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SyDiG: Uncovering Synteny in Distant Genomes

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Abstract:

Current methods for detecting synteny work well for sets of genomes with high degrees of inter- and intra-species chromosomal homology, such as mammals. In this paper we define a new algorithm for synteny computation. The main originality of this method is that it is well-suited to genomes covering a large evolutionary span. It is based on a three-step process: identification of initial microsyntenic homologous regions, extension of homologous boundaries using a transitivity relation, and reconstruction of syntenic blocks by identification of groups of homologous genomic segments that are conserved in every subject genome. Our method performs as well as GRIMM-Synteny on mammalian genomes, and outperforms it for clades with much greater evolutionary distances such as the Hemiascomycetous yeasts. The analysis of the algorithms and computed results pinpoints the fact that direct DNA alignments and anchor computation do not provide a sufficient support for synteny recovery in clades covering large evolutionary distances.

Keywords: synteny; algorithm; multiplicon.

Biographical notes: Graldine Jean received her PhD in Computer Science, specialty Bioinformatics at the University of Bordeaux. She currently holds a postdoctoral position at Friedrich Miescher Laboratory of the Max Planck Society, Tbingen. Her research interests include issues related to genome evolution and in particular various rearrangement models as well as algorithms in machine learning. She has published research paper at national and international levels, as well as conference proceedings.

Macha Nikolski has received her doctoral degree in Computer Science from the University of Bordeaux on the subject of binary decision diagrams and their application to the reliability analysis and has subsequently worked for Synopsys, before returning to public research to a position of a Research Scientist with the Centre National de Recherche Scientifique (CNRS). In particular she has worked in two distinct but related subjects: algorithms for pattern recognition, inference, and search for optimal solutions in large search spaces; and modeling, for building rigorous descriptions of complex dynamic

systems and establishing formal properties about their behaviors. She has published research paper at national and international levels, conference proceedings as well as chapters of books.

1 Introduction

Comparative analysis of complete genomes has over the past ten years provided increased understanding of the processes and mechanisms of evolution, development, and gene regulation. One area where significant insight has been obtained is genome rearrangements, where the mechanisms of chromosomal dynamics have been explored through comparison of chromosomal maps within and between species. A key prerequisite for such studies is the accurate identification of *genome synteny*, since conserved gene order between related species indicates chromosomal homology inherited from their common ancestor. Once carefully identified, synteny information is used for computing rearrangement distances (Hannenhalli and Pevzner, 1995) or scenarios (Tesler, 2002), inferring the least common ancestor and rearrangement trees (Bourque and Pevzner, 2002). The implications of the analysis of genomic synteny can reach even further, providing insights into the manner by which evolution proceeds. This latter topic has generated a quite lively debate on the differences between random breakage and fragile breakage models of evolution (Pevzner and Tesler, 2003a,b; Trinh *et al.*, 2004).

Nadeau and Taylor (Nadeau and Taylor, 1984) were the first to define *conserved segments* as segments having a preserved gene order with no rearrangements between them. *Synteny blocks* are built of these conserved segments, smoothing over the noise due to microrearrangements. These blocks constitute gene markers that are the starting points for further analysis.

The focus of this paper is the computational identification of genome synteny in complete sequences of distant genomes. A number of methods has been developed in this area. They can be classified in two main categories: alignment-based and profile-based methods.

The most commonly used methods are alignment-based, such as CHAINNET (Kent *et al.*, 2004) and GRIMM-Synteny (Pevzner and Tesler, 2003a; Bourque *et al.*, 2004, 2005). They determine synteny blocks from an initial signal provided by BLASTZ alignments of nucleotide sequences (Schwartz *et al.*, 2004). Since many pairwise relations between DNA segments identified in this manner will be spurious, for example due to domain conservation in protein coding genes, alignment-based methods apply strict filtering policies to link related alignments and remove the spurious ones. Such techniques have been applied with success to sets of mammalian genomes and fly genomes, sets which have a high degree of chromosomal homology,¹ and significant conservation in DNA sequences. Such cases of closely related genomes are of course extremely interesting, particularly in biomedical applications, but they are the ‘low-hanging fruit’ for synteny detection.

The profile-based i-ADHoRe routine (Simillion *et al.*, 2004, 2008), extends the pairwise ADHoRe method of (Vandepoele *et al.*, 2002) by iteratively building profiles of intervals of syntenic genes, that are used to search the same genome(s)

again to determine “higher level” multiplicons. This method was originally developed to identify multiple rounds of whole genome duplication in *Arabidopsis thaliana*, events that leave overlapping signals of self-similarity as is also seen in the genomes of *Tetraodon nigroviridis* (Jaillon *et al.*, 2004) and *Paramecium tetraurelia* (Aury *et al.*, 2006). In this method the initial signal is provided by Blastp alignments of predicted translation products, and genomes are represented as lists of genes. The algorithm essentially looks for statistically significant pairs of intervals in these lists with similar gene order and contents. These segments of chromosomal homology are called *multiplicons*. Multiplicons of level n are used to define *profiles*, lists of genes defining a consensus between the two intervals in the multiplicon, that are used again in pairwise comparisons with each of the target genomes. The result are multiplicons of level $n + 1$, and so on.

