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Influence of control strategy on the global efficiency of a Direct Wave Energy Converter with electric Power Take-Off (revised version)

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Abstract—The choice of control strategy for Direct Wave Energy Converters (DWEC) is often discussed without taking into account the limitations of electric Power Take-Off (PTO): limits of torque or force and power, as well as losses in the electric chain. These assumptions leads to large and expensive electric systems, that prevent leading to a global minimization of the per-kWh cost. We propose herein a simple loss model in order to design a better control strategy.

Keywords—Wave energy conversion; Point absorber; Control strategies; electric Power Take-Off (PTO); irregular waves

I. INTRODUCTION

Achieving sustainable development requires the use of more renewable sources in the energy mix. Renewable marine sources like tidal current and wave energy devices offer consistent potential with low environmental impact and hence might become a part of the future solution [1].

Many principles have been developed for the purpose of converting energy from water waves. Among these principles, Direct Wave Energy Converters (DWEC) with electric Power Take-Off (PTO) are the most direct and most flexible [2]. They may make use of mechanical transmission (gear box, rack and pinion, etc) or may not (direct drive) [3]. They lead to the possibility of higher efficiency and reliability, yet feature higher power fluctuations in the grid than WEC with hydraulic or mechanical storage systems.

Control design however must take into account the limitations of an electric PTO, i.e.: power limitations, force or torque limitations, losses in the electric chain. But the problem is often see as decoupled. Thus, two types of papers classically deal with control strategies in DWEC: the theoretical optimization of control with no or very little considerations for the limits of realization [5]; and optimization using a given electric system [6]. Only a few papers have dealt with the coupling between control strategy and sizing [7,8].

II. WAVE ENERGY CONVERTER MODEL

In this study, we will be focusing on the control of a generic point absorber device with a single degree of freedom. The system considered is a floating vertical cylinder constrained to only move in heave motion only, under the action of wave excitation forces (see Fig. 1). The theoretical work presented herein may be applied to other floating bodies, but this simple example will be useful for illustrating and comparing various control strategies.
on the radiation transfer function with hydrodynamics simulations. In the case of equation (1), the vertical speed of the buoy, \( v = \xi \) the vertical speed of the buoy, \( M \) the buoy mass and \( K \) a hydrostatic stiffness. \( f_{exc} \) and \( f_{PTO} \) denote respectively the wave excitation force and PTO force. We apply the Cummins decomposition [10] of radiation forces through an added mass term \( a_e \) and convolution product with a kernel \( h(t) \), which is typically called the radiation impulse response function.

This equation can now be rewritten in the s-domain (i.e. Laplace transformation) using mechanical impedance \( Z_{Buoy}(s) \), in order to use an electric analogy in the following:

\[
Z_{Buoy}(s) = \frac{F_{exc}(s)}{V(s)} = \frac{F_{tot}(s)}{s \Xi(s)}
\]

with \( Z_{Buoy}(s) = |Z_{Buoy}(s)|e^{i\eta_{exc}(s)} \)

Upper case characters are used for the s-domain and lower case for the time domain, hence: \( \Xi(s), V(s), H(s), F_{tot}(s) \) respectively the Laplace transform of \( \xi(t), v(t), h(t) \) and \( f_{tot}(t) \). In the case of equation (1), the buoy impedance is:

\[
Z_{Buoy}(s) = (M + a_e) + \frac{K}{s} \]

The values adopted in this study correspond to a buoy with a radius of 5 m and a height of 10 m. The parameters have been computed in the AQUAPLUS seakeeping code for hydrodynamics simulations [11] (see Table I). It should be noted here that the real part of buoy impedance depends only on the radiation transfer function with \( s = j\omega \). This real part must be positive in order to respect the law of conservation of energy:

\[
\Re \{ Z_{Buoy}(j\omega) \} = \Re \{ H(j\omega) \}
\]

The excitation force \( f_{exc}(t) \) is correlated with wave elevation \( h(t) \), and this relationship can be written in the Laplace domain as follows:

\[
F_{exc}(s) = H_{exc}(s)EL(s)
\]

### B. Energy Conversion Chain

A DWEC contains two major energy conversion in a (see Fig. 2): hydro-mechanical and electromechanical. The hydro-mechanical conversion is the transition from wave hydrodynamic power to mechanical power; it is obtained through the buoy and the PTO control strategy. The electromechanical, on the other hand, is the transition from mechanical power to electric power feeding the grid; it is obtained through the electric chain, i.e. the electric machine and the power electronic converters.

