In vitro ultrasonic and mechanic characterization of the modulus of elasticity of children cortical bone
Jean-Philippe Berteau, Martine Pithioux, Cécile Baron, Launay Franck, Patrick Chabrand, Philippe Lasaygues

To cite this version:

HAL Id: hal-00937888
https://hal.archives-ouvertes.fr/hal-00937888
Submitted on 28 Jan 2014

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers.

L’archive ouverte pluridisciplinaire HAL, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d’enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.
Abstract: The assessment of elastic properties in children's cortical bone is a major challenge for biomechanical engineering community, more widely for health care professionals. Even with classical clinical modalities such as X-ray tomography, MRI, and/or echography, inappropriate diagnosis can result from the lack of reference values for children bone. This study provides values for elastic properties of cortical bone in children using ultrasonic and mechanical measurements, and compares them with adult values. 17 fibula samples from 8 children (4 to 16 years old, mean age 10 years old +/- 4.5) were compared to 16 fibulae samples from elderly adults (more than 75 years old). First, the dynamic modulus of elasticity (MOEdyn) and Poisson's ratio (ν) are evaluated via an ultrasonic method. Second, the static modulus of elasticity (MOEsta) is estimated from a 3-point microbending test. The mean values of longitudinal and transverse wave velocities measured at 10 MHz for the children's samples are respectively 3.2 mm/µs (+/- 0.5) and 1.8 mm/µs (+/- 0.1); for the elderly adults' samples, velocities are respectively 3.5 mm/µs (+/- 0.2) and 1.9 mm/ µs (+/- 0.09). The mean MOEdyn and the mean MOEsta for the children's samples are respectively 15.5 GPa (+/- 3.4) and 9.1 GPa (+/- 3.5); for the elderly adults' samples, they are respectively 16.7 GPa (+/- 1.9) and 5.8 GPa (+/- 2.1). MOEdyn, ν and MOEsta are in the same range for children's and elderly adults' bone without any statistical difference; a ranking correlation between MOEdyn and MOEsta is shown for the first time.
Title: In vitro ultrasonic and mechanic characterization of the modulus of elasticity of children cortical bone

Jean-Philippe Berteau
Laboratory of mechanics and acoustics (LMA) CNRS UPR 7051 Aix -Marseille University
Centrale Marseille, 31 chemin Joseph-Aiguier F-13402 Marseille cedex 20 France
Aix-Marseille University CNRS, ISM UMR 7287, 13288, Marseille cedex 9, France
Cécile Baron, Martine Pithiouxf, Franck Launay and Patrick Chabrand
Aix-Marseille University CNRS, ISM UMR 7287, 13288, Marseille cedex 9, France
Philippe Lasaygues
Laboratory of mechanics and acoustics (LMA) CNRS UPR 7051 Aix -Marseille University
Centrale Marseille, 31 chemin Joseph-Aiguier F-13402 Marseille cedex 20 France

Abbreviated title: Cortical bone elastic properties in children

Correspondence:
J-Ph. Berteau
Institute of Biomechanics, TUHH Hamburg University of Technology, Denickestrasse 15, 21073 Hamburg, Germany, Tel: +49 (0)40 42878 4376, Fax: +49 (0)40 42878 2996, e-mail:jph.berteau@gmail.com
2. Abstract

The assessment of elastic properties in children's cortical bone is a major challenge for biomechanical engineering community, more widely for health care professionals. Even with classical clinical modalities such as X-ray tomography, MRI, and/or echography, inappropriate diagnosis can result from the lack of reference values for children bone. This study provides values for elastic properties of cortical bone in children using ultrasonic and mechanical measurements, and compares them with adult values. 17 fibula samples from 8 children (4 to 16 years old, mean age 10 years old +/- 4.5) were compared to 16 fibulae samples from elderly adults (more than 75 years old). First, the dynamic modulus of elasticity (MOEdyn) and Poisson’s ratio (ν) are evaluated via an ultrasonic method. Second, the static modulus of elasticity (MOEsta) is estimated from a 3-point microbending test. The mean values of longitudinal and transverse wave velocities measured at 10 MHz for the children’s samples are respectively 3.2 mm/µs (+/- 0.5) and 1.8 mm/µs (+/- 0.1); for the elderly adults’ samples, velocities are respectively 3.5 mm/µs (+/- 0.2) and 1.9 mm/µs (+/- 0.09). The mean MOEdyn and the mean MOEsta for the children’s samples are respectively 15.5 GPa (+/- 3.4) and 9.1 GPa (+/- 3.5); for the elderly adults’ samples, they are respectively 16.7 GPa (+/- 1.9) and 5.8 GPa (+/- 2.1). MOEdyn, ν and MOEsta are in the same range for children’s and elderly adults’ bone without any statistical difference; a ranking correlation between MOEdyn and MOEsta is shown for the first time.

