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A simple correction method of inner filter effects affecting FEEM and its application to the PARAFAC decomposition

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Abstract

In this paper we introduce a new inner filters correction method for standard fluorometer. The Controlled Dilution Approach (CDA) deals with highly absorbing solutions using the Fluorescent Excitation-Emission Matrix of a controlled weak dilution. Along with the non linear FEEM of the original solution, these two informations allow to estimate the linearized FEEM. The method relies on inner filter effects modelization. Beyond its numerical simplicity, the main interest is that CDA only requires fluorescence measurements. The method was validated using a set of known mixtures and a set of dissolved organic matter samples. In addition we show that the corrected FEEM can be used efficiently for advanced multilinear analysis. Therefore CDA is presented here as a relevant pretreatment to the PARAFAC decomposition of highly absorbing mixtures.

Key words: EEM, inner filter effects, PARAFAC, 3D fluorescence

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1 Introduction

1.1 Non linearities in fluorescence spectroscopy

Fluorescent molecular components (fluorophores) can be easily distinguished by their spectroscopic properties and more particularly by their fluorescence spectra [1]. Recent fluorimeters provide successive measurements of the fluorescence intensity emitted by a solution of one or several fluorophores. By scanning excitation and emission wavelength domains, Fluorescent Excitation-Emission Matrices (FEEM) gather a lot of informations about the solution. These spectra are now widely used in various scientific domains such as medicine [2], analytical chemistry [3] or environmental sciences [4,5]. Ideally, considering the FEEM (I_{3D}) of a single fluorophore, its norm is proportional to the fluorophore concentration in the solution and its pattern is given by the outer product between the excitation spectrum and the emission spectrum of the fluorophore. This is the classical linear model of fluorescence. However it is well known that its pertinence decreases with the concentration [6]. Actually, non linear deviations mean that the gradual absorption by the solution of both exciting and fluorescent lights cannot be neglected. These effects are known as inner filter effects and affect both I_{3D} norm and I_{3D} pattern. Therefore, in presence of inner filter effects, one cannot deduce any correct information about the solution directly from I_{3D} .

Fig. 1. Evolution of the quinine sulphate 3D spectrum for three different concentrations: 3.54 ppm (left spectrum), 51.54 ppm (middle spectrum), 108.75 ppm (right spectrum)

Example of inner filter effects is given on figure 1. This example clearly shows that the FEEM pattern can be severely affected even in the simple case of a single fluorophore solution. In other respects, considering several solutions of the same diluted fluorophore

measured in different conditions, many other factors such as diffusion, temperature variations, pH variations, fluorescence quenching or ionic strength can affect the FEEM linearity [1]. In this work, we only focus on inner filter effects correction.

1.2 Inner filter effects correction

Inner filter effects are observed and studied for a long time now [7,8]. Two main correction methods are used to prevent these deviations. Since inner filter effects can be neglected for weak absorbances *i.e.* weak concentrations, a common procedure is to strongly dilute the solution until maximal absorbance is inferior than 0.1 [1]. There is an obvious drawback with this dilution method as a too strong diluting factor would severely reduce the signal to noise ratio. Moreover this procedure must be applied very carefully to avoid contamination or physico-chemical changes. Therefore, ensuring the linearity of the data set is no easy task. The second approach uses a mathematical model of inner filter effects [9–11]. Then one can deduce a correction factor in order to estimate element by element, a corrected FEEM (I_c) from I_{3D} . It is assumed that if the correction factor is suitable then I_c will follow the linear model. This approach relies on the Beer-Lambert law [1] which gives the elementary variation dI of the light intensity through an elementary optical path dl at wavelength λ :

$$dI = -I(\lambda)\alpha(\lambda)dl \quad (1)$$

where α is the absorption coefficient of the solution. Then, the integrated law describes the light absorption through the entire optical path. If I_0 is the intensity of the exciting light, the transmitted intensity outside a cell of length l is simply given by the relation:

$$I(\lambda) = I_0(\lambda)e^{-\alpha(\lambda)l} = I_0(\lambda)10^{-A(\lambda)} \quad (2)$$

The absorbance spectrum of the solution is then defined by

$$A(\lambda) = \log_{10} \left(\frac{I_0(\lambda)}{I(\lambda)} \right) = \frac{l\alpha}{\log(10)} \quad (3)$$

Figure 2 shows a schematic diagram of absorbance measurement. A is obtained by measuring the transmitted intensity through the diluted solution (I_T) and the transmitted intensity through the solvent (I_R) at successive wavelength:

$$A(\lambda) = \log_{10} \left(\frac{I_R(\lambda)}{I_T(\lambda)} \right) \quad (4)$$

In right angle fluorescence spectroscopy, classical model of inner filter effects is given by equation 5.

Fig. 2. Absorbance measurement

$$I_{3D}(\lambda_{ex}, \lambda_{em}) = I_c 10^{-\frac{A(\lambda_{ex}) + A(\lambda_{em})}{2}} \quad (5)$$

Thereby, one can use the measured absorbance spectrum to compute the correction factor and then deduce I_c . Similar methods were proposed in [12–14]. In the following, this approach will be identified as the Absorbance Correction Approach (ACA). ACA is commonly used in applicative papers dealing with fluorescence spectroscopy [15,16]. However absorbance measurement is much less sensitive than fluorescence measurement. In addition it requires an other experimental device whose characteristics are different, introducing its own error in the chain. Finally, the short linear range of absorption measurement is another important drawback of ACA. In this work we propose an original correction method: the Controlled Dilution Approach (CDA) which combines the advantages of both methods. CDA uses the FEEM of a diluted solution instead of absorbance measurement in order to estimate I_c . The crucial point is that the dilution factor can be chosen small enough to avoid the drawback of the dilution approach. Indeed, the linearity of this second FEEM is not required. Consequently, CDA keeps the main advantage of ACA which is a very simple numerical correction, but it only requires fluorescence spectra. Analyzed solutions are generally mixtures of several fluorophores. Therefore, many applications involve a separation step to recover the underlying individual spectra and concentration profiles of each fluorophore. Number of chemometric methods were proposed in the literature in order to perform multilinear decompositions of FEEM [17–20]. Based on original works of Harshman [21], PARAllel FACtor analysis (PARAFAC) was introduced in this context by Bro [22]. During the last decade PARAFAC has proved to be the most relevant approach. For instance, in environmental sciences, it is currently the reference tool to characterize and trace Dissolved Organic Matter (DOM) [23–25]. In return, it do not take into account inner filter effects [26,27]. Consequently there is an irreversible loss of performance when dealing with highly absorbing mixtures.

Like other inner filter effects correction methods, CDA is independent of this separation step. However, we take into consideration that a large part of FEEM applications, uses this kind of decomposition. As a consequence, in order to ensure the reliability of CDA, we also present in this paper its performance as a PARAFAC pretreatment of highly absorbing mixtures.

1.3 Paper organization

CDA is detailed on section 2 of this paper. First the modelization of inner filter effects is given in section 2.1 then CDA is described on section 2.2. Lastly, practical aspects of CDA are presented in section 2.3 notably in the case of FEEM sets analysis. The PARAFAC application to the CDA corrected FEEM is shortly describe.

