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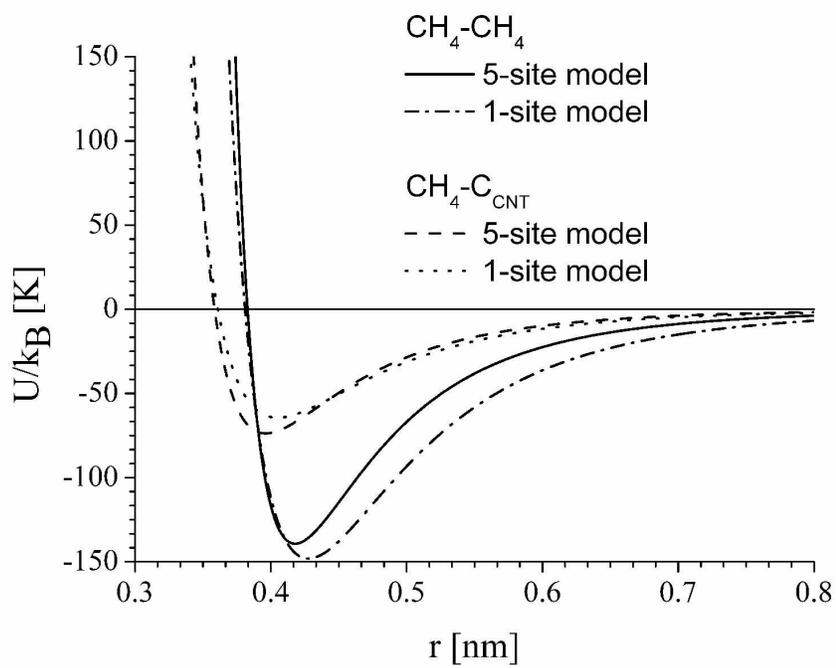
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Methane in carbon nanotube – molecular dynamics simulation

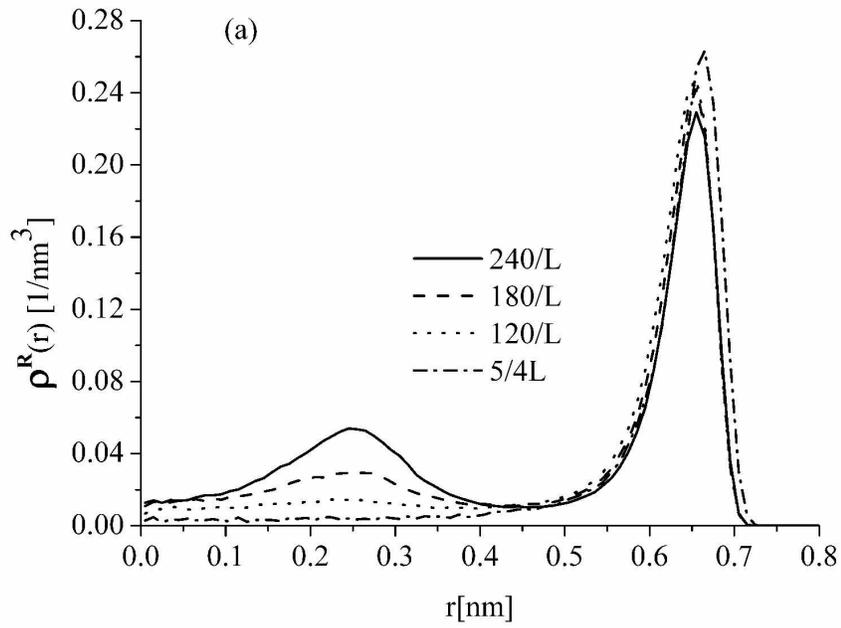
