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Rare earth element sorption onto hydrous manganese oxide

A modeling study

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Keywords: rare earth element, manganese oxyhydroxides, surface complexation modeling.

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Abstract

Manganese oxides are important scavengers of rare earth elements (REE) in hydrosystems. However, it has been difficult to include Mn oxides in speciation models due to the lack of a comprehensive set of sorption reactions consistent with a given surface complexation model (SCM), as well as discrepancies between published sorption data and predictions using the available models. Surface complexation reactions for hydrous Mn oxide were described using a two surface site model and the diffuse double layer SCM. The specific surface area, surface side density and pH$_{zpc}$ were fixed to 746 m$^2$/g, 2.1 mmol/g and 2.2, respectively. Two site types (≡XOH and ≡YOH) were also used with pK$_{a2}$ values of 2.35 (≡XOH) and 6.06 (≡YOH). The fraction of the high affinity sites was fixed at 0.36. Published REE sorption data were subsequently used to determine the equilibrium surface complexation constants, while considering the influence of pH, ionic strength and metal loading. Log K increases from light REE to heavy REE and, more specifically, displays a convex tetrad effect. At low metal loading, the ≡YOH site type strongly expresses its affinity towards REE whereas at higher metal loading, the same is true for the ≡XOH site type. This study thus provides evidence for heterogeneity in the distribution of the Mn oxide binding sites among REE.

Keywords: lanthanide, manganese oxides, surface complexation modeling, PHREEQC, PhreePlot

1. Introduction

The distributions of rare earth elements (REE) in natural waters have been intensively investigated for more than forty years [1, 2]. The absolute and relative concentrations of 14 stable REE have been determined in a variety of open ocean
environments [3], estuaries [4], rivers [5], lakes [6], groundwaters [7], and hydrothermal fluids [8]. Although the complexation of hydrated trivalent REE with various inorganic anions (carbonate, hydroxide, sulfate, fluoride and chloride) has been intensively studied [9], REE partitioning and fractionation between solution and relevant mineral surfaces is much less understood. To date, few studies have been dedicated to REE sorption onto mineral surfaces [10-15] and the most frequently used solids were Fe-oxyhydroxides [10, 11, 13-15]. REE sorption by amorphous ferric hydroxide was measured over a pH range of 3.5 to 9.0 and over a large ionic strength (IS) range. For a constant pH and individual REE, the magnitude of the estimated distribution coefficients differs by a factor of around 400. Although Mn-oxyhydroxides are as ubiquitous as Fe-oxyhydroxides and present high surface areas and a strong affinity for many elements [16], fewer studies have focused on REE adsorption by Mn-oxyhydroxides [10, 13, 17-19]. However, several studies have demonstrated that Mn-oxyhydroxides partly controlled REE fractionation and mobility in natural water. Thereby, they provided evidence that a negative Ce anomaly in solution is developed through the oxidation/scavenging of Ce(III) onto the MnO₂ surface [10, 17, 19]. REE scavenging by ferromanganese nodules was also identified as a major process in controlling REE fractionation in seawater [8, 20, 21]. The lack of data for REE binding by Mn-oxyhydroxides may be attributed to the high variety of Mn-oxyhydroxide minerals and the heterogeneity of the published surface properties which complicate modeling studies. However, in order to accurately describe REE behavior, it is essential that REE binding to Mn-oxyhydroxides is quantitatively modeled. Many surface complexation models have been established to study and quantify cation sorption onto mineral surfaces. Each of them has their own solid–solution interface description, model parameters and set of thermodynamic data.
and many provide satisfactory fits to experimental data (e.g., [22]). Partially as a result of this model flexibility, ion sorption data on Mn-oxyhydroxides have been fit using a number of different surface complexation models (e.g. SCM). Thereby, a triple-layer SCM was used to evaluate and predict the surface complexation constants for hydrous manganese oxide (HMO) [23]. A variation on the constant capacitance model [24] was included in SCAMP to determine the model parameters for sorption on Mn oxyhydroxides [25]. Crystallographic data were used as the basis for a new surface complexation model formulation [26]. More recently, Tonkin et al. [16] provided consistent surface complexation constants for several cations for a generic HMO and a diffuse double layer SCM for a system in which HMO is an important scavenger.

