

High Resolution Difference Bands of Ethane C2H6 from torsionally Excited Lower States: Rotation-Torsion Structure of the $\nu 2$, $\nu 11$ and $\nu 4 + \nu 11$ Vibrational States.

Carlo Di Lauro, Franca Lattanzi, Veli-Matti Horneman

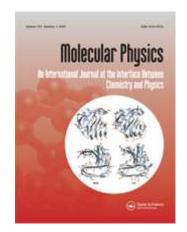
► To cite this version:

Carlo Di Lauro, Franca Lattanzi, Veli-Matti Horneman. High Resolution Difference Bands of Ethane C2H6 from torsionally Excited Lower States: Rotation-Torsion Structure of the $\nu 2$, $\nu 11$ and $\nu 4 + \nu 11$ Vibrational States.. Molecular Physics, 2011, pp.1. 10.1080/00268976.2011.614283 . hal-00736796

HAL Id: hal-00736796 https://hal.science/hal-00736796

Submitted on 30 Sep 2012

HAL is a multi-disciplinary open access archive for the deposit and dissemination of scientific research documents, whether they are published or not. The documents may come from teaching and research institutions in France or abroad, or from public or private research centers. L'archive ouverte pluridisciplinaire **HAL**, est destinée au dépôt et à la diffusion de documents scientifiques de niveau recherche, publiés ou non, émanant des établissements d'enseignement et de recherche français ou étrangers, des laboratoires publics ou privés.



High Resolution Difference Bands of Ethane C2H6 from torsionally Excited Lower States: Rotation-Torsion Structure of the v2, v11 and v4+v11 Vibrational States.

Journal:	Molecular Physics			
Manuscript ID:	TMPH-2011-0182.R1			
Manuscript Type:	Full Paper			
Date Submitted by the Author:	29-Jul-2011			
Complete List of Authors:	di Lauro, Carlo; University of Naples, retired Lattanzi, Franca; University of Naples Federico II, Medicinal Chemistry Horneman, Veli-Matti; University of Oulu, Physics			
Keywords:	high resolution infrared spectra, Infrared difference bands, Torsional splitting, Barrier to internal rotation, Torsional Coriolis coupling			
Note: The following files were submitted by the author for peer review, but cannot be converted to PDF. You must view these files (e.g. movies) online.				

figures.zip



High Resolution Difference Bands of Ethane C_2H_6 from torsionally Excited Lower States: Rotation-Torsion Structure of the v_2 , v_{11} and v_4+v_{11} Vibrational States.

Franca Lattanzi^a, Carlo di Lauro^{a*}, and Veli-Matti Horneman^b

^a Chimica Fisica, Università di Napoli Federico II, Via D. Montesano 49, I-80138 Napoli, Italy

b Departement of Physics, University of Oulu, Oulu, Finland

Corresponding author: Carlo di Lauro, Via Bonito 27/C, I-80129 Napoli, Italy. <u>car.dilauro@gmail.com</u>

Abstract

A high resolution Fourier transform infrared spectrum of C_2H_6 , measured with a pressure of 173.3 Pa and an optical path of 153.2 m, was analyzed between 1050 and 1295 cm⁻¹.

Extensive absorption due to the difference band v_{11} - v_4 , and several rotation-torsion lines of the difference band v_2 - v_4 , in the region of the x,y-Coriolis resonance of v_2 and v_{11} , were observed.

This allowed us to perform a detailed rotation-torsion analysis of the upper states v_{11} and v_2 .

The anomalous torsional structure, found in the non-degenerate vibrational state v_2 , can be explained as the effect of an Hamiltonian term accounting for a strong dependence of the torsional barrier height on the normal vibrational coordinate q_2 . The value of the barrier height derivative

 $\frac{\partial V_3}{\partial q_2}$ is estimated to be 127±10 cm⁻¹.

We also could detect and assign "hot" difference transitions belonging to the $(v_4+v_{11})-2v_4$ band, yielding information on the upper state v_4+v_{11} . We believe that transitions from $3v_4$ to $2v_4+v_{11}$ are also detectable in the investigated region.

Keywords

High resolution infrared spectra. Infrared difference bands. Torsional splitting.Barrier to internal rotation. Vibration-rotation Coriolis coupling. Torsional Coriolis coupling.

1. Introduction

Ethane is a key molecule owing to its highly symmetric geometry and peculiar internal rotation dynamics. It is also a relevant species in the applied research, because of its presence in the atmospheres of the Earth and outer planets, and in comets. For these reasons, the infrared active fundamental transitions of ethane have been extensively studied under high resolution, in spite of the particular complexity of the absorption spectrum, characterized by a high density of lines and anomalous rotation-torsion patterns generated by the interaction of several vibrational states, see Ref. [1-3] to mention only the most recent contributions. One may think that a detailed knowledge of the infrared inactive fundamental vibrational states under D_{3d} , the point group of the "rigid" staggered conformations) also occur in combination states that are involved in the complex interaction mechanisms affecting the observable absorption spectrum. Thus an accurate knowledge of the infrared inactive modes is quite helpful in the study of these complex mechanisms.

