Fiber optics sensor for sub-nanometric displacement and wide bandwidth systems
Luc Perret, Luc Chassagne, Suat Topsu, Pascal Ruaux, Barthélemy Cagneau, Yasser Alayli

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L. Perret, L Chassagne*, S. Topçu, P. Ruaux, B. Cagneau, Y. Alayli
Laboratoire d'Ingénierie des Systèmes de Versailles, Université de Versailles Saint-Quentin, 45 avenue des Etats-Unis, 78035 Versailles, France
Corresponding author: luc.chassagne@uvsq.fr +33 1 39 25 44 78

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Abstract
In this paper, we report fiber optics sensor with sub-nanometric resolution and wide bandwidth. It relies on an increase of the reception fibers number and on low-noise electronics. Moreover, a reference channel has been implemented using a semi-reflective plate to eliminate the source fluctuations and the fiber sensor was isolated to limit external influence of temperature and pressure. Thus we achieve both a sub-nanometric resolution on a 400 ms integration time and a long-term drift as low as 40 nm.h⁻¹. The setup has been also adapted to high speed applications by increasing the bandwidth up to 38 kHz. It can display a 28 nm peak-to-peak limit of resolution on an aluminized piezoactuator. It has been successfully used to test the resonance frequency of a vibrating plate actuated by two high-frequency prototypes of piezoactuators. These improvements lead to low cost fibers optic sensors interesting for non-contact displacement measurements with high sensitivity.

Keywords: Fiber optics, high resolution sensor, distance measurement, vibration measurement, high bandwidth sensor, low-noise electronics.

1. Introduction
Many non-contact measurement systems have been explored to reach the sub-nanometric resolution, in order to satisfy the need in nanopositioning and nanomanipulation fields such as Atomic Force Microscopy (AFM) and Scanning Near-Field Optical Microscopy (SNOM), electronic lithography, atomic and molecular physics, or to characterize low amplitudes vibrations and to achieve high-speed servo-loops. The most efficient systems are based on interferometry but they need expensive equipments, of tens of thousands euros. For instance, the Michelson heterodyne architecture can reach typically sub-nanometric resolution and repeatability over millimeters range for nanorobotics systems [1-5]. The Fabry-Pérot architecture, using multi-reflections between a fiber sensor and the target, reports a resolution of 2 pm on a 25 nm range with a working distance up to 40 µm and a bandwidth of 1 kHz [6]. A speckle interferometer can also be implemented to achieve a nanometric resolution over a 100 µm range for rough surfaces [7]. White-light (or low-coherence) interferometry is widely used in profilometers where it can achieve a 0.1 nm resolution; it has been adapted for position...
measurement using fiber optics with a 6 nm resolution over a 100 µm range [8]. Interferometry is widely used too in vibration measurements: for example in the experiment of this paper, we used an old Polytec OFV-303 optical head, which is a Mach-Zehnder with a round trip to the target on one arm and a Bragg cell modulator on the other. It allows frequency comparison to determine the sense and speed of movement thanks to the Doppler effect, and the displacement from the phase with a 85 nm peak-to-peak limit of resolution and a 0.5 Hz to 250 kHz frequency range. Nowadays, performances have evolved since then with resolutions below the nanometer and bandwidths beyond the MHz. Digital holography is another optic solution for applications in modal analysis of MEMS (micro-electromechanical systems) [9] and dynamic endoscopy [10] for instance, with a sub-micrometric resolution and a bandwidth of a few kHz. Another non-contact solution is the capacitive gauge; nowadays commercial systems report resolution as good as 0.01 nm over a 100 µm range in static case and 0.02 nm with a 10 kHz bandwidth in dynamic case [11], after software correction of mechanical errors and non-linearities. New setups are studied to increase the range, such as periodically patterned gauges which display a 25 nm resolution on fine motion over 100 µm and a 260 nm resolution on coarse motion over 1.6 cm [12]. Longer range solutions include optical encoders with a nanometric resolution within a signal period and a repeatability better than 0.5 µm over tens of centimeters [13-15]. However they remain expensive (thousands of euros). The triangulation technique offers a good compromise too, with a resolution and a repeatability of 10 nm, a range of a few millimeters and a sampling frequency up to 50 kHz (vibration measurement up to 25 kHz) [16].

