behaviour of dry stone retaining walls.

There is good historical literature relating to dry stone [2, 6], describing primarily, based on the empirical understanding of the relevant time, empirical methods for determining the dimensions of these walls. However, these are not usable for deriving modern engineering standards.

The principal difference between dry stone retaining walls and those constructed from concrete, or mortared masonry, is the absence of cohesion between the stones, which allows internal deformation. Moreover, the layering of the stone introduces sliding planes, which may open. It is proposed that these points should be accounted for in determining dimensions.

The modelling of a dry stone wall is difficult, because behind the apparent regularity of an existing wall face, many variations are hidden. These relate to the use of the natural materials

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available at the local level, and result in some heterogeneity of the geometry, arrangement and even strengths of the various stones of the wall, which are not taken into account by existing theoretical approaches:

- The model based on periodic homogenisation of masonry [5] as a regular block stack cannot take the stone variability or movement into account.
- The Discrete Element Method (DEM) used to model dry stone masonry by Dickens [8], Harkness [9] and Claxton [4] gives remarkable results for large displacements, but knowledge of stiffness parameters is required. These parameters are difficult to determine by experiment, particularly because of the strong heterogeneity of the walls. Modelling the real geometry of all blocks requires considerable work.
- the FEM used by Zhang et al. [12] has similar problems to DEM.

An alternative approach was therefore preferred, with a simpler model based on experimental observations, one more easily adopted in engineering practice. Experimental tests were conducted to characterize the constitutive elements of the wall (the stones, and the interfaces between them), and then the masonry itself, using hydrostatic loading of full scale walls.

This article is structured in three parts. The first part presents the experiments carried out in the laboratory on components of the wall: interface shear tests between two individual stones, and between two beds of stone.

The second part describes the proposed theoretical model, which considers the stability of the wall as a homogeneous structure on a rigid foundation. Its originality comes from the fact that it takes account of the characteristics of the material – the irregularity of the geometry of the stones and their arrangement – using the parameter θ , measured on site, which is the slope of the internal shear band compared to the initial stone bed. It is shown that it is necessary to take into account this internal failure, because it leads to the instability of the structure.

The third part presents the experimental in situ loading test of five walls by hydrostatic pressure. These tests were carried out on dry stone walls of 2 and 4 m height, built by skilled masons, in conformity with current and traditional best practice. They made it possible to quantify and validate the parameters of the model for two types of stone: limestone and schist.

Close attention was paid to displacement measurement analysis during the experiments, because the model cannot give information on displacements. The use of stereophotogrammetry [7] on the end elevation of a length of wall allows determination of local displacements on an entire section of wall, thus checking the two-dimensional displacement behaviour. This information was compared with observations using sensors on the front elevation, and with the direct measurement of the parameter θ .

2. Mechanical behaviour of “dry stone” material

The integrity of a dry stone wall is related to the stones which make it up. But Villemus [11] showed that the compression

Fig. 1. Two stone beds inside the LIRIGM shear box 100 cm $\times$ 100 cm.

strength of stone within a wall height lower than 6 m, which represents approximately 90% of existing walls in France on the national road network, seems sufficient. On the other hand, in the case of soft foundations, the compressive strength of the soil is critical in determining the dimensions of the wall.

2.1. Interface behaviour measured by the shear test

The shear strength of dry stone beds must be high enough to limit the displacement of the stone, in order to guarantee monolithic behavior of the wall. As a first investigation, the interface behavior between two cut stones was measured on samples 6 cm $\times$ 6 cm and 30 cm $\times$ 30 cm, using a shear box 30 cm $\times$ 30 cm at the LIRIGM of Grenoble and a traditional 6 cm $\times$ 6 cm, direct shear box. The cut sample faces removed the problem of macrorugosity.

However, to measure in a more realistic way what occurs in situ, shear tests were also carried out using a very large shear box, allowing the effect of interactions between the stones due to a wall's vertical and horizontal joints to be taken into account. In addition, this made it possible to represent correctly the macrorugosity of the various stones. The prototype shear box of 100 $\times$ 100 cm² [1] at LIRIGM of the Grenoble J. Fourier University was used. This allowed dry stone to be made in the lower box, to be sheared by a second bed, assembled in the upper box, Fig. 1.

For the filling of the lower half-box, the stones were selected so as to ensure a relatively flat upper surface of the stone bed, lying as close as possible to the shear plane of the box. Once arranged, the stones were wedged in place using small stones.

During the filling of the upper half-box, the vertical joints were crossed carefully to avoid continuous vertical joints across the shear plane. Wooden wedges and stiff barbed polymer geomembranes were placed between the stones and the horizontal plate of the shear box to ensure that all the stones had at least one contact with the plate transmitting the vertical load.