In this study, a quantitative SCM model for REE sorption by HMO at low substrate loadings (from 1.6 to 100 mg/L) was proposed using the generic HMO surface parameters provided by Tonkin et al. [16]. The REE-HMO binding constant was extrapolated using the linear free energy relationship (LFER) methodology and by fitting experimental datasets with the PhreePlot program [27]. Published experimental data cover an ionic strength range from 0 to 0.7 mol/L and a relatively wide pH range from 4 to 9 [10]. This model was further used to discuss the nature and importance of REE sorption by manganese oxyhydroxides in the open ocean.

2 Materials and methods

2.1 Surface complexation model description

The diffuse double layer SCM describes the sorption of solutes onto oxide
surfaces. This model is the central component of the generalized two-layer model used to compile the database of surface reactions for hydrous Fe(III) oxide (HFO) provided by Dzombak and Morel [28]. In this work, the SCM was chosen because of its relative simplicity and its success in describing cation sorption to HMO [16]. Surface equilibrium reactions are written as combination sorption reactions (Eq. 1 to 6) to specific hydroxyl sites on the oxide surface, to which a coulombic term that represents the electrochemical work of sorption is added. This coulombic term is calculated from the Gouy–Chapman electrical double layer theory and is included in the apparent equilibrium constants used by the model, \( P = \exp(-F\psi/RT) \), where \( F \) is the Faraday constant, \( \psi \) is the electrostatic potential, \( r \) is the gas constant and \( T \) is the absolute temperature.

\[
\begin{align*}
\equiv X - \text{OH} & \Leftrightarrow X - \text{O}^- + \text{H}^+ & K_{a_{2X\text{--OH}}} & (1) \\
\equiv Y - \text{OH} & \Leftrightarrow Y - \text{O}^- + \text{H}^+ & K_{a_{2Y\text{--OH}}} & (2) \\
\equiv X - \text{OH} + M^{n+} & \Leftrightarrow X - \text{OM}^{(n-1)+} + \text{H}^+ & K_{X\text{--OM}} & (3) \\
\equiv X - \text{OH} + M^{n+} + \text{H}_2\text{O} & \Leftrightarrow X - \text{OMOH}^{(n-2)+} + 2\text{H}^+ & K_{X\text{--OMOH}} & (4) \\
\equiv Y - \text{OH} + M^{n+} & \Leftrightarrow Y - \text{OM}^{(n-1)+} + \text{H}^+ & K_{Y\text{--OM}} & (5) \\
\equiv Y - \text{OH} + M^{n+} + \text{H}_2\text{O} & \Leftrightarrow Y - \text{OMOH}^{(n-2)+} + 2\text{H}^+ & K_{Y\text{--OMOH}} & (6)
\end{align*}
\]

The HMO surface properties (specific surface area (SSA), surface site density, and acidity constants), REE-HMO stability constants and concentration of a non-specifically adsorbing electrolyte solution are required. Data for HMO were obtained from Tonkin et al. [16] (Table 1). The SSA value input to the model fixed at 746 m\(^2\)/g is calculated and is therefore higher than the values determined by the BET-N\(_2\) method, which range from 0.048 to 359 m\(^2\)/g [29]. The total HMO concentration of the surface sites (mol/g) was divided into fractions for the two site types (\(\equiv X\text{OH} \) and \(\equiv Y\text{OH} \)), which present high and low affinity for REE binding, respectively. REE sorption onto HMO is therefore simulated assuming that two types of sites are
available on the oxide surface (Table 1). Modeling calculations were performed with PHREEQC and PhreePlot [27, 30]. Three keyword data blocks are required to define the surface-complexation data for a simulation: (i) SURFACE_MASTER_SPECIES, (ii) SURFACE_SPECIES, and (iii) SURFACE. The SURFACE_MASTER_SPECIES data block defines a binding site, named “Hmo” (HMO; [16]), with two binding sites, “Hmo_w” and “Hmo_s”, for the “weak” and “strong” binding sites. Inorganic speciation was then performed; the Nagra/PSI database [31] was used and updated including the same well-accepted stability constants at infinite dilution (25°C) for the REE inorganic complexes (hydroxide, sulfate and carbonate; [32-34]. As Bau and Koschinsky [35] proposed, Ce(III) is oxidized after its sorption onto oxyhydroxide and therefore only REE(III) were considered in the proposed SCM.