According to the theory of impedance matching, in order to maximize power transfer, the receiver impedance must be the complex conjugate of the generator impedance. The theoretical maximum wave power as a function of pulsation is then expressed as:

\[
P_{Wave}(\omega) = \frac{4 \Re \{ Z_{Buoy}(j\omega) \}^2}{4 \Re \{ H(j\omega) \}^2} \frac{\left| H_{exc}(j\omega) \right|^2 EL_{rms}(\omega)^2}{\left| H(j\omega) \right|^2}
\]

where \( F_{exc}(\omega) \) being the root mean square of a sinusoidal excitation force of pulsation \( \omega \), \( Z_{Buoy}(j\omega) \) the generator impedance defined in (5), \( H_{exc}(j\omega) \) the excitation transfer function defined in (7) and \( EL_{rms}(\omega) \) the root mean square of a sinusoidal water elevation of pulsation \( \omega \).

A reciprocity relationship exists between excitation and radiation; this relationship can be written between the modulus of the excitation transfer function \( |H_{exc}(j\omega)| \) and the real part of the radiation transfer function. In the case of an axisymmetrical heaving point absorber, within the framework of linear potential theory and under the hypothesis of infinite water.
power will thus be equal to:

\[ |H_{elec}(j\omega)| = \left| \frac{4 \Re\{H(j\omega)\}}{2\omega} \right|^{\frac{3}{2}} \]

(9)

where \( \rho \) is the mass density of sea water (1025 kg/m\(^3\)), and \( g \) the earth's gravity (9.81 m/s\(^2\)). The average wave power can then be rewritten as:

\[ P_{wave}(\omega) = \frac{g}{2\omega} \cdot EL_{ave}(\omega)^2 \]

(10)

The average wave power can be determined by means of the integration in the frequency domain in so far as the elevation spectrum is known; as an example:

\[ \overline{P}_{wave} = \int_0^\infty P_{wave}(\omega) \, d\omega \]  

(11)

The mechanical power and grid power are both defined in the time domain. The mechanical power is simply defined as:

\[ P_{Mech}(t) = \xi(t) f_{PTO}(t) = v(t) f_{PTO}(t) \]

(12)

The grid power is defined from electrical losses within the electric chain:

\[ P_{Grid}(t) = P_{Mech}(t) - P_{loss,elec}(t) \]

(13)

Losses in the electric chain stem from multiple sources: iron losses (hysteresis and eddy current losses) and copper losses in the electrical machine; and conduction and commutation losses in the power electronic converters. All of these losses depend on the design and sizing of the various electric chain components. The sizing of the machine-converter set depends on the force-speed profile, and thus on the specific control strategy. A strong correlation exists between sizing and control. To resolve this issue, the choice is to introduce a simple and generic loss model for the electric chain, i.e.:

\[ P_{loss,elec}(t) = c_{loss} \cdot |P_{Mech}(t)| \]

(14)

This definition is illustrated in Fig. 3. The loss coefficient \( c_{loss} \) lies between 0 (no loss) and 1 (no energy recovery). This model remains simple, though the study is being conducted for a preliminary design in order to limit the ratio between the energy exchange and average power. The loss coefficient \( c_{loss} \) is chosen via a technological culture in order to match the smallest loss coefficient capable of being achieved with a reasonable cost. Upon initial sizing of the electric chain, the model may be refined for greater precision. The average grid power will thus be equal to:

\[ \overline{P}_{Grid} = \int_{t_{PTO}} \int_{t_{PTO}} - c_{loss} \cdot |v(t) f_{PTO}(t)| \]

(15)

In the following discussion, \( c_{loss} \) has been set equal to 0.1.