Keywords: Ultrasonic wave velocities -Elastic properties-Pediatrics-Cortical bone
3. Introduction

Cortical bone is an organic structure with mineral comprises approximately 80% of the human skeleton. Pathologies impacting human cortical bone quality include osteoporosis [1] in adults and osteopenia [2], Crohn’s disease [3] or osteopetrosis [4] in children. In addition to its cost in terms of health, European estimates predict that the direct cost of osteoporotic fracture will reach 76.7 billion € by 2050 due to demographic changes, notably the ageing of European populations [5]. A low bone mass in childhood is now recognized as a high risk factor for osteoporosis in later life [6] and authors consider the assessment of bone mineral status in children as a priority [7,8]. The Bone Mineral Density (BMD), which is one of the most gold standard parameters to assess mineral status, requires in the first intention, the use of the dual energy X-ray absorptiometry (DXA). The reference study [9] concerns only 7-17-year-old children, and was conducted with a Hologic DXA scanner (Hologic Inc., Waltham, MA, USA), ruling out comparison with values obtained via other scanners. However, the pediatric evaluation of the BMD raises problems of interpretation when the size of the bone varies related to the statural age of the child. The BMD is not correlated with the bone micro-architecture, and several studies have shown the ability of ultrasound measurement to assess the quantity and the quality of the explored bone area (elasticity and structure) [10,11].

There is a tremendous lack of data on young bone strength and mechanical behaviors: several papers [12,13,14] report age-dependence for ultrasonic axial transmission data but, to our knowledge, the elastic properties of cortical bone in children have been quantitatively investigated by only two in vitro mechanical studies [15,16], both using destructive tests on dry samples. In both cases, the experimental values for bone in children support the theoretical optimization hypothesis [17] of an increasing bone modulus of elasticity from neonate values to adult values, which is currently used in pediatric computational methods. All this would suggest the likelihood of lower ultrasonic wave velocities and modulus of
elasticity in children compared to adults. Yet the findings of a recent study performed by our
team on rib cortical bone from teenagers with scoliosis [18] do not support that hypothesis.
Although our study concerned pathological bone, our conclusion was that the \textit{in vitro}
ultrasonic wave velocities and the MOE values were close to the elderly adult values found in
the current literature. The lack of reference concerning normative pediatric ultrasonic wave
velocities and elastic properties of children’s prevents the medical community from using the
diagnosis devices based on analytic model of ultrasound scattering dedicated to adult’s
population (Quantitative ultrasound and echography). Consequently, the data collection and
the development of relevant models of bone growth is a critical need to investigate an
effective device of diagnosis and to meet the needs expressed by the medical community.

The aim of this study was to obtain ultrasonic wave velocities, dynamic and static
modulus of elasticity, and Poisson’s ratio for cortical bone samples from children, and then to
compare these results with elderly adult cortical bone samples. Our two-stage study
proceeded first by performing experimental ultrasound measurements to assess ultrasonic
wave velocities, dynamic modulus of elasticity ($\text{MOE}_{\text{dyn}}$) and Poisson’s ratio ($\nu$) and second,
via 3-point microbending tests, to assess static modulus of elasticity ($\text{MOE}_{\text{sta}}$).

4. Materials and Methods

Figure 1 is a diagrammatic representation of the method used.

