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PAGAI: a path sensitive static analyzer

Julien Henry    David Monniaux    Matthieu Moy

July 17, 2012

Abstract

We describe the design and the implementation of PAGAI, a new static analyzer working over the LLVM compiler infrastructure, which computes inductive invariants on the numerical variables of the analyzed program.

PAGAI implements various state-of-the-art algorithms combining abstract interpretation and decision procedures (SMT-solving), focusing on distinction of paths inside the control flow graph while avoiding systematic exponential enumerations. It is parametric in the abstract domain in use, the iteration algorithm, and the decision procedure.

We compared the time and precision of various combinations of analysis algorithms and abstract domains, with extensive experiments both on personal benchmarks and widely available GNU programs.

1 Introduction

Sound static analysis automatically computes properties on programs, such as the possible values of their variables during execution. Applications include: showing that a program cannot encounter a runtime error (such as arithmetic overflow, division by zero, array access out of bounds), as in e.g. the Astrée analyzer [7]; computing invariants for use with assisted proof systems (such as the B method [1]), thereby lessening the burden on the user; computing invariants for advanced optimization techniques in compilation (e.g. showing that two array cells are distinct, in order to allow instruction reordering between assignments to these cells). All these applications need invariants on numerical quantities.

This article introduces PAGAI, a new tool for fully automatic static analysis. PAGAI takes as input a program in the “bitcode” intermediate representation of LLVM [13, 14], a modern compilation framework. LLVM bitcode is a target for several industrial-strength compilers, most notably Clang (supporting C, C++, Objective-C and Objective-C++) and llvm-gcc (supporting, in addition to these, Fortran and Ada); furthermore, a growing number of analysis tools, testing tools, etc. are currently built around this platform (Calysto, KLEE, LAV, LLBMC).
The output of PAGAI is a list of inductive invariants for a selected subset of the control nodes of the original program: for structured source programs, PAGAI will provide an inductive invariant for loop headers.

At present, PAGAI checks user-specified safety properties provided through assertions using the standard C/C++ `assert(condition)` macro. The tool will attempt proving that the assertion failure is unreachable and, if unsuccessful, provide a warning message (the tool does not at present include bounded model checking or path exploration techniques for reconstructing an actual failure trace, thus such a warning message should be interpreted as a possible assertion failure). It also allows user-specified assumptions, through the `assume(condition)` macro. Executing traces falsifying assertions or assumptions are considered to terminate when executing the macro; thus, user-specified assertions may be used to guide the analyzer by providing invariants that it was not able to synthesize by itself. Possible extensions could include checking for memory safety of array accesses.

PAGAI is based on abstract interpretation, a general framework for fully automatic static analysis. PAGAI infers invariants of a selected form; by default it performs linear relation analysis, which obtains invariants as conjunctions of linear inequalities (or, equivalently, convex polyhedra), but it also supports other abstract domains through a runtime option. Depending on the iteration algorithm selected, PAGAI may also infer invariants as disjunctions of elements of the abstract domain (e.g., unions of convex polyhedra).

Textbook descriptions of abstract interpretation-based static analysis state that an inductive invariant is computed at every control point of the program. In contrast, PAGAI abstracts straight-line sequences of statements en bloc, computing invariants only at points where control flow branches or merges. Furthermore, several algorithms implemented in PAGAI compute invariants only at the heads of loops (or, in general control-flow graph, at nodes forming a feedback vertex set, whose removal breaks all cycles in the graph), expanding the rest of the control flow to a possibly exponential number of straight-line sequences of statements between the selected nodes. In order to avoid explicit enumerations of exponential sets, PAGAI uses decision procedures for arithmetic theories, based on the satisfiability modulo theory (SMT) approach: each path is enumerated only if needed, in response to a positive satisfiability query.