In the frequency domain, the excitation transfer function frequency response gain is equal to:

\[ \left| H_{elec}(j\omega) \right| = \left| \frac{4 \Re\{H(j\omega)\}}{2\omega} \right|^{\frac{3}{2}} \]

The problem here is to maximize the function \( P_{control} \), which is a linear combination of the average mechanical power and the average of the absolute mechanical power:

\[ \overline{P}_{control}\left(c_{control}\right) = \overline{P}_{Mech} - c_{control} \left| \overline{P}_{Mech} \right| \]

(16)

where \( 0 \leq c_{control} < 1 \) is a coefficient used to design the control strategy for calibrating the objective function between a maximization of the final energy and limitation of the reactive power flow. All solutions correspond to a maximization of the mechanical production with the minimization of power flow; a trade-off between these two conflicting objectives is then weighted by the coefficient \( c_{control} \).

According to the electric loss hypothesis adopted herein (see (14)), the following relation between objective function and grid power is obtained:

\[ \overline{P}_{control}\left(c_{control}\right) = \overline{P}_{Grid} \]

(17)

Let's now rewrite the objective function with \( \overline{P}_{Grid} \) and \( \overline{P}_{loss,elec} \):

\[ \overline{P}_{control}\left(c_{control}\right) = \overline{P}_{Grid} - c_{loss} - c_{control} \left| \overline{P}_{loss,elec} \right| \]

(18)

Given the hypothesis adopted here for losses, solutions with \( c_{loss} \leq c_{control} \leq 1 \) also represent also multiple trade-offs between the two conflicting objectives, i.e.: final electrical...
energy and losses in the electric chain. The fact that these two objectives are conflicting is not natural, yet nonetheless illustrates why the coupling between electric chain design and control design is so important.

### B. Design of a Control Strategy

To devise a new control strategy, a simple test case will be studied, (see [4][12]). The excitation is assumed to be sinusoidal:

\[ f_{\text{exc}}(t) = F_{\text{exc rms}} \sqrt{2} \cos(\omega t) \]  

The maximum mechanical power can thus be found by applying (8).

\[ P_{\text{wave}} = \frac{F_{\text{exc rms}}^2}{4Z_{\text{Buoy}}} = \frac{F_{\text{exc rms}}^2}{4|Z_{\text{Buoy}}|\cos(\theta_{\text{Buoy}})} \]  

The pulsation dependency is no longer show since the pulsation in this case. The PTO force is chosen to be linear with respect to the vertical speed of the buoy, i.e. the relationship between PTO force and vertical speed can be represented by a transfer function. At this point, let’s introduce the receiver mechanical impedance:

\[ F_{\text{PTO}}(s) = Z_{\text{PTO}}(s) s \Xi(s) \]  

with \( Z_{\text{PTO}}(s) = |Z_{\text{PTO}}(s)| e^{i\theta_{\text{PTO}}(s)} \)

This choice introduces a major restriction. More specifically, discrete solutions (latching, declutching) [12] lie outside this family, although these controls seem to be suitable for a hydraulic actuator and do not use all of the flexibility provided by an electric chain. Power or force leveling [6] has not been studied here either, as the goal of these leveling mechanisms often consists of reducing peak values without significantly reducing the production. It must be kept in mind that the peak values may be significantly reduced thanks to leveling mechanisms.