Owing to the selection rule $u \leftrightarrow g$ holding for electric dipole transitions, g-fundamental vibrational states cannot be reached from the vibrational ground state (which is a g-state), but only from lower u-states, in the so called difference transitions. The lowest u-vibrational state of ethane is the first excited torsional state v_4 , about 289 cm⁻¹ above the ground state, and this is the most favourable lower state for difference transitions, being the most populated u-state at the thermal equilibrium. Apart from the fact that the v_4 state is less populated than the ground vibrational state, there is another factor that makes the difference transitions quite weak: they imply the change of two units (at the least) in the vibrational quantum numbers. Thus difference bands normally can be observed only in spectral regions free from stronger absorption,

The spectral region of ethane between the high-frequency wing of the fundamentals v₉ (centered at 823 cm⁻¹) and the low-frequency wing of the fundamental v₈ (centered at 1472 cm⁻¹), approximately between 1000 and 1300 cm⁻¹, is quite free from absorption and then it is a favourable region for the observation of difference bands. There are two g-vibrational fundamentals observable in this spectral region, as upper states in difference transitions from v₄: They are v₂ (about 1397 cm⁻¹) with v₂-v₄ = ~ 1108 cm⁻¹, and v₁₁ (about 1468 cm⁻¹) with v₁₁-v₄ = ~ 1179 cm⁻¹.

Thus we decided to measure a high resolution Fourier transform infrared spectrum of ethane in the above spectral region, using a very long optical path, in the aim to measure and analyze the difference bands v_2 - v_4 and v_{11} - v_4 .

2. Experimental details

The experimental laboratory work was carried out in the Infrared laboratory at the University of Oulu with the BRUKER IFS 120 HR Fourier spectrometer. A C_2H_6 sample for laboratory use were obtained from Sigma-Aldrich. The studied weak absorption region from 940 to 1260 cm⁻¹ required a very long recording time, 127 hours, with the sample at the pressure of 173 Pa in a multi-pass sample cell [4] with the absorption path length of 153.2 m. In the measurement the cell was provided with two potassium bromide (KBr) windows, a glowbar source was used, a germanium film on KBr was employed as a beam splitter and the infrared radiation was detected with a liquid nitrogen cooled mercury cadmium telluride (MCT) detector. The instrumental resolution due to the maximum optical path difference of the interferometer was 0.0016 cm⁻¹. The aperture broadening was 0.0018 cm⁻¹ at 1100 cm⁻¹ . Together with the Doppler broadening these instrumental effects gave the final spectral resolution 0.002 cm⁻¹, near the lower wavenumber end of the spectral region, and 0.0029 cm⁻¹ near the higher end. All the spectra were calibrated using the transitions of carbonyl sulfide (OCS) in the 2v₂ band. [5].

3. Description of the spectrum

The dominant extended feature observed in the investigated spectral region, between 1040 and 1295 cm⁻¹, is a perpendicular band that can be easily identified as the difference band v_{11} - v_4 . In fact, the spacing of its Q-sub-branches is compatible with the value of the ζ -Coriolis constant expected for v_{11} , and the differences of P, Q and R combinations sharing the same upper state correspond to the appropriate rotational energy differences in the v_4 lower state. The *J*-structure of the Q-sub-branches degrades toward the high wavenumbers, because the *B*-rotational constant has a smaller value in the lower state, v_4 . The torsional splitting of the transition lines is of the order of 0.2 cm⁻¹ as in v_4 , but with opposite sign, showing that v_4 is the lower state and that the splitting in the upper state is considerably smaller. We could find and assign transitions of v_{11} - v_4 with $K''\Delta K$ from -17 to 14, denoting by K'' the absolute value of the quantum number associated with the total angular momentum component on the quantization axis, in the lower state. The ^rQ₃ sub-branch, with its two torsional components, is shown in Fig. 1.

Molecular Physics

The density of the spectral lines becomes quite low far in the low-wavenumber wing, so that we could observe and identify very weak features, down to $K''\Delta K = -17$. On the contrary, the line density remains high in the high-wavenumber wing, where the absorption due to the fundamentals v_6 and v_8 eventually starts. This is also due to the fact that "hot difference bands", mostly $(v_4+v_{11})-2v_4$ and $(2v_4+v_{11})-3v_4$, occur at higher wavenumbers than $v_{11}-v_4$, due to the large anharmonicity of the torsional mode v_4 . The fact that these "hot difference bands" are strong enough to be observed, can be understood by considering that the expressions for their transition of probabilities, contain the square the matrix element $\langle \mathbf{v}_4, \mathbf{v}_{11} = 0 | (\partial^2 \mu_{\alpha} / \partial \mathbf{q}_{11} \partial \mathbf{q}_4)_0 \mathbf{q}_{11} \mathbf{q}_4 | \mathbf{v}_4 - 1, \mathbf{v}_{11} = 1 \rangle$, with $\alpha = \mathbf{x}$ or y, and then they are proportional to v₄. Thus, assuming for v₄, $2v_4$, and $3v_4$ the estimated anharmonic values 289, 545 and 757 cm⁻ ¹, from transition probabilities and lower level populations one finds that that the strengths of $v_{11}-v_4$, $(v_4+v_{11})-2v_4$ and $(2v_4+v_{11})-3v_4$ are in the ratios 1.00: 0.58: 0.31 at 296 K.

We were able to identify several sub-branches of $(v_4+v_{11})-2v_4$. They show a large torsional splitting, about 4 cm⁻¹, mostly due to the lower state. Fig. 2 shows the ^rQ₃ sub-branch of $(v_4+v_{11})-2v_4$.

A few additional weaker Q-branches, which cannot be assigned to v_{11} - v_4 nor to (v_4+v_{11}) - $2v_4$, are apparent at even higher wavenumbers. We believe that they belong to $(2v_4+v_{11})$ - $3v_4$, on the basis of the intensity consideration of above.

The v_2 - v_4 parallel band is very weak. Its Q-branch transitions occur as an irregular dense series of weak lines, between 1003 and 1007 cm⁻¹, but no line assignments could be done. However, several P-transition lines, activated by the x,y-Coriolis interaction of v_2 and v_{11} near resonance, could be detected and identified for *K* between 10 and 15. This will be discussed in the next paragraph.