Over the past decade, fibers optical sensors (FOS) for distance measurements have been extensively developed due to their resolution of a few nanometers, low encumbrance and low cost. They can be used in many domains such as robotics, biomedical, translation plates for AFM or lithography and in harsh environment, such as cryogenics for supraconductors devices [17]. They have also been adapted to vibration measurement through intensity modulation with a bandwidth of 8.5 kHz and a resolution of 10 nm peak-to-peak [18-19]. Most of them consist of one emission fiber and one or several reception fibers around, collecting the light reflected by the target. Their displacement range is therefore limited by the reception fibers diameter, typically a few hundred micrometers. It can reach longer ranges by implementing several circles of reception fibers [20] but increasing the number of fibers may increase the environmental noise level; another proposal can reach centimetric displacements by addition of a large grating [21-22] but at the cost of resolution (15 to 27 nm) due to the angle between the displacement axis and the sensor axis. Finally, a hybrid setup was made with a sensor based on the same principle of reflection photometry, but where the emission fiber is replaced by a Vertical Cavity Surface Emitting Laser (VCSEL) and the reception fibers are replaced by photodiodes [23], which features a larger intrinsic range but a limited resolution. Some works based on fiber ring resonators have also been developed to convert displacement to frequency sensitivity with a nanometric resolution demonstration over micrometric range [24].

This non-contact optical sensor based on fiber bundle is largely used in precision mechanics (measurements of straightness and angle deviations) because of the non-contact advantage and relatively cheap design. Nevertheless, the limitation of the resolution and especially the drift of the response make them difficult to use in metrology applications because long-time measurements are not possible without calibration process. Moreover for existing prototypes, high resolution is obtained to the detriment of the bandwidth. In this paper, we report the enhancement of the resolution to a sub-nanometric scale which relies on low-noise electronics, a reference channel, the increase of the reception fibers number and their thermal and
pressure isolation. We demonstrate also a strong reduction of the long-term drift that makes the sensor able to be used for long-time acquisitions. Furthermore, the bandwidth of tens of kilohertz is also competitive and a setup for vibrometric or high-speed measurements at high frequencies, based on the same FOS, is presented.

2. Sub-nanometric resolution in static case

The fiber sensor consists of a central emitting fiber and several reception fibers around which collect the reflected cone of light. A scheme is illustrated in Fig. 1a (more detailed schemes can be found in [18-22]). Our source is a red LED (650 nm), commonly preferred to laser diodes in order to avoid interferences of multiple reflections and because of their low cost and ease of use. The signal measured at the output of the reception fibers by a single Si photodiode is doubly linked to the distance \(d\) of the target by Equation 1 (reflected intensity profile) and 2 (illuminated surface of a reception fiber) [25]:

\[
I_r = I_0 \cdot \frac{r_0^2}{(r_0 + 2d \cdot \tan(\theta_0))^2} \cdot \exp\left(\frac{-r^2}{(r_0 + 2d \cdot \tan(\theta_0))^2}\right),
\]

\[
S_r = \int dS_r(d, r, \theta_0),
\]

with \(r_0\) the emission fiber radius, \(\theta_0\) the emission cone angle, \(I_0\) the central intensity at the emission fiber output, \(r\) the radial variable and \(dS_r\) the surface element of a reception fiber. The illuminated surface depends also on the geometry of the sensor (gap between fibers, fibers diameters, see [25] for details).

The typical response of the fiber sensor is therefore a quasi-linear ascending curve up to the complete covering of the receiving fiber radius, and then exponentially descending [18, 21, 25]. The part of main interest is the ascending section which features the highest sensitivity with regard to displacement. This quasi-linear ascending section goes from \(d = 75 \mu m\) to \(d = 275 \mu m\) in our configuration. In the following of the paper, the measurements have been done around a nominal point of 100 \(\mu m\) to minimize residual power fluctuations of the LED source. Considering equations 1 and 2, it appears that the most important parameters to get a high sensitivity are the Numerical Aperture (NA = \(\sin(\theta_0)\)) of the emitting fiber and the number of reception fibers [26]. We tested a sensor with 1 emitting fiber of 1 mm diameter and 16 receiving fibers of 250 \(\mu m\) diameter; it has a sensitivity 6 times higher than a typical FOS (47 mV/\(\mu m\) instead of 8 mV/\(\mu m\)) which has an emitting fiber of 500 \(\mu m\) diameter and 4 receiving fibers of 250 \(\mu m\) diameter. Note that several commercial manufacturers (for example Omron or Keyence) deliver a large catalogue of bundles with different characteristics of dimensions and numbers of fibers. Specific home-made bundle could be developed but we choose here a cheap (less than one hundred dollars) commercial one from Keyence (FU-23X) to maximize the number of fibers and the collecting surfaces.