In this work, CDA correction is experimentally tested on two very different sets of mixtures. The first set is composed of standard laboratory mixtures of fluorescein and quinine sulphate. Consequently, thist first data set is used to strictly validate CDA and compare with classical ACA. On the other side, the second data set is constituted by unknown samples of DOM catchments and gives an example of how the method can help in a realistic case. Section 3 describes the experimental part of these tests. Results obtained on both data sets before and after the PARAFAC decomposition are presented and discussed in section 4.

2 Theory

2.1 Modelization of inner filter effects

Like ACA, CDA relies on equation 5. Few authors give detailed mathematical justifications of this model, particularly in the most general case of 3D spectra of fluorophore mixtures. In this subsection a rigorous interpretation of equation 5 is proposed.

We consider here a mixture of N fluorophores. For each fluorophore n , we note c_n its concentration in the solution, $\varepsilon_n(\lambda_{ex})$ its molar extinction coefficient at the excitation wavelength λ_{ex} , Φ_n its the quantum yield of fluorophore n , $\gamma_n(\lambda_{em})$ its emission probability at wavelength λ_{em} and $\alpha_n(\lambda_{ex})$ its absorption coefficient which is equal to the product of c_n by $\varepsilon_n(\lambda_{ex})$. We assume that the absorption and emission spectra of fluorophore n are normalized values of respectively $\varepsilon_n(\lambda_{ex})$ and $\gamma_n(\lambda_{em})$. In the linear approximation, every fluorescing particles are treated equally as if the whole sample cell was an ele-

mentary point. In order to improve this model, one should takes into account the particular geometry of the problem.

Fig. 3. Schematic diagram of right angle fluorescence measurement

Figure 3 recalls basically the experimental device of right angle standard fluorimeters. The excitation light ($I_0(\lambda_{ex})$) is absorbed through the sample cell (length l) by the fluorophores, inducing the fluorescent light. Finally, a fraction ($I_{3D}(\lambda_{em})$) of the emitted signal is collected perpendicularly to the exciting beam. λ_{ex} and λ_{em} scanings allow to measure the FEEM.

In this study, several approximations were made. First of all, we took into consideration the symmetry of the problem, therefore the influence of the z spatial dimension was neglected.

Fig. 4. Scheme of the sample cell, view from above

129 Secondly, only two main optical paths were considered. They represent the
 130 excitation beam and emission beam in figure 4 scheme. This means that the
 131 fraction of the exciting light which do not reach the "influence zone" Z_e was
 132 neglected as well as the fluorescence light issued from the region outside Z_e .
 133 Then each elementary segment of the "excited face" of Z_e was supposed to
 134 receive the same energy from the rectilinear exciting beam. In the same way,
 135 we assumed that each elementary segment of the "emission face" of Z_e provides
 136 the same energy to the detector. Furthermore, diffusion and re-emission effects
 137 were also neglected. Actually we only consider the elementary optical paths
 138 represented in figure 5.

Fig. 5. Elementary cutting of the "influence zone" in the directions of exciting and emitted lights

139 The integrated Beer-Lambert law describes the light absorption through the
 140 optical path. If I_0 is the light intensity at the point x_0 of the dilute solution,
 141 the intensity in x is simply given by the relation: $I = I_0 e^{-\alpha(\lambda_{ex})(x-x_0)}$ where α
 142 is the mixture total absorption coefficient: $\alpha = \sum_n \alpha_n$. The influence zone was
 143 divided into horizontal and vertical elementary strips of respective dimension
 144 $dy \times l$ and $l \times dx$. Then each horizontal strip receives an equal elementary
 145 fraction of the exciting light: $\frac{dy I_0}{\Delta_y}$ and the Beer-Lambert law quantifies the
 146 intensity transmitted to x . A fraction $\alpha_n dx$ is absorbed by fluorophore n , and
 147 the total intensity absorbed by fluorophore n in the "influence zone" (I_{An}) is
 148 given by:

$$I_{An}(\lambda_{ex}) = \frac{dy I_0}{\Delta_y} \alpha_n(\lambda_{ex}) \int_{\frac{l-\Delta_x}{2}}^{\frac{l+\Delta_x}{2}} e^{-\alpha(\lambda_{ex})x} dx \quad (6)$$

$$I_{An}(\lambda_{ex}) = 2 \frac{I_0}{\Delta_y \alpha(\lambda_{ex})} \alpha_n(\lambda_{ex}) e^{-\frac{\alpha(\lambda_{ex})l}{2}} \sinh\left(\frac{\alpha(\lambda_{ex})\Delta_x}{2}\right) dy \quad (7)$$

149 The fluorescence signal emitted by the dy strip at wavelength λ_{em} is equal
 150 to $\sum_n \Phi_n \gamma_n(\lambda_{em}) I_{An}(\lambda_{ex})$ and the Beer-Lambert law integrated on all the ele-
 151 mentary horizontal strips gives the ratio of the fluorescence signal transmitted
 152 outside the sample cell in the y direction, $I_{3D}(\lambda_{ex}, \lambda_{em})$.

$$I_{3D}(\lambda_{ex}, \lambda_{em}) = \int_{\frac{l-\Delta_y}{2}}^{\frac{l+\Delta_y}{2}} \sum_n \Phi_n \gamma_n(\lambda_{em}) I_{An}(\lambda_{ex}) e^{-\alpha(\lambda_{em})y} \quad (8)$$

$$I_{3D}(\lambda_{ex}, \lambda_{em}) = \frac{4I_0 e^{-\frac{\alpha(\lambda_{ex})l}{2}} \sinh\left(\frac{\alpha(\lambda_{ex})\Delta_x}{2}\right) e^{-\frac{\alpha(\lambda_{em})l}{2}} \sinh\left(\frac{\alpha(\lambda_{em})\Delta_y}{2}\right)}{\Delta_y \alpha(\lambda_{ex}) \alpha(\lambda_{em})} \sum_n \alpha_n(\lambda_{ex}) \Phi_n \gamma_n(\lambda_{em}) \quad (9)$$

153 $\frac{\alpha(\lambda_{ex})\Delta_x}{2}$ and $\frac{\alpha(\lambda_{em})\Delta_y}{2}$ are supposed to be small enough to make the following
 154 approximation:

$$I_{3D}(\lambda_{ex}, \lambda_{em}) = I_0 \Delta_x \left(\sum_n \alpha_n(\lambda_{ex}) \Phi_n \gamma_n(\lambda_{em}) \right) e^{-\frac{\alpha(\lambda_{ex})l}{2}} e^{-\frac{\alpha(\lambda_{em})l}{2}} \quad (10)$$

155 Then we can define $g = \frac{l}{2}$ and $G_n = I_0 \Delta_x \Phi_n$. This leads to the final expression
 156 of the model:

$$I_{3D}(\lambda_{ex}, \lambda_{em}) = \left(\sum_{n=1}^N G_n c_n \varepsilon_n(\lambda_{ex}) \gamma_n(\lambda_{em}) \right) \prod_{n=1}^N e^{-g(c_n \varepsilon_n(\lambda_{ex}) + c_n \varepsilon_n(\lambda_{em}))} \quad (11)$$

157 In the following we define

$$L(\lambda_{ex}, \lambda_{em}) = \sum_{n=1}^N G_n c_n \varepsilon_n(\lambda_{ex}) \gamma_n(\lambda_{em}) \quad (12)$$

158 then we have

$$I_{3D}(\lambda_{ex}, \lambda_{em}) = L e^{-g(c_n \varepsilon_n(\lambda_{ex}) + c_n \varepsilon_n(\lambda_{em}))} \quad (13)$$

159 This equation is clearly equivalent to equation 5 with $I_c = L$. Its first order
 160 approximation is justified for small enough concentrations. In this case, since
 161 the exponential term tends to 1 one obtains the linear model of fluorescence.
 162 Correction of inner filter effects simplifies spectral analysis. It is interesting
 163 to note that their modelization is also used in another context. Actually, a
 164 recent article [28] highlighted the major contribution of inner filter effects in
 165 the phenomenon of concentration-dependent red-shift [29,30]. In this work, a
 166 similar model has been successfully used to optimize synchronous fluorescence
 167 spectroscopy of concentrated mixtures of fluorophores.

