Multi-Level Modeling of Quotation Families
Morphogenesis
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Abstract—This paper investigates cultural dynamics in social media by examining the proliferation and diversification of clearly-cut pieces of content: quoted texts. In line with the pioneering work of Leskovec et al. [1] and Simmons et al. [2] on meme dynamics we investigate in deep the transformations that quotations published online undergo during their diffusion. We deliberately put aside the structure of the social network as well as the dynamical patterns pertaining to the diffusion process to focus on the way quotations are changed, how often they are modified and to what extent these changes shape diverse families and sub-families of quotations. Following a biological metaphor, we try to understand in which way mutations can transform quotations at different scales and how mutation rates depend on various properties of the quotations.

I. INTRODUCTION

“Memeticists”, whose forefather Richard Dawkins [3] was the first to coin the term *meme* in 1976 in analogy to gene, defend the thesis that culture is subjected to evolutionary processes in the same way that living beings are. This trend of research has suffered strong oppositions especially from ethnographers and anthropologists [4] criticizing in particular the assumption that culture could be divided into individual objects called cultural entities [5], and more generally the lack of empirical validation [6]. Social media offer at last this opportunity for studying social and cultural dynamics *in-vivo*. In this paper, we claim that tracking the transformations of quotations in the blogosphere is a good way to tackle such empirical endeavour. If quotations admittedly cannot catch the complex properties found in every cultural traits, their atomic structure is, by nature, an opportunity that should be seized to put the memetic program, at least partially, into practice.

We are then interested in the diffusion of quotations which builds on the notion of “intertextuality”, frequently used in political discourse studies. Intertextuality refers to the fact that fragments of discourse are repeated, re-used and progressively modified in different ways. It is thus possible to track the stability or the progressive distortion of an utterance over time. Following Kristeva [7], we assume that these distortions are not neutral and reflect the way ideas diffuse in different communities.

Diffusion studies have attracted much interest from pioneering sociological approaches [8] to more contemporary studies observing diffusion dynamics in online media. Whatever the nature of the diffusive entity: drugs [9], books recommendations [10], citations [11], or URLs [12], the process at stake in each of these studies assumes that objects are perfectly replicated, their stability being a necessary condition for studying their diffusion. Like the previously mentioned objects, quotations can be tracked because whatever their changes they still refer to the same singular external event. But contrarily to them, quotations can undergo transformations, opening the way to the systematic quantitative analysis of regular patterns underlying these changes.

When it comes to characterizing changes that can affect quotations, it may be useful to follow the biological metaphor provided by memetics. A sequence of genes can be altered by mutations which may affect only one nucleotide or a large sequence of nucleotides. Small-scale mutations encompass point mutations (substitute a single nucleotide with another), deletions and insertions. We claim that such an ontology distinguishing between small-scale and large-scale changes is fruitful for addressing quotation transformation dynamics. We then introduce a different typology than the one described by Simmons et al. in their analysis of the same dataset. In [2] authors discriminate between “reframing” and “alteration” events: if a phrase is transformed into a superstring or substring, then reframing takes place, otherwise one should talk about alteration. The relation of inclusion between two quotations then defines the type of transformation. We prefer to use a different typology directly inspired from the biological mutation process. We will then simply consider on the one hand micro-mutations affecting only one word whatever the type of transformation (i.e. a word can be added, deleted or even replaced by another one) and on the other hand macro-mutations affecting more deeply the composition of phrases. Intuitively small-scale and large-scale mutation events stand for different underlying cognitive processes. Micro-mutations are small changes in the original quotation which can be introduced voluntarily or simply by error with no special intention to alter the original meaning of the replicated quote.
In the other case, macro-mutations are more probably due to voluntary changes by bloggers or journalists that only want to stress the attention of readers toward a subpart of the original quoted text.

Our goal will then be to describe how micro-scale and macro-scale mutations progressively transform quotations during their diffusion. The first part of the article will be devoted to a very short description of our empirical dataset. An original algorithm for detecting coherent families of quotations is then introduced. Based on these families, we will then introduce stability and diversity indexes which help us describing the transformation process at different levels (words, quotes and families). In the last part we will empirically measure mutation rates according to different properties of the quotations and will propose a morphogenesis model for building realistic families of quotations.