Both of these existing methods work well on the cases that they were designed for, but perform poorly on the increasingly more common case of sets of related species with highly divergent or extensively reshuffled genomes (see section 3 for comparisons). Recent improvements to sequencing technology are making it feasible to obtain complete sequences from a large number of species of biotechnological interest, and global detection of synteny in such groups is of great practical use for studying chromosome dynamics linked to, e.g. quantitative traits. Despite their phylogenetic relations, such groups of species may be highly divergent. The industrially useful Hemiascomycete yeasts, for example, despite their small, compact genomes and similar ecological niches, are evolutionarily distant. With GC contents ranging from 40% to 52% and an average amino-acid identity of 20% (Dujon, 2006), alignment of DNA sequences is not informative. While alignment of translation products does provide a recognizable signal for gene homology, extensive map reshuffling leads to quite small syntenic segments of 10-15 genes, and iterated profile searching finds few segments conserved in many species (see section 3).

In this paper we present a new method called SyDiG (Synteny in Distant Genomes) that has the ability to handle species having a large evolutionary span. It requires complete genome sequences and infers inter-species synteny in the general case of $N \geq 2$ genomes. It follows a three-step process. First, we perform a pre-processing step that consists in determining orthologous genes and, from those, in computing multiplicons of level two. Second, using a novel graph encoding of homology between genomic segments and overlaps of multiple segments on the same chromosome, we extend certain homology relationships at the boundaries of segments by transitivity. Finally, we use the initial orthology information and the identified supplementary homologous elements in order to reconstruct synteny blocks. In the rest of the paper, when speaking of homologous groups we understand the subdivision of these groups in subgroups of orthologs by the SONS method.

In what follows, we present in the first section a formal definition of the SyDiG method and its algorithms. In the second section, we compare Grimm-Synteny and SyDiG on both mammal and yeast genome sets. Finally, in the third section, we present a practical application to Hemiascomycetous yeasts that leads to the rearrangement analysis presented in (Jean *et al.*, 2009).

2 SyDiG algorithm

2.1 Pre-processing

The starting point for synteny identification is the definition of pairwise orthology relationships between genomes. We use our consensus clustering algorithm from (Nikolski and Sherman, 2007) on a mix of complementary partitions (see section 3.3), although raw clustering methods can be used such as (Enright *et al.*, 2002). Furthermore, within these homologous groups, orthologous subgroups are identified by the SONS method (Dujon *et al.*, 2009). While in principle sequence similarity can generally be detected either at the DNA level or by aligning the translation products of coding sequences, in practice for distant genomes only the latter recovers significant similarity. In this case, one essentially constructs comparative genome maps and the study of gene order makes it possible to detect homology even for highly divergent chromosomal regions. This is exactly the role of the ADHoRe method briefly described above (Vandepoele *et al.*, 2002; Simillion *et al.*, 2004, 2008).

Recall that a multiplicon is formed by one or several homologous genomic segments and its level indicates the number of iterations used to obtain it. In SyDiG we use i-ADHoRe to identify short (microsyntenic) segments as a starting point, but restricted to pairwise computations and thus to computing only level two multiplicons. We will call these segments simply ‘multiplicons’ in the rest of the paper even though more than one genome is involved. The restriction to level 2 multiplicons comes from an empirical observation that use of profiles provides little benefit and, by stringently requiring a synteny relation to have exactly the same boundaries in many species, it retains few segments at every iteration.

Notice that i-ADHoRe determines the multiplicons based on gene order. Hence, the coordinate system used is at gene level: each element of a genomic segment is mapped to a gene and each chromosomal segment is delimited by two genes, one on each side. Multiplicons obtained by i-ADHoRe correspond to homologies between two genomic segments (belonging to the same genome or not). The goal now is to refine these homologies into synteny blocks for the set of considered genomes $\{G_1, \dots, G_N\}$. We do this by analyzing the composition of each multiplicon and computing the synteny blocks using transitivity relations.

2.2 Synteny graph

The first step is to assemble all the information contained in the multiplicons into a graph. This graph has to represent two types of information: first, homology between genomic segments; second, possible overlaps between multiple segments of the same chromosome. Let $\{G_1, \dots, G_N\}$ be the set of genomes for which we want to compute synteny blocks and $\mathcal{M}$ be the set of multiplicons obtained by ADHoRe for these genomes.