4. The energy matrix and perturbations.

In the analysis of the spectrum we considered for the upper state the vibrational levels v_2 (mainly symmetric CH₃ umbrella vibration of the two methyl groups, of A_{1s} symmetry under the extended molecular group G₃₆(EM), see Bunker and Jensen [6]) and v_{11} (mainly degenerate symmetric CH₃ deformation of the two methyl groups, of E_{2d} symmetry under the extended molecular group G₃₆(EM)). These two states are coupled by an x,y-Coriolis interaction, like the

corresponding asymmetric modes v_6 and v_8 [2]. Later on we realized that an additional x,y-Coriolis interaction, between the states v_{11} and v_3+2v_4 , helped to improve the fit.

Small torsional splitting in a given vibrational state was accounted for as usual by the oneparameter expression [7, 8]

$$v^{0}(\vec{v}, \Gamma_{t}) = v^{0} - 2(-1)^{V_{4}} X_{v} \cos(\sigma 2\pi/6) .$$
⁽¹⁾

where \bar{v} represents the ensemble of vibrational quantum numbers, inclusive of the torsionalvibration quantum number v₄, X_v is a generally positive parameter whose value increases rapidly with v₄, but depends also on the excitation of the small amplitude vibrational modes, and $\sigma = 0, 1,$ 2, 3 for the components of torsional symmetries $\Gamma_t = A_{1s}$ (or A_{3s}), E_{3d} , E_{3s} and A_{3d} (or A_{1d}), using A_s and E_d vibrational basis functions. For larger splittings, a v⁰-value has to be determined for each of the four torsional components. Note that the components A_{1s} and A_{3d} occur with the even values of v₄, whereas the components A_{3s} and A_{1d} occur with the odd values of v₄. The torsional splitting in the v₂ state is rather anomalous and we had to use four different values v⁰ for the the different torsional components A_{1s}, E_{3d}, E_{3s} and A_{3d} , Diagonal matrix elements were given as usual by

$$E [(\vec{v}, \Gamma_{t}, (\pm l), J, K] = v^{0}(\vec{v}, \Gamma_{t}) + (A - B)K^{2} + BJ(J + 1)$$

- $D_{J}J^{2}(J + 1)^{2} - D_{JK}J(J + 1)K^{2} - D_{K}K^{4}$
 $\mp [2A\zeta - \eta_{J}J(J + 1) - \eta_{K}K^{2}]K$ (2)

In the off-diagonal matrix elements, the torsional symmetries of interacting states depend on the specific states and on the shifts of quantum numbers. They can be determined following the procedures of Ref. [9].

The *l*-interaction with $\Delta k = \Delta l = \pm 2$, henceforth referred to as l(2,2), was taken into account within the state v_{11} , with matrix elements

$$\left\langle \vec{v}_{s}, \Gamma_{t}, l = \pm 1, J, k \pm 1 \middle| \boldsymbol{H} \middle| \vec{v}_{s} \Gamma_{t}, l = \mp 1, J, k \mp 1 \right\rangle$$
$$-2(F + k^{2}F_{K}) \left\{ \left[J(J+1) - k(k+1) \right] \left[J(J+1) - k(k-1) \right] \right\}^{1/2}$$
(3)

The x,y-Coriolis interaction was considered in the vibrational pairs v_2 and v_{11} and v_3+2v_4 and v_{11} , with matrix elements

$$\left\langle \vec{v}_{s}, \Gamma_{t}, l = \pm 1, J, k \pm 1 \middle| \boldsymbol{H} \middle| \vec{v}_{r}, \Gamma_{t}, l = 0, J, k \right\rangle = \\ \pm 2^{1/2} \left[Z_{r,s} + Z_{r,sJ} J(J+1) \right] \left[J(J+1) - k(k\pm 1) \right]^{1/2}$$
(4)

The *l*-type interactions with $\Delta l = \pm 2$ and $\Delta k = \mp 1$, henceforth referred to as *l*(2,-1), within the state v₁₁ occurs with matrix elements

$$\left\langle \mathbf{v}_{11}, \ \mathbf{\Gamma}_{\mathbf{t}}, \ l = \pm 1, \ J, k \left| \boldsymbol{H} \right| \mathbf{v}_{11}, \ \mathbf{\Gamma}_{\mathbf{t}} \times \mathbf{A}_{3d}, l = \mp 1, \ J, k \pm 1 \right\rangle = (E + k^2 E_K) \left(2k + 1\right) \left[J(J + 1) - k(k \pm 1) \right]^{1/2}$$
(5)

Fig. 3 shows the Coriolis interactions of v_{11} with the parallel vibrational states v_2 and v_3+2v_4 , in the region of the resonance. We could detect and assign P-transitions from v_4 to v_2 , enhanced by the mixing of v_2 and the (-*l*)-side of v_{11} , in the region near the resonance (*K* from 10 to 15), see Fig. 4. For *K* equal to 12 and 13 both stronger and weaker transitions to the split torsional components of v_2 were observed.

Fig. 3 also shows that the levels of v_{11} which can be coupled by an interaction with $\Delta l = \pm 2$ and $\Delta k = \pm 1$ (l(2,-1) coupling) are always rather close to each other. Their energy separation is also influenced by the effect of the concomitant x,y-Coriolis interactions.