II. DATASET DESCRIPTION

We analyze the MemeTracker corpus which is made of quotations automatically extracted from 90 millions news and blog articles collected over the final three months of the 2008 U.S. Presidential Election and the following three months [1]. More precisely, we downloaded the MemeTracker dataset from the publicly available website memetracker.org, that consists of 310 457 distinct quotations collected from news and blog articles from August 2008 till the end of January 2009. Each quotation had to be mentioned at least 5 times in order to be included in the corpus. As we will primarily focus on characterizing how quotes are being transformed, the effects stemming from the underlying social network are out of the scope of this article. We then decided to neglect all the hyperlinks between articles and concentrate only on the textual data, i.e. the quotes themselves, and their number of mentions.

III. BUILDING QUOTATION FAMILIES

In order to analyze the MemeTracker corpus, it is necessary to identify families of quotations, which means as “seed” quotation (i.e. an original quoted text that can be subsequently re-used, duplicated or modified). This analysis is done in three steps: (i) all the quotations are linguistically analyzed and normalized (by lemmatizing the quotes and removing stop words); (ii) similarity between every pair of quotations is calculated and the quotes whose similarity is above a given threshold are linked so as to obtain a graph of quotations; (iii) a clustering algorithm is applied to detect communities (i.e. cohesive subgraphs in the graph) that will correspond to our families. We detail this process in the following subsection, followed by an evaluation of our results and a discussion.

A. A hybrid linguistic and structural approach

While the clustering method of Leskovec and his colleagues [1] builds on structural relations between phrases mainly defined according to their potential string inclusion, we tried to design a proximity measure between quoted phrases following more linguistic hypotheses.

A domain of interest regarding our objective is the paraphrase detection task, which is useful for various natural language applications, including information extraction, automatic summarization and machine translation. Paraphrase detection is highly difficult since it theoretically requires both a semantic and a syntactic analysis of sentences to give valuable results. In practice, most approaches are based on the identification of similar words between couples of sentences, which makes it possible to calculate a similarity value (using a similarity measure like cosine) [13]. Various refinements can be explored in order to get more accurate results, like trying to calculate word similarity (using for example a resource like Wordnet for English) or trying to identify relations between words. For example, Qiu et al. [14] use the Charniak parser to get a syntactic analysis of the sentence and try to map predicate-argument patterns (for example, a verb with its arguments) between sentences, which makes the method more precise.

In this study, we preferred to design a simple strategy for building quotation families which features basic text processing techniques and makes use of a refined proximity measure. First we substituted every word with its lemma using the TreeTagger software [15] and eliminated all the stop words. This step is supposed to conserve only the chore semantic part of each quoted text so that our proximity measure only focuses on the most informative part of each phrase. Lemmatization allows to unify into one single class simple variations of the same word like singular/plurals, or verbs at different tenses. Stop words, also called “empty words”, are usually considered as noise when comparing the semantic content of two phrases.

We make use of the traditional Levenshtein distance to assess the dissimilarity between two cleaned quotes. But we still need to add some sophistication to take into account word frequency in our measure, considering that rare words are more informative than frequent ones. We then computed the $tft*idf$ score [16] for every word $w$ of quotation $q$ defined as $tft*idf(w,q,Q) = tf(w,q) * idf(w,Q)$, where $tf(w,q)$ is the word $w$ frequency in the quotation $q$ and $idf(w,Q) = \log |Q|/|\{q \in Q : w \in q\}|$ where $|Q|$ is the cardinality of the set $Q$ of all the quotations. The first term gives more weight to frequent words (in the quotation) and the second one adjusts this value by penalizing words that are too frequent in the dataset since these words are considered to be not discriminative enough.

Then for every couple of quotations $q$ and $q'$ (with $|q| \geq |q'|$) we computed an adjusted Levenshtein distance treating words as tokens and weighting them with their $tft*idf$ scores. Classically, the Levenshtein distance - also called edit-distance - computes the minimum number of additions, deletions or substitutions necessary to transform an ordered sequence of object into another. Our weighted Levenshtein distance $L$ then allows to compare two quotations, defined as two ordered sequences of words following this formula:

$$L(q,q') = \frac{\sum_{w \in q'} \min edit \ path f(w,q,q')(1-\delta(w,w'))}{\sum_{w \in q'} \min edit \ path f(w,q,w',q')}$$
where “min edit path” is the minimum edit path found by the
algorithm to compute the Levenshtein distance, \( \delta(w, w') = 1 \)
if \( w = w' \), 0 otherwise, and

\[
f(w, q, w', q') = \begin{cases} 
\max(tf^*idf(w, q, Q), tf^*idf(w', q', Q)) & \text{if } w = w' \text{ or } w \text{ substituted } w' \text{ or vice-versa} \\
tf^*idf(w, q, Q) & \text{if } w \text{ was inserted or } w' \text{ was deleted}
\end{cases}
\]

The rationale behind this method is to use a proximity measure
based on sequences of words since word order clearly matters
(as opposed to bag-of-word approaches where words are
considered independently of their order of appearance). But
we also give more weight to more discriminating words with
their tf*idf score.