For the needs of the method, we propose a more formal definition of the notion of multiplicon. Let $M = \langle I_1, I_2, A \rangle$ be a (level two) multiplicon where I_1 and I_2 denote the genomic segments that it contains, and A is the set of anchors within it. We note a genomic segment I_i as a sequence of genes $I_i = (g_b^i, \dots, g_e^i)$ such that g_b^i and g_e^i represent the gene boundaries of this segment. A gene g_j^i of a genomic

segment I_i is a pair $\langle p_j, c_j \rangle$ such that p_j is its relative position on the chromosome c_j . If two genes $g_i^1 \in I_1$ and $g_j^2 \in I_2$ form an anchor in M , then $\langle g_i^1, g_j^2 \rangle \in A$.

Figure 1 shows an example of multiplicons for $N = 5$ genomes. This same example will be followed through the paper.

Figure 1 Level 2 multiplicons for genomes $\{G_1, \dots, G_5\}$. Each genome G_i is shown on a separate line with chromosomes denoted by $c_1^i, c_2^i, \dots, c_k^i$ (k the total number of chromosomes for G_i). A genomic segment $(g_j^i, g_{j+1}^i, \dots, g_{k-1}^i, g_k^i)$ on G_i is represented by a bold line on the chromosome and is explicitly delimited by its boundaries g_j^i and g_k^i . Dots along chromosomes represent gene locations. A grey (dark, respectively) line materializes an anchor formed by genes (gene boundaries, respectively) at its extremities.

The *synteny graph* G is defined from the set $\mathcal{M}$ of multiplicons for the N genomes under study.

Definition 2.1: A synteny graph $G = (V, E)$ is a non-oriented edge-colored graph such that

- $V = \{g_j^i \mid g_j^i \in I_i \in M \in \mathcal{M}\}$ is the set of all genes participating in a multiplicon,
- E is the edge set such that $\forall e = \{g_n^i, g_m^j\} \in E$ either g_n^i and g_m^j form an anchor in a multiplicon of $\mathcal{M}$ (dashed edge), or g_n^i and g_m^j are consecutive on the same chromosome (black edge).

In this graph, we can distinguish three types of vertices: (1) *boundary vertices* correspond to gene boundaries of genomic segments participating in a multiplicon, (2) *anchor vertices* correspond to genes that form an anchor with some other gene and are not boundaries of any genomic segments, (3) *interleaving vertices* are the other vertices that are neither a boundary nor an element of an anchor.

Note that boundary vertices always form an anchor, since ADHoRe computes multiplicons in such a way that extremities of genomic segments that define them are determined by the leftmost and rightmost coordinates of their anchors. Thus, a gene can be both a boundary of one or several genomic segments taking part in

multiplicons and a simple anchors in other segments. An anchor vertex is a gene that forms an anchor strictly inside one or several multiplicons.

Figure 2 shows the synteny graph obtained for the 5 genomes and their multiplicons of figure 1.

Figure 2 Synteny graph obtained for the data shown on figure 1. Dashed edges represent homologies while black ones represent gene adjacency. Boundary vertices (anchor vertices, and gene vertices, respectively) are represented by diamonds (white circles and full circles, respectively).

2.3 Extension of homologous boundaries

The synteny graph represents gene relationships within and between genomes: physical relationships are modeled by black edges, which represent gene adjacencies, while dashed edges model homology information contained in multiplicons. From synteny graph, we define two kinds of dependency between elements.

2.3.1 Extended segments

Genomic segments taking part in multiplicons can be physically dependent, since some of them overlap. It is from this kind of dependency that we can infer new homology relationships by combining the information contained in multiplicons related by overlapping genomic segments. Thus, we isolate the set of genes that are dependent only due to chromosomal overlaps. All of these genes will belong to the same *extended segment*.

Definition 2.2: An extended segment for a given genome is a maximal genomic segment $I_{max} = (g_b, \dots, g_e)$ defined from the set of genomic segments $\{I_1, \dots, I_k\}$ belonging to the same chromosome c such that

- (i) $g_b = \langle p_{b_{min}}, c \rangle \in I_i$ with $1 \leq i \leq k$ such that $p_{b_{min}} = \min(\{p_i \mid g_i = \langle p_i, c \rangle \in I_i, 1 \leq i \leq k\})$,
- (ii) $g_e = \langle p_{e_{max}}, c \rangle \in I_i$ with $1 \leq i \leq k$ such that $p_{e_{max}} = \max(\{p_i \mid g_i = \langle p_i, c \rangle \in I_i, 1 \leq i \leq k\})$,

- (iii) 2 consecutive genes on the extended segment belong to the same genomic segment: $\forall g_i, g_{i+1} \in I_{max}, \exists I \in \{I_1, \dots, I_k\}$ such that $g_i \in I$ and $g_{i+1} \in I$,
- (iv) the extended segment satisfies the criterion of maximality: $\forall I \notin \{I_1, \dots, I_k\}$ and $\forall j \in [1, k]$, I and I_j do not overlap.

The set of extended segments obtained for a given synteny graph G is computed from the connected components of the subgraph of G induced by the black edges of G . In fact, the resulting subgraph can be decomposed into paths that correspond to extended segments.