4.1 Samples

In accordance with the stipulations of the French ethical committee, we studied
cortical bone samples from Caucasian patients (4 to 16 years old, mean age 10 years old +/-
4.5) of the University Hospital in Marseille who required auto transplant surgery. Surgical
waste bone, largely consisting of cortical bone from fibula diaphysis was studied; the selected
population was composed of walking children not on drugs disturbing their bone metabolism.
All auto transplant samples were excised from a non-pathological location in the fibula 5 cm above the ankle (figure 1). The elderly adult bone fibula samples were extracted from the same location as for the children’s samples, but from cadavers (+ 75 YO) at Inserm U1033 and UMR-T 9406 Ifsttar/UCBL (Lyon, France) bone bank. Samples for study were obtained by cutting the waste fragments in parallelepipeds (plane and parallel surfaces) using a low-speed diamond saw (Isomet 1000, Buehler; Lake Bluff, IL, USA). A total of 17 cortical bone parallelepipeds extracted from 8 children fibula samples were obtained and measured with a digital caliper. Great care was required due to the small size of the bone samples from the children: 15 to 35 mm long (bone axis direction), 10 to 20 mm wide and 2 to 3.5 mm deep (transverse directions). Sixteen elderly adult (+75 years old) bone samples excised from cadavers were similarly prepared. Each sample was designated (F or M for sex)-(age)-(F for fibula)-(number for each piece) and stored at -20°C in phosphate buffered saline with less than 5 freezing cycles.

4.2. Ultrasonic measurements

We used an ultrasonic protocol specifically developed, as detailed in Pithioux et al. [19] and Loosvelt et Lasaygues [20], to process small and thin samples, and which has been validated on standard materials and animal and human adult bones. The ultrasonic bench [18] used consisted of a main arm carrying two linear stages. Each linear stage was carrying the end-rod transducer, and was moved linearly with increments of hundredths of millimeters. The parallelepiped bone sample to be tested was placed in the presumed geometrical center of the bench so that the maximum distance between the transducers and the center was 30 mm. The surrounding fluid medium was water at a temperature of 18°C.

The surrounding fluid medium was water at a temperature of 18°C. Two focused broadband transducers (2R, figure2) at 10 MHz, (5 mm diameter, 6 dB-bandwidth ranging
from 9 to 13 MHz; Imasonic, Besançon, France), facing each other with their axes aligned, were used to scan along transverse parallel directions through the sample (perpendicular to the bone axis). The focal area (X_a x X_L, figure 2) of the transducer was 3 x 3 mm with a focus set (F, figure 2) at 30 mm. At this distance, the wave front was assumed to be plane, and the effect of the secondary lobes can be considered negligible. The wave reached the interface, also assumed to be plane at this scale, perpendicularly. Because the thickness of the samples ranged from 2 to 3.5 mm, a nominal frequency of 10 MHz was chosen, making the wavelength in water ten times greater than the sample thickness. Only propagation processes were taken into account and the ultrasonic wave attenuation was assumed to be weak. Longitudinal and transversal waves are excited when the incident sound wave strikes the bone surface under appropriate incident angles $\theta_i$ ($\theta_i \in [0^\circ, 90^\circ]$) and therefore only the time-of-flight (TOF) of the waves was measured.

For each sample, thickness $e$ was first calculated using the pulse-echo technique. TOFs of the propagating waves were determined in the reflection mode, from the left (respectively right) transducer to the left (respectively right) interface of the sample. The TOF measured between transducers without samples was used as reference. All measured thicknesses were compared to caliper measurements.

The velocities $V_l$, (respectively $V_t$) of the longitudinal (respectively transverse) waves in the samples were determined in the transmission mode using the equation (1):

$$ V_{l,t} = \frac{C_{water}}{\sqrt{1 + C_{water}\frac{M}{e}(C_{water}\frac{M}{e} - 2\cos\theta_i)}} $$

$C_{water}$ is the ultrasonic wave velocity in water, measured without bone sample, using the distance between both transducers and the TOF of the wave in between, $e$ the thickness of the sample. $\theta_i$ is the incidence angle and for each incidence angle, $\Delta t$ is the maximum of the cross-correlation between the first signal going through the zero stage with the sample, and
the reference signal measured earlier without the sample. When $\theta_i$ is lower than the first critical angle $\theta_c$, we consider that the wave velocity estimated is the velocity of longitudinal waves ($V_l$) and when $\theta_i$ is greater than $\theta_c$, we consider that the wave velocity estimated is the velocity of transverse waves ($V_t$). Each parameter was assessed by performing the tests in triplicate. Given the density ($\rho$), the transverse dynamic modulus of 
elasticity $\text{MOE}_{\text{dyn}}$ and Poisson’s ratio $\nu$ were calculated using the following equations (2 and 3) [21] [19]:

$$\text{MOE}_{\text{dyn}} = \rho \frac{V_t^2 (3V_t^2 - 4V_l^2)}{(V_t^2 - V_l^2)} \quad (2)$$

$$\nu = \frac{V_t^2 - 2V_l^2}{2(V_t^2 - V_l^2)} \quad (3)$$

The US protocol tested the transversal axis of each bone samples, consequently only the transversal dynamic modulus of elasticity is calculated here.