After this pre-processing step, we constructed a similarity
network with the set of quotations, in which every quotation is
a node. We assign a weighted edge between two quotations \( q \)
and \( q' \) if they have at least two (full) words in common and if
their similarity score, calculated as \( 1 - L(q, q') \), is greater than
0.35, a value that we empirically found to be an appropriate
threshold. The weight of the edge equals \( 1 - L(q, q') \).

The final step was to apply an algorithm for community
detection in networks in order to identify different quotation
families. For this purpose we chose the Infomap algorithm by
Rosvall and Bergstrom [17], an information theoretic approach
algorithm which uses the probability of flow of random walks
on a network as a proxy for information flow in the real system
and decomposes the graph into communities by compressing a
description of the probability flow. Lancichinetti and Fortunato
tested various community detection algorithms [18] and found
that Infomap has an excellent performance combined with
low computational complexity, which enables to analyze large
systems like our dataset.

B. Result evaluation and comparison

Clustering methods are widely used for natural language
processing applications that require grouping different sets
of elements. However, evaluating the output of clustering
methods remains challenging since gold standards\(^1\) are rarely
available and different partitions of the data may often make
sense depending on the task and the context.

As for our experiment, no gold standard was available but
it is possible to use the result of the MemeTracker project
experiment as a comparison point. We chose to rely on a
manual evaluation of a relevant sample of clusters randomly
selected from those produced by our method and those pro-
duced by the MemeTracker method. We randomly selected
30 of our families, and for each family we also selected
every MemeTracker family that had at least one quotation in
common with the original family. Then for each family we
made two lists: the first one containing all the quotations in
the family, and the second one containing all the quotations
which belonged to the corresponding selected families of
the MemeTracker project. Then we did the opposite with
30 families of the MemeTracker project. The size of the
initial clusters used for evaluation varies from 3 to 150 text
snippets/sentences.

The list was then assessed by two judges, who were told that
every first list represents a subset of closely related quotations
and to mark any quotation that they thought should not belong
to the family. Then they had to look at the second list and mark
if any of the quotations should be added to the family.

Before detailing the result of this evaluation, it is necessary
to quickly examine some methodological issues. First, a num-
ber of text snippets were not real quotations but titles (“high
school musical”), short expressions with no clear meaning
out of context (“a little bit”) or foreign words (“la vida no
vale nada”) between brackets. The corresponding clusters were
excluded from the evaluation\(^2\). Second, the identification of
the main information expressed in a set of snippets is a difficult
task, especially given the variation in length of the different
snippets. The instruction given to the evaluators was to first
have a look at the whole set of snippets before determining
the prominent information, which seems to have worked pretty
well. Lastly, the instruction was to tag as equivalent snippets
that were reporting the same main information even if some
secondary information was missing. It was possible to tag a
snippet as uncertain.

Despite the minimal set of instructions given to our evalua-
tors, we obtained interesting and reliable results. We compared
the evaluation produced by two annotators and obtained a high
inter-annotator agreement (Cohen’s kappa is 0.69, which is
surprisingly high given the relative subjectivity of the task
and the scarcity of instructions provided to the evaluators).

We obtained the following results for precision and relative
recall (the recall is relative since we performed an evaluation
based on a comparison between two methods and not with
respect to a gold standard), where precision is calculated as
the fraction of quotations considered relevant in the first list,
recall as the number of relevant quotations in the first list over
the same number plus the number of relevant quotations found
in the second list.

<table>
<thead>
<tr>
<th>Clustering Method</th>
<th>Precision</th>
<th>Relative Recall</th>
<th>F-measure</th>
</tr>
</thead>
<tbody>
<tr>
<td>Ours</td>
<td>.58</td>
<td>.90</td>
<td>.70</td>
</tr>
<tr>
<td>MemeTracker</td>
<td>.47</td>
<td>.78</td>
<td>.58</td>
</tr>
</tbody>
</table>

Our method outperforms Leskovec et al.’s approach both
in precision and relative recall. This increase in precision is
probably due to the linguistic preprocessing step that makes
the whole process more precise (our analysis is focused on
content words that are themselves weighted according to
their discriminative power). The increase in relative recall is
probably due to the fact that the MemeTracker clusters contain
also a lot of snippets that are very small fractions of the seed
quotation and were thus considered by the judges not to carry
enough information to be unambiguously part of the family.