The PAGAI tool is dedicated to experimenting with new analysis algorithms. It allows independent selection of the abstract domain and the iteration strategy, and partially independent selection of decision procedure and thus is well-suited for comparisons. We thus conducted extensive experiments both on examples we produced ourselves (sometimes inspired by industrial code) and on

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1 A preliminary analysis pass selects a subset of nodes that cuts all cycles in the control-flow graph, by selecting all targets of return edges in a depth-first search traversal; when applied to a structured program, it selects loop headers.

2 Certain abstract domains express relationships, such as linear congruences, that certain decision procedures cannot deal with. It is at present necessary that the decision procedure reflects semantics at least as precise as those of the abstract domain. This limitation will be lifted in the future.
GNU programs, for which the ability to run on any C or C++ code, through the LLVM system, was especially useful. Front-ends for many analysis tools put restrictions (e.g. no backward goto instructions, no pointer arithmetic...), often satisfied by safety-critical embedded programs, but not by generic programs; our tool suffers no such restrictions, though it may in some cases apply coarse abstractions which may possibly yield weak invariants.

After illustrating the limitation of traditional abstract interpretation on an example in section 2, we will describe PAGAI’s implementation in section 3, and comment on the results of extensive experiments in section 4, allowing the comparison of state of the art techniques on real-life programs.

2 Motivating Example

In most forward abstract interpretation-based analyses, when control flows from several nodes into a single node, the abstract value at that node is obtained by computing the least upper bound of the incoming abstract values in the abstract domain (in backward analysis, this occurs when control flows from a single node to several nodes). If the abstract domain is convex polyhedra, then this means computing the convex hull of the incoming polyhedra. Such an operation may induce unrecoverable loss of precision by introducing spurious states that cannot occur in concrete program runs.

An example of program where such a loss of precision occurs is depicted in Fig. 1. In this program, the loop body has two feasible paths that are executed alternatively, depending on a variable “phase”. Such programs, with active code paths depending on global “mode” or “phase” variables, often occur in reactive systems.

Removing program point \( n_0 \) breaks all cycles; we are thus primarily concerned with obtaining an inductive invariant at that point. We consider the domain of convex polyhedra and thus wish to obtain this invariant as a polyhedron. Because convex polyhedra form a lattice of infinite height, we use Kleene iterations (pushing abstract values through control-flow edges) with a widening scheme, which ensures convergence in finite time to an inductive invariant, followed by decreasing (narrowing) iterations.

At program point \( n_5 \), classical forward abstract interpretation with convex polyhedra computes the convex hull of three incoming polyhedra over variables (phase, x, t). This convex hull introduces extra states, unreachable in the concrete programs, for the analysis of the fragment from \( n_5 \) to \( n_9 \). When analyzing the whole loop, these extra states prevent proving \( x < 100 \).

To cope with this problem, a solution is to compute disjunctive invariants at all intermediate nodes: at \( n_5 \), keep an explicit list of three polyhedra, and thus obtain a list of nine polyhedra at \( n_9 \). We pass the convex hull of these polyhedra to the widening operator at point \( n_0 \) (which operates on polyhedra, not on lists of polyhedra). The drawback is that the number of elements in the lists may grow exponentially with the number of successive tests.

A second solution, equivalent to the preceding with respect to final results
but different in its operation, is to distinguish all nine paths inside the loop (from $n_0$ to $n_9$), compute the final outcome of each path, and compute the convex hull of these outcomes. Instead of enumerating all nine paths explicitly, we consider them in succession, only as needed. We start with an empty polyhedron at $n_9$ (more generally, it should contain initial states at this control point), and process paths as long as they make this polyhedron grow. The next path to consider is obtained from a model of an arithmetic formula expressing this growth condition $[16]$; if this formula is unsatisfiable, this means there is no such path and thus the convex hull encompasses the outcome of all paths.