2.2 REE-HMO sorption stability constants

2.2.1. Extrapolation of the linear free energy relationship

The linear free energy relationship (LFER) or the correlation between the first hydrolysis constant for aqueous species and the corresponding surface complexation constant was used to estimate the sorption stability constant as has been previously done in numerous studies [16, 28, 36, 37]. The LFER can be used to extend results from a limited dataset to other metals. The REE-HMO stability constants were estimated by the same extrapolation method used by Tonkin et al. [16]. These authors observed that a LFER exists for HMO between \( \text{log } K_{\equiv XOMe} \), \( \text{log } K_{\equiv XOMeOH} \), \( \text{log } K_{\equiv YOMe} \) and \( \text{log } K_{\equiv YOMeOH} \) and the first hydrolysis (OH) constant for the metals (\( \text{log } K_{\text{MeOH}} \)).
However, Tonkin et al. [16] caution against assuming a LFER for all metals on HMO, notably with regards to the possible oxidation/scavenging mechanisms on the HMO surface. The estimated stability constant of REE binding to HMO is reported in Table 2. The first hydrolysis constant of REE, log $K_{\text{REE-OH}}$, is taken from the NIST database [38]. The REE-HMO stability constants extrapolated from the LFER methodology are listed in Table 3 with the REE-OH stability constant used for the calculation.

2.2.2. PhreePlot modeling

The pKa, $\alpha$ values and published REE sorption data [10] were subsequently used to determine the equilibrium surface complexation constants for the whole REE series ([REE] = 125 µg/L; [HMO=δ-MnO$_2$] = 10 mg/L; room temperature; IS fixed with NaNO$_3$; no control of the CO$_2$ species). They were modeled using the computer program PhreePlot [27] and the Nagra/PSI database [31], which was modified to include the well-accepted infinite dilution (at 25°C) of inorganic species [32, 33]. Intrinsic constants for the surface complexation model were optimized by Powell’s non-linear least squares method using PhreePlot’s fitting options. The REE-HMO stability constants are listed in Table 4. Only log $K_{\text{XOMe}}$ and log $K_{\text{YOMe}}$ were further considered because log $K_{\text{XOMeOH}}$ and log $K_{\text{YOMeOH}}$ are low and thus negligible.

3. Results and discussion

The speciation calculations presented below were performed using a diffuse double layer SCM in the PhreePlot program with the LFER extrapolated and PhreePlot fitted REE-HMO stability constants. The database was modified to
integrate the extrapolated and fitted REE-HMO stability constant, as well as the
infinite dilution (25°C) stability constants for the REE inorganic (chloride and
carbonate) complexes [32, 33]. To test the validity of the extrapolated and fitted REE-
HMO stability constant and the diffused double layer SCM, the modeling calculations
were compared to the REE-HMO sorption experimental datasets [10, 13, 18, 19].

3.1. REE-HMO modeling with extrapolated stability constant

3.1.1. LFER extrapolated stability constant

The dataset for the extrapolated REE-HMO stability constants was
subsequently used to calculate the distribution of La under various experimental
conditions [10, 13, 18]. The comparison between the experimental and calculated data
provide evidence that the dataset for the extrapolated REE-HMO stability constants
cannot be used to reproduce the experimental distribution of REE onto HMO
regardless of the pH, IS (Figure 1; pH ranging from 4.0 to 9.5 and IS varying from
0.001 to 0.7 mol/L) and metal loading ([REE] varying from 5 µg/L to 0.2 mg/L and
[HMO=δ-MnO₂] ranging from 3.2 mg/L to 100 mg/L). The calculated proportion of
bound REE is strongly underestimated. Therefore, the datasets for the extrapolated
constants were not used hereafter.