\(^1\)In natural language processing, a gold standard is a set of manually
annotated data. Most of the time, the data is annotated by several annotators
to ensure a reliable result based on a high inter-annotator agreement.

\(^2\)Note that our families will be filtered in a second phase in order to delete
these kinds of pathologic families.
We also measured the statistical significance between the two F-measure values through the SIGF V2 test [19], which implements an assumption-free randomization framework. It allows to assess whether the difference in performance between two sets of predictions is significant. We found a p-value of 0.049, which means that the F-scores are different with a 5% significance level.

C. Family filtering

Since the dataset contains many quotations that are either not in English either too short to convey a real unit of meaning, we first decided to filter it by considering only quotations containing at least 5 words in English.

D. Family description

We plotted the distribution of family sizes defined as the total number of quotations mentioned in a family, the distribution of the number of distinct versions found in each family and the distribution of the number of mentions per quotation (Fig. 1). The shapes of all the three distributions can be approximated as a power-law and are comparable to distributions found in [1] although the families were defined differently.

IV. MULTI-LEVEL TRANSFORMATION ANALYSIS

Before going into further details, let’s first have a look at an actual family identified as a family gathering 7 different quotes from the MemeTracker dataset. On Sep 3, 2008, Carly Fiorina, former boss of computer-making giant Hewlett-Packard, told a press conference: “The Republican party will not stand by while Sarah Palin is subjected to sexist attacks ... and as women, I think all of us are sensitized and outraged when we see sexist treatment”. The quote is genuinely replicated 16 times in the dataset but it can also be found in 6 alternative forms, the most frequent of them being mentioned 56 times in a much shorter form than the original one: “the republican party will not stand by while sarah palin is subjected to sexist attack”.

Observing the diversity of quotes within the family, it appears that 3 main sub-families clearly emerge gathering either the first, the second or both parts of the original quote. Within each sub-family, we also observe small variations between different versions of the quotations due to different spellings of the same word (sensitised/sensitized), words trimmed or added (sarah palin/gov palin/gov sarah palin, is being subjected/its subjected).

As we wish to take into account the diversity of possible changes, we will distinguish in the following between small-scale transformations observed when a single word is changed, added or removed, and large-scale transformations occurring when the quote is significantly trimmed into a smaller version.

A. Definitions

Before providing a more formal definition of these transformations, we first define the edit-distance graph as the network connecting quotes whose edit-distance is no larger than 1. Edit distance is defined as a Levenshtein distance between two quotes considering words as single characters. The edit distance between two quotes is then the minimum number of edits needed to transform one quote into the other, with the allowable edit operations being insertion, deletion, or substitution of a single term. The maximum number of allowed edits is fixed to one. Please note that in this case and in all the following analysis no preliminary linguistic processing is applied to quotes before computing their edit-distance.

4We have chosen to consider only the edit-distance graph connecting quotes at the smallest possible edit-distance i.e. 1. However, we have checked that our results are qualitatively unchanged when considering larger transformations (edit distance at most 2 or 3).
Contrarily to the strategy we adopted for detecting families, we naturally do not wish to alter quotations at this step as we are interested in identifying every possible transformation.

For every family, we then build the edit-distance graph $G$ connecting its quotations, and extract its connected components. These connected components define the sub-families, i.e. sets of quotes which can only be differentiated by small-scale changes. Applied to our former example, edit distance graph indeed allows us to exhibit three different sub-families including various micro-level variants (see Fig. 2). The edit distance graph is not only useful to define sub-families since it will also be used to identify - given a target quote $q$ - which quotes are found in its immediate neighbourhood $\mathcal{V}_q$\(^5\) (i.e. quotes that are directly competing for the attention of bloggers or journalists). We then introduce three different measures that will help us to assess the transformation dynamics at different levels.