168 2.2 Controlled Dilution Approach

169 The previous model describes non linear effects but the related equation can
 170 still be considered as a bilinear decomposition involving some modified indi-
 171 vidual spectra $\varepsilon'_n(\lambda_{ex})$ and $\gamma'_n(\lambda_{em})$:

$$I_{3D}(\lambda_{ex}, \lambda_{em}) = \sum_{n=1}^N \varepsilon'_n(\lambda_{ex}) \gamma'_n(\lambda_{em}) \quad (14)$$

172 with,

$$\varepsilon'_n(\lambda_{ex}) = G_n c_n \varepsilon_n(\lambda_{ex}) e^{-\sum_{p=1}^N g c_p \varepsilon_p(\lambda_{ex})} \quad (15)$$

$$\gamma'_n(\lambda_{em}) = \gamma_n(\lambda_{em}) e^{-\sum_{p=1}^N g c_p \varepsilon_p(\lambda_{em})} \quad (16)$$

173 It is well known that bilinear decompositions have an infinite number of equiv-
 174 alent solutions in the least square sense. Therefore, without additional infor-
 175 mation, no mathematical tool can diagnose whether a FEEM is affected by
 176 inner filter effects or not. *A fortiori* additional informations are also needed to
 177 correct inner filter effects. In ACA this information is the solution absorbance
 178 spectrum. This section shows how the correction can be made with fluorescent
 179 spectra only.

180 According to equation 11 the FEEM I_{3D} of a N fluorophores mixture is the
 181 product of a linear (L) term in respect of concentrations and spectra by a non
 182 linear one, denoted H :

$$H(\lambda_{ex}, \lambda_{em}) = \prod_{n=1}^N \exp(-g(c_n \varepsilon_n(\lambda_{ex}) + c_n \varepsilon_n(\lambda_{em}))) \quad (17)$$

183 So we can write:

$$I_{3D}(\lambda_{ex}, \lambda_{em}) = L(\lambda_{ex}, \lambda_{em}) H(\lambda_{ex}, \lambda_{em}) \quad (18)$$

184 Now, let's I_{3D_p} be the FEEM of the same mixture, diluted by a factor p , then
 185 we have:

$$I_{3D_p}(\lambda_{ex}, \lambda_{em}) = \left(\sum_{n=1}^N G_n \frac{c_n}{p} \varepsilon_n(\lambda_{ex}) \gamma_n(\lambda_{em}) \right) \prod_{n=1}^N e^{-g(\frac{c_n}{p} \varepsilon_n(\lambda_{ex}) + \frac{c_n}{p} \varepsilon_n(\lambda_{em}))} \quad (19)$$

$$I_{3D_p}(\lambda_{ex}, \lambda_{em}) = \frac{1}{p} L(\lambda_{ex}, \lambda_{em}) H^{\frac{1}{p}}(\lambda_{ex}, \lambda_{em}) \quad (20)$$

186 The analytical resolution of 18 and 20 gives

$$L(\lambda_{ex}, \lambda_{em}) = \left(\frac{(p I_{3D_p}(\lambda_{ex}, \lambda_{em}))^p}{I_{3D}(\lambda_{ex}, \lambda_{em})} \right)^{\frac{1}{p-1}} \quad (21)$$

$$H(\lambda_{ex}, \lambda_{em}) = \left(\frac{I_{3D}(\lambda_{ex}, \lambda_{em})}{p I_{3D_p}(\lambda_{ex}, \lambda_{em})} \right)^{\frac{p}{p-1}} \quad (22)$$

The L term is the corrected FEEM estimated by CDA, corresponding to the linear model of fluorescence. As previously mentioned, the correction only requires the original FEEM and the diluted FEEM and the value of the dilution factor p .

The sensitivity of the estimator of L to p is difficult to quantify. A first order approximation of the variability of L (Δ_L) leads to:

$$\frac{\Delta_L}{L} = \frac{(p - 1 - \log(p) - \log(I_{3Dp}) + \log(I_{3D}))\Delta_p}{(p - 1)^2}$$

187 According to this equation, a high factor should be preferred. However it would
188 involve the drawbacks of a strong dilution (see section 1.2). Finally, we advo-
189 cate for a dilution factor corresponding to the simplest dilution process, thus
190 the experimental uncertainty Δ_p is minimized. This was the case for all the
191 experiments presented in this study.

192 Owing to the term by term division in equation 21, noisy values in the mea-
193 sured FEEM could affect the estimation of L . Actually if the division involves
194 two small values relatively to the noise level, some very narrow and localized
195 peaks can appear. Fluorescent spectroscopy is a very sensitive technique there-
196 fore this kind of deviation are rarely observed in practical situations. Otherwise
197 those peaks appear outside the main fluorescing areas. In consequence, they
198 can be easily detected and filtered without damaging the fluorescent peaks.

199

200 2.3 CDA and multilinear analysis of concentrated fluorescing mixtures

201 We consider now a set of I mixtures and $c_n(i)$ denotes the concentration of
202 fluorophore n in mixture i . CDA methodology is simple, the correction is done
203 sample by sample. The first step consists in choosing the dilution factor p for
204 each sample (see the end of section 2.2). Obviously the same value can be used
205 for every sample. Then, the corresponding controlled dilution is performed
206 and both FEEM I_{3D} and I_{3Dp} are measured. Before correction, Rayleigh and
207 Raman scatters must be corrected carefully on each FEEM. This is the end
208 of the experimental and pre-processing steps.

209 Finally, for each sample i , the estimation $L(i, \lambda_{ex}, \lambda_{em})$ of the linearized FEEM
210 is obtained directly from equation 21. At this stage, the correction of the inner
211 filter effects is completed.

212 Actually we have to take into account measurement and modelization errors.
213 In addition we can define $\tilde{c}_n(i) = G_n c_n(i)$. Therefore in practice, definition 12
214 is rewritten:

$$L(i, \lambda_{ex}, \lambda_{em}) = \sum_{n=1}^N \tilde{c}_n(i) \varepsilon_n(\lambda_{ex}) \gamma_n(\lambda_{em}) + E(i, \lambda_{ex}, \lambda_{em}) \quad (23)$$

where E is the error term. Equation 23 is a rank N decomposition of the 3 way tensor L or in other words a 3-way PARAFAC model of rank N . For each fluorophore n , the loading vectors of the decomposition $\tilde{c}_n$, ε_n , and γ_n are linearly linked to its concentration profile, its excitation spectrum and its emission spectrum respectively. Moreover, the solution of this decomposition is unique up to trivial scaling and position indeterminacy [31,32]. Finally, several efficient algorithms were proposed and compared for the estimation of the loading vectors. These are largely described in the literature [33–35]. Those three physical, mathematical and practical reasons made the PARAFAC decomposition the most suitable tool for analysing linear(ized) FEEM. Tutorials and examples of PARAFAC application to FEEM analysis can be found elsewhere [36,22,37].