4.3. Mechanical measurements

We designed a 3-point microbending testing system specifically to deal with such small samples (figure 1), mounted on a Universal Testing Machine (Instron 5566A, Norwood, MA). To evaluate the cortical bone samples, a span-to-depth ratio of 16:1 is a general rule; but in small samples it cannot be achieved, the shortest sample tested here was 15 mm to guarantee that 85-90% of the flexure of the bone is due to bending [22] leading to a minimum span-to-depth ratio of 10:1 for all samples. The thinnest sample was 1.5 mm leading to a mean width-to-thickness ratio around 4, which corresponds to a shear factor of 0.833 [23]. Consequently, the number of samples from children was reduced to 12 and the number of elderly adult samples to 8. A pre-force of 5 N was applied on the sample before testing until rupture. The displacement speed was 0.2 mm/min, close to static testing conditions; the test provided a force/displacement curve for each sample, which was transformed into a strain/stress curve from which the static modulus of elasticity, $\text{MOE}_{\text{sta}}$, was estimated.
The F3P protocol tested the longitudinal axis of each bone samples, consequently only the longitudinal static modulus of elasticity is calculated here.

4.4. Statistical Analysis

The Shapiro-Wilk test was performed to evaluate the distribution of results, Student’s t-test was performed for normal distribution and a Spearman correlation was performed for abnormal distribution. The significance level is $p < 0.05$. All data generated by the experimental setup were analyzed using Excel 2007 and Analyse-it (Microsoft, Redmond, WA, USA).

5. Results

All the experimental results are presented as mean values in SIU (signal interface unit) with +/- standard deviation in brackets.

5.1 Ultrasonic measurements

Figure 3 shows the longitudinal and transverse wave velocities calculated for the 17 bone samples from children. The mean values of the longitudinal and transverse wave velocities measured at 10 MHz for the children’s bone samples are respectively 3.2 mm/$\mu$s (+/- 0.5) and 1.8 mm/$\mu$s (+/- 0.1); for the elderly adults’ bone samples, values are respectively 3.5 mm/$\mu$s (+/- 0.2) and 1.9 mm/$\mu$s (+/- 0.09). The measurement uncertainty for ultrasonic wave velocity on our bench is estimated at 2.25%. The mean density ($\rho$) for each group is reported in table 1, as are the deduced dynamic modulus of elasticity (MOE$_{dyn}$) and the Poisson’s ratio ($\nu$).
5.2 Mechanical measurements

The three-point microbending test provided a mean MOE_{sta} for each group, as shown in Table 1. The measurement uncertainty for the cell-force is estimated at 0.23%.

5.3 Statistical analysis

The ultrasonic measurements show no statistical difference between the bone from children and from elderly adults with respect to longitudinal wave velocities, transverse wave velocities, $\rho$, MOE_{dyn} and $\nu$ (Student’s t-test, $p>>0.05$) (Table1). The mechanical measurements show no statistical difference between the bone from children and from elderly adults with respect to mean MOE_{sta} (Student’s t-test, $p>>0.05$) (Table1). In the bone from children, the distribution of MOE_{dyn} values is normal (Shapiro-Wilk test; $W = 0.96$, $p = 0.81$) and the distribution of the MOE_{sta} values is abnormal (Shapiro-Wilk test; $W = 0.88$, $p = 0.08$). The MOE_{dyn} measured by ultrasound and the MOE_{sta} measured by 3-point microbending test for the children are plotted in figure 4 with white circles. A Spearman rank correlation test between MOE_{dyn} and MOE_{sta} for the children’s bone shows a positive value ($R = 0.765$, $p = 0.0014$).

6. Discussion

The assessment of cortical bone mineral status in children via non-radiating and non-invasive techniques using ultrasound technics may well enhance diagnosis in pediatrics, but their successful use must rely on gold-standard reference values. The aim of the study was first to measure ultrasonic wave velocities ($V_l$ and $V_t$) in children’s cortical bone samples excised from the fibula from which to calculate the elastic properties (MOE_{dyn}), then to experimentally obtain the elastic properties for the same samples via a mechanical test.
(MOE_{\text{sta}}), and finally to compare these bone values from children with elderly adult’s cortical bone samples excised from the fibula bone values obtained via the same protocol.