a) Term level: we are first interested in the relative stability of terms\(^6\) found in a quotation. Given a quote $q$ and a term $t \in q$, we define the stability of this term in this quote $s(t|q)$ as the proportion of quotes in $\mathcal{V}_q$ that share the same term. The global stability of a term $t$ is then defined as the weighted average of term stabilities computed for every quote it belongs to, that is to say: $s(t) = \sum_{q \in q \in \mathcal{V}_q} w_q s(t|q)$, where $w_q$ stands for the total number of mentions of $q$ in its immediate neighborhood: $S(q) = \sum_{q' \in q} \frac{w_{q'}}{w_q}$. At this stage, we voluntarily focus on micro changes, excluding large-scale transformations that may occur when copying only a subpart of a quotation for example.

b) Quote level: we simply define the stability of a quote $q$ as the proportion between the number of mentions of $q$ and the total number of mentions of quotes in its immediate neighborhood: $S(q) = \sum_{q' \in q} \frac{w_{q'}}{w_q}$. At this stage, we voluntarily focus on micro changes, excluding large-scale transformations that may occur when copying only a subpart of a quotation for example.

c) Family level: we also wish to appraise how much a family or a sub-family composition is heterogeneous. We compute the entropy of the distribution of number of mentions for every quote in the family / sub-family: $H_F = -\sum_{q \in F} p_q \log(p_q)$ where $p_q$ holds for the proportion of mentions of quotes $q$ in its family / sub-family: $p_q = \frac{w_q}{\sum_{q' \in F} w_{q'}}$.

B. Term level

The observation of the list of the most unstable words exhibits some well known patterns, the first one being the slight orthographic variations that exist for certain words in English. We thus observe the following alternations: “defence/defense”, “programme/program” and, among many others, “behaviour/behaviour”. Other variations include words with a dash (“cease-fire/ceasefire”), abbreviations (“gov/governor”) and foreign words (“al-qaeda/al-qaida”). Lastly, slang words are frequently omitted, which makes them more subject to variation than ordinary words (for example, “fuck” is in the top 20 most instable words in the corpus; it can be either suppressed or replaced by a simple “f” in indirect quotes).

Besides these qualitative observations, more systematic patterns emerged when analyzing term stability according to different properties. We also wish to describe which features can provide quotes or terms higher-fidelity replication rates. Put differently, we are asking which properties at the term or quote level may systematically account for a higher or lower mutation rates? Formally, the stability of any feature attached to a term/quote is defined as the weighted average of every terms/quotes sharing this property\(^8\).

Figure 3 shows that word frequency significantly affects term stability. More frequent terms are significantly more likely to be stable. More precisely terms with more than 100 occurrences in our quote corpus have a stability higher than 99%, this value reaching up to 99.5% for the most frequent terms. The rarer the term the more dramatically its stability falls. We checked that this pattern is still present after removing stop-words from our set of terms. The same pattern can be observed even when selecting only certain grammatical types of terms, suggesting that frequency of terms plays a central role when it comes to memory issues or when one has to decide whether a given term should undergo a change. This observation may seem counter-intuitive if one considers that less frequent terms may convey more specific meaning. Yet rare terms may also be more prone to change as they may be misspelled or simply more difficult to spell precisely because of their scarcity. The same kind of observation has actually been made in studies examining the long-term evolution of language. For example, in [20],

\(^5\) $\mathcal{V}_q$ will define the set of quotes whose edit-distance with $q$ is less than or equal to 1 and that belong to $q$’s family. Note that $q \in \mathcal{V}_q$.
\(^6\) More formally the stability of $t$ in a given quote $q$ is defined as: $s(t|q) = \frac{\sum_{q' \in \mathcal{V}_q, t \in q'} w_{q'}}{\sum_{q' \in \mathcal{V}_q} w_{q'}}$, where $w_q$ stands for the total number of mentions of $q$.
\(^8\) For example for assessing the stability of terms with a given total frequency in the corpus $n$ we will compute: $s(f = n) = \frac{\sum_{t, f(t) = n} \sum_{q, t \in q} w_{q} s(t|q)}{\sum_{t, f(t) = n} \sum_{q, t \in q} w_{q}}$.
authors showed that the regularization rate of irregular English verbs was rapidly decreasing with their frequency, indicating that low frequency irregulars verbs are subject to more errors, leading to their “rapid” regularization. Besides, specificity is not synonymous with stability. A recent study analyzing the same dataset used Wordnet\(^9\) to rank terms according to their genericity. They showed that the more specific the terms the more likely they are to be replaced, especially by more generic ones [21]. This “natural preference” for more generic terms may also account for the shape of the curve we observe as it is probable that more specific terms occur less frequently than more polysemic ones.