The advantages of this second method over the preceding one are twofold: there is no exponentially large list of abstract elements, and the satisfiability query for the formula is handed over to a *satisfiability modulo theory* (SMT) solver. Modern SMT-solvers are very efficient; their caching mechanisms may, for instance, remember that taking a certain branch in the code is incompatible with taking another one (if a Boolean is associated with passing through each branch, then this is just a *blocking clause* inside the underlying SAT-solver). The algorithms implemented in PAGAI are variants of this approach of implicitly representing of exponentially-sized sets of paths and enumerating them as needed.

```c
int x = 0;
int t = 0;
int phase = 0;

while (t < 100) {
    if (phase == 0)
        x = x + 2;
    else
        x = x - 1;
    phase = 1 - phase;
    t++;
}
assert (x <= 100);
```

Figure 1: Example of program, where the loop behaviour vary depending on a variable *phase*. 
Table 1: List of analyzed open-source projects, with their respective number of lines of code, and their number of control points in $P_R$

| Name       | kLOC | $|P_R|$ |
|------------|------|------|
| a2ps       | 55   | 2012 |
| gawk       | 59   | 902  |
| gnu chess  | 38   | 1222 |
| gnugo      | 83   | 2801 |
| grep       | 35   | 820  |
| gzip       | 27   | 494  |
| lapack/blas| 954  | 16422|
| make       | 34   | 993  |
| tar        | 73   | 1712 |

3 Implementation

PAGAI is a prototype interprocedural static analyzer, that implements our recent combined techniques \[11\] as well as the classical abstract interpretation algorithm, and the state-of-the-art techniques Path Focusing \[16\] and Guided Static Analysis \[10\]. Abstract domains are provided by the APRON library \[12\], and include convex polyhedra (from the built-in Polka “PK” library), octagons, and products of intervals. It also has an interface with the Parma Polyhedra Library \[3\], giving access to more abstract domains (e.g., a reduced product of polyhedra and linear congruences, producing invariants such as $0 \leq x \leq 1001 \land x \equiv 0 \pmod{7}$).

For SMT-solving, our analyzer uses Yices \[9\] or Microsoft Z3 \[8\] through their C API. An implementation of communications with the SMT-solver by textual messages sent through a pipe following the SMT-Lib 2 standard \[4\] is underway, and now partially supports Z3, MathSAT 5 and SMTInterpol \[3\].

3.1 Analysis algorithm

For each program, we distinguish a set $P_W$ of suitable widening points by a simple algorithm: initialize $P_W = \emptyset$ and for each procedure, compute the strongly connected components of its control-flow graph using Tarjan’s algorithm; the targets of the back-edges of the depth-first search are added to $P_W$. The resulting cut set or feedback vertex set is not necessarily minimal, but is sufficient to disconnect all cycles — more sophisticated techniques are discussed in e.g. Bourdoncle \[2\] \[4\]. It is however unclear whether more advanced selection tech-

\[4\] It is unfortunately impossible to ignore differences between solvers behind the supposedly standard interface, since different solvers may support slightly different sets of operators and settings and may return models in different formats.

\[4\] It would be possible to obtain a feedback vertex set minimal with respect to inclusion by successive removal of nodes. Obtaining one of minimal cardinality is an NP-complete
niques would finally yield stronger invariants; the current simple scheme has the advantage that, when run over a control-flow graph obtained from a structured program, it marks heads of loops, which is a “natural” choice.

While [11, 16] provide for another set $P_R \supseteq P_W$, with abstract join operators (as opposed to widenings) being applied at points in $P_R \setminus P_W$, our tool does not currently such technique, which is meant to reduce the complexity of SMT formulas at the expense of analysis precision.

LLVM bitcode is in static single assignment (SSA) form: a given scalar variable is given a value at a single syntactic point in the program. In concrete terms, an assignment $x=2x+1$ gets translated into a definition $x_2 = 2x_1 + 1$, with distinct variables $x_1$ and $x_2$ corresponding to the same original variable $x$ at different points in the program. Because LLVM generally assigns rather straightforward names (e.g. $x.0$ for the first renaming of variable $x$), the user can map the invariants back to the original source code; an automatic and more robust back-to-source mapping, based on debugging information, is being developed.