The ultrasonic method results for the children (Figure 3) indicate that $V_1$ is in the lower range of the acoustic experimental values generally found for adult cortical bone (between 2.7 and 3.8 mm/µs [24] and between 3.5 and 3.9 mm/µs [25]). Similarly, the mean MOE_{dyn} and the mean $\nu$ (Table 1) are in the lower range of the acoustic experimental values generally found for adult cortical bone. MOE_{dyn} values in the literature generally range between 18.5 GPa and 33.1 GPa [25], most being roughly 20 GPa [21,26], but these previous studies concerned femur bone and to our knowledge no values concerning the fibula are available. The $\nu$ values generally range between 0.22 and 0.42 [27]. Nevertheless, our results are close to the ultrasonic wave velocities already obtained with cortical bone from rib cortical samples of scoliotic teenagers (15 and 17 years old) using the same ultrasonic bench (respectively 3.2 mm/µs and 1.7 mm/µs for $V_1$ and $V_t$) [18]. Similarly, the mean MOE_{dyn} and the mean $\nu$ found in that study (respectively 14.9 GPa and 0.26) are in the same range as ours. The elasticity of cortical bone is largely dependent on its mineral constituents [28], and major changes in elasticity properties and mineral quality of physiological cortical bone have been quantified in ageing [29], or in adulthood [30]. However, little data is available on bone quality in childhood, so our findings here make a useful contribution to the literature.

When we compared the ultrasonic measurement results for the children with those for the elderly adults (+75YO), we found no statistical difference. This finding contradicts the theoretical optimization hypothesis [17] of stiffer bones in adults compared to children, which is currently used in computational models. Interestingly, Drozdzowska et al. [31] in their in vivo study found the speed of sound (SOS) evaluated at the phalanx roughly the same for children around 10 years old and people aged 70-80. The authors conclude that the SOS at the phalanx increases linearly to a maximum value reached at around 25 years old, and then the
values decrease more slowly until the age of 80. Given the age of our population (4-16 YO for children and +75 YO for elderly adults), our *in vitro* results support their *in vivo* evaluation. Moreover, similarly to Drozdzowska et al., an *in vivo* study [32] using peripheral quantitative computed tomography showed that bone mineral mass in a 1-mm-thick slice of the cortical bone cross-section of the proximal radius increased from childhood (6 years old) to adulthood (up to 40 years old). Clearly, the impact of age on bone mineral status could be explored more thoroughly if samples from younger adults were included. However, for an *in vitro* study on fresh bone, it is extremely difficult to obtain a wide range of donor ages. Furthermore, one limitation exists in the preparation process even if all the samples have been prepared in the same way, the children samples were fresh and the elderly population samples came from cadavers, however to our knowledge and up to date, no impact of that difference has been shown on ultrasound propagation. The main difference lies in the time of freezing which is hard to set with bone from several origins, but frozen bones can safely be used for mechanical testing, at least for storage periods of up to one year [33] which is consistent with our process.

One of the critical points concerning acoustical measurements is the sensitivity of $V_l$ and $V_t$ to the ratio $e/\Delta t$ (equation 1). In figure 5, we plot the longitudinal wave velocity measured in bone at normal incidence as a function of $e/\Delta t$ for a given wave propagation velocity in water $C_{\text{water}}=1.48 \text{ mm}/\mu\text{s}$. The black crosses represent the theoretical $V_l$ values obtained from equation (1) for the experimental values of $e/\Delta t$. It is noteworthy that in a range between 1 and 2 mm/$\mu$s the sensitivity of $V_l$ is very high, whereas it becomes more acceptable over 2 mm/$\mu$s. The critical value corresponds to $C_{\text{water}}$, and if we look at the accuracy of $V_l$ estimation versus the error in $e/\Delta t$ for different $e=\Delta t$ ratios between 2 and 5 mm/ $\mu$s (corresponding to experimental range), it appears that the sensitivity of $V_l$ estimation decreases when the ratio increases. For example, an error of 10% in the estimation of a ratio around 2 induces an error of 16% in the estimation of $V_l$; and an error of 6% in the estimation
of a ratio around 5 induces an error of 7% in the estimation of $V_l$. This example highlights one of the limitations of the ultrasonic method, based on the pulse-echo mode. Research is underway to tackle these limitations, and new ultrasonic measurement approaches and novel signal-processing methods are currently being investigated [20]. Theory suggests another issue concerning acoustical measurement, which is that SOS is influenced by the elasticity of bone as well as bone mass density; but, measured according to the Archimedes’ principle here (Table 1), the bone mass density ($\rho$) of cortical bone from fibula is in the usual range of literature values.