The vertical load produced an average normal stress varying from 30 to 130 kPa, roughly equivalent to the base of a wall 7.5 m high at the upper end. The shear rate was not constant, but was kept below 3 mm/min. The test was carried out on the same sample four times, with increasing values of normal stress. The displacement response from this procedure may not be equivalent to the real shear displacement, but this does not have serious implications on the calculation of the parameters c_m and the φ of the Coulomb law.

Table 1
Friction angle measured by 3 types of shear test

Stone name	6 × 6 cm ² box, cut samples	30 × 30 cm ² box, cut samples	100 × 100 cm ² box, uncut samples
Limestone from fields	37 ± 2°	37 ± 1°	38 ± 2°
Limestone of “St Gens”	36 ± 1°	36 ± 1°	Not measured

Fig. 2. Lower stone bed after shear testing of two stone beds 100 cm × 100 cm (limestone). The white zone consists of crushed pieces of stone.

During the test, stones sometimes broke by flexure, especially under high loadings. The surface of the stones was abraded, especially by sand created by crushing of the stone, as shown in Fig. 2.

Cohesion is always neglected, since it is induced by the very large shear box. The angle of friction obtained is close to that found by the other shear boxes, Table 1. It is extraordinary that the test with the small shear box makes it possible to directly obtain the friction at the interface between two stone beds. Following this finding, the angle of friction of the schists of “St Germain de Calberte” used in Section 4 was only measured by the 6 × 6 cm² shear box.

3. Limit equilibrium analysis of a dry stone masonry retaining wall

Dry stone retaining walls are load bearing retaining walls, which have long been analysed by considering the equilibrium of forces and moments applied to the wall treated as a rigid solid. This assumption is checked by determining if the resultant force lies within the central third of the foundation. In current engineering, external forces are usually obtained using the earth pressure coefficients given by Caquot et al. [3]. However, the test walls described here were loaded by water, giving simple hydrostatic pressure $\vec{p}_w$, with no shear component on the back of the wall, see Fig. 3.

A priori, a dry stone wall cannot be regarded as a rigid solid, even if the middle third rule is satisfied at the level of each stone bed, so that the wall is carrying the vertical compression throughout. A potential internal shear failure within the masonry AO (see Fig. 3) is defined by the angle θ and the height h_o where it emerges at the wall face, Fig. 3.

3.1. Wall behaviour assumptions

The following assumptions are made regarding the behaviour of the wall:

- There is no interaction between failure by the sliding/shearing of joints, and failure by rotation.
- The friction mobilised in shearing in the joints in the wall is given by the stone–stone friction measured in the laboratory, and corresponds to a pure Coulomb type of angle of friction φ_m , see Section 2.
- The inclination of the failure plane for shearing on the dry joints is given by an angle θ to horizontal, which may differ from the orientation of the construction bedding planes at an angle η to the horizontal. The inclination of the failure plane relative to the bedding planes is given by Θ , Fig. 3. This is because the irregularity of the stones allows rotation, crushing or displacement as the load is applied.

The two parameters, angle θ and height h_o , are thus characteristics of the wall construction, geometry and loading. They must be measured by experiment. The height h_o is a priori null if the foundation is a soft soil. The first stone bed will punch the soil, allowing rotation to the angle θ . In the case of the experimental walls, the foundation was rigid and one to two joints were necessary to enable rotation. We are assuming $h_o = 0$ gives larger loads, and so errs in the direction of safety.

3.2. Internal stability

If a linear stress distribution is assumed within the stone beds, the sections of the wall always remain compressed when the resultant force stays inside the central third of the wall section, which limits the relative eccentricity to $k = \frac{1}{6}$. As the dry stone construction has no tensile strength in the joints, if the resultant lies in front of the middle third, then there is no compression at the back of the wall, and the linear stress distribution starts from zero at a point which moves closer to the wall face as the eccentricity increases. Considering the moment equilibrium about the front of the wall gives a limiting value $k = \frac{1}{2}$. Between $\frac{1}{6}$ and $\frac{1}{2}$ the wall is still potentially stable, but as the value approaches $\frac{1}{2}$, the vertical stresses increase rapidly, reaching infinity at $k = \frac{1}{2}$. The simple assumption of linear stress distribution would, of course, be incorrect well before this stage is reached, if it is ever even approximately correct in a dry stone wall, which tends to deform primarily in shear rather than in the pure bending which is implicit in the assumption of a linear stress distribution.

In order to evaluate internal shear stability, the equilibrium of the forces is examined, Fig. 3. There is stability when

Fig. 5. Wall 5 construction; left: stone size heterogeneity, right: wall basement construction.