The synteny graph of figure 2 contains 9 extended segments, namely:

- $S_1^1 = (g_1^1, \dots, g_7^1)$ belonging to G_1 ,
- $S_1^2 = (g_1^2, \dots, g_7^2)$ belonging to G_2 ,
- $S_1^3 = (g_1^3, \dots, g_3^3)$ and $S_2^3 = (g_4^3, \dots, g_9^3)$ belonging to G_3 ,
- $S_1^4 = (g_1^4, \dots, g_3^4)$, $S_2^4 = (g_4^4, \dots, g_6^4)$ and $S_3^4 = (g_7^4, \dots, g_9^4)$ belonging to G_4 ,
- $S_1^5 = (g_1^5, \dots, g_2^5)$ and $S_2^5 = (g_3^5, \dots, g_5^5)$ belonging to G_5 .

2.3.2 Groups of homologous genes and boundaries

The goal of our algorithm is to determine synteny blocks for N genomes under study. We use transitivity of the relation defined by the multiplicons in order to solve the missing homologies between genomic segments. Thus, if I_1 is homologous to I_2 that is itself homologous to I_3 , we consider that I_1 and I_3 are also homologous. Not all homologies are that simple to solve. For example, in figure 1, the genomic segment $I_2^2 = (g_3^2, \dots, g_7^2)$ of genome G_2 does not have a homolog (direct or by transitivity) with any genomic segment of genome G_1 . However, I_2^2 is included in $I_2^1 = (g_1^1, \dots, g_7^1)$ that itself is homologous with $I_1^1 = (g_1^1, \dots, g_7^1)$ of G_1 . This homology makes it possible to deduce a new boundary in G_1 that “cuts” I_1^1 into two distinct intervals such that one of them is homologous with I_2^2 .

Recovering homology relationships between genomic segments can then be reduced to looking for specific genes that are boundaries, and reconstructing the corresponding genomic segments. In order to do that we first partition genes forming at least an anchor in *groups of homologous genes* and in parallel, by considering only the set of gene boundaries, *groups of homologous boundaries*.

Definition 2.3: Groups of homologous genes are a partition of genes forming at least one anchor such that a part of this partition is a set of genes that are either directly homologous, or that share a gene with which they form an anchor.

Definition 2.4:

Groups of homologous boundaries are a partition of gene boundaries such that a part of this partition is a set of boundaries that are either directly homologous, or that share a gene with which they form an anchor.

homologous boundaries	homologous genes
g_1^1, g_1^2	g_1^1, g_1^2
g_7^1, g_7^2, g_8^3	g_2^1, g_2^2
$g_1^3, g_1^4, g_1^5, g_5^3, g_4^4, g_5^5$	g_5^1, g_6^2
$g_3^3, g_3^4, g_2^5, g_4^3, g_3^2$	g_7^1, g_7^2, g_8^3
$g_3^5, g_6^4, g_7^3, g_7^4$	g_5^2, g_6^3, g_5^4
g_9^3, g_9^4	$g_1^3, g_1^4, g_1^5, g_5^3, g_4^4, g_5^5$
	$g_3^3, g_3^4, g_2^5, g_4^3, g_3^2, g_3^1$
	$g_3^5, g_6^4, g_7^3, g_7^4$
	g_9^3, g_9^4

Table 1 Groups of homologous boundaries and genes obtained from the synteny graph of figure 2

Groups of homologous genes obtained for a given synteny graph G are computed from the connected components of the subgraph of G induced by the anchor and boundary vertices, and the dashed edges of G rather than groups of homologous boundaries of G are computed from the connected components of the subgraph of G restricted to boundary vertices and the dashed edges of G . The group of homologous boundaries is obtained for a given synteny graph G , in an analogous way, from the the subgraph of G induced by the boundary vertices, and the dashed edges of G .

Starting from the synteny graph from figure 2, we obtain groups of homologous genes and groups of homologous boundaries shown respectively in table 1.

2.3.3 Adding and positioning of new boundaries

The next step is to check each boundary to see whether it creates new boundaries in other genomes. Each extended segment is a genomic segment defined by a maximal set of overlapping genomic segments. Hence, in each extended segment there exist boundaries of genomic segments that are included in others. For example, boundary g_3^2 of I_2^2 is included in the interval I_2^1 of the extended segment S_1^2 . However, genomic segment I_1^1 homologous to I_2^1 does not contain any boundary homologous to g_3^2 . This is precisely the situation where the need for adding new boundaries arises. In order to do this we search in the groups of homologous genes for a boundary homologous to g_3^2 in I_1^1 (see table 1). In this case, we find the gene g_3^1 .