Some peculiar effects on the spectrum of these Coriolis perturbations are opposite to those described by di Lauro and Mills [10], because of the asymmetry of the lower vibrational state v_4 with respect to a reflection through a plane σ_{xz} containing the molecular z-axis, and its bearing on selection rules. In fact, if we denote by \pm the symmetrized vibration-rotation functions defined as

$$\left|\pm\right\rangle = \left(\left|K,l\right\rangle \pm \left|-K,-l\right\rangle\right)/\sqrt{2}, \qquad (6)$$

the vibration-rotation electric dipole selection rules (asymmetric \leftrightarrow symmetric with respect to σ_{xz}) are $+\leftrightarrow$ - for Q-transitions and $\pm\leftrightarrow\pm$ for P and R-transitions, contrary to what would hold for transitions from a symmetric lower state. As a consequence of this, the above x,y-Coriolis

interactions have no effect on the ${}^{r}R_{0}$ and ${}^{r}P_{0}$ sub-branches of v_{11} and a larger effect than elsewhere (by a factor $\sqrt{2}$ in the matrix elements) on the sub-branch ${}^{r}Q_{0}$, see also Ref. [2].

Fig. 5 shows the *l*-type interaction mechanisms acting within the v_{11} state. The *l*(2,2) interaction $(\Delta k = \Delta l = \pm 2)$ is always resonant for the *l*=*k*=±1 pair, causing its splitting into the symmetrized combinations as in Equation (6). This splitting is transmitted to the *l*=∓1, *k*=±2 pair by the *l*(2,-1) interaction $(\Delta l = \pm 2, \Delta k = \mp 1)$, with the coupling selection rule +↔-. Thus the transition lines with *K*" ΔK =-3, ending to the above levels, appear each with four components, owing to the simultaneous effects of torsional and *K*-splitting, see the ^pQ₃-transitions in Fig. 6.

This interaction mechanism and the *K*-doubling of the $K''\Delta K=-3$ levels in v_{11} is quite similar to what has been observed in v_8 , see Ref. [2]. However the effects on the spectrum are different, because in the present case the lower state is v_4 (asymmetric with respect to the reflection through the mentioned symmetry plane σ_{xz}) instead of the ground state. In fact, in the present case the selection rules in the + and – labels are $\pm \leftrightarrow \pm$ for transitions with even $\Delta K + \Delta J$, and $+ \leftrightarrow \pm$ for transitions with odd $\Delta K + \Delta J$, contrary to what holds for the v_8 fundamental. The details are discussed in the Appendix of Ref. [2].

The l(2,2)-splitting in the $l=k=\pm 1$ pair increases with *J*, and eventually its – component crosses the + component with $k=\pm 2$ coupled to it by the l(2,-1) interaction, inverting the sign of the level displacements, see Fig. 5. This happens at J=15, and the most evident effect is a sudden change of the *J*-spacing from J=14 to J=15 (an increase of the spacing in the ^rQ₀ sub-branch, and a decrease in the K+ components of ^pQ₃, see Fig. 6). Because of the effect of this crossing, K+ is higher than K- up to K=14 included, and then becomes lower, This can be easily checked in Fig, 6, because the K+ transitions are stronger for odd *J* and the K- transitions for even *J*, for each torsional symmetry.

The effect of the *J*-crossing between 14 and 15 is also detectable in the sub-branch ${}^{r}Q_{0}$, where the displacements of the levels with *J*= 14 and 15 are obviously opposite to those observed in ${}^{p}Q_{3}$, see Fig. 7. The strong level mixing near resonance can activate transitions with $\Delta K = \pm 2$, an in fact we could observe three ${}^{s}Q_{0}$ transitions ($\Delta K = 2$), at *J*=14 (for the stronger torsional component) and *J*=15 (for both torsional components), also shown in Fig. 7.

5. Analysis and results.

The body of data processed in an iterative least squares calculation, according to the Hamiltonian model of the previous paragraph, consisted of wavenumbers corresponding to 1386 different

Molecular Physics

rotation-torsion upper states belonging to the v_{11} and v_2 vibrational states. Namely, we used 1277 wavenumbers of the v_{11} - v_4 transition (^PP-transitions for *K*" ΔK from -1 to -17, ^rR-transitions for *K*" ΔK from 0 to 14, ^rQ₀ transitions, and three ^sQ₀ transitions, with a maximum *J*-value of 37) and 109 wawenumbers of the v_2 - v_4 transition (^qP-transitions activated by the x,y-Coriolis resonance of v_2 with v_{11} , for *K* from 10 to 15 and a maximum *J*-value of 28). As mentioned, we considered also the state v_3 +2 v_4 , as a Coriolis perturber of v_{11} . The account for an anharmonic interaction of v_2 and v_3 +2 v_4 did not improve the fit, and this interaction was disregarded. Eventually the iterative calculations converged to a root mean square (RMS) deviation of 2.52×10⁻³ cm⁻¹, with the parameter values reported in Table 1.

Due to the lack of data relative to v_3+2v_4 , we could determine only the values of v° , *X*, *A* and *B* for this vibrational state.

The v_{11} state

The values of the parameters for this state (mainly symmetric deformation of the two methyl groups) are rather similar to those found for v_8 (mainly asymmetric deformation of the two methyl groups) in Ref. [2]. This holds also for the *l*-type interaction parameters (*F* and *E*), and in fact these interactions are quite important in both vibrational states. However, the infrared active fundamental band v_8 appears much more complex than the difference band v_{11} - v_4 , because of the effect of the combination state v_4+v_{12} occurring quite close to v_8 . Also in v_{11} the torsional splitting is considerably smaller than in non-degenerate states in the torsional lowest state (*X*=0.00110 cm⁻¹, against the ground state value of 0.00189 cm⁻¹) as expected from theory, see [11] and references therein. The x,y Coriolis interaction between v_{11} and v_2 is quite similar to that between v_8 and v_6 (v_2 and v_6 are mostly symmetric and asymmetric umbrella vibrations of the two methyl groups). The mechanisms generating the *K*-doubling of the levels $k=\pm 2$, $l=\mp 1$ in v_{11} and v_8 [2] are quite similar: In v_{11} too the splitting can be accounted for by the combined effect of the *l*(2,2) and *l*(2,-1) interactions, as already discussed, without considering an effective direct interaction ($\Delta K=\pm 4$, $\Delta l=\mp 2$) within the vibration-rotation components of the doublet.