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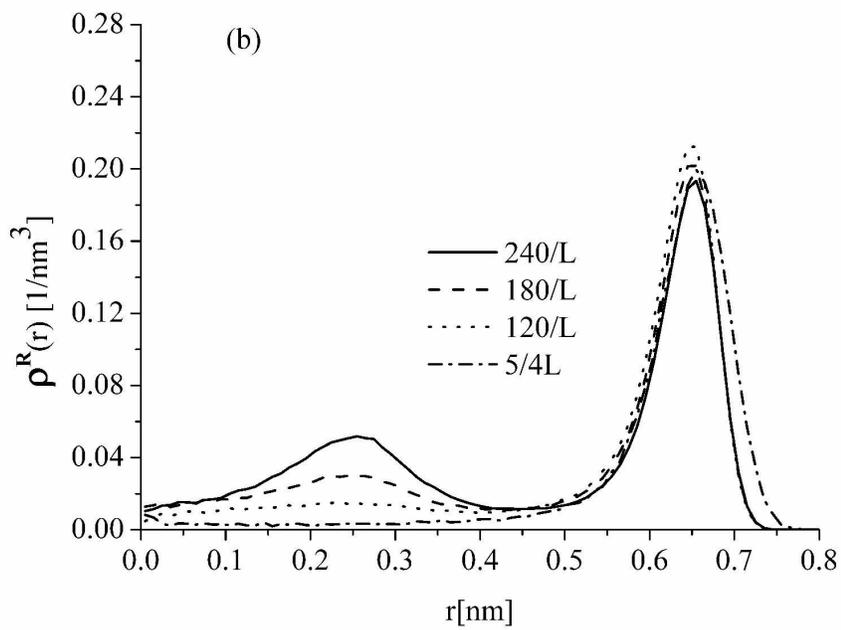


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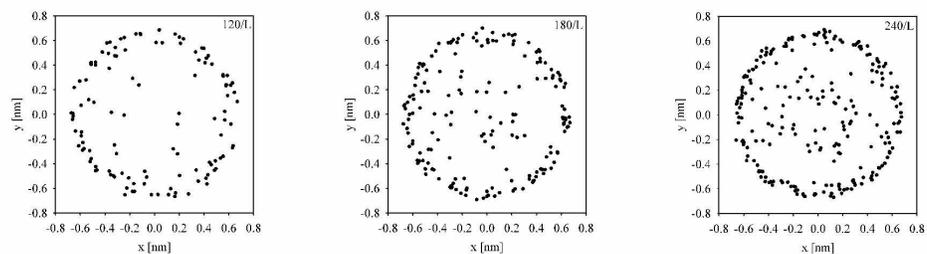
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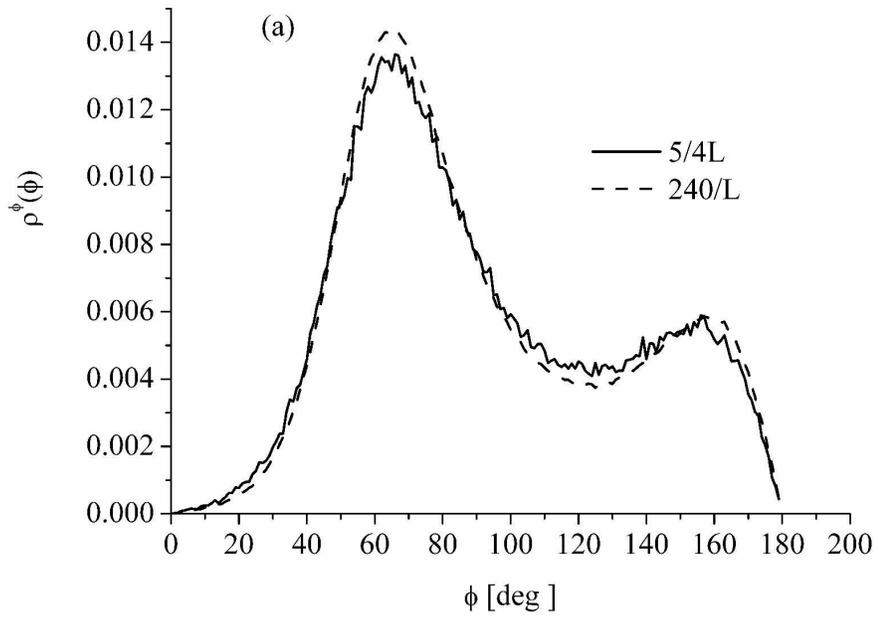