Eventually, the PARAFAC decomposition can be run normally on the corrected FEEM set in order to find out real individual spectra and concentration profiles of each fluorophore.

3 Experimental

3.1 Data set 1, standard mixtures

Seven solutions ($S_1^i, i = 1 \dots 7$) with different concentrations of fluorescein (Aldrich) and quinine sulphate (Merck) were prepared in 0.1M H_2SO_4 (Aldrich) in order to validate the correction method. All chemicals are analytical grade. Concentrations in fluorescein and quinine sulphate are given in table 1 along with solution absorbances. These two fluorophores and their concentrations in the solutions were chosen because of their good fluorescing ability and their overlapped spectra in order to emphasize inner filter effects.

Table 1

Concentrations, maximal absorbances and mean absorbances of the original solutions of quinine sulphate and fluorescein.

Solution	S_1^1	S_1^2	S_1^3	S_1^4	S_1^5	S_1^6	S_1^7
c_{SQ} (ppm)	0	11.02	32.6	54.38	76.15	97.73	108.75
c_F (ppm)	83.15	74.72	58.23	41.58	24.92	8.43	0
Absorbance max.	2.30	2.18	1.83	1.32	1.17	1.38	1.47
Mean Absorbance.	0.42	0.40	0.37	0.33	0.29	0.27	0.24

Concentrations in quinine sulphate (c_{SQ}) and fluorescein (c_F) are given in parts per million (ppm). Maximum and mean value of absorbance are relative to the 275 to 500 nm excitation range.

Seven twice diluted solutions ($S_{1D}^i, i = 1 \cdots 7$) were obtained by mixing equal volumes of initial solutions S_1^i and 0.1M of H_2SO_4 . Table 2 gives the actual value of the dilution factor for the seven solutions and the standard deviation due to the pipet precision.

Table 2

Dilution factors used for the seven solutions of fluorescein and quinine sulphate.

Solution	S_{1D}^1	S_{1D}^2	S_{1D}^3	S_{1D}^4	S_{1D}^5	S_{1D}^6	S_{1D}^7
p	2.11	2.08	2.07	2.07	2.07	2.08	2.11
σ_p	0.034	0.032	0.030	0.029	0.030	0.032	0.034

σ_p is the estimated standard deviation of the dilution factor due to the experimental dilution

Reference solutions ($S_{1R}^i, i = 1 \cdots 7$) were obtained by diluting 100 μ L of S_1^i in 3000 μ L of 0.1M of H_2SO_4 . In this case of simple mixtures, this dilution prevents inner filter effects without physico-chemical changes.

All measured spectra were obtained with a fluorometer Hitachi F4500. FEEM of the three solutions sets S_1, S_{1D} and S_{1R} , were recorded at 30000 nm/min scan speed from 350 to 700 nm in emission by step of 5 nm and for excitation wavelength from 275 to 500 nm by step of 5 nm. Excitation and emission bandwidth were 5 nm. Fluorescence intensity was corrected from PM response using manufacturer setting. Data for FEEM treatment were extracted by FLWinLab software for emission and excitation range stepped every 5 nm. Rayleigh and Raman scatters were removed numerically by the method proposed by Zepp in [38]. In the following, measured FEEM from original, diluted and reference solution i will be referred as I_{1U}^i, I_{1D}^i and I_{1R}^i respectively. Absorption spectra of solutions S_1 were obtained from transmittance spectra recorded with absorbance mode of the F4500 (speedscan 240 nm/min) from 200 to 800 nm with 5 nm bandwidths in excitation and emission. 2D reference spectra of fluorescein and quinine sulphate were recorded from S_{1R}^1 and S_{1R}^7 respectively, at 240 nm/min scan speed by step of 1 nm with 5 nm bandwidth in excitation and 2.5 nm bandwidth in emission. Quinine sulphate (I_{SQ-ex}) and fluorescein (I_{F-ex}) excitation spectra were recorded from 275 to 500 nm at 450 nm and 510 nm emission wavelength respectively. Their emission spectra (I_{SQ-em} and I_{F-em}) were recorded from 350 to 700 nm at 340 nm and 440 nm excitation wavelength respectively.

I_{1R} and I_{1U} compose the groups of reference and uncorrected FEEM respectively. Using absorption spectra in equation 5, we could compute the ACA corrected FEEM (I_{1ACA}^i) from $I_{1U}^i, i = 1 \cdots 7$. In the same way, using I_{1D}^i in equation 21 with dilution factor values of table 2, we could apply CDA to I_{1U}^i and compute the CDA corrected FEEM (I_{1CDA}^i), $i = 1 \cdots 7$. I_{1ACA} and I_{1CDA} compose the groups of ACA and CDA corrected FEEM respectively.

These four groups of FEEM are considered as four 3-way tensors of dimensions $7 \times 46 \times 51$. Trilinear decompositions of these tensors were performed with the PARAFAC-ALS algorithm of the nway toolbox for Matlab [39].

277 The second data set is composed of FEEM obtained from eleven samples
 278 of concentrated humic acid solutions which were extracted from catchments
 279 of Cameron soils. For each sample, 1 g of soil was extracted by 30 mL of
 280 HCl (1M) solution. After separation, the supernatant solution was cleaned on
 281 XAD-8 resin and stored at $4^\circ C$ in dark. The resting soil was then extracted
 282 with 30 mL of 1M $NaOH$ solution. After separation, this second supernatant
 283 contains humic acid substance. Purification was done by acidic precipitation
 284 and sodic redissolution. Humic acid gave dark brown solution and fulvic acid
 285 yellow solution. Original solutions ($S_2^i, i = 1 \cdots 11$), were obtained by dilut-
 286 ing 100 μL of the extracted solutions in 3000 μL of 0.1M $NaOH$ buffer. All
 287 chemicals are analytical grade. Eleven twice diluted solutions in 0.1M $NaOH$
 288 buffer ($S_{2D}^i, i = 1 \cdots 11$) were also prepared. Finally, reference solutions with-
 289 out inner filter effect ($S_{2R}^i, i = 1 \cdots 11$) were obtained by 15 times dilutions of
 290 S_{2D}^i .

291 FEEM of S_2^i (I_{2U}^i), S_{2D}^i (I_{2D}^i) and S_{2R}^i (I_{2R}^i) were recorded for $i = 1 \cdots 11$, at
 292 30000 nm/min scan speed from 340 to 650 nm in emission for excitation wave-
 293 length from 240 to 600 nm, by emission and excitation step of 5 nm and with
 294 10 nm bandwidth in excitation and 5 nm bandwidth in emission. Rayleigh
 295 and Raman scatters were consistently corrected [38].