We also computed the average stability of terms according to their grammatical type (see Fig. 4). Results are as expected. Most common grammatical types approximately have the same level of stability. Yet we note that besides interjections which we could expect to feature lower stability, proper noun tend to be more than twice more unstable than average. Indeed proper nouns may produce more mutations as they can be misspelled or undergo more transformations as illustrated in our example in Fig. 2.

C. Quote level

We computed quote stability and plotted stability against quote length, i.e the number of words that it contains (see Fig. 5). Quote stability is minimal for a certain length (around 8 words). Smaller quotes are less keen to change, while longer quotes also feature higher stability. On such a digital medium, two processes may be in competition when it comes to editing quotes: i) a blogger may read/hear a quote in a newspaper, Twitter, or more broadly catch it from any media and try to replicate it by memory or ii) he can simply copy & paste the quote from a digital source. The first copy process is probably more used for quotes that are not too long (a 10-15 words long quote seems already quite difficult to memorize), and is also more keen to introduce variations than a pure copy & paste process (note that variations depend on the length of the quote: very short quotes are easier to memorize and are thus quite stable; longer quotes are more unstable, 8 words long quotes being the most unstable ones). On the other hand, it seems plausible that longer quotes have greater chances to have been replicated from an existing source (for quotes over 8 words long, copy & paste is probably the preferred option, hence the increase in stability for longer quotes). This competition between low and high-fidelity replication along with the uneven probability to introduce errors according to the size of the quote may explain the particular shape of the curve.

We also investigated whether a quote stability is affected or not by its total frequency. In Figure 6 we plotted the weighted average stability of quotes according to their frequency and observe that the curve increases logarithmically. Two explanations may account for the higher stability of high frequency quotes. People trying to replicate them may produce less errors simply because they are inherently better replicators (this property also explaining their popularity). Another cause of their stability may simply be that they are being copied - because of their spread - significantly more often than their alternative forms, increasing in the long-run the disparity between their frequency and alternative forms which are less and less likely to get copied. The two processes may also be taking place at the same time: popular quotes tend to be naturally copied more frequently, while their number may decrease the chances to introduce mistakes in the copying process as it would seem more unlikely for someone to alter a quote she/he has already read several times.

D. Family / sub-family level

To better understand how families are composed and more precisely their inner diversity we also measured their entropy. We both measured the entropy of sub-families and of families as a whole. We recall that families group together every quote related to an original quote whatever the scale of transformations it may have undergone, while sub-families gather quotes from the family that can be connected through micro-

\(^9\)Wordnet is a lexical database of English featuring synonymous relations between words (http://wordnet.princeton.edu/).
level changes. The Shannon entropy, which was originally applied to letters [22], is classically used as a diversity index. Applied to quotes, the entropy measures the diversity of quotes composing a family or a sub-family. Entropy at the sub-family and family levels exhibits very different patterns. Figures 7 shows how entropy correlates with the family / sub-family size. We observe that the value of the entropy for the families with a certain number of mentions is always much higher than the value of the entropy of the sub-families of the dataset gathering the same number of mentions. Put differently sub-families exhibit less diversity than families, suggesting that - at the micro-level - the competition among different versions of the same phrase eventually leads to a situation in which there is one version that is predominant regarding the number of mentions with respect to other versions, whereas - at the macro-level - there is more heterogeneity due to the coexistence of different relatively independent sub-families.

V. MODELING QUOTATION FAMILY GENERATION

We now propose a model of quotation family morphogenesis that accounts for their composition in terms of sub-family size distribution, and regarding their diversity at both levels. To design a realistic model, we still need to precisely define how quotations are being changed when the family is growing. In this section we will then have a closer look at the temporal evolution of families, examining how many and which type of mutations are introduced during the process.

A. Mutation rates

We have shown that two types of mutations could occur when copying a quote. When the quotation is not perfectly replicated, one may observe a macro-level mutation - only a subpart of the original quotation is selected - or a micro-level mutation - small changes affecting only one word in the quotation. In the first case, we will consider that a new sub-family is produced, in the second case that the sub-family the original quote belongs to is simply enriched by a new version. We make the assumption that the chances that a mutation produces a version that had been already published before is negligible.

As we assume that every new version is triggered by a mutation event, we can assess mutation rates a posteriori at both levels by comparing the number of different versions in a given subset and the total number of mentions these different versions received. More precisely, the average mutation rate can be computed at both micro / macro level as the ratio between the number of micro / macro-mutation events (number of versions in the sub-family minus one / number of sub-families in the family minus one), and the total number of copying steps (mentions in the sub-family / family minus one).