The algorithm *add_boundaries* implements this operation. Function *extended_segment* returns the extended segment to which a given genomic segment belongs. In the case of the addition of a supplementary boundary, if the current boundary has no homologous gene in the target genomic segment, then it is necessary to pick a gene in this segment as the homologous one. This is done by the routine *locate*: the homologous gene is the one that is proportionately located

in the target segment at the same place than the current boundary in its genomic segment.

Algorithm 1 `add_boundaries( $\mathcal{S}$ )`

Require: Set of extended segments $\mathcal{S}$

Ensure: Set of extended segments $\mathcal{S}$ with new boundaries

```

1: Let  $\mathcal{B}$  be the set of boundaries for  $\mathcal{S}$ 
2: while  $\mathcal{B} \neq \emptyset$  do
3:    $b = \text{shift}(\mathcal{B})$ 
4:   Let  $\mathcal{I}$  be the set of genomic segments in which  $b$  is included
5:   for all  $I \in \mathcal{I}$  do
6:     for all  $I'$  such that  $\exists M = \langle I, I', A \rangle \in \mathcal{M}$  do
7:       if  $\nexists b_h \in I'$  such that  $b_h$  and  $b$  are two homologous boundaries then
8:         if  $\exists b_a \in I'$  such that  $b_a$  and  $b$  are two homologous genes then
9:            $S' = \text{extended\_segment}(I', \mathcal{S})$ 
10:          Mark  $b_a$  as boundary in  $S'$ 
11:          Add  $b_a$  in  $\mathcal{B}$ 
12:          Add  $b_a$  in the group of boundaries homologous to  $b$ 
13:         else
14:            $S' = \text{extended\_segment}(I', \mathcal{S})$ 
15:            $\text{locate}(b_{\text{new}}, S')$ 
16:           Mark  $b_{\text{new}}$  as boundary in  $S'$ 
17:           Add  $b_{\text{new}}$  in  $\mathcal{B}$ 
18:           Add  $b_{\text{new}}$  in the group of gene homologous to  $b$ 
19:           Add  $b_{\text{new}}$  in the group of boundaries homologous to  $b$ 
20:         end if
21:       end if
22:     end for
23:   end for
24: end while
25: return  $\mathcal{S}$ 

```

For the example of figure 1, six new boundaries are added. All the new boundaries are shown in figure 3. The resulting groups of homologous boundaries are shown in table 2.

2.4 Reconstructing synteny blocks

Once boundary homology is completely solved, we define the genomic segments and their homology relations. In an extended segment, two boundaries form a genomic segment that is necessarily homologous with at least one other genomic segment. In order to obtain genomic segments that are disjoint for a given chromosome, it is sufficient to go through each extended segment in order, where two successive boundaries delimit a genomic segment. Then, from boundary homology, we deduce homologies between segments delimited by these boundaries. This implies finding the two corresponding boundaries in another genome. If the boundaries are ordered in the same way for the two segments, then the mutual

Final groups of homologous boundaries
g_1^1, g_1^2
$g_7^1, g_7^2, g_8^3, b_6 = g_8^4$
$g_1^3, g_1^4, g_1^5, g_3^3, g_4^4, g_5^5, b_2 = g_4^1, b_4 = g_4^2$
$g_3^3, g_3^4, g_2^5, g_4^3, g_3^2, b_1 = g_3^1$
$g_3^5, g_6^4, g_7^3, g_7^4, b_3 = g_5^1, b_5 = g_6^2$
g_9^3, g_9^4

Table 2 Groups of homologous boundaries obtained from groups of table 1 after *add_boundaries* routine.

Figure 3 New gene boundaries $\{b_1, \dots, b_6\}$ added for the example from figure 1. Boundaries connected by edges represent homologous boundaries. The dashed edges show the homology between the new boundaries and those originally present.

Finally, to obtain *synteny blocks* for the N genomes under study, these groups are filtered in order to keep only those that contain at least one segment per genome. Final synteny blocks for the example of figure 1 are shown in figure 4.

Moreover, additional filters make it possible to adapt obtained syntenic blocks as common markers used in the elaboration of signed permutations in order to study rearrangement events.

Generally, the permutation model does not allow duplication events, so the SyDiG algorithm proposes to keep only the longest segment in a synteny block where more than one segment belongs to one genome. The intuition behind this filter parameter is that the longer the segment, the smaller the probability that synteny was computed by chance. Nevertheless, other parameters to choose between duplicate segments should be considered such as for example synteny block neighboring. This is the subject of future work.

In the same permutation model, identifiers represent synteny blocks. Under the parsimony criterion, two identifiers that are adjacent in all the considered genomes cannot be separated to be joined again later. That is why, two modes are implemented in SyDiG algorithm. The first one provides all the synteny blocks and permits one to study their respective genomic segments. The second mode consists in concatenating synteny blocks that appear consecutively in all the

considered genomes. This leads to the construction of signed permutations with fewer identifiers, but encoding exactly the same information as far as a study of rearrangements is concerned.