296 I_{2R} and I_{2U} compose the groups of reference and uncorrected FEEM respec-
 297 tively. Using I_{2D}^i in equation 21 with $p = 2$, we could apply CDA to I_{2U}^i and
 298 compute the CDA corrected FEEM (I_{2CDA}^i), $i = 1 \cdots 11$. I_{2CDA} compose the
 299 group of CDA corrected FEEM. Comparison with ACA was not made on this
 300 data set.

301 Hence, three tensors of dimensions $11 \times 73 \times 63$ were obtained and decomposed
 302 by PARAFAC-ALS [39].

303 4 Results and discussion

304 In the following the PARAFAC applications to uncorrected, reference, ACA
 305 corrected and CDA corrected groups of FEEM will be referred as U-PARAFAC,
 306 R-PARAFAC, ACA-PARAFAC and CDA-PARAFAC respectively.

307 4.1 Data set 1

308 Each CDA corrected FEEM ($I_{1CDA}^i, i = 1 \cdots 7$) are firstly compared to I_{1R}^i ,
 309 I_{1U}^i and I_{1ACA}^i . Representative examples of these FEEM are presented on figure
 310 6 for $i = \{1, 3, 4, 6\}$. In these examples, CDA provides satisfying estimations

of the reference FEEM in spite of a small distortion in the fluorescein peak (440/510nm), particularly on I_{1CDA}^1 . In order to quantify these comparisons three relative squared residual error terms (r_{1CDA}^i , r_{1U}^i and r_{1ACA}^i) were computed as follow for each solution i and stored in table 3.

$$r_{1CDA}^i = \frac{\sum_{j,k} (I_{1R}^i(j, k) - I_{1CDA}^i(j, k))^2}{\sum_{i,j} I_{1R}^i(j, k)^2} \quad (24)$$

$$r_{1U}^i = \frac{\sum_{j,k} (I_{1R}^i(j, k) - I_{1U}^i(j, k))^2}{\sum_{j,k} I_{1R}^i(j, k)^2} \quad (25)$$

$$r_{1ACA}^i = \frac{\sum_{j,k} (I_{1R}^i(j, k) - I_{1ACA}^i(j, k))^2}{\sum_{j,k} I_{1R}^i(j, k)^2} \quad (26)$$

The significance of the non linear term in equation (11) increases with the Table 3

Comparison of the relative squared residual error terms(in %) for the seven solution of data set 1.

Solution	1	2	3	4	5	6	7
r_{1U}	117	109	81	46	29	20	13
r_{1ACA}	31	38	59	33	14	7	8
r_{1CDA}	11	5	2	1.8	0.3	0.06	0.03

solution absorbance. Therefore comparing tables 1 and 3, there is an obvious correlation between r_{1U} and the mean absorbances as both values decrease regularly from solutions 1 to 7. The same observation holds true regarding r_{1CDA} . The correlation is less apparent for r_{1ACA} but globally the error is greater for solutions 1 to 4 than for the least absorbing solutions. r_{1U} values are comprised between 13% and 117%. After CDA correction, these boundary values decreased to 0.03% and 11% respectively . These results are very satisfying for solutions 2 to 7. The first solution shows a stronger error but there is still a clear improvement in comparison of the original FEEM. CDA results are always clearly better than ACA ones. Actually, in the more favourable case in respect to ACA results (solution 1), r_{1ACA} is almost 3 times greater than r_{1CDA} .

These results showed that CDA provided a better estimation of I_{1R} than ACA. In order to verify if CDA correction is satisfying for further analysis, the PARAFAC-ALS algorithm was applied to the four groups of FEEM. For each group, the core consistency diagnostic (CORCONDIA) [40] suggested two as the right number of components. Consequently, each PARAFAC decomposition provides an estimation of the quinine sulphate and fluorescein excitation and emission spectra and an estimation of their relative concentrations trough the data set. After normalisation, the relative squared error (r^c , r^{ex} and r^{em}) between the PARAFAC loadings and the real variables are compared on tables 4 to 6. In the case of the spectral loadings, two other spectroscopic criteria are also used: the relative error to the maximum value of the

Fig. 6. Illustrations of I_{IR} , I_{IU} , I_{IACA} and I_{ICDA} for solutions 1, 3, 4 and 6 of data set 1.

spectrum and the shift on the position of the maximum. In addition, load-
ings obtained from U-PARAFAC and CDA-PARAFAC are shown on figures
7 to 9, along with real spectra and profiles. A first global remark should be
made: the perfect agreement on the three modes between the real variables and
R-PARAFAC loadings demonstrates that estimation errors of U-PARAFAC,

344 ACA-PARAFAC and CDA-PARAFAC are mainly due to inner filter effects
 345 and not to the PARAFAC decomposition.

346

Table 4

Data set 1, concentration mode results. Relative squared residual error in percent between the real profiles and their estimation from I_{1R} (r_{1R}^c), I_{1U} (r_{1U}^c), I_{1ACA} (r_{1ACA}^c) and I_{1CDA} (r_{1CDA}^c).

Fluorophore	r_{1R}^c	r_{1U}^c	r_{1ACA}^c	r_{1CDA}^c
Quinine sulphate	0.1	8.3	0.7	0.2
Fluorescein	0.08	23	0.4	4.2

Fig. 7. Data set 1, PARAFAC loadings of the concentration mode: Real spectra (solid * line), U-PARAFAC loadings (dot $\diamond$ line) and CDA-PARAFAC loadings (dash $\triangle$ line)

347 Results for the concentration mode are presented in table 4 and figure 7.
 348 The shape of the concentration profile of the quinine sulphate is slightly af-
 349 fected by filter effects ($r_{1U}^c = 8.3\%$). However CDA-PARAFAC gives much
 350 more accurate results for each solution ($r_{1CDA}^c = 0.2\%$). ACA-PARAFAC is
 351 also satisfying but it is not as efficient as CDA. The concentration profile of
 352 the fluorescein is more distorted ($r_{1U}^c = 23\%$). CDA-PARAFAC performs well
 353 ($r_{1CDA}^c = 4.2\%$) but the relative error is still high for the first solution. It
 354 should be noted that ACA-PARAFAC ($r_{1ACA}^c = 0.4\%$) do better than CDA-
 355 PARAFAC. This last result is surprising because it is in contradiction with
 356 the five other loadings.

357

358 Results for the excitation mode are presented in table 5 and figure 8. The
 359 excitation mode is the most affected by inner filter effects, with r_{1U}^{ex} values of
 360 12.9% and 95.15% for quinine sulphate and fluorescein respectively. Consid-
 361 ering figure 8, quinine sulphate excitation spectrum is widened and flattened
 362 by inner filter effects. These distortions are completely eliminated by CDA-

Table 5

Data set 1, excitation mode results. Comparison with the real spectra among three criteria: relative error on the maximum value (%), shift (nm) and relative squared error (%)

Fluorophore	Criterion	Ref.	Unc.	ACA cor.	CDA cor.
Quinine sulphate	Rel. err. max. val.	0.4	24	23	0.5
	Shift.	0	20	0	0
	r^{ex}	0.06	12.9	4.1	0.08
Fluorescein	Rel. err. max. val.	2.5	50.5	15	17
	Shift	0	20	5	5
	r^{ex}	0.07	95.15	9.3	3.4

Fig. 8. Data set 1, PARAFAC loadings of the excitation mode: Real spectra (solid line), U-PARAFAC loadings (dot line) and CDA-PARAFAC loadings (dash line)