Table 2
Geometric and mechanical data about tested walls

	Wall 1	Wall 2	Wall 3	Wall 4	Wall 5
Height $h + h_o$ (m)	2	2	4	2	4.25
Free height unblocked at the basement (m)	1.85	1.85	3.85	1.90	4.10
Top width (m)	0.6	0.9	1.2	0.65	1.16
Basement width (m)	0.9	0.9	1.8	0.9	1.8
Batter fl (%)	15	0	15	12	15
ε	0.5	0	0.5	0.38	0.5
Volumic weight (kN/m ³)	15.4	15.0	15.7	16.0	18.0
Void percentage	25	27	24	23	32
Stone friction angle (in degree)	36 limestone	36 limestone	36 limestone	36 limestone	28.5 schist
Inclination of stone bed	Horizontal	Horizontal	Horizontal	$\eta = 4^\circ$	$\eta = 8.5^\circ$

Each wall was weighed after testing, so that together with measurements of the volume of the wall, the masonry's unit weight could be obtained, Table 2. For example, wall 3 was built with twenty-nine tons of stone.

4.2. Displacements measurement

From 8 to 10 displacement sensors measured the movement of the central section of the face of each wall during the loading. To supplement these measurements, photographic slides of one side of the wall were taken from a fixed point. The stereophotogrammetric analysis of these slides enabled the displacement of each stone to be determined, allowing the:

- comparison of the movement of the central part of the face measured by the sensors with the movements on one end of the wall at the same time, and hence validation of the assumption of plane strain.
- determination of the kinematics of failure, by observing the slip lines as well as the overall rotation.

The particular use of stereophotogrammetry in this project involves the photographic recording of two images of the same plane object undergoing a plane strain. The two images are

photographed from the same place, but at two different times. Slides measuring 6 cm by 6 cm were used. When viewed with a stereoscope, a false relief appears where there has been displacement within the plane between the two images. This false relief is proportional to the displacements which have occurred, and can be observed and recorded using normal stereographic procedures. This work was done in Laboratory 3S of Grenoble (data stereo-scope and processing). Further details of the technique are given by Desrues [7].

The displacements determined have an accuracy limited by the scale factor. The measurements on the images allowed an accuracy of ± 0.005 mm. Wall 3, which was 4 m high, was represented by 51 mm on the slide, giving a scale factor of 78.4. The resulting accuracy of displacement measurement was ± 0.4 mm, similar to that of the cable sensors.

The strain field was obtained using the Anadef software developed by Desrues [7]. From the points measured by a stereoscope, this software carries out a triangulation of the measured displacement field, the material being regarded as continuous, and hence mapping the strain tensor. The four-metre high walls comprised about 30 stone beds, each bed including 6–10 stones from the front to the back of the wall. The simplification of continuity for the purposes of stereographic

Fig. 6. Wall 5, left: wall facing displacement for varying relative eccentricity k ; right: horizontal displacement u versus stone position y_2 with a dilated scale.

mapping of displacements was thus found to be acceptable for qualitative interpretations.

4.3. Wall 5 loading test analysis

Only the results of wall 5 are presented in detail here. The full results are given in Villemus [11]. The model presented in Section 3 gives the following requirements for stability of the walls:

- k for overturning: marginal stability in the range $|k| < \frac{1}{2}$, certain stability for $|k| < \frac{1}{6}$,
- F_g for translation: stability for $F_g > 1$.

4.3.1. Displacements of the front face

The study of the movement of the front face of wall 5 (Fig. 6) showed the following characteristics, which had also been shown by the other walls:

- As the load increased, the wall remained a monolith until a load corresponding to $k = 1/6$ ($F_g > 1.2$). Beyond this load, the internal displacements were high but the wall remained stable.
- The wall is sheared from the base, the shear band increasing with the loading.

The Fig. 7 shows the wall before and after the failure. The belly-shaped deformation may be seen from both ends of the wall. Even after high displacements, the wall remained stable thanks to internal reorientation of the masonry, which is characteristic of the material.

Fig. 8(a) shows the relationship between displacements of points of the facing obtained from the cable sensors at the middle of the wall and the height of the water applying pressure to the back of the wall. These curves are of the same type as those obtained by direct shear testing of the stone interface. Full frictional strength was mobilised with displacements of just a few mm.

4.3.2. Comparison with stereophotogrammetric data

Stereophotogrammetric measurements were obtained for the entire cross section of the wall on the end elevation, whereas the cable sensors relate to the median of the external face of the wall. It is thus useful to check if the movement of the wall was uniform along its length, so that the measurements obtained by the two methods were the same. In Fig. 8(b), for the slide pair 01–03, the results obtained by the two methods are seen to be close together. The levels of loading corresponding to the slides are shown in Fig. 8(a). This indicates that the hypothesis of plane behaviour was correct.