Under these conditions, we are permitted to use an analogous electric system, as shown in Error! source de la référence non trouvée. Both the speed and PTO force are sinusoidal as well, since the system is assumed to be linear:

\[ \xi(t) = V_{\text{rms}} \sqrt{2} \cos(\omega t - \phi_{\text{speed}}) \]  

\[ f_{\text{PTO}}(t) = |Z_{\text{PTO}}| V_{\text{rms}} \sqrt{2} \cos(\omega t - \phi_{\text{speed}} + \theta_{\text{PTO}}) \]  

\[ V_{\text{rms}} = \frac{F_{\text{exc rms}}}{|Z_{\text{PTO}} + Z_{\text{Buoy}}|^{\frac{1}{2}}} \]

The problem therefore is to choose \( Z_{\text{PTO}} \) that maximizes the function \( P_{\text{control}} \) presented in (16).
continuous controls using a system with a loss coefficient of \( c_{\text{loss}} = 0.10 \). This control depends on the choice of \( c_{\text{control}} \) used to find the maximum: complex conjugate control \((c_{\text{control}} = 0)\), passive control \((c_{\text{control}} \to 1)\) and optimum control for the global conversion \( c_{\text{control}} = c_{\text{control}} = 0.10 \), which will be referred as the Trade-Off control.

C. Results for the Monochromatic Case

The buoy impedance \( Z_{\text{Buoy}} \) of the system and the three continuous control impedances \( Z_{\text{PTO}} \) for the three continuous control strategies are represented in Fig. 7. It is important to have a passive model of the radiation force for this study, to respect the energy conservation principle.

The average of the power grid is given by the relation (cf. (17) and (31)):

\[
\bar{P}_{\text{grid}} = F_{\text{exc,me}}^2 \frac{|Z_{\text{PTO}}|}{|Z_{\text{PTO}} + Z_{\text{Buoy}}|^2} \left( \cos(\theta_{\text{PTO}}) - c_{\text{loss}} g(\theta_{\text{PTO}}) \right) \]  

(36)

To identify production capacity losses due to a non-ideal electric chain, an evaluation must be performed of: the control efficiency \( \eta_c \), the electric efficiency \( \eta_e \), and the global efficiency \( \eta_c \eta_e \). The maximum mechanical power is given in (20), the mechanical power in (28) and the electric grid power in (36).

\[
\eta_c = \frac{P_{\text{mech}}}{P_{\text{wave}}} = \frac{4 |Z_{\text{Buoy}}||Z_{\text{PTO}}| \cos(\theta_{\text{Buoy}}) \cos(\theta_{\text{PTO}})}{|Z_{\text{PTO}} + Z_{\text{Buoy}}|^2} \]  

(37)

\[
\eta_e = \frac{P_{\text{mech}}}{P_{\text{grid}}} = \frac{\cos(\theta_{\text{PTO}}) - c_{\text{loss}} g(\theta_{\text{PTO}})}{\cos(\theta_{\text{PTO}})} \]  

(38)

For the three control strategies, the efficiency of both the control \( \eta_c \) and electric chain \( \eta_e \) can be compared.
graphs in Fig. 8 display these three efficiencies as a function of pulsation. The first solution could consist of using the complex conjugate control near the natural resonance of the buoy and the passive control far from the resonance. It is obvious however that the Trade Off control offers a much higher global efficiency than either of the two others, even when combined.

For $c_{\text{loss}} = 0.1$, the effect of the control coefficient $c_{\text{control}}$ for a given pulsation ($\omega = 0.65 \text{ rad.s}^{-1}$) can be observed in . The global recovery is naturally maximized when $c_{\text{control}}$ is equal to $c_{\text{loss}}$ (0.1), though the global efficiency for $c_{\text{control}} \in [0.056; 0.18]$ is still greater than 90% of the maximum. Hence, the strategy appears to be sufficiently robust.