For this device, the resolution is defined as the ratio of sensitivity over noise, so that other teams work with high amplification gains behind the photodetector to get sensitivity up to 60 mV/\(\mu m\) [21] and lock-in detection to enhance the Signal to Noise Ratio (SNR) [18, 21, 22, 26]. We chose to increase the sensitivity through the number of reception fibers, and to use low-noise electronics. Moreover, increasing the number of fibers demands a better isolation and mechanical stability to avoid mode coupling and bending losses. It is well-known that fibers are very sensitive to temperature [27]: it modifies the refractive index, which changes the NA, and the fibers lengths and diameters, which changes the sensor geometry and thus the sensibility and the
range. Temperature has also a non-negligible influence on the electronic parts of the sensor (source, photodiode and amplification circuit) [28]. We selected a commercial source (FS-V31M from Keyence) based on a LED at 650 nm and internal regulation to minimize power noise. For the detection circuit, we used an OPA606 operational amplifier and low temperature coefficient resistors (25 ppm) in a transimpedance circuit. To limit the dark current, the photodiode is not polarized. A capacitor avoids the auto-oscillation of the OPA606. As the noise sources (shot noises and thermal noises) are proportional to the square root of the measurement bandwidth, the resolution is enhanced when the integration time increases. In our case, with a 400 ms integration time, it lowers down to 3.6 nm.

We added a reference circuit of the light source to enhance the SNR. The aim of the reference path is to normalize the amplitude to avoid power fluctuations of the source. A 1 cm² Si photodiode and its transimpedance circuit are positioned behind a beamsplitter plate at normal incidence (Fig. 1b). It implies a loss of sensitivity on the reflected signal, but when we calculate the ratio of both reflected (target) and transmitted (reference) intensities, it finally increases the SNR by a factor 2 compared to the setup with a silver mirror, with a resulting resolution of 1.9 nm rms (Table 1). Finally, we placed the setup in a box made of barson, a special isolating material (barson is mainly rubber and lead) to isolate the fiber sensor from pressure and temperature variations, which make us gain an additional factor 3 over noise and a factor 10 over drift (Table 1). We reach thus a resolution of 0.6 nm over a 200 µm range with a 400 ms integration time (Fig. 2) and the drift is dramatically reduced to 41 nm over a full hour (Fig. 3), which is probably due to the residual thermal drift of the tabletop and other mechanical parts. Note that the direction of the drifts depends mainly on the temperature variations and can be then either positive or negative if the distance between fibers and mobile mirror is going up or down, depending on the time of the day when the measurements are launched. This setup could be further compacted by placing only the fiber wound in a small barson box. Moreover, the beamsplitter, the reference photodiode and its transimpedance circuit are compacted (3×3×4 cm³) to be stuck on a target.

3. High bandwidth for dynamic case

Former works on vibrometry using fiber sensors were based on amplitude modulation of the source and on synchronous demodulation [18]. The system bandwidth was therefore limited by the high-pass and low-pass filters and was demonstrated up to 8.5 kHz with an accuracy of 2 nm rms (10 nm peak-to-peak) limited by the SNR of the fiber sensor and of the electronic circuit. Another system using 2 circles of reception fibers has been tested up to 1440 Hz; its originality is to measure the ratio of both reception fibers sets to avoid loss of sensitivity with the increase of the working distance (it exploits the descending part of the FOS characteristic and thus has a limited resolution) [29]. We adapted our setup by increasing the bandwidth and consequently by reducing the gain, using a lower resistor-capacitor couple through the transimpedance cut-off frequency equation [30]:

\[
f_c = \frac{GB}{\sqrt{2\pi \cdot R \cdot (C + C_{PD})}},
\]

where \(C_{PD}\) is the photodiode capacity, \(GB\) is the gain bandwidth product of the operational amplifier, and \(R\) and \(C\) are the resistor-capacitor elements of the transimpedance circuit.

We are able to measure directly the intensity variation without any modulation technique but we need an anti-aliasing filter before our acquisition card to eliminate the high-frequency
components due to the commercial source (beyond 125 kHz). The anti-aliasing filter is a MAX274 8th order Butterworth low-pass filter with a cut-off frequency of 50.2 kHz and a peaking of 1.15 dB at 40 kHz; it amplifies the signal by a factor 3.48 (10.8 dB) within its flat bandwidth part. We calibrated the frequency response of all the detection system by lighting directly the photodiode with an intensity-modulated LED. The Bode diagram of the circuit gives a cut-off frequency of 28.2 kHz. Therefore the global sensor chain (transimpedance circuit and anti-aliasing filter) shows a cut-off frequency of 38 kHz. The signal is then sampled at a frequency rate of 250 kHz. We use an additional software filter, a Butterworth bandpass under LabView, mainly to eliminate the environmental and DC components (we do not use the reference channel neither the barson box anymore), and to further isolate the frequencies of interest if needed.