3.1.2. PhreePlot fitted stability constants

The fitted stability constants were subsequently used to calculate the
distribution of La, Eu and Lu under De Carlo et al.’s [10] experimental conditions.
Figure 2 compares the experimental and calculated datasets. The model reproduces reasonably well the increasing light REE (LREE; illustrated by La) binding onto HMO with pH and IS. However, for heavy REE (HREE; illustrated by Lu), although the model predicts a decreasing binding strength, the experimental data show that 100% of REE are sorbed onto HMO. In Table 5, the rmse (root mean square errors) are reported between the experimental and modeling data for the three REE and IS conditions. The important rmse values for Eu and Lu at IS= 0.7 were expected with regards to the irregularity observed in the experimental dataset [10]. Moreover, Figure 2 shows that the discrepancy between the experimental and calculated data also increases with pH, IS and the REE atomic number. Lee and Byrne [39] demonstrated that REE binding by carbonate in solution increases with the REE atomic numbers. The most important difference observed for the heavy REE (HREE) therefore indicates that the model predicts larger concentrations of HREE bound to carbonate than in the experimental conditions.

### 3.2. PhreePlot modeling

#### 3.2.1. pH dependence

Figure 2 also compares the experimental and calculated datasets. The model reproduces reasonably well the increasing LREE binding onto HMO with pH and IS. However, the model predicts a decreasing binding strength at an alkaline pH for HREE. As already shown by De Carlo et al. [10], a large extent of the variability in the sorption efficiency is observed at low pH with the IS. This is generally evidenced by a shift in the adsorption edges towards an alkaline pH and reduced REE sorption with increasing IS, especially at an acidic pH. The differences appear more pronounced for LREE than HREE.
3.2.2. REE patterns

The REE distribution between suspended HMO (at an IS of 0.5 mol/L) over the pH range from 4.79 to 6.80 [13] was further modeled using the previously described SCM procedure. The calculated REE patterns onto HMO are shown in Figure 3a. The patterns exhibit extremely large positive Ce anomalies and a convex tetrad effect (well developed for the first two tetrads). These two features were already apparent in the experimental datasets of De Carlo et al. [10] and Ohta and Kawabe [13]. The same features occur for Davranche et al.’s [18] dataset: the REE patterns exhibit large positive Ce anomalies (Fig. 3b), as well as convex tetrad curves. However, they are less developed. This discrepancy might be explained by the rather different experimental conditions used in Davranche et al. [18] as compared to those used in De Carlo et al. [10] from which the constants are derived.

Among these results, an interesting feature is that the modeling approach reproduces the strongly enhanced adsorption of Ce from acidic solution by HMO, relative to the other REE. The adsorption edge in the HMO suspension is therefore below pH 4 for Ce, whereas for strictly trivalent REE, it occurs near neutral pH. It should be noted that at ambient conditions and in the absence of strong ligands, tetravalent Ce is only stable in solid phase [40], or when it is derived from the oxidation/scavenging of Ce(III) onto the metal oxyhydroxide surface [35]. Thus, the Ce-HMO constant calculated in this study is a conditional constant which considers the global oxidation-scavenging of the Ce(III, IV) mechanism onto the HMO surface.

3.2.3. Model validity and application
In order to check the validity of the model, calculations were performed with data from the literature [13, 18]. Irrespective of the pH, IS (Figure 1; pH ranging from 4.0 to 9.5 and IS varying from 0.001 to 0.7 mol/L) and metal loadings ([REE] varying from 5 µg/L to 0.2 mg/L and [HMO=\delta-MnO_2] ranging from 3.2 mg/L to 100 mg/L), the modeling is in agreement with the experimental results. In further detail, data from Ohta and Kawabe [13] for a high IS (i.e., 0.5 mol/L) are well reproduced, as was observed in De Carlo et al.’s [10] experimental conditions. However, data from Davranche et al. [18] for the lowest IS (i.e., 0.001 mol/L) are not well reproduced. The main differences between these experimental conditions, apart from the IS, are that different metal loadings are tested (i.e., 0.875 for Ohta and Kawabe [13]; 0.175 for De Carlo et al. [10]; 0.0007 for Davranche et al. [18, 19]).