The values of the parameters of v_{11} determined by Fernández and Montero from the Raman spectrum [12] (v^0 =1468.4, A=2.6575, B=0.66666, A ζ = -0.8886, all in cm⁻¹), are in reasonable agreement with ours.

Although the observation of transitions to the v_2 state is limited to the *K*-range between 10 and 15, near the Coriolis resonance with v_{11} , the parameters of the v_2 state could be determined quite well. In fact, it is worth to note that the body of observed ^pP-transitions to v_{11} brings information on v_2 even beyond the mentioned *K*-range, because of the interaction of the two states.

The torsional splitting of v_2 is rather complex, and cannot be accounted for by the simple oneparameter expression of Equation (1). In fact, we had to use four independent vibrational origins for the torsional components, see Table 1. The values determined for these four vibrational origins in v_2 agree with their displacements predicted for the interaction with the torsional manifold correlating with $6v_4$, as shown in Fig. 8.

The anomalous torsional pattern in v_2 is generated by the same mechanism causing a similar effect in v_3 , and explained by Bermejo et al. [13]. The mechanism involves the linear dependence of the torsional barrier parameter V_3 on the normal coordinate q_2 .

Using a simple approximation, we write the torsional Hamiltonian as

$$\boldsymbol{H}_{\text{tors.}} = \boldsymbol{H}_0 + \boldsymbol{H}' \tag{7}$$

with

$$H_0 = A \mathbf{J}_{\tau}^2 + \frac{1}{2} \mathbf{V}_3^0 (\cos 3\tau + 1) + \frac{1}{2} \mathbf{V}_6 (\cos 6\tau - 1)$$
(8)

and

$$\boldsymbol{H}' = \left(\frac{\partial \mathbf{V}_3}{\partial \mathbf{q}_2}\right)_0 \mathbf{q}_2 (\cos 3\tau + 1) \tag{9}$$

assuming that the torsional angle τ is zero in the conformation of maximum energy (eclipsed). A term (9) is allowed by symmetry for each totally symmetric normal coordinate (A_{1s} symmetry under the extended molecular group G₃₆(EM), that is q₁, q₂ and q₃). The anomalous torsional pattern in v₂ is caused by the term (9), therefore we tried to determine the value of the barrier

derivative $\left(\frac{\partial V_3}{\partial q_2}\right)_0$. Starting with a free internal rotor basis, we calculated the torsional eigenfunctions of H_0 , for v₄ up to 8, with $A=2.674677 \text{ cm}^{-1}$, $V_3 =1013.28 \text{ cm}^{-1}$ and $V_6 =8.798 \text{ cm}^{-1}$. Using the eigenvectors, we also calculated the matrix elements of (cos3 τ +1), needed in the final calculation, in the basis of the eigenfunctions of H_0 . Then we built up the final matrix, on the basis of the functions (v₂=0,v₄,\Gamma_t), (v₂=1,v₄,\Gamma_t) and (v₂=2,v₄,\Gamma_t), with v₄ varying from 0 to 8.

We assumed that the eigenvectors of these basis functions, in terms of the free internal rotor functions, were independent of the value of v_2 . The matrix factors into four blocks, corresponding to the different symmetry species Γ_t , that is E_{3s} , E_{3d} , A_{1s} or A_{1d} , and A_{3d} or A_{3s} (A_{1s} and A_{3d} occur for even v_4 and A_{1d} and A_{3s} occur for odd v_4). Owing to the operator \mathbf{q}_2 and its selection rules, the matrix elements of \mathbf{H}' link the functions with $v_2=1$ to those with $v_2=0$ and

v₂=2. They contain the value of the derivative $\left(\frac{\partial V_3}{\partial q_2}\right)_0$, to be determined. The vibrational origins,

 $v_2(\Gamma_t) - v_4(\Gamma_t \times A_{3s})$, were calculated by diagonalization of the four matrix blocs, as eigenvalue differences $E(v_2=1,v_4=0,\Gamma_t) - E(v_2=0,v_4=1,\Gamma_t \times A_{3s})$. They were compared to the values determined from the analysis of the spectrum, and the value of the derivative $\left(\frac{\partial V_3}{\partial q_2}\right)_0$ was iteratively adjusted by the least squares procedure.

Using a dimensionless normal coordinate q_2 , we eventually found $\left(\frac{\partial V_3}{\partial q_2}\right)_0 = 127 \pm 10 \text{ cm}^{-1}$, the

large uncertainty being mostly related to the approximations involved in the calculations. This value is considerably smaller (in the absolute value) than the barrier derivative with respect to q_3 determined by Bermejo et al. [13], -276 cm⁻¹, in agreement with the theoretical predictions of Kirtman et al. [14]. We note that the relative shifts of the four components of v_2 are actually determined by the interaction with the manifold $6v_4$ shown in Fig. 7, owing to the resonance conditions. However a considerable global shift toward the low energy is caused by the interaction with the levels ($v_2=2,v_4=0, \Gamma_t$), because of the large matrix elements.

6. "Hot" difference bands: $(v_4+v_{11}) - 2v_4$.