The mechanical measurements performed here found the mean $MOE_{sta}$ of the children’s bone samples to be in the typical range of human cortical bone values obtained from three-point bending tests (between 8.6 (+/-1.5) GPa [34] and 12.5 GPa [35]). Concerning the comparison with the first study of children bone [15], using samples extracted from the mid-shaft of the femur (eighteen subjects with age range: 2 to 48 years old), it showed that the bone specimens taken from children were weaker and less stiff than those taken from adults. The second [16], with samples extracted from the top part of the femur diaphysis (12 children from 4 to 15 years old and 12 adults from 22 to 61), showed that bone from children and adults differed in cortical strength and stiffness, depending on ash density, although the compressive yield strain was the same. Both studies found a mechanical difference between children’s and adults’ bone with regard to stiffness, but the findings of both should be taken with caution. The first tested bone from cadavers, with insufficient samples to provide statistics on differences between children and adults for the elasticity parameters. The second studied bone samples close to cancer locations, which cannot be considered physiological tissue. Here, we didn’t find any statistic difference concerning static modulus of elasticity but the span-to- depth ratio of 10:1 is not theoretically adequate to assess the MOE of bone material. Indeed, the contribution of shear deformation cannot be
neglected, and consequently the MOE_{sta} evaluated in this study may be influenced by the
dimensions of the samples and may lead to an underestimation of the MOE of cortical bone.
However, a recent study [36] aiming at design and validate bending test method for
characterization of miniature pediatric cortical bone specimens showed that a span to depth
aspect ratio (5 : 6) provided reasonable results for both Young’s modulus and flexural
strength in bovine bone; this aspect ratio is not consistent with the general rule admitted.
Nevertheless, since all the samples tested here showed the same span-to-depth ratio, we are
able to compare results for the children with those for the elderly adults. Comparison of the
children’s MOE_{sta} with the elderly adults’ MOE_{sta} obtained via mechanical tests shows no
statistical difference in the Student T-test (Table 1); this finding contrasts with the literature
[15,16]. One explanation of this absence of statistical difference may be the nature of the bone
tested. Fibula ossification commences in the lower end in the second year; *in vivo*, DeSouza et
al. [37] and El Haj et al. [38] pointed out the key role of mechanical stimulation in healing,
remodeling and regeneration of bone. Even though the fibula bears relatively little weight in
comparison with the tibia, walking may well stimulate the mineralization process of the
bottom part of the fibula more strongly than other bones in the skeleton. However, the fibula
being the preferred location for cortical bone auto transplants, we were unable to obtain other
fresh bone.

Ultrasound offers two advantages over static measurements: i) it is a non-destructive
tool; ii) it can be performed *in vivo*. However, the literature on biological tissue
characterization shows that values obtained for static and dynamic elastic moduli differ. The
values of the modulus of elasticity obtained through the ultrasonic method are usually higher
than those found with static deflection. This difference exists not only for bone but also for
biological material like wood. In wood, Halabe et al. [39] explained the difference between
the two moduli of elasticity as follows: wood is a viscous, elastic and highly impact-absorbent
material, so its behavior depends on the duration of the excitation: the shorter the excitation is (ultrasound excitation), the stiffer the material appears. Here, due to the small size of our samples and the difficulty of obtaining usable surgical waste, we could only assess transversal elasticity (perpendicularly to bone axis) via acoustical measurements and longitudinal elasticity via mechanical measurements. However, adult cortical and trabecular bone are orthotropic [40], so it might be assumed that children’s cortical bone is also an anisotropic tissue. Consequently, future studies on children’s bone should also explore the other axes of the bone for a more thorough comparison of static and dynamic MOE. Nevertheless, the values for both MOE\textsubscript{dyn} and MOE\textsubscript{sta} reported here (Table 1) are consistent with those usually reported in the literature [41], and a Spearman ranking correlation between the two moduli of elasticity is obtained (Figure 4). To our knowledge, the correlation obtained here is the first to establish a strong link between dynamic and static moduli for human cortical bone in children, or even for human cortical bone in general. In a recent study [41] of women’s cortical bone, the authors obtained only a marginal negative correlation between MOE\textsubscript{dyn} (ultrasonic measurement with guided waves) and MOE\textsubscript{sta} (three-point bending). Investigating a linear correlation between MOE\textsubscript{dyn} and MOE\textsubscript{sta} and exploring the hypothesis of anisotropy of children’s bone will require further experiments with more and thinner samples, a challenging undertaking.

In conclusion, this study contributes a new set of ultrasonic wave velocities and elasticity values for children’s cortical bone. Furthermore, for the first time it provides a ranking correlation between children’s cortical bone elasticity values obtained using two different approaches (acoustical and mechanical measurements). Finally, the comparison performed here with elderly adults’ bone does not support the theoretical optimization hypothesis [17] of an increasing bone modulus of elasticity values from neonate to adult which is currently used in pediatric computational methods.
7. Acknowledgements

This study was based on research supported by the French National Research Agency (BioGMID Program ANR under Grant n°183692 and MALICE Program ANR under Grant n°BS09-032). We thank the Timone Hospital surgery team and the donors or their legal guardians who gave informed written consent to providing their tissues for investigation, in accordance with the French Code of Public Health (Code de la Santé Publique Française) and approved by the Committee for the Protection of Persons. This work benefited from the very fruitful help of Georges Boivin, and Hélène Follet from INSERM U1033 and from UMR-T 9406 Ifsttar/UCBL. We thank Marjorie Sweetko for English language revision.

8. Conflict of Interest statement

There is no conflict of interest.

9. References


<table>
<thead>
<tr>
<th></th>
<th>$\rho$ (kg/m$^3$)</th>
<th>MOE$_{\text{dyn}}$ (GPa)</th>
<th>$\nu$</th>
<th>MOE$_{\text{sta}}$ (GPa)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Children</td>
<td>1.84 ± 1.12</td>
<td>15.5 ± 3.4</td>
<td>0.24 ± 0.08</td>
<td>9.1 ± 3.5</td>
</tr>
<tr>
<td>Elderly adults</td>
<td>1.73 ± 0.08</td>
<td>16.7 ± 1.9</td>
<td>0.27 ± 0.05</td>
<td>5.8 ± 2.1</td>
</tr>
<tr>
<td>Student T-test</td>
<td>P$&gt;&gt;$0.05</td>
<td>P$&gt;&gt;$0.05</td>
<td>P$&gt;&gt;$0.05</td>
<td>P$&gt;&gt;$0.05</td>
</tr>
</tbody>
</table>

Table 1: Mean values (+/- SD) of density $\rho$, MOE$_{\text{sta}}$, $\nu$ and MOE$_{\text{dyn}}$ for the children’s (mean age: 10 years old +/- 4.5) and the elderly adults’ bone samples (+ 75 years old)

Figure 1: a. samples preparation: the waste fragment from auto transplant which was selected to prepare one of the children’s cortical bone samples tested, b. plan of the special ultrasonic bench to assess acoustic elastic properties, in a water tank the bone sample is located between transducers (T1 and T2), all of them mounted on 3D rotational axis c. picture of one sample during mechanical measurements via the three-point microbending setup.

Figure 2: Aperture of the 10MHz-transducer (Imasonic®); R and H are respectively the radius and the length of the transducer; ; F is the focusing distance; Xa and XL are respectively the focal length and the slice thickness.

Figure 3: Longitudinal (black crosses) and transverse (black dots) wave velocities measured at 10 MHz for children’s bone samples

Figure 4: MOE$_{\text{dyn}}$ measured by ultrasound and MOE$_{\text{sta}}$ measured by three-point bending test on children’s bone (white circles)

Figure 5: longitudinal wave velocity measured in bone at normal incidence as a function of $e/\Delta t$ for a given wave propagation velocity in water $C_{\text{water}}$=1.48 mm/µs. The black crosses represent the theoretical $V_1$ values obtained from equation (1) for the experimental values of $e/\Delta t$. 
Highlights

- The mean values of longitudinal and transverse wave velocities for children’s bone are respectively 3.2 mm/µs (+/- 0.5) and 1.8 mm/µs (+/- 0.1).

- Dynamic moduli of elasticity are in the same range for children’s and elderly adults’ bone without any statistical difference.

- A ranking correlation between dynamic modulus of elasticity and static modulus of elasticity is shown for children cortical bone samples.