The maps of the displacement vectors from slide pairs 01–04 are given in Fig. 9(a). The end section of wall photographed was not visible entirely, because the formwork retaining the PVC liner containing the water hid 30 cm of the back of the wall. The contours of displacement measured by stereophotogrammetric analysis therefore do not cover the entire cross-section of the wall. Nevertheless, a good representation is given of internal displacements of the wall, since the visible part corresponds to 80% of the total surface of the section. For clarity, the displacement vectors are drawn to an exaggerated scale. The measured area after deformation is represented on Fig. 9(a) by the dotted line.

The displacement vectors of (Fig. 9(a)) highlight the kinematic nature of the failure, which is an overall horizontal slip (pair 02–03 and 03–04). There is a rearrangement of the stones at a downward angle of approximately 11° (pair 01–02); for the following pairs, the slip tended to be approximately horizontal on the first “free” dry stone bed (located above the bed blocked by the foundation), and very slightly tilted (2.5° downwards) for the second “free” bed.

The failure of wall 5 was localized at the base of the wall; the remainder of the wall had a behavior under loading which was close to a rigid behavior, Fig. 9.

Fig. 7. Wall 5, left: before loading, centre and right: after loading “belly shape”.

Fig. 8. Wall 5, left: horizontal displacement u for 2 facing stones. Slides 02, 03 and 04 (resp. $k = 0.173$; 0.232 ; 0.296). Right: face stone displacement by 2 methods.

4.4. Summary of the 5 tested walls at failure

A clear distinction has been drawn between the shear slip and internal overturning failure mechanisms, described by independent factors of stability. All the walls (given in Fig. 4 and Table 2) showed shear (slip) failure mechanisms, and therefore Eq. (1) can be used for all the five walls. Walls 2 and 4 also displayed overturning mechanisms in conformity with the model.

The dry stone retaining walls' specific mechanism of failure, namely internal shear, was characterised by means of the parameter θ , which is the inclination of the slip failure compared to the horizontal. It is then possible, using $\theta = -\eta + \theta$, to define θ in relation to the form of the construction, i.e. in terms of the stone shape and the masonry quality.

It is now possible to calculate the value of θ , and therefore Θ for the full-scale tests, using Eq. (1) and the experimental

values of the failure load measured on site. ϕ_m , η and h_w were measured, the last giving p_w and then H . The unit weight was measured on site, giving V ; then letting $F_g = 1$ to represent the failure state enables the calculation of the theoretical θ , and hence Θ , in Table 3. The calculated values of Θ range from 5.5° to 11° , obtained on five tests and two types of stone (limestone and schist).

In order to use this simple model in practice, it is necessary to make the assumption that Θ will always be approximately in the range 5° – 11° , on the basis of the observations of walls 3, 4 and 5 (Table 3), for two types of stone (limestone and schist). If this assumption were found to be valid for a wider range of geometries and loading conditions, then Θ could be regarded as characteristic of dry stone masonry retaining walls in general. Then the calculation of F_g for any geometry and any load condition would enable simple design and assessment in practice.

Fig. 9. Wall 5, from left to right slide pairs 01–02, 02–03, 03–04, (a) displacement vectors, (b) distortion.

Table 3

Angle at failure from calculation and experiment, N.M.= Not Measured

	Value from	Wall 1	Wall 2	Wall 3	Wall 4	Wall 5
Failure slope	Theoretical	11.3	9.4	10.5	1.5	−0.5
θ (degree)	Photogrammetry	N.M.	N.M.	11.5	3.5	0–2.5
Stone rotation	Theoretical	11.3	9.4	10.5	5.5	8
Θ (degree)	Photogrammetry	N.M.	N.M.	11.5	7.5	8.5–11

5. Conclusions

The aim of sustainable construction and development has given rise to work within the European Region aimed at rehabilitating the use of dry stone masonry. This article aims to support the development of a scientific basis for its analysis and design, in order to reintroduce dry stone into current civil engineering practice.

In this article, our modelling follows a very pragmatic approach, by simplifying dry stone retaining walls as homogeneous, but taking into account their specific real characteristics, namely the problem of internal stability due to the shear planes naturally made by stone joints. Laboratory experiments showed that the interface shear behavior of these walls is governed by a pure friction law (non-cohesive), which does not depend on the sample size.

Then full-scale tests on dry stone retaining walls loaded by a hydrostatic pressure were analysed by stereophotogrammetry. This analysis described the internal mode of failure by shear (slip), which occurs after a local rearrangement of the stones that results in a rotation Θ of stones, leading to the failure slope

θ . Knowing the initial slope η of the dry stone beds of a wall (compared to the horizontal), and having an estimate of the values of Θ for two stone types, the relationship $\theta = \Theta - \eta$ may be checked.

Therefore, it is easy to take into account the internal shearing of a wall on a slope of θ , which differs from that of the initial stone bed, by using a simple equilibrium model. The calculated factor of stability of the slip, F_g , describes this type of failure satisfactorily, with the sliding occurring for values of F_g close to 1 ($F_g = 1 \pm 0.07$).

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