We could identify transitions from $2v_4$ to v_4+v_{11} , with $K''\Delta K$ from -2 to 9. The bias of this range, in favour of the positive values, is due to the fact that the origin of the band $(v_4+v_{11})-2v_4$ is higher than that of $v_{11}-v_4$ by about 34 cm⁻¹. Therefore the sub-branches of this "hot" difference band with positive values of $K''\Delta K$ move to the high wavenumbers, far from the center of $v_{11}-v_4$, as K'' increases. On the contrary, the sub-branches with negative $K''\Delta K$ move to the crowded center of the stronger $v_{11}-v_4$, and become hardly detectable. The line assignment, very difficult at the beginning, became easier when the values of the lower state *J*-structure parameters could be guessed from the line assignments already acquired.

In Table 2 we report the values of the rotational constants for the different torsional components of the $2v_4$ state, eventually determined from the differences of the observed wavenumbers of transitions sharing the same rotation-torsion level of v_4+v_{11} . Pairs whose calculated and observed differences deviated by more than 0.001 cm⁻¹ were disregarded.

We also calculated values of B, D_J and D_{JK} assuming that they were equal in all torsional components. They are reported in the last column of Table 2.

A simple explorative least squares fit calculation of the observed wavenumbers showed that the levels of the stronger torsional component of the v_4+v_{11} state with $k=\pm 2$, $l=\pm 1$ are heavily perturbed. Even excluding transitions to these levels from the body of data, we could obtain a fit of the observed data with a RMS deviation of 0.028 cm⁻¹, showing that a rather sophisticated model would be needed to try to analyze this state. We believe that the $(v_4+v_{11})-2v_4$ system would be conveniently analyzed together with the v_4+v_{11} combination transition, having a common vibrational upper state. The latter has been studied by Susskind [7], but under the resolution of a grating spectrometer.

7. Conclusions.

Although the v_{11} and v_2 fundamentals of C_2H_6 are infrared inactive, a high resolution rotationtorsion analysis of these vibrational states has been performed through the investigation of the relative difference bands from the v_4 torsional state. The detailed knowledge of these states can be relevant also in the applied research, because they can occur in infrared active combinations perturbing the absorption regions of atmospheric and planetary interest. In particular, the detailed knowledge of the infrared inactive v_{11} and v_2 , together with the corresponding active modes v_8 and v_6 , can be useful for the study of the 7 micron spectral region of ${}^{13}C^{12}CH_6$, expected to be quite similar to that of the main 12,12 isotopomer, but with all these four fundamentals active, because of the lowered symmetry.

The observation of the "hot" difference $(v_4+v_{11})-2v_4$ provides informations both on the lower state $2v_4$ and on the upper state v_4+v_{11} .

References

[1] J.R. Cooper, N. Moazzen-Ahmadi, J. Mol. Spectrosc. 239 (2006) 51-58.

[2] F. Lattanzi, C. di Lauro, J. Vander Auwera, Mol. Phys. in press,

[3] C. di Lauro, F. Lattanzi, J. Vander Auwera, J. Mol. Spectrosc. 267 (2011) 71-79.

Molecular Physics

- [4] T. Ahonen, S. Alanko, V.-M. Horneman, M. Koivusaari, R. Paso, A.-M. Tolonen, and R.
- Anttila, J. Mol. Spectrosc. **181** (1997) 279 286.
- [5] V.-M. Horneman, J. Opt. Soc. Am. B 21 (2004) 1050-1064.
- [6] P.R. Bunker, P. Jensen, Molecular Symmetry and Spectroscopy, Second ed., NRC
- ResearchPress, Ottawa, 1998.
 - [7] J. Susskind, J. Mol. Spectrosc. 49 (1974) 1-17.
 - [8] J. T. Hougen, J. Mol. Spectrosc. 82 (1980) 92-116.
 - [9] C. di Lauro, F. Lattanzi, A. Valentin, Mol. Phys. 89 (1996) 663-676
 - [10] C. di Lauro, I.M. Mills, J. Mol. Spectrosc. 21 (1966) 386-413.
 - [11] C. di Lauro, F. Lattanzi, Mol. Phys. 103 (2005) 697-708.
 - [12] J.M. Fernández-Sánchez, S. Montero, J. Chem. Phys. 118 (2003) 2657-2672.
 - [13] D. Bermejo, J. Santos, P. Cancio, J.M. Fernández-Sánchez, S. Montero, J. Chem. Phys. 97 (1992) 7055-7063.
 - [14] B. Kirtman, W.E. Palke, C S. Ewig, J. Chem. Phys. 64 (1976) 1883-1890.



Legends of Tables

Table 1

Vibration-rotation-torsion parameters in cm⁻¹ determined for the vibrational states v_{11} , v_2 and v_3+2v_4 . Numbers in parentheses are standard deviations in units of the last quoted digit.

Table 2

Values in cm⁻¹ of the rotational constants B, D_J and D_{JK} determined for the torsional components

of $2v_4$, See text.