2.5 Complexity

The SyDiG algorithm determines synteny blocks by constructing synteny graph and performing operations on this graph. Synteny graph construction is linear in the number of genes involved in genomic segments participating in multiplicons. Moreover, computing extended segments in the particular subgraph of the synteny graph induced by black edges can be computed in linear time in terms of the number of vertices. Finding groups of homologous genes and groups of homologous boundaries can be computed in both cases in linear time in terms of the number of vertices and dashed edges. Boundaries addition is computed in $O(n^3)$ in the worst case, where n denotes the number of vertices in the synteny graph. Finally, the reconstruction of synteny blocks is realized by scanning the extended segments and the groups of homologous boundaries: the complexity in time is thus $O(n^2)$. Thus, SyDiG algorithm can be computed in a simple way in $O(n^3)$ where n denotes the number of genes involved in genomic segments.

3 Applications

3.1 GRIMM-Synteny versus SyDiG algorithm

In order to realize this comparison, we re-implemented GRIMM-Synteny as the software is not publicly available. Our reimplementation was validated using back-to-back comparison with results available on the author's webpage (Tesler, 2004).

The considerable challenge for comparing the behavior of these algorithms is the judicious choice of data processing. Indeed, GRIMM-Synteny and SyDiG rely on different data. The former proceeds by direct sequence alignment at DNA level (cleaned up by RepeatMasker (Smit *et al.*, 2004)). The latter relies on the existence of pre-computed protein families. While DNA alignments such as BLASTZ are reasonable for closely related genomes such as mammals, only alignments at protein level can recover distant similarities for species such as yeasts (Dujon, 2006). The data presented below was retrieved from public databases on the 17th of June 2008.

- Mammal genomes human, mouse and rat, for which two sets of data were retrieved from Ensembl (release 49) and Uniprot (UniRef50, release 13.5, the 10th of June 2008) data.
- Yeast genomes *Ashbya gossypii* (Ergo), *Kluyveromyces lactis* (Klla), *Kluyveromyces thermotolerans* (Klth), *Zygosaccharomyces rouxii* (Zyro), and *Saccharomyces kluyveri* (Sakl), data provided by the Génolevures Consortium (Sherman *et al.*, 2009).

3.1.1 Yeast results

In order to apply Grimm-synteny to yeast data, we have computed 3 data sets from TBLASTX alignments: (1) unrefined alignments (206191 alignments), (2) the longest alignments when several ones overlap (51085 alignments), (3) the shortest alignments when several ones overlap (59028 alignments).

Anchors were computed by GRIMM-Anchor for the levels from 2 to 5. Results for levels 2 to 4 are shown for each data set in supplementary materials (see supplementary tables S1, S2 and S3). No 5-level anchors are found for unrefined and longest sets and only one 5-way anchor is found for the shortest set. Based on these results it was not possible to run GRIMM-Synteny and uncover synteny blocks, since the number of anchors is insufficient.

From orthology and synteny relations identified using Génolevures protein families (Nikolski and Sherman, 2007), SyDiG was used to compute synteny blocks for the same species. Numbers of synteny blocks for respectively two, three and four organisms are shown in supplementary materials (see supplementary tables S1, S2 and S3). A total of 640 synteny blocks are defined for the set of the 5 genomes (without concatenation). As can be noted from figure 5 (A), the number of anchors obtained for any dataset (unrefined, longest and shortest) goes dramatically down as the number of genomes increases. The comparison between multiplicons and synteny blocks on figure 5 (B) shows that the number of synteny blocks obtained by SyDiG slightly grows with each added genome while it is not the case for the multiplicons. The reason for this when going from n to $n + 1$ genomes, is the splitting of certain synteny blocks.

We tried to determine whether results computed by the SyDiG algorithm detect true synteny or not. In order to do this, we performed the synteny block computation on random genome data. The data were generated as follows. Each random genome set contains 5 genomes. Each of these genomes is generated starting from the complete set of the loci from one of the yeast genomes, say $L \in \{Klla, Ergo, Zyro, Sakl, Klth\}$. First, a random number of chromosomes c between 1 and 8 is generated. Second, the number n_i of loci to belong to each of the c chromosomes is generated randomly so that $\sum_{i=1}^c n_i = n$ where $n = |L|$. Each set of n_i loci is then chosen randomly from L to be placed on the corresponding chromosome. Finally, the orientation (positive or negative) of each locus is also chosen randomly. In total we have generated 1000 random sets of 5 genomes. The pre-processing step that consists in computing level 2 multiplicons by i-ADHoRE and using exactly the same parameters as for the real yeast data, has yielded no synteny signal whatsoever.