LLVM makes it easy to follow definition-use and use-definition chains: for a given variable (say, $x_2$) one can immediately obtain its definition (say, $2x_1 + 1$). One may see conversion to SSA form as a static precomputation of some of the symbolic propagations proposed by Miné [15] to enhance the precision of analyses.

SSA introduces $\phi$-functions at the head of a control code to define variables whose value depends on which incoming edge was last taken to reach this control node. For instance, for $\textbf{if } (...) \{ \ x = 2x + 1; \ \} \textbf{else } \{ \ x = 0; \}$, then $x_2$ is defined as $\phi(2x_1 + 1, 0)$.

In this framework, each variable is uniquely defined as an arithmetic (+, −, ×, /) function of other variables that themselves may not be representable as arithmetic functions, because they are defined using $\phi$-functions, loads from memory, return values from function calls, or other numerical operations (e.g. bitwise operators) that are not representable with our class of basic arithmetic operations. We may vary the class of arithmetic operations, for instance, by restricting ourselves to linear ones.

This motivates a key implementation decision of our tool: only those variables $v_1, \ldots, v_n$ that are not defined by arithmetic operations are retained as coordinates in the abstract domain (e.g. as dimensions in polyhedra), assuming they are live at the associated control point.

For instance, assume that $x, y, z$ are numerical variables of a program, $x$ is defined as $x = y + z$, and $x, y, z$ are live at point $p$. Instead of having $x$ as a dimension for the abstract value at point $p$, we only have $y$ and $z$. All the properties for $x$ can be directly extracted from the abstract value attached to $p$ and the relation $x = y + z$. This is an optimisation in the sense that there is redundant information in the abstract value if both $x, y$ and $z$ are dimensions of $X_p$. The classical definition of liveness can be adapted to our case:

problem, but Shamir [18] showed that it can be done in linear time for a class of graphs including reducible graphs, that is, those obtained from structured programs. This latter algorithm is being implemented.
Definition 1 (Liveness by linearity). A variable $v$ is live by linearity at a control point $p$ if and only if one of these conditions holds: (i) $v$ is live in $p$. (ii) There is a variable $v'$, defined as a linear combination of other variables $v_1, v_2, \ldots, v_n$, so that $\exists i \in \{1, \ldots, n\}, v = v_i$, and $v'$ is live by linearity in $p$.

Finally, a variable is a dimension in the abstract domain if and only if it is live by linearity and it is not defined as a linear combination of program variables.

A basic block of code therefore amounts to a parallel assignment operation between live-by-linearity variables $(v_1, \ldots, v_n) \mapsto (f_1(v_1, \ldots, v_n), \ldots, f_n(v_1, \ldots, v_n))$: such operations are directly supported by APRON. This has three benefits: (i) it limits the number of dimensions in the abstract values, since polyhedra libraries typically perform worse with higher dimensions; (ii) the abstract operation for a single path in path-focusing methods also is a (large) parallel assignment; (iii) as suggested by Miné [15], this approach is more precise than running abstract operations for each program line separately: for instance, for $y = x; z = x - y$; with precondition $x \in [0, 1]$, a line-by-line interval analysis obtains $y \in [0, 1]$ and $z \in [-1, 1]$ while our “en bloc” analysis symbolically simplifies $z = x - x = 0$ and thus $z \in [0, 0]$.

In the event that a node is reachable only by a single control-flow edge (which may occur because of dead code, or during the first phases of guided static analysis), the $\phi$ operation reduces to a copy of the values flowing from that edge. In this case, our tool just propagates symbolic values through the predecessor node, without introducing $\phi$-variables.

3.2 Use
PAGAI takes as input an LLVM bitcode file, and outputs an inductive invariant for each control point in $P_R$ (typically, the widening points). When a program contains an assert (...) function call, PAGAI also outputs whether the statement has been proved. It is also possible to add some preconditions about the variables, etc, using a function assume(...). Both assert and assume are implemented as C macros. assert($x$) is roughly defined as if (! $x$) _assert_fail ();, and the tool just tests for the reachability of _assert_fail (): if it is unreachable, then the assertion is true. assume works with the same principle, and is defined as if (! $x$) _assumption_declared(). Both _assert_fail and _assumption_declared are noreturn functions, terminating the program immediately.

3.3 Current limitations of the tool, possible future works
Our tool currently only operates over scalar variables from the SSA representation and thus cannot directly cope with arrays or memory accessed through

\footnotetext{The additional dimensions express linear equalities between variables, which are directly handled by polyhedra library. They should therefore cost little assuming some sparse representation of the constraints. Alas, several libraries, including APRON, compute with dense vectors and matrices, which means that any increase in dimensions slows computations.}
pointers. We therefore run it after the “memory to registers” (mem2reg) optimization phase in LLVM, which lifts most memory accesses to scalar variables. The remaining memory reads are treated as nondeterministic choices, and writes are ignored. This is a sound abstraction.\footnote{As rightly pointed out by a referee, this is a sound abstraction only if memory safety is assumed. The mem2reg preprocessing phase also assumes memory safety, as well as, possibly, the absence of other undefined behaviors as defined by the C standard. This is the price of using the front-end from a generic compiler: C compilers have the right to assume that undefined behaviors do not occur, including in preprocessing and optimization phases.}

The analysis is currently intraprocedural: function calls are ignored in a sound way (the return value is a nondeterministic choice, the value of all variables escaping from the local scope is discarded...). In order to increase precision, we apply function inlining as an LLVM optimization phase. Plans for interprocedural analysis include computing input/output summaries for functions as elements of the abstract domain (e.g. if the function operates over variables \(x\) and \(y\), then one could compute a polyhedron over \((x, y, x', y')\) encompassing all input-output pairs) or as more general formulas.

Since it is often advantageous to distinguish whether a loop has been executed at least once\footnote{Consider the very simple loop \(\text{for}(\text{int}\ i=0; i<n; i++)\). The obvious loop invariant is \(0 \leq i \leq n\), but it is valid only if \(n > 0\). One would thus need to use disjunctive loop invariants to obtain \(0 \leq i \leq n \lor (i = 0 \land n \leq 0)\). It is much simpler to unroll the loop once.} we unroll every loop once, again with a LLVM optimization phase.

Our tool currently assumes that integer variables are unbounded mathematical integers (\(\mathbb{Z}\)) and floating-point variables are real (or rational) numbers. Techniques for sound analysis of bounded integers, including with wraparound, and of floating-point operations have been developed in e.g. the Astrée system\footnote{E.g. an operation \(z = x + y\) over \(n\)-bit signed integers would appear as the disjunction of three statements \(z = x + y \land -2^{n-1} \leq x + y < 2^{n-1}\), \(z = x + y + 2^n \land -x + y < -2^{n-1}\), \(z = x + y - 2^n \land x + y \geq 2^{n-1}\): one “normal” control path and two “overflow” paths.}, but porting these techniques to our iteration schemes using SMT-solving requires supplemental work. It is unclear whether one should use bitvector arithmetic inside the SMT formula, or use mathematical integers with explicit splits for wraparound.\footnote{Our implementation of path-focusing currently does not use true acceleration techniques, as proposed by Monniaux et Gonnord\cite{MonniauxGonnord2009}. Instead, it simply runs widening and narrowing iterations on a single path.}

Our implementation of path-focusing currently does not use true acceleration techniques, as proposed by Monniaux et Gonnord\cite{MonniauxGonnord2009}. Instead, it simply runs widening and narrowing iterations on a single path.

We currently analyze each strongly connected component of the control-flow graph in topological order; thus each loop nest gets analyzed as a single fixed point. An alternative method would be to recursively decompose the strongly connected components (for structured programs, this amounts to reconstructing the nested loop structure) and summarize the inner loops before analyzing the outer loop.

The analysis is currently only forward, even though nothing in the techniques implemented is specific to forward analysis. A possible extension would therefore be backward analysis from the \texttt{assert fail()\ } statements.
Table 2: Results of the comparison of the various techniques described in this paper: classic Abstract Interpretation (S), Guided Static Analysis (G), Path-focusing (PF), our combined technique (G+PF), and its version using disjunctive invariants (DIS). For instance, G/S compares the benefits of Guided Static Analysis over the classic Abstract interpretation algorithm. \( \subset \) (resp. \( \supset \)) gives the percentage of invariants stronger (more precise; smaller with respect to inclusion) with the left-side (resp. right-side) technique, and “uncomparable” gives the percentage of invariants that are incomparable, i.e. neither greater nor smaller; the code points where both invariants are equal make up the remaining percentage.

4 Experiments

We conducted extensive experiments on real-life programs in order to compare the different techniques, mostly on open-source projects (Tab. 1) written in C, C++ and Fortran.

4.1 Precision of the various techniques

For each program and each pair \( (T_1, T_2) \) of analysis techniques, we list the proportion of control points in \( P_R \) where \( T_1 \) (resp. \( T_2 \)) gives a strictly stronger invariant, denoted by \( \subset \) (resp. \( \supset \)), and the proportion of control points where the invariants given by \( T_1 \) and \( T_2 \) are incomparable for the inclusion ordering (the remainder of the control points are thus those for which both techniques give the same invariant). We use convex polyhedra as the abstract domain.

Let us briefly comment the results given in more details in Table 2. Guided Static Analysis from Gopan et Reps [10], improves the result of the classical Abstract Interpretation in 2.21% of the control points in \( P_R \). Path-focusing from Monniaux et Gonnord [10] finds better invariants in 4.13% of the control points.

However, these two techniques also lose precision in an important number (4.64% for G, 5.14% for PF) of control points, and obtain worse results than the classical many times. This result is unexpected, and could be partially explained by bad behaviour of the widening operator.

Finally, our combined technique gives the most promising results, since it is statistically more precise than the other techniques. It improves the precision of the inductive invariant in 8.29% to 9.86% of the control points compared to
Table 3: Execution time for each technique, expressed in seconds

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<tr>
<th>Benchmark</th>
<th>S</th>
<th>G</th>
<th>PF</th>
<th>G+PF</th>
<th>DIS</th>
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</tr>
</tbody>
</table>

4.2 Precision of Abstract Domains

For each program and each pair \((D_1, D_2)\) of abstract domains, we compare by inclusion the invariants of the different control points in \(P_R = P_W\) (Tab. 4).
Statistically, the domain of convex polyhedra gives the better results, but commonly yields weaker invariants than the domains of octagons/intervals; this is a known weakness of its widening operator \[17\]. The Octagon domain appears to be much better than intervals; this is unsurprising since in most programs and libraries, bounds on loop indices are non constant: they depend on some parameters (array sizes etc.).

The Lapack/Blas benchmarks are unusual compared to the other programs. These libraries perform matrix computations, using nested loops over indices; such programs are the prime target for polyhedral loop optimization techniques and it is therefore unsurprising that polyhedra and octagons perform very well over them.

The analysis of linear equalities (PKEQ) performs very fast compared to other abstract domains, but yields very imprecise invariants; it only detects relations of the form \[\sum a_i x_i = C\] where \(a_i\) and \(C\) are constants.

Using the reduced product of convex polyhedra with linear congruences (PKGRID) improves the analysis by 2.52%.

Finally, we evaluated the benefits of the improved version of the widening operator for convex polyhedra from Bagnara et al. \[2\], compared to the classical widening. We found that the improved version from Bagnara et al. \[2\] yields more precise invariants for 3.70% of the control points in \(P_R\).

### 4.3 Future Work

It is not totally relevant to compare by inclusion the abstract values obtained by the various analysis techniques. Indeed, a slightly smaller invariant may not always be useful to prove the desired properties. Future work should thus include experiments with better comparison metrics, such as (i) the number of...
assert that have been proved in the code. Unfortunately, it is difficult to find good benchmarks or real life programs with many assert statements; (ii) the number of false alarms in a client analysis that detects array bound violations, arithmetic overflows, etc.

References