Unlike the various experimental conditions, differences between the experimental observations and modeling are probably due to the generic parameters chosen to represent the Mn-oxyhydroxides. In fact, there are different Mn-oxyhydroxide varieties and their properties are highly variable [29, 41]. As an example, pH_{zpc} values for HMO can vary from 2 to 9.6 [29]. Ohta and Kawabe [13] and De Carlo et al. [10] consider vernadite with a pH_{zpc} of 2.25 [42], whereas Davranche et al. [18] consider pyrolusite with a pH_{zpc} of 5.8.

Apart from these discrepancies, a faithful reproduction of the data from the literature constitutes an even better test of model's ability. While the conditional nature (IS, pH and metal loading) of the determined stability constants would render such an exercise rather meaningless for a single element, the unique attributes of the REE series can be used to examine whole log K patterns. The REE pattern shape (i.e., REE fractionation) is governed by the chemical properties of the REE and does not depend
on the sorbent properties, which depend on its synthesis method which controls, for example, its crystallinity and specific surface area. [43]

This type of SCM development can be used to improve the understanding of REE fractionation in seawater. Indeed, the experimental conditions are closed to those of marine system. Moreover, an interesting feature is that modeling approach can reproduce the high adsorption of Ce relative to the other REE under acidic conditions. This behavior is also observed in seawater when dissolved REE are scavenged by $\delta$-MnO$_2$ [10]. The Ce anomaly is recognized as one of the fundamental features of lanthanide geochemistry due to its redox sensitivity [44]. Cerium is a prime proxy for ocean–atmosphere evolution over geological timescales [45]. The contribution of oxidative scavenging toward the removal of Ce from solution is most pronounced at acidic pH, where the strictly trivalent REE exhibit little propensity for sorption onto $\delta$-MnO$_2$. It has been suggested that the behavior of REE and Ce in the marine environment is more closely coupled to that of Mn than to that of Fe due to the oxidative scavenging of Ce by Mn-oxyhydroxides [44].

4 Concluding remarks

Surface complexation modeling was used to test REE sorption onto HMO by considering LFER to determine log K. However, this methodology does not allow experimental data to be reproduced. Therefore, these experimental data were further used to extrapolate equilibrium surface complexation constants by fitting them for a large dataset [10]. The determined constants can reproduce pH dependence and REE fractionation over a wide variety of conditions (i.e., pH ranging from 4.0 to 9.5, IS varying from 0.001 to 0.7 mol/L, [REE] varying from 5 µg/L to 0.2 mg/L and
[HMO=δ-MnO₂] ranging from 3.2 mg/L to 100 mg/L). SCM development of this type can be used to improve the understanding of REE fractionation in seawater. However, these results emphasize the relevance of conducting further experiments and modeling for a better understanding of natural systems and have considerable implications for the assessment of REE mobility.

Acknowledgments

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Tables and Figures Captions

Table 1 SCM parameters for HMO [16].

Table 2 Stability constants used for the LFER established by Tonkin et al. [16].

Table 3 REE-HMO stability constants extrapolated from the LFER established by
Tonkin et al. [16].

Table 4 REE-HMO stability constants fitted with PhreePlot from De Carlo et al.'s

Table 5 Rmse (root mean square error) calculated between the experimental datasets
[10] and the datasets calculated from the REE-HMO fitted stability constant.

Figure 1 Proportion of La sorbed to HMO as a function of pH. The dots correspond
to experimental data from the literature and the solid line represents modeled data
using extrapolated constants obtained from LFER (a) (b) (c) De Carlo et al. [10]; (d)
Ohta and Kawabe [13]; (e) Davranche et al. [18].

Figure 2 A comparison between the experimental and calculated proportion of La, Eu
and Lu bound to HMO using the fitted REE-HMO stability constants under the
experimental condition's provided by De Carlo et al. [10]. The dots correspond to the
displayed experimental data and the solid line corresponds to the calculated data.

Figure 3 Modeled vs. experiments REE patterns showing Ce/Ce* for the
experimental conditions described in (a) Fig. 2 in Ohta and Kawabe [13], and (b) Fig.
4 in Davranche et al. [19] and Fig. 6 in Davranche et al. [18].
Figure 2
Figure 3
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Table 4

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References