PARAFAC. Indeed, the CDA-PARAFAC estimated spectrum is really close
to the real spectrum ($r_{1CDA}^{ex} = 0.08\%$). ACA-PARAFAC ($r_{1ACA}^{ex} = 4.1\%$) glob-
ally improves U-PARAFAC result ($r_{1U}^{ex} = 12.9\%$). The relative error on the
maximum value is negligible with CDA-PARAFAC (0.5%) while it is impor-
tant with ACA-PARAFAC (23%) as without correction (24%). The 20 nm
shift on the position of the maximum is perfectly corrected by both CDA-
PARAFAC and ACA-PARAFAC. These observations hold true for the fluo-
rescein spectrum but the gaps between the different estimations are wider.
The spectrum estimated by U-PARAFAC is totally distorted in respect to the
real spectrum, $r_{1U}^{ex} = 95.15\%$. In spite of some residual distortions (flattening
and widening), the spectrum shape is almost fully recovered with CDA
correction ($r_{1CDA}^{ex} = 3.4\%$). ACA-PARAFAC global estimation is not as good
($r_{1ACA}^{ex} = 9.3\%$). In absence of correction, the relative error on the maximum
value is very high (50.5%). ACA-PARAFAC and CDA-PARAFAC relative
error are equivalent with 15% and 17% respectively. In the same way the

378 maximum shift is limited by ACA-PARAFAC and CDA-PARAFAC to the
 379 fluorometer excitation step (5 nm) against 20 nm with U-PARAFAC.

Table 6

Data set 1, emission mode results. Comparison with the real spectra among three criteria: relative error on the maximum value (%), shift (nm) and relative squared error (%)

Fluorophore	Criterion	Ref.	Unc.	ACA cor.	CDA cor.
Quinine sulphate	Rel. err. max. val.	1.4	4.1	4.1	0.7
	Shift	0	5	5	0
	r^{em}	0.06	1.8	0.17	0.1
Fluorescein	Rel. err. max. val.	3.9	4	4.7	0.6
	Shift	0	0	15	0
	r^{em}	0.4	7.6	15	0.5

Fig. 9. Data set 1, PARAFAC loadings of the emission mode: Real spectra (solid line), U-PARAFAC loadings (dot line) and CDA-PARAFAC loadings (dash line)

380 Results for emission mode are presented in table 6 and figure 9. The emis-
 381 sion spectrum of quinine sulphate is well estimated by U-PARAFAC ($r_{1U}^{em} =$
 382 1.8%). However ACA-PARAFAC and CDA-PARAFAC still improve this re-
 383 sult in different proportions ($r_{1ACA}^{em} = 0.17\%$ and $r_{1CDA}^{em} = 0.1\%$). One should
 384 note that the relative error on the maximum value is the same with ACA-
 385 PARAFAC than with U-PARAFAC (4.1%). This small error is corrected by
 386 CDA-PARAFAC (0.7%). In the same way, The 5nm shift is only corrected
 387 by CDA-PARAFAC. A closer look should be given to fluorescein spectrum.
 388 This for two reasons: Firstly, CDA-PARAFAC removes the shift of the right
 389 slope and corrects the large distortion on the left slope of the peak (figure 9).
 390 It also creates a weaker distortion on the right slope. This distortion is neg-
 391 ligible but it is very similar to the spectral distortion observed on the CDA
 392 corrected FEEM of solution 1 (figure 6). Secondly, ACA-PARAFAC shows its

393 real limitation on this loading as the estimated spectrum is worse than the one
 394 estimated by U-PARAFAC regarding the three criteria (table 6). The relative
 395 squared error is twice higher (15% against 7.6%) with ACA-PARAFAC than
 396 with U-PARAFAC while it is negligible with CDA-PARAFAC (0.5%). The
 397 relative error on the maximum value is quite small with U-PARAFAC (4%)
 398 and ACA-PARAFAC (4.7%) but it is totally corrected by CDA-PARAFAC
 399 (0.7%). Eventually, ACA-PARAFAC introduces a 15 nm shift on the position
 400 of the maximum which do not exist with U-PARAFAC and CDA-PARAFAC.
 401 In conclusion to this test, as expected, U-PARAFAC provides the worst re-
 402 sults. These are very bad, specially for the fluorescein excitation spectrum and
 403 quinine sulphate emission spectrum whose the wavelength domains strongly
 404 overlap. ACA-PARAFAC improves these results. Regarding ACA results, load-
 405 ings estimation is better than expected. However, it is outperformed by CDA-
 406 PARAFAC at the exception of the fluorescein concentration profile. CDA-
 407 PARAFAC results are indeed closer to those obtained with the reference
 408 FEEM although a larger error is observed on fluorescein excitation (table
 409 5) and concentration loadings (table 6). This must be seen as the PARAFAC
 410 manifestation of the small distortion observed on the CDA correction of so-
 411 lution 1 (figure 6) and more generally this is an indication of the CDA lim-
 412 itations. Actually, CDA is limited to a certain domain of validation because
 413 equation 11 is obtained after several approximations. This holds true for any
 414 correction method relied on equation 11. Regarding the results of table 3 and
 415 figure 7, this limitation has probably been reached with solution 1. In these
 416 cases of very high absorbance (equal or above 2), more sophisticated models
 417 should be used. Nevertheless, we have demonstrated here that the validation
 418 domain of CDA is much larger than the linear one. Then the FEEM provided
 419 by CDA are close enough to the ideal linear FEEM to allow advanced spectral
 420 data analysis such as the PARAFAC decomposition while this is not the case
 421 with uncorrected FEEM or with ACA to a lesser extent. This example also
 422 show that CDA-PARAFAC improves both kinds of PARAFAC results: On the
 423 one hand it allows to recover the overall profile of strongly distorted loadings,
 424 on the other hand it provides some very accurate estimations of less affected
 425 loadings.

426 4.2 Data set 2, application to field

427 In this section, performances of CDA and CDA-PARAFAC are shown for the
 428 correction and the decomposition of mixtures of model molecules. The first
 429 stage of the test is a comparison between the reference FEEM (I_{2R}), the un-
 430 corrected FEEM (I_{2U}) and the CDA corrected FEEM (I_{2CDA}) of data set 2.
 431 Four representative examples of these different FEEM are presented on figure
 432 10. Regarding these examples a main distortion appears on the fluorescence
 433 pattern if no correction is applied. It turns out that filter effects increase the

peak around (480 nm, 520 nm) and decrease the intensity of the fluorescence signal located under 400 nm in excitation. This area is composed by several peaks which are partially recovered by CDA. The PARAFAC decompositions should show whether this finer aspect of the correction is satisfying or not. The relative squared residual error terms (r_{2U} and r_{2CDA}) of the whole data set are given in table 7. FEEM obtained with CDA are not as closed to the reference FEEM as for data set 1. Actually, r_{2CDA} average value is about 4% while it is about 55% for r_{2U} . Hence, it proves that CDA correction is still very beneficial relatively to the uncorrected FEEM.