### IV. POLYCHROMATIC CASE

#### A. Wave Elevation Spectrum and Capture Width

The time-domain model expressed in (1) can be easily simulated. A time-series excitation force is required however to run a simulation. In order to evaluate some of these examples, it is necessary to examine the wave elevation. A sea state is characterized by the energy spectrum of the wave elevation. The modified Pierson-Moskowitz spectrum recommended by the International Ship Structure Committee (ISSC) is used in this paper; this spectrum accurately models the behavior of real sea waves [15]:

$$S_{el}(\omega) = \frac{5}{32\pi} H_s^2 T_p \left( \frac{2\pi}{\omega T_p} \right)^5 \exp\left(-\frac{5}{4} \left( \frac{2\pi}{\omega T_p} \right)^4 \right)$$

where $H_s$ is the significant wave height and $T_p$ the peak wave period. We are now able to complete (10):

$$P_{\text{Wave}}(\omega) = \frac{\rho g}{2\omega} E_{\text{rms}}(\omega)^2 = \frac{\rho g^3}{2\omega} S_{el}(\omega) d\omega$$

The theoretical maximum energy for a given sea-state $(H_s, T_p)$ can then be derived as follows:

$$\overline{P}_{\text{Wave}} = \int_0^\infty \frac{\rho g^3}{2\omega} S_{el}(\omega) d\omega \approx 94.8 H_s^2 T_p^3$$

with $\overline{P}_{\text{Wave}}$ in watts, $H_s$ in meters and $T_p$ in seconds. This is a unique result for a given system and hypothesis.

In order to better define the resource for all wave systems, the wave energy transport $J_{\text{wave}}$ is expressed in watts per meter of wave front, i.e.:
\[ J_{\text{wave}} = \int_0^\infty \frac{\rho g^2}{2\omega} S_\alpha(\omega) d\omega = 421 H^2 T_p \]  
(42)

with \( J_{\text{wave}} \) in watts per meter, \( H \) in meters and \( T_p \) in seconds.

The equivalent capture width is thus a common measurement in the wave energy system, it is the ratio of the converted power to the wave energy transport \( J_{\text{wave}} \). For an axisymmetric heaving buoy, with the spectrum used herein, the upper limit for the capture width is:

\[ L_{\text{max}} = \frac{C_{\text{wave}}}{J_{\text{wave}}} = 0.225 T_p^2 \]  
(43)

with \( L_{\text{max}} \) in meters and \( T_p \) in seconds. This result corresponds to a unitary global efficiency (i.e. both control and electric). The transition between efficiency and width ratio is a very simple one:

\[ L = \eta_c(H_s, T_p) \eta_c(H_s, T_p) L_{\text{max}}(T_p) \]  
(44)

where \( L \) is the capture width of the complete system.

**B. Time Series Excitation Force**

The transfer functions \( H_{\text{wave}}(s) \) gives the relation between wave elevation and excitation force:

\[ S_{\text{exc}}(\omega) = |H_{\text{wave}}(j\omega)|^2 S_{\alpha}(\omega) \]  
(45)

Let’s now approximate the excitation force by summing monochromatic excitations:

\[ F_{\text{exc}}(t) = \sum_{k=1}^N F_{\text{exc,}\omega_k} \sqrt{2} \sin(\omega_k t + \phi_k) \]  
(46)

The phases \( \phi_k \) are set randomly. The pulsations \( \omega_k \) used are 981 regular spaced pulsations (\( \Delta \omega = 10 \text{ rad.s}^{-1} \)) between 0.2 rad.s\(^{-1} \) and 10 rad.s\(^{-1} \). In our case, this configuration is similar to the solution of a reconstructed wave elevation with a random phase, as presented in [12]. Thanks to (45), the following approximation can now be written:

\[ F_{\text{exc,}\omega_k} = |H_{\text{exc}}(j\omega_k)| \sqrt{S_{\alpha}(\omega_k)} \Delta \omega_k \]  
(47)

**C. Approximation of the Monochromatic Strategies**

The optimal solutions for control impedance are provided in (34) and (35). For the monochromatic case, it is easy to perform the control; however, it is difficult; or even impossible in some cases, to respect the two relationships for multiple frequencies. In particular, passive control with a frequency-dependent damping coefficient is impossible to achieve.