3.1.2 Mammal results

Results for GRIMM-Synteny are available on the webpage "Human-mouse-rat alignments" (by Glenn Tesler, the 16th of March 2004) (Tesler, 2004). In order to run SyDiG on the mammalian genome data, an approximation of protein families is required. We have considered two different sets:

1. the Ensembl mcl clustering results (pairwise homology relationships and gene ordered lists) (Hubbard *et al.*, 2007),

Figure 5 A. Mean and standard deviation of number of anchors in red (black, yellow, respectively) for the unrefined (longest, shortest, respectively) dataset, of multiplicons (blue) and of syntenic blocks (cyan) as a function of number of genomes. B. Zoom on mean and standard deviation of number of multiplicons (blue) and syntenic blocks (cyan) as a function of number of genomes.

2. the UniRef50 clusters (pairwise homology relationships and gene ordered lists) (Consortium, 2008).

In order to be coherent with the results obtained in (Bourque and Pevzner, 2002), we have chosen the following i-ADHoRe parameters: a gap size of 15, a

cluster gap size of 20 and 9 as minimum number of anchor points. The number of synteny blocks obtained by the SyDiG algorithm is shown in table 3 for each set of data.

genomes	Ensembl	UniRef50	Grimm
Human-Mouse	144	380	280-394
Human-Rat	137	215	278-417
Mouse-Rat	147	244	105-162
Human-Mouse-Rat	230	465	289-391

Table 3 Synteny blocks for mammalian genomes obtained by SyDiG algorithm based on two datasets (Ensembl and UniRef50) compared to those obtained by Grimm-Synteny (see (Bourque *et al.*, 2004)) algorithm

3.1.3 Discussion

The two methods studied here identify very similar number of synteny blocks for mammalian genomes. However, the number of anchors for yeast genomes obtained by GRIMM-synteny is very low compared to the number of alignments, and moreover the signal within genomes is lost bit by bit when the number of considered genomes increases: with as few as five yeast genomes, no anchors are found.

The main issue boils down to the observation that homologous genes correspond neither to DNA alignments, nor to anchors of level 2. Indeed, two anchors of level 2 cannot consist of the same nucleotide sequences from the same genome. Quite to the contrary, one gene from one genome G_i can be homologous to 2 (or indeed many more) genes in another genome G_j (see figure 6).

Analysis of these results shows that for mammalian genomes SyDiG performs comparably to Grimm-Synteny. While the two data sets (UniRef50 and Ensembl) generate slightly different results, they are both comparable (for appropriately-chosen i-ADHoRe parameters) with the results published in (Bourque *et al.*, 2004). However, when dealing with distant species such as yeasts, GRIMM-Synteny performs quite poorly. The only way to coax out any kind of signal was to perform quite strong alignment pre-filtering of the TBLASTX result.

A particularly acute problem is that the GRIMM-Synteny procedure discards n -ary homologies. Not only do these paralogous families contain biologically pertinent information, they are often the best candidates for conserved markers between genomes: in the yeasts, for example, half of the genes conserved between species are members of paralogous families of up to 30 members, and discarding these homologies can lead to drastic under-identification of chromosomal homology.

3.2 I-ADHoRe versus SydiG algorithm

3.2.1 Yeast results

We compared the i-ADHoRe method and the SyDiG algorithm on the same five species of yeasts previously presented in section 3.1. Multiplicons and synteny

Figure 6 Difference between anchors and homologous genes. We have gene homologies between (g_1, g_7) , (g_2, g_7) , (g_3, g_8) , (g_4, g_9) , (g_5, g_{10}) , (g_6, g_{11}) . However, (SI_1, SI_7) and (SI_2, SI_7) can not correspond to any anchor since SI_7 is common to two couples. Other couples (SI_3, SI_8) , (SI_4, SI_9) , (SI_5, SI_{10}) , (SI_6, SI_{11}) represent anchors.

blocks from SyDiG were computed for the levels 2 to 5 (see supplementary tables S1, S2, S3 for respectively two, three and four organisms). We found 136 of 5-level multiplicons i-ADHoRe compared to 640 syntenic blocks (without concatenation) with SyDiG.

3.2.2 Discussion

Since our SyDiG algorithm starts with the ADHoRe multiplicons of level 2, the number of multiplicons and syntenic blocks obtained by the i-ADHoRe routine and the SyDiG algorithm respectively are equivalent for the pairwise comparison of species. However, profile integration for higher levels leads to a low number of multiplicons for the majority of genome triplets and quadruplets, while SyDiG uncovers homologies by considering all of the available information. In fact, on average i-ADHoRe obtains 26.4 multiplicons of level 3 (46.6 multiplicons of level 4, respectively) compared to 431.8 syntenic blocks level 3 (551.2 syntenic blocks level 4, respectively) for SyDiG algorithm. For the case of 5 genomes, i-ADHoRe finds 136 multiplicons. Profiles constructed from lower levels lead to an important number of 5-level multiplicons compared to those of levels 3 and 4. However, SyDiG finds more than 600 syntenic blocks for all of the 5 genomes.

3.3 Application to yeast genomes

We have applied the SyDiG algorithm in the context of the Génolevures project (Dujon *et al.*, 2004) for the case of non-WGD Hemiascomycetous yeasts. The data consists in 5 completely sequenced protoploid yeasts from the *Saccharomycetaceae* clades: *Kluyveromyces lactis* (Klla), *Saccharomyces kluyveri* (Sakl), *Zygosaccharomyces rouxii* (Zyro), *Ashbya (Eremothecium) gossypii* (Ergo)

and *Kluyveromyces thermotolerans* (Klth). These genomes have little genome redundancy and a relatively high (for yeasts) conservation of synteny.

From orthology and synteny relations identified using Génolevures protein families (Nikolski and Sherman, 2007), the SyDiG algorithm obtains 487 synteny blocks for these genomes (mean size 51 genes). These syntenic blocks contain 8–200 genes and cover roughly 60% of each genome. Basing these permutations only on protein-coding genes is sufficient, since yeast genomes are highly compact (protein-coding genes cover approximately 80% of the genome), and gene relics are quite rare (approximately 4%) (Dujon, 2006). For frequency distribution of synteny blocks, please refer to (Dujon *et al.*, 2009).

By combining pairwise syntenies, each genome was factored into a sequence of ordered syntenic blocks, from which a set of distinct blocks common to all genomes was determined. An arbitrary reference genome was chosen, and all the blocks forming this genome were numbered by unique sequential identifiers from 1 to n . By keeping the longest blocks, permutations of 120 identifiers are constructed, that are representative of the pairwise evolutionary distances for these genomes. We are able to place active and inactive centromeres in each genome permutation by locating the flanking genes. Each of 9 centromeres is encoded by two identifiers, resulting in 15 additional blocks. Thus, each genome is represented as a signed permutation of 135 elements, in which chromosomal rearrangements (fusion, fission, translocation, inversion) can be studied (see (Jean *et al.*, 2009)).

A high degree of synteny, and a limited number of large-scale rearrangements, is observed between *K. thermotolerans* and *S. Kluyveri*; they share many common adjacencies and their rearrangement distance is half of that seen between other pairs of genomes. Note that *K. lactis* presents two syntenic breaks in centromere areas: the centromere of *Klla0F* is located between the flanking genes of centromeres *h* and *b*, and the centromere of *Klla0A* is located between the flanking genes of centromeres *h* and *e*. Moreover, *S. kluyveri* has an active centromere (the centromere *i*), that was disabled in all the other studied genomes.

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genomes	UNR	LON	SHO	SB	MULT
Ergo-Klth	3659	3887	4629	278	274
Ergo-Sakl	3383	3615	4288	248	245
Ergo-Zyro	3578	3792	4353	338	327
Klla-Ergo	3159	3333	3856	384	364
Klla-Klth	3221	3407	3974	328	314
Klla-Sakl	3028	3202	3716	303	288
Klla-Zyro	2926	3107	3537	381	361
Sakl-Klth	3152	3376	3961	93	93
Zyro-Klth	3313	3567	4116	247	240
Zyro-Sakl	3249	3508	4044	199	200

Table S1 Number of 2-level anchors (unrefined (UNR), longest (LON) and shortest (SHO) datasets), synteny blocks (SB) and multiplicons (MULT) on Hemiascomycete yeasts obtained by GRIMM-Synteny, SyDiG and i-ADHoRe, respectively.

genomes	UNR	LON	SHO	SB	MULT
Ergo-Sakl-Klth	174	184	440	324	63
Ergo-Zyro-Klth	214	202	441	439	5
Ergo-Zyro-Sakl	104	103	262	405	17
Klla-Ergo-Klth	320	181	353	490	8
Klla-Ergo-Sakl	348	211	387	484	8
Klla-Ergo-Zyro	314	162	345	554	2
Klla-Sakl-Klth	47	82	156	386	61
Klla-Zyro-Klth	112	87	170	480	1
Klla-Zyro-Sakl	98	124	296	472	16
Zyro-Sakl-Klth	89	187	247	284	83

Table S2 Number of 3-level anchors (unrefined (UNR), longest (LON) and shortest (SHO) datasets), synteny blocks (SB) and multiplicons (MULT) on Hemiascomycete yeasts obtained by GRIMM-Synteny, SyDiG and i-ADHoRe, respectively.

genomes	UNR	LON	SHO	SB	MULT
Ergo-Zyro-Sakl-Klth	0	0	14	465	83
Klla-Ergo-Sakl-Klth	4	4	20	542	63
Klla-Ergo-Zyro-Klth	17	3	21	619	6
Klla-Ergo-Zyro-Sakl	11	1	24	604	10
Klla-Zyro-Sakl-Klth	1	3	12	526	71

Table S3 Number of 4-level anchors (unrefined (UNR), longest (LON) and shortest (SHO) datasets), synteny blocks (SB) and multiplicons (MULT) on Hemiascomycete yeasts obtained by GRIMM-Synteny, SyDiG and i-ADHoRe, respectively.