Table 1

	v_{11}	v_2	$v_3 + 2v_4$	ν_4
,°	1467.99167 (22)		1541.403 (690)	289 ^a
K	0.00110 (5)		1.2530 (585)	0.07870^{a}
$V^{\circ}(A_{1s})$		1396.53269 (710)		
$\nu^{\circ}(E_{3s})$		1396.51036 (791)		
$v^{\circ}(E_{3d})$	0	1396.54163 (751)		
$v^{\circ}(A_{3d})$		1396.51334 (820)		
4	2.6594550 (515)	2.6756371 (827)	2.64684 (506)	2.669693 ^b
3	0.66451488 (126)	0.6612137 (115)	0.652705 (236)	0.6604969 ^b
$0^5 \times D_J$	0.106149 (199)	0.104302 (762)	0.103174 ^c	0.10231 ^b
$0^5 \times D_{JK}$	0.23273 (100)	0.25602 (651)	0.26604 ^c	0.2726 ^b
$0^5 \times D_K$	0.89205 (233)	0.9178 (243)	0.885 ^c	0.885 ^b
$A\overline{\zeta}$	-0.8956103 (198)			
$0^6 \times \eta_J$	0.691 (102)			
$0^4 \times \eta_K$	-0.50880 (279)			
$10^3 \times F$	0.203976 (366)			
$0^5 \times F_K$	0.1081 (98)			
$0^2 \times E$	0.173046 (633)			
$0^6 \times E_K$	-0.4134 (359)			
$Z_{2.11}$	= 0.3320924(309),	$10^5 \times Z_{J2,11} = -0.218$	$36(99), Z_{344,11} = 0$.011287 (121)

^a Assumed

^b Ref. [2] ^c As in the

As in the vibrational ground state, Ref. [2]

Table 2

	A _{1s}	E _{3d}	E _{3s}	A _{3d}	All
n. data ^a	14	47	58	44	77
$K''\Delta K$	6	1, 3, 5, 7	-2, 2, 4, 8	-3, 1, 3, 9	-3 to 9
J _{max}	20	19	22	21	22
В	0.65810	0.658106	0.658187	0.658225	0.658179
$10^5 \times D_J$	0.1364	0.1021	0.1019	0.1010	0.1006
$10^5 \times D_{JK}$		0.2651	0.2770	0.2784	0.3050

^a number of combination differences used in the calculation.

Fig. 1

^rQ₃ sub-branch of v_{11} - v_4 , showing the *J*-structure and the splitting into the two components with torsional symmetries A_{1d} (stronger) and E_{3d} (weaker) in the lower state. Transmittance in arbitrary units is reported on the ordinates.

Fig. 2

Component of torsional symmetry A_{3d} in the lower state (stronger torsional component) of the ${}^{r}Q_{3}$ sub-branch of $(v_{4}+v_{11})-2v_{4}$. The weaker torsional component, E_{3d} , occurs about 4 cm⁻¹ at the higher wavenumbers.

Fig. 3

Coriolis interactions about the x,y axes of v_{11} with the parallel vibrational states v_2 and v_3+2v_4 , shown as solid lines connecting interacting pairs of levels. Resonance occurs at *K* between 12 and 13 in v_2 (with the (-*l*)-side of v_{11}) and between 11 and 12 in v_3+2v_4 (with the (+*l*)-side of v_{11}). Dotted lines connect pairs of levels of v_{11} interacting by l(2,-1) coupling, with $\Delta l=\pm 2$ and $\Delta k=\mp 1$. The energy levels have been calculated for J=15 at several values $\pm K$, with disregard of these Coriolis interactions (zero-order energies).

Fig. 4

P-transitions from v_4 to v_2 with torsional splitting, identified as K_J (quantum numbers of the lower state), for K=11, 12, 13. They are made observable by intensity stealing from the stronger transitions from v_4 to v_{11} , in the region of near Coriolis resonance of v_2 and v_{11} . See text.

Fig. 5

l-type interactions in the v_{11} vibrational state of ethane. The l(2,2) interaction causes the splitting of the $l=k=\pm 1$ pair, which is transmitted to the $l=\mp 1$, $k=\pm 2$ pair by the l(2,-1) coupling, see text.

Fig. 6

 ${}^{p}Q_{3}$ sub-branch, showing the effects of torsional and K-splitting. The split K₊ and K₋ components are defined according to Equation (6), applied to the upper state wavefunctions, see text and Fig. 5. The torsional splitting (A_{1d} and E_{3d} components in the lower state) is almost constant, whereas the K-splitting increases with the total angular momentum quantum number *J*. The K+ and K- components show opposite intensity alternations with the parity of *J*, the former being stronger at the odd values and the latter at the even values. Note the small separation of the lines with *J* equal to 14 and 15 in K+, and the inversion of the relative positions of K+ and K-starting at *J*=15. See text, and Fig. 5 and 6.

Fig. 7

^rQ₀ sub-branch of v_{11} - v_4 , showing the torsional splitting (A_{3s} and E_{3s} torsional symmetries in the lower state) and the typical intensity alternation with the parity of *J*. These transitions occur to the components – of the *l*-doublets with $k = l = \pm 1$. Note the large separation between the lines with *J* equal to 14 and 15, caused by the *J*-crossing in a *l*(2,-1) resonance, and the s-type transitions (ΔK =2), marked by a prime, activated by this resonance at *J*= 14 and 15. See text and Fig. 5 and 7.

Fig. 8

Splitting induced in the v_2 state by the interaction with the nominal $6v_4$ state, exhibiting large torsional splittings. The interaction matrix elements are represented by dotted lines, and the relative displacements induced on the torsional components of v_2 (much exaggerated) are qualitatively represented by arrowed lines. The pattern of the torsional components of v_2 , in the order of increasing energies, becomes E_{3s} , A_{3d} , A_{1s} , E_{3d} . See text.