But accessing average mutation rates is not enough to realistically reconstruct family and sub-family morphogenesis: we also need to take into account the relevant properties affecting mutation rates. In the previous section, we showed that quote stability is modified according to their length and their popularity, which suggests that mutation rates could strongly differ according to those two properties. Besides, those properties may critically depend on the diffusion dynamics. That is the reason why we should dynamically assess the rate at which new versions are being produced in the empirical process according to those different conditions.

We then define the following strategy to dynamically measure mutation rates. Each family is considered as a growing set progressively populating the various sub-families with new quotes. Each time a new quotation is produced, we record whether it is a perfect copy of a previously mentioned quotation, or a new version that had never been observed before. In the latter case we also record whether the original quotation is enriching an existing sub-family or creating a completely new sub-family. We compile those events according to the original
Fig. 8. Micro and Macro mutation rates according to the sub-family total number of mentions, along with their fitted model. $\rho_M(n) = 0.225n^{-0.703}$ and $\rho_M(n) = 0.057n^{-0.730}$. The figure is obtained by creating 15 equally populated quantiles and averaging the mutation rate values corresponding to each quantile. Error bars stand for confidence interval (5%).

state of the family and sub-family\textsuperscript{10}, \textit{i.e.} we enumerate micro-changes, macro-changes and perfect copying events according to the average sub-family size and average quotation length. From there on, it is straightforward to define the micro / macro-mutation rate according to a given average length or a given total number of mentions as the proportion of replication events producing a micro / macro change. We will call the so computed micro and macro mutation rates $\rho_\mu$ and $\rho_M$ respectively.

From figure 6 we can suspect that the number of mentions is crucial for determining the precise mutation rate of a quotation. Therefore we plotted (Fig. 8) the micro (and respectively macro) mutation rates according to the total number of mentions observed in the sub-family. As expected we find that both mutation rates decrease with the number of mentions (see figure caption for further details about the fitting functions used). This behaviour confirms our hypothesis that more popular quotations are less keen to changes. Very popular quotations may be so ubiquitous in the environment that the probability to introduce micro-mutations by error is lowered (many copies can recall the agents how the correct version should be spelled) or that “successful” quotations have such high “fitness” that any further refinements is unnecessary.

Figure 5 showed that quotation stability is sensibly modified according to their length $l$. We plotted in Fig. 9 the mutation rates according to the average length of the family / sub-family quotations. We observe that the macro-mutation rate is growing with quotation length. While small quotations (less than 5 words) can naturally not undergo any macro mutation given the definition of our family categorization, the macro-mutation rate reaches a threshold for quotations over 20 words. In our model, we use an exponential function to express the dependence of the macro mutation rate with quotation size (see Fig. 9 caption for further details). A plausible explanation is that a quotation can hardly be trimmed before reaching a certain critical length. Above 20 words the quotation is certainly made of different phrases or sentences that individually carry some autonomous meaning even when separated from their original environment.

The correlation between $l$ and the micro mutation rate seems more complex. A peak of the micro mutation rate is reached for mid-size quotations around 8 words. After the maximal value is reached, we observe an exponential decrease until the curve plateau at the minimal mutation rate. As already hypothesized when commenting the shape of quotation stability with length, micro-change dynamics seems to be driven by two processes acting in different directions regarding the number of words. First, it seems clear that mistakes introduced during the copying process are possible only when the quotation is not simply copy & paste. It seems reasonable to postulate that the probability for a quotation to be retrieved from memory rather than copy & paste is exponentially decreasing with quotation length. If the quotation was retrieved from memory then chances are that some mistakes will be introduced. If we refer to classical works in psychology [23], human brain can hold up to a certain number of objects or chunks in memory. This so-called “magic number” below which short term memory is almost perfectly accurate is precisely around 5 for words. This is the reason why we chose to fit the correlation between micro mutation rate and length with a more complex equation made of the product of two probabilities: the probability that the quoted phrase is not replicated by a copy & paste event (which is exponentially decreasing with $l$) and the probability that an error is introduced by chance (which is assumed to be linear for quotations larger than the magical number 5). This product models the probability that the quotation is replicated with an error. We also add a baseline in the fitting function to account for the constant probability that a blogger or a journalist

\textsuperscript{10}We make the hypothesis that a new quotation enriching a pre-existing sub-family was necessarily copied from one member of this sub-family

}\textsuperscript{10}
data
model

may then undergo a mutation according to its length $l$ which a quotation is picked for replication. The quotation is centered around a specific kernel of meaning and is then characterized with its own autonomous dynamical process. This is the reason why we randomly select a sub-family from a random quote from a random sub-family. We assume that each sub-family and sub-family level in time. We rely on a classical Polya urn principle like in [2].