The vibration is produced by an aluminized piezoelectric translator (APZT, reference AE0505D08F from Thorlabs) that we calibrated with the commercial interferometric vibrometer from Polytec described earlier (measurement resolution of 85 nm). The PZT displays a cut-off frequency of 2.2 kHz and its amplitude can be measured up to 10 kHz. We then tested our modified setup on this APZT (Fig. 4) up to 10 kHz and found that it reproduces well the PZT response measured by the interferometric vibrometer (Fig. 5), with a conversion coefficient of 15.6 mV/µm. The limit of detection is better than the one of the interferometric vibrometer and is experimentally evaluated at 28 nm peak-to-peak, according to the PZT voltage-to-µm conversion rate. According to the noise level, the theoretical resolution should be 10 nm peak-to-peak, but could not be verified experimentally because of the inaccuracy of our vibrometer. This setup is interesting for many applications in term of resolution, bandwidth and simplicity.

At higher frequencies, we used a vibrating membrane built by the Laboratoire de Génie Electrique de Paris (LGEP) and with a resonance at 27.8 kHz with an amplitude of 3 µm peak-to-peak. It consists of a long plate of aluminium excited at one end by a high-frequency piezoactuator which is aimed to be implemented in a micro-pump [31]. On this surface, our setup features a 9.2 mV/µm sensitivity and a theoretical resolution of 17 nm peak-to-peak. Measurements are possible up to 35 kHz with a detection limit of 66 nm peak-to-peak. The part a of the Fig. 6 shows the acquired signal at 27.8 kHz by our FOS. The part b of the Fig. 6 is the Fast Fourier Transform (FFT) of the signal, demonstrating the good SNR. The resonance frequency was determined with a resolution of 1 Hz and was found to vary in a 30 Hz interval centred on 27.8 kHz in agreement with expectations, and a peak-to-peak amplitude of 4 µm. The small variation of the frequency is due to mechanical variations of the clamping points at the start of excitation; once excited, it stays constant in time. The vibration signal has also been measured with the interferometric vibrometer with results in good agreement.

4. Conclusion

In this paper, we reported the improvement of a fiber optics sensor based on one emitting fiber and 16 receiving fibers around. By using low-noise electronics and by implementing a reference behind a semi-reflective plate we gain a factor 2 on the SNR. We additionally placed the fiber optics in a barson box, which enhanced the long term stability by a factor 10 and the SNR by an additional factor 3. The final results are a drift of 40 nm.h⁻¹ and a resolution of 0.6 nm (1σ) for 400 ms integration time. Then the setup has been adapted to high dynamic measurements by correcting the bandwidth of the electronics circuit which reaches 38 kHz with a 15.6 mV/µm sensitivity on an aluminized piezoelectric actuator, without any modulation.
The limit of detection is evaluated at 28 nm peak-to-peak. Measurements have been made on another unpolished aluminum plate actuated by piezoactuators from LGEP up to 35 kHz with 66 nm peak-to-peak limit of detection; the resonance frequency at 27.8 kHz was clearly seen. The compactness and the low cost of these fiber sensors, along with their good resolution in amplitude and frequency could be used in applications such as modal analysis and multi-point surface deformation monitoring.

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References
Vitae:

**Luc Perret** received the Engineer degree in instrumentation from ENSICAEN, France, in 2003, and the Ph.D. degree in photonics from the University of Strasbourg, France, in 2007. After a post-doctoral position at the Laboratoire des Systèmes Photoniques, Strasbourg, on absolute distance interferometry and tunable lasers, he is now a post-doctoral fellow at the LISV where he works on fiber optics sensors for distance and vibration measurements.

**Luc Chassagne** is graduated from Engineer degree of Supelec (France) in 1994 and received his Ph.D. in optoelectronics from the University of Paris XI, Orsay, France in 2000 for his work in the field of atomic frequency standard metrology. He is now Professor at the LISV and the topics of interest in its research are nanometrology, precision displacements, sensors and AFM instrumentation.