Table 7

Comparison of the relative squared residual error terms (in %) for the eleven solution of data set 2

Sample	1	2	3	4	5	6	7	8	9	10	11
r_{2U}	51	66	35	59	35	44	83	76	83	10	60
r_{2CDA}	3	3	5	1.4	5	3	4	5	6	5	2

The PARAFAC-ALS algorithm was applied to I_{2R} , I_{2U} and I_{2CDA} . In opposition to set 1, the real number of fluorophore is unknown. This is actually the main problem with PARAFAC analysis of unknown FEEM. We compared the results provided by three classical tests: residual variance analysis, split half analysis and CORCONDIA. Finally, three components were used for the decompositions. These will be labelled fluorophore 1, 2 and 3 in the following. The real fluorophores are also unknown, consequently, R-PARAFAC loadings are taken as references for the evaluation of U-PARAFAC and CDA-PARAFAC results. This comparison is made on tables 8 to 10 and figures 11 to 13.

Table 8

Data set 2, concentration mode results. Relative squared residual error in percent between the reference loadings and U-PARAFAC loadings (r_{2U}^c) or CDA-PARAFAC loadings (r_{2CDA}^c).

Fluorophore	r_{2U}^c	r_{2CDA}^c
1	6.6	5.6
2	26	4
3	7.3	8.2

Results for the concentration mode are presented in table 8 and figure 11. Inner filters and CDA correction have little effects on the profile of fluorophore 1 ($r_{2U}^c = 6.6\%$ and $r_{2CDA}^c = 5.6\%$) and 3 ($r_{2U}^c = 7.3\%$ and $r_{2CDA}^c = 8.2\%$). On the opposite, fluorophore 2 is far more affected. The concentration profile estimated by U-PARAFAC is clearly unsatisfying ($r_{2U}^c = 26\%$). CDA-PARAFAC provides an acceptable estimation as the error term decreases to 4 % . Finally

Fig. 10. Illustrations of I_{2R} , I_{2U} and I_{2CDA} for samples 1, 4, 6 and 9 of data set 2.

the three estimated profiles by CDA-PARAFAC are satisfying at the exception of sample 8 and 9. At the opposite of r_{2U}^c , r_{2CDA}^c is greater for fluorophores 1 and 3. This is mainly due to the larger estimation errors on samples 8 and 9.

Results for excitation mode are presented in table 9 and figure 12. Excitation mode is the most affected mode of the decomposition as for data set 1. Estimation of fluorophore 1 excitation spectrum takes a clear advantage of

Fig. 11. Data set 2, PARAFAC loadings of the concentration mode: R-PARAFAC loadings (solid * line), U-PARAFAC loadings (dot $\diamond$ line) and CDA-PARAFAC loadings (dash $\triangle$ line)

Table 9

Data set 2, excitation mode results. Comparison with the reference loadings among three criteria: relative error on the maximum value (%), shift (nm) and relative squared error (%)

Fluorophore	Test	Unc.	CDA cor.
1	Rel. err. max. val.	18	11
	Shift	185	15
	r^{ex}	110	1.5
2	Rel. err. max. val.	30	20
	Shift	20	0
	r^{ex}	9.6	2.1
3	Rel. err. max. val.	27.5	0.2
	Shift	10	5
	r^{ex}	35	0.6

468 CDA-PARAFAC. Regarding shape and position, the spectrum estimated by
469 U-PARAFAC is a far cry from the reference spectrum ($r_{2U}^{ex} = 110\%$). On the
470 opposite, CDA-PARAFAC provides a very good estimation ($r_{2CDA}^{ex} = 1.5\%$).
471 The relative error on the maximum value is smaller (11 % against 18 %)
472 but above all, the large shift (185 nm) is brought back to 15 nm. Despite U-
473 PARAFAC estimation of fluorophore 2 spectrum is acceptable ($r_{2U}^{ex} = 9.6\%$),
474 CDA-PARAFAC improves this result ($r_{2CDA}^{ex} = 2.1\%$). In absence of correc-
475 tion, the double peak disappears. CDA-PARAFAC correctly restores this fea-
476 ture but the relative error on the maximum value remains high (20%). On
477 the other hand, the 20 nm shift is completely corrected. U-PARAFAC estima-

Fig. 12. Data set 2, PARAFAC loadings of the excitation mode: R-PARAFAC loadings (solid line), U-PARAFAC loadings (dot line) and CDA-PARAFAC loadings (dash line)

tion of fluorophore 3 spectrum is not satisfying ($r_{2U}^{ex} = 35\%$). One of the two peaks almost disappears while the second one is overestimated. Nevertheless, its estimation by CDA-PARAFAC is almost identical to the reference spectrum ($r_{2CDA}^{ex} = 0.6\%$). The relative error on the maximum value is significant with U-PARAFAC (27.5%) but it becomes negligible with CDA-PARAFAC (0.2%). The shift is also reduced from 10 nm to 5 nm.

Table 10

Data set 2, emission mode results. Comparison with the real spectra among Comparison with the reference loadings among three criteria: relative error on the maximum value (%), shift (nm) and relative squared error (%)

Fluorophore	Test	Orig.	Corr.Dil.
1	Rel. err. max. val.	13	12
	Shift	40	25
	r^{em}	21	4
2	Rel. err. max. val.	21	1.8
	Shift	60	10
	r^{em}	63	6
3	Rel. err. max. val.	5.2	1.4
	Shift	20	10
	r^{em}	8.8	0.9

Results for emission mode are presented in table 10 and figure 13. Estimation of fluorophore 1 emission spectrum by U-PARAFAC is mitigated ($r_{2U}^{em} = 21\%$). CDA-PARAFAC overall result is very acceptable ($r_{2CDA}^{em} = 4\%$). The spectrum is overestimated by both U-PARAFAC (relative error to the maximum

Fig. 13. Data set 2, PARAFAC loadings of the emission mode: R-PARAFAC loadings (solid line), U-PARAFAC loadings (dot line) and CDA-PARAFAC loadings (dash line)

value of 13%) and CDA-PARAFAC (12%). On the opposite, CDA-PARAFAC limits to 25 nm the large shift (40 nm) observed when no correction is applied. Fluorophore 2 spectrum is more severely affected by inner filter effects. CDA-PARAFAC provides a very satisfying estimation of this spectrum ($r_{2CDA}^{em} = 6\%$) in respect to U-PARAFAC result ($r_{2U}^{em} = 63\%$). The relative error to the maximum value observed with U-PARAFAC is important (21%) but it is well corrected by CDA-PARAFAC (1.8%). In the same way, the 60 nm shift is limited to 10 nm. Fluorophore 3 spectrum is correctly estimated by U-PARAFAC ($r_{2U}^{em} = 8.8\%$). CDA-PARAFAC still improves the estimation ($r_{2CDA}^{em} = 0.9\%$). The relative error to the maximum value is lower (1.4% against 5.2%) and the shift is reduced from 20 nm to 10 nm.

CDA-PARAFAC results on data set 2 are also conclusive. All the loading are indeed correctly estimated. Relative concentrations of only one fluorophore in only two samples out of eleven are poorly estimated and all the estimated spectra are close enough to the corresponding reference spectra. The crucial point on this second example is that in a real case situation of DOM tracing, CDA-PARAFAC would probably give interpretative results while the uncorrected FEEM would provide misleading estimations. Moreover, excitation spectra of fluorophores 1 and 3 illustrate the two main kinds of spectral deviations due to inner filters. Fluorophore 1 shape is distorted and its position is shifted from 275 nm to 480 nm. On the opposite, the position of fluorophore 3 is unchanged, its global shape is almost correct but the respective magnitude of its two peaks is largely modified. CDA-PARAFAC provides an impressive correction of both deviations.