As a next step, the strategies presented in the previous section will be approximated using a classical tunable reactive form [16] in order to confirm that this strategy yields good results in a more realistic case:

\[ Z_{\text{PTO}}(s) = M_{\text{PTO}}(T_p) s + B_{\text{PTO}}(T_p) + \frac{K_{\text{PTO}}(T_p)}{s} \]  
(48)

where \( M_{\text{PTO}}, B_{\text{PTO}} \) and \( K_{\text{PTO}} \) are respectively an emulated mass, an emulated damping and an emulated stiffness.

To choose the optimal values for these three coefficients, the choice here was to maximize a cost function given by:

\[ \bar{P}_{\text{control,poly}} = \int_0^\infty P_{\text{control}}(s) p_{\text{wave}}(s) \]  
(49)

with \( p_{\text{control}}(s) \) given in (33). The assumption made here is that the frequency approach yields results that closely compare to the time-domain results, even though the Parseval’s identity cannot be used (as the loss model is not quadratic). This assumption proves to be very useful in reducing computation time.

Average mechanical power or average grid power can now also be predicted:

\[ \bar{P}_{\text{mech}} = \int_0^\infty \eta_c(s) p_{\text{wave}}(s) \]  
(50)

\[ \bar{P}_{\text{grid}} = \int_0^\infty \eta_d(s) p_{\text{wave}}(s) \]  
(51)

with \( \eta_c(s) \) and \( \eta_d(s) \) given in (37) and (38).

**D. Stability Constraints on the Emulated Terms**

Emulated terms must be used carefully due to the stability limits. Stability margins are reduced whenever negative mass or spring terms are emulated. It can indeed be seen, we can see in Erreur : source de la référence non trouvée that the open loop (OL) transfer function of the system (buoy and control) is given by:

\[ H_{OL}(s) = \frac{Z_{\text{PTO}}(s)}{Z_{\text{buoy}}(s)} \]  
(52)

\[ H_{OL}(s) = \frac{M_{\text{PTO}}(T_p) s^2 + B_{\text{PTO}}(T_p) s + K_{\text{PTO}}(T_p)}{M + a_\infty s^2 + H |s| s + K} \]  
(53)

In our case, we can easily calculate two important limits for the overall system stability (\( H(s) \)) has finite limits in zero and positive infinity:

\[ \lim_{s \to 0} H_{OL}(s) = \frac{K_{\text{PTO}}(T_p)}{K} \]  
(54)

\[ \lim_{s \to \infty} H_{OL}(s) = \frac{M_{\text{PTO}}(T_p)}{M + a_\infty} \]  
(55)

The critical point is \( H_{OL}(s) = -1 \). In order to control the distance between the open loop transfer function and this critical point (and thus control the system stability), the choice for two of the three coefficients must be constrained. Three cases have been tested herein: no constraint, a weak constraint
and a strong constraint. The weak constraint (wc) corresponds to a gain margin of 6 dB:

\[ M_{PTO_{wc}}(T_p) > -(M + a_\infty)/2 \quad (56) \]

\[ K_{PTO_{wc}}(T_p) > -K/2 \quad (57) \]

The strong constraint (sc) corresponds to an infinite gain margin, i.e.:

\[ M_{PTO_{sc}}(T_p) > 0 \quad (58) \]

\[ K_{PTO_{sc}}(T_p) > 0 \quad (59) \]

Hydrodynamic tests must be conducted in order to select the stability limits to be used in this case.

E. Results for the Polychromatic Case

Since the numerator of the mechanical impedance transfer function in (48) has a higher degree than the denominator, the transfer function is not causal and, as such, can not be realized. The function used for the time-domain simulations is as follows:

\[ Z_{PTO}(s) = \left( M_{PTO}(T_p)s + B_{PTO}(T_p) + \frac{K_{PTO}(T_p)}{s} \right) \frac{1}{1 + \tau s} \quad (60) \]

with time constant \( \tau \) being small compared to the wave pulsation (set here at 10 ms). This is a causal, flexible and easy-to-implement control strategy; moreover, it features the same equations as a Proportional-Integral-Derivative (PID) controller.