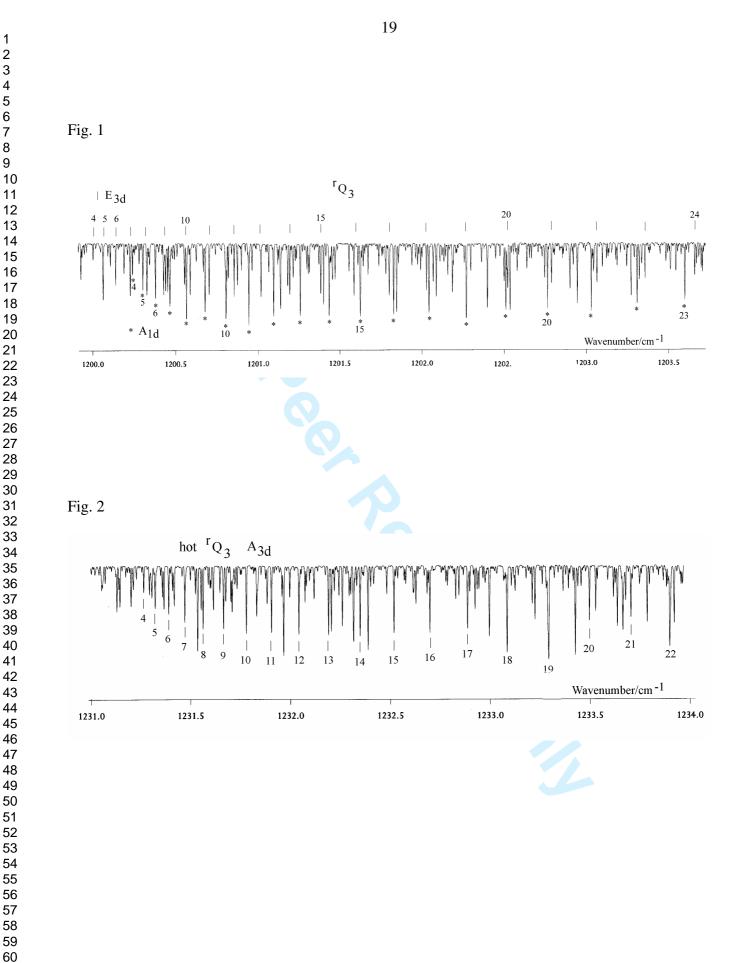
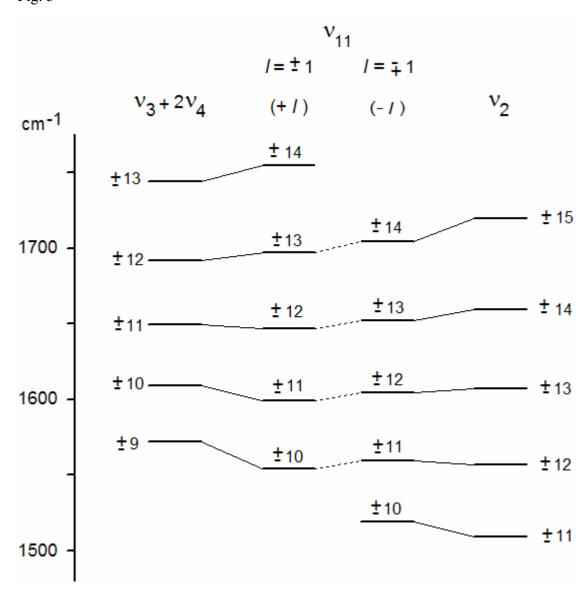
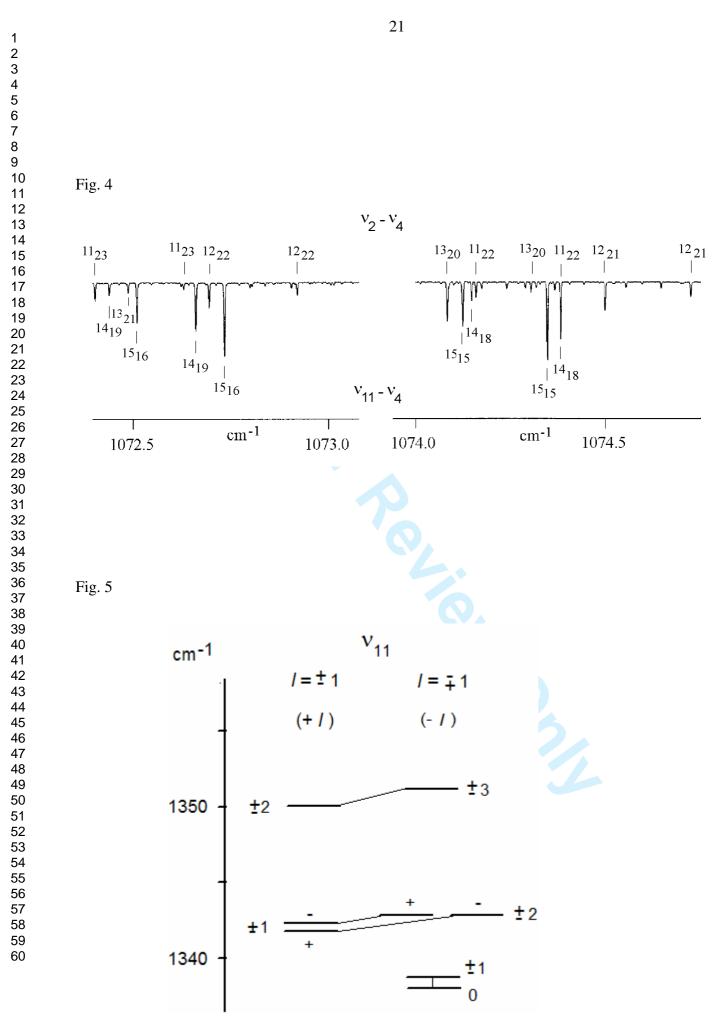


Fig. 3





URL: http://mc.manuscriptcentral.com/tandf/tmph