**B. Model Design**

We now propose a generative process producing families of quotations. Our aim is to find a realistic agent-based process that accounts for the distribution of the size of subfamilies as well as for the shape of the increase of diversity at the family and sub-family level in time. We rely on a classical Polya urn principle like in [2]. We assume that each sub-family is centered around a specific kernel of meaning and is then characterized with its own autonomous dynamical process. This is the reason why we randomly select a sub-family from which a quotation is picked for replication. The quotation may then undergo a mutation according to its length $l$ and its number of mentions $n$.

More formally, a family $F$ is initialized with a quotation $q$ of a given length $l$ ($F = \{q\}$). This first quotation is also assigned a sub-family $f$. The simulation then iterates over every time step as follows (see Figure 10 for an illustration):

1) One randomly chooses a sub-family $f$ of $F$ and then a quotation $q \in f$ with probability proportional to the number of mentions of $q$.
2) With a probability given by the combination of the two micro mutations rates $\rho_{\mu}(l)$ and $\rho_{\mu}(n)$ the quotation undergoes a micro-change, resulting in a new quotation $q'$ that differs from the original one by only one edit (deletion, insertion or substitution). If above this probability the quote is not modified.
3) Then, if long enough, the quotation can also be trimmed into a smaller quotation with a probability given by the macro mutation rates which depend on the quotation length $l$ and number of mentions $n$ according to the fitted values of $\rho_{M}(l)$ and $\rho_{M}(n)$. If so, a new shorter quotation $q''$ is created.
4) If the quotation did not undergo any mutation on steps 2 and 3, it is perfectly replicated (copy&paste) and a new quotation $q$ is produced.
5) The possibly mutated ($q'$ or $q''$) or unchanged ($q$) version of the original quotation is added to the family.

The process is repeated from step 1 until the family is considered complete, i.e. when it has received the total number of quotations we observed in the empirical distribution.

**C. Model Results**

Our simulation almost produced the same number of distinct versions and sub-families than in our original dataset (less than 1% error). We also observe that the proposed model accounts for the size distribution of sub-families and for the diversity of families and sub-families. Figure 11 shows a very good fit between the empirical and the simulated sub-family size distributions, suggesting that our model succeeds in reproducing the

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11Precisely the global probability to observe a mutation given the total number of mentions and average length is given by $\rho = \frac{\rho_{\mu}(l)\rho_{\mu}(n)}{1 + \rho_{M}(l) + \rho_{M}(n)}$. As one can not simply infer which was the original quote from which a new quote was replicated, we computed the stylized behaviour linking mutation rates with $l$ and $n$ considering average lengths and estimated cumulated number of mentions in the sub-family. We are now making the hypothesis that mutation rates can be directly computed based on the quotation length and number of mentions. Lengths being homogeneously distributed, the approximation seems reasonable. Since the distribution of mentions is heterogeneous and given that our process preferentially selects the most cited quote, it is very likely that the number of mentions of a random quote is well approximated by the total number of mentions in the sub-family.
In this paper we introduced a new algorithm for quotation clustering as a first step towards the analysis of quotation family structure and transformations. We showed how these families can be characterized at a meso level by retrieving the corresponding sub-families, i.e. the connected components of a graph of edit distances of at most one edit. This multi-level analysis allowed us to find new interesting results, such as the difference in the entropy level at the two scales, suggesting that the strong competition among very similar quotations leads to a more homogeneous situation with respect to the co-existence of the different sub-families. Moreover, we presented a model that attempts to describe the morphogenesis of these families of quotations and accounts for their composition in terms of sub-family size distribution and for the difference of diversity measured at both levels. The model relies on the analysis of quotation stability, through which we showed that quotations undergo a different number of mutations according to their length and their number of mentions, concluding that quotations that are already very popular have less chances to be transformed. In future work we would like to take into account the underlying social network in order to enrich the analysis of the driving forces determining quotations transformation. Moreover, our model could be significantly more realistic with a finer description of temporal patterns pertaining to quotation diffusion.

VI. Conclusions

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Fig. 12. Family and sub-family entropy produced by the model in function of the total number of mentions of their quotations. The figure is obtained by creating 10 equally populated quantiles. Error bars stand for confidence interval (5%).