The case studied here as an example corresponds to a sea-state with a significant wave height \( H_s = 2.5 \) m and a peak wave period \( T_p = 9.5 \) s. The simulations last 628 s and are repeated 20 times with different random draws for the excitation force phases. In all, 100 different values of \( c_{\text{control}} \) have been tested.

The time-domain simulations were run using Matlab/Simulink.

The global efficiency as a function of control parameter \( c_{\text{control}} \) is shown in Fig. 10. The frequency computations are shown in dashed lines: the approximation appears to be correct, and the assumption is thus considered to be verified. The three control strategies are illustrated with examples of power time series in Fig. 11.

The control strategies determined with \( c_{\text{control}} > c_{\text{loss}} \) forms a Pareto front in a production-loss diagram (See Fig. 12 (a)). For a given production, the result is the solution offering the minimum losses. The solution with the minimum stability constraint always yields better results in this diagram.

Fig. 10. Global efficiency as a function of control parameter \( c_{\text{control}} \) for \( T_p = 9.5 \) s under the hypothesis \( c_{\text{loss}} = 0.10 \). The Global efficiency is the product of the control efficiency \( \eta_C \) and the electric efficiency \( \eta_E \). Solid lines represent the time-domain simulation and dashed lines the approximation in the frequency domains. Blue lines correspond to the solutions without stability constraints (w/o c), green lines with weak stability constraints (wc) and red lines with strong stability constraints (sc).

Fig. 11. Example of power time series for a given random draws for the excitation force phases. The graphs compare the three control strategies: Complex-Conjugate (C-C) \( (c_{\text{control}} = 0) \), Passive (P) \( (c_{\text{control}} \rightarrow 1) \) and Trade-Off (T-O) \( (c_{\text{control}} = 0.1) \). The loss coefficient is \( c_{\text{loss}} = 0.10 \), the sea-state is \( T_p = 9.5 \) s and \( H_s = 2.5 \) m. The constraint for stability is weak (see (56) and (57)). Note that the scale for the power in the three case are not the same.
Production maximization is not the ultimate goal of these control strategies. Given the over-sizing required to achieve the production maximization, the solution with maximum grid power is not optimal for per-kWh cost. A complete study of the cost of both the generator and its converter is needed in order to draw a conclusion on the best control strategy.

We can reasonably suppose that the peak and root mean square value of the force are correlated with the linear generator cost. Fig. 12 (b) therefore depicts the two following ratios for comparing these various solutions:

\[
rf_{rms} = \frac{f_{PTO\,rms}}{P_{grid}} \quad \text{and} \quad rf_{peak} = \frac{f_{PTO\,peak}}{P_{grid}} \tag{61}
\]

We can also reasonably suppose that the peak and root mean square value of the mechanical power are correlated with the converter cost. Fig. 12 (c) then represents the two following ratios for comparing these various solutions:

\[
r_{P_{rms}} = \frac{P_{mech\,rms}}{P_{grid}} \quad \text{and} \quad r_{P_{peak}} = \frac{P_{mech\,peak}}{P_{grid}} \tag{62}
\]

V. CONCLUSION AND OUTLOOK

This paper has focused on the potential resource for a Direct Wave Energy Converter, in a global context of kWh cost minimization. Electrical chain losses and force or power amplitude constraints play an important role in designing the electric chain, and hence in its cost. Moreover, they play a key role in the conversion mechanism. For this reason, the control strategy and the electric chain design are highly correlated.

This paper has proven that taking account of electrical losses in the design of a control strategy improves global efficiency of the conversion chain compared to classical solutions, i.e.: a passive strategy or complex conjugate strategy. Power and force leveling must be tested with this strategy in order to minimize the chain size introduced to achieve a given production.

Converted energy maximization may help to minimize the per-kWh cost; however recovery optimization is not an end in itself. The final system, including the electric chain and control strategy, must minimize the per-kWh cost. In the case presented here, the continuous variation of a control parameter offers multiple possibilities. Economic considerations must be taken into account when approximating the per-kWh cost optimization.

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