Actually, CDA-PARAFAC appears to be a critical improvement of U-PARAFAC or even ACA-PARAFAC in the case of strong inner filter effects.

514 5 Conclusion

515 It is possible to correct inner filter effects by using simply a controlled dilution
516 approach (CDA). This analytical solution is better than usual absorbance cor-
517 rection and quicker and safer than strong dilution, under absorbance of 0.3.
518 It has been demonstrated in this work the good ability of CDA and CDA-
519 PARAFAC in the case of standard mixtures of two fluorophores and in the
520 case of real DOM samples. In this study, CDA performed very well for solu-
521 tion absorbances up to 1.83. Further investigation should be made outside this
522 range. We conjecture that an other theoretical model of fluorescence measure-
523 ment should be used for absorbance higher than 2.
524 In respect to the PARAFAC decomposition, better results were obtained on
525 the spectral loadings. We have also highlighted the limit of ACA for the cor-
526 rection of strong filter effects. Consequently, we recommend the use of CDA
527 for FEEM experiment and PARAFAC pretreatment to avoid error and misin-
528 terpretation.

529 References

- 530 [1] B. Valeur, Molecular Fluorescence. Principles and Applications, Wiley-VCH,
531 Weinheim, 2002.
- 532 [2] A. Hansch, D. Sauner, I. Hilger, J. Böttcher, A. Malich, O. Frey, R. Bräuer and
533 W.A. Kaiser, Academic Radiology, 11 (11) (2004) 1229-1236.
- 534 [3] E. Sikorska, T. Gorecki, I.V. Khmelinskii, Sikorski and D. de Keukeleire, Food
535 chemistry, 96 (4) (2006) 632-639.
- 536 [4] G.P., Coble, Marine Chemistry, 51 (1996), 325-346.
- 537 [5] C.A. Stedmon, S. Markager, Limnology and Oceanography, 50 (2) (2005).
- 538 [6] J.R., Lakowicz, Principles of Fluorescence Spectroscopy, Plenum Press, NY,
539 1983.
- 540 [7] C.A. Parker, W.J. Barnes, The analyst, 82 (1957) 606-618.
- 541 [8] J.J. Mobed, S.L. Hemmingsen, J.L. Autry, and L.B. McGown, Environmental
542 Science and Technology, 30 (10) (1996) 3061-3065.
- 543 [9] J.F. Holland, R.E. Teets, P.M. Kelly and A. Timnick, Analytical Chemistry, 49
544 (6) (1977) 706-710.
- 545 [10] C. M. Yappert and J.D. Ingle, Applied Spectroscopy, 43 (5) (1989) 759-767.
- 546 [11] S.A. Tucker, V.L.Amszi, W.E. Acree, Journal of Chemical Education, 69 (1992).

- 547 [12] B.C. MacDonald, S.J.Lvin and H. Patterson, *Analytica Chimica Acta*, 338
548 (1997) 155-162.
- 549 [13] A. Credi, and L. Prodi, *Spectrochimica Acta Part A*, 54 (1998) 159-170.
- 550 [14] J. Riesz, J. Gilmore, P. Meredith, *Spectrochimica Acta part A* (2004).
- 551 [15] T. Ohno, *Environmental Science and Technology*, 36 (4) (2002) 742-746.
- 552 [16] D.M. MacKnight, E.W Boyer, P.K. Westerhoff, P.T. Doran, T. Kulbe and D.T.
553 Andersen, *Limnology and Oceanography*, 46 (2001) 38-48.
- 554 [17] F. Cuesta Sanchez, S. Rutan, M. Gil Garcia and D. Massart, *Chemometrics
555 and Intelligent Laboratory Systems*, 36 (1997) 153-164.
- 556 [18] A. Garrido Frenich, D. Picon Zamora, J. Martinez Vidal and M. Martinez
557 Galera, *Analytica Chimica Acta*, 449 (2001) 143-155.
- 558 [19] J. Boehme, P. Coble, R. Conmy and A. Stovall-Leonard, *Marine Chemistry*, 89
559 (2004) 3-14.
- 560 [20] J.M. Andrade, M.P. Gomez-Carracedo, W. Krzanowsky and M. Kubista,
561 *Chemometrics and Intelligent Laboratory Systems*, 72 (2004) 123-132.
- 562 [21] R.A. Harshman, *UCLA Working Papers in Phonetics*, 16 (1970) 1-84 (UMI
563 *Serials in Microform*, No. 10,085).
- 564 [22] R. Bro, *Chemometrics and Intelligent Laboratory Systems*, 38 (1997) 149-171.
- 565 [23] C.A. Stedmon, S. Markager and R. Bro, *Marine Chemistry*, 82 (3-4) (2003)
566 239-254.
- 567 [24] R.D. Holbrook, J.H. Yen and T.J. Grizzard, *Science of The Total Environment*,
568 361 (1-3) (2006) 249-266.
- 569 [25] X. Luciani, S. Mounier, H.H.M. Paraquetti, R. Redon, Y. Lucas, A. Bois, L.D.
570 Lacerda, M. Raynaud and M. Ripert, *Marine Environmental Research*, 65 (2)
571 (2008) 148-157.
- 572 [26] D. Baunsgaard, Department of Dairy and Food Science, The Royal Veterinary
573 and Agricultural University, (1999).
- 574 [27] G.G. Anderson, K.D. Brian and K.S. Booksh, *Chemometrics and Intelligent
575 Laboratory Systems*, 49 (1999) 195-213.
- 576 [28] O. Divya and A.K. Mishra, *Analytica Chimica Acta*, 630 (2008) 47-56.
- 577 [29] P. John, I. Soutar, *Analytical Chemistry*, 48 (1976) 520-524.
- 578 [30] D. Patra and A.K. Mishra, *Analyst*, 125 (2000) 1383-1386
- 579 [31] R.A. Harshman, *UCLA Working Papers in Phonetics*, 22 (1972) 111-117 (UMI
580 *Serials in Microform*, No. 10,085).
- 581 [32] N.D. Sidiropoulos and R. Bro, *Journal of Chemometrics*, 14 (3) (2000) 229-239.

- 582 [33] N.M. Faber, R. Bro and P.K. Hopke, Chemometrics and Intelligent Laboratory
583 Systems, 65 (2003) 119-137.
- 584 [34] G. Tomasi, R. Bro, Computational Statistics & Data Analysis, 50 (7) (2006)
585 1700-1734.
- 586 [35] P. Paatero, Chemometrics and Intelligent Laboratory Systems, 38 (2) (1997)
587 223-242.
- 588 [36] R.A. Harshman and M.E. Lundy, Computational Statistics & Data Analysis,
589 18 (1994) 39-72.
- 590 [37] C. Andersen, R. Bro, Journal of Chemometrics, 17 (2003) 200-215.
- 591 [38] R.G. Zepp, W.M. Sheldon and M.A. Moran, Marine Chemistry, 89 (2004) 15-36.
- 592 [39] C.A. Andersson and R. Bro, Chemometrics and Intelligent Laboratory Systems,
593 52 (2002) 1-4.
- 594 [40] R. Bro and H.A.L. Kiers, Journal of Chemometrics, 17 (2003) 274-286.