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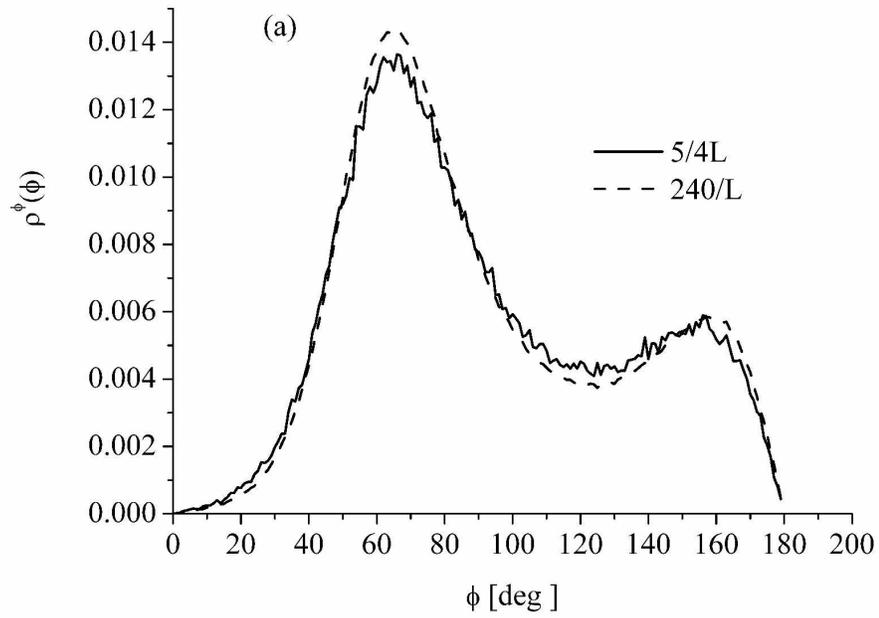
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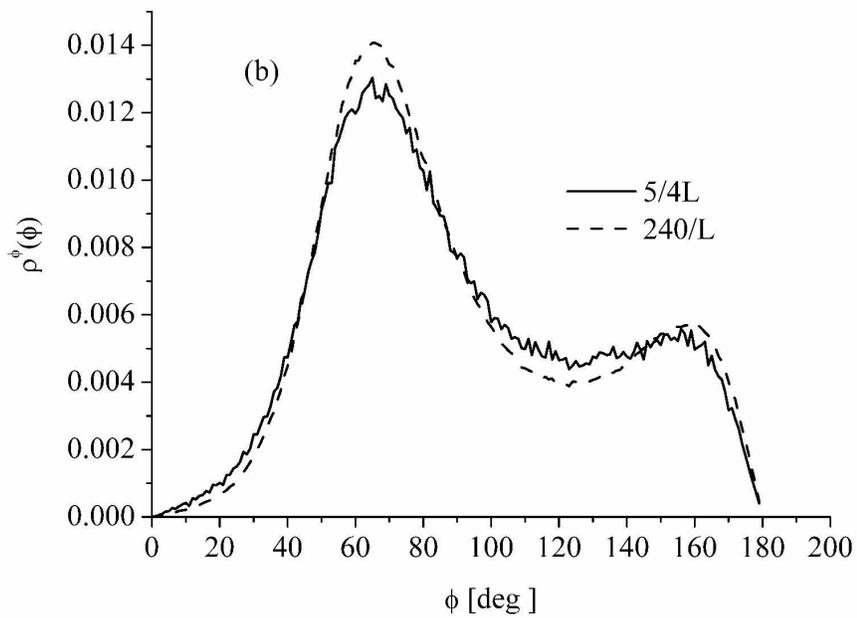
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