**Suat Topçu** received his PhD from Compiègne University of Technology (Compiègne, France) in 2001. Since 2002, he works as an assistant professor at the University of Versailles in LISV laboratory. His fields of research are interferometry, dimensional metrology, ellipsometry and recently laser cooling and trapping process. He is professor at LISV since 2010.

**Pascal Ruaux** received the Ph.D. degrees in Robotic from the University of Pierre & Marie Curie–Paris 6, Paris, France in 1998 to LRP (Laboratoire de Robotique de Paris). He became Associate Professor in 2001 with the LISV. He worked on technical assistant to disability. Since 2006, the centers of interest are control micro- and nano-precision on millimeter displacement, AFM large image and nano-manipulation.

**Barthélemy Cagneau** received the Ph.D. degrees in mechanical engineering from the University of Pierre & Marie Curie–Paris 6, Paris, France in 2008. After a postdoctoral position in nanorobotics at ISIR (Institut des Systèmes Intelligents et de Robotique, Paris), he became Associate Professor in 2009 with the LISV (Laboratoire d'Ingénierie des Systèmes de Versailles, Versailles). His research interests include force control, adaptive control, and robust bilateral couplings for micro- and nano-robotics.

**Yasser Alayli** received his PhD in applied physics from Pierre et Marie Curie University of Paris (Paris, France) in 1978. He is professor at Versailles Saint-Quentin University, France, and director of the LISV. His research interests include precision engineering domain with sub-nanometric accuracy and nanotechnologies.
Figure 1
Figure 2
Figure 3
Figure 6
Figure caption

Figure 1: Setup of the sensor measuring the distance $d$. (a) Scheme of the fiber bundle disposition. In our experiments, $n = 16$, diameters of the emitting and receiving fibers are 1 mm and 250 µm respectively. (b) Setup using a reference channel; BS: beam splitter, PDC: photodiodes and their transimpedance circuits, FOS: fiber optics sensor, TS: translation stage (manual or PZT). The whole setup can be placed into an isolating box as drawn.

Figure 2: Ratio characteristic with the reference channel and an integration time of 400 ms; dot: experimental data, line: linear part of interest (linearity of 1.33%) with a coefficient of $2.8 \times 10^{-3} \, \text{µm}^{-1}$ over a range of 200 µm.

Figure 3: Drift of the fiber sensor over 1 hour (integration time for each point is 400 ms). (a) on the measurement channel (reflection from the beamsplitter), (b) ratio of the measurement and reference channels, (c) ratio inside an isolating box.

Figure 4: Setup for the vibrometric measurement. FOS: fiber optics sensor, APZT: aluminized piezoelectric translator, SFG: synthesized function generator, PDC: photodiode transimpedance circuit (neither reference nor barson box in this setup, but two different suspended tabletops to avoid vibration propagation).

Figure 5: Bandwidth of the aluminized piezoelectric translator evaluated with a commercial vibrometer (squares) and with the fiber sensor (triangles).

Figure 6: Acquisition at the resonance frequency (27.791 kHz) of the LGEP vibrating plate; (a) the corresponding displacement amplitude is 3.9 (6) µm peak-to-peak, (b) the FFT of the corresponding signal.
<table>
<thead>
<tr>
<th>Setup</th>
<th>Standard deviation</th>
<th>Sensitivity</th>
<th>Resolution [nm]</th>
<th>Drift [nm.h⁻¹]</th>
</tr>
</thead>
<tbody>
<tr>
<td>Direct reflection from a silver mirror</td>
<td>0.169 mV</td>
<td>47.2 mV.µm⁻¹</td>
<td>3.6</td>
<td>&gt; 1000</td>
</tr>
<tr>
<td>Direct reflection from the beamsplitter plate</td>
<td>0.144 mV</td>
<td>13.8 mV.µm⁻¹</td>
<td>10.4</td>
<td>707</td>
</tr>
<tr>
<td>Target/Reference ratio without barson</td>
<td>5.4×10⁻⁶</td>
<td>0.0028 µm⁻¹</td>
<td>1.9</td>
<td>437</td>
</tr>
<tr>
<td>Target/Reference ratio with barson</td>
<td>1.8×10⁻⁶</td>
<td>0.0028 µm⁻¹</td>
<td>0.6</td>
<td>41</td>
</tr>
</tbody>
</table>

Table 1

**Table captions list**

Table 1: Standard deviation, sensitivity, resolution and long term drift for different setup of fiber optics position sensors based on 1 emission fiber and 16 reception fibers; integration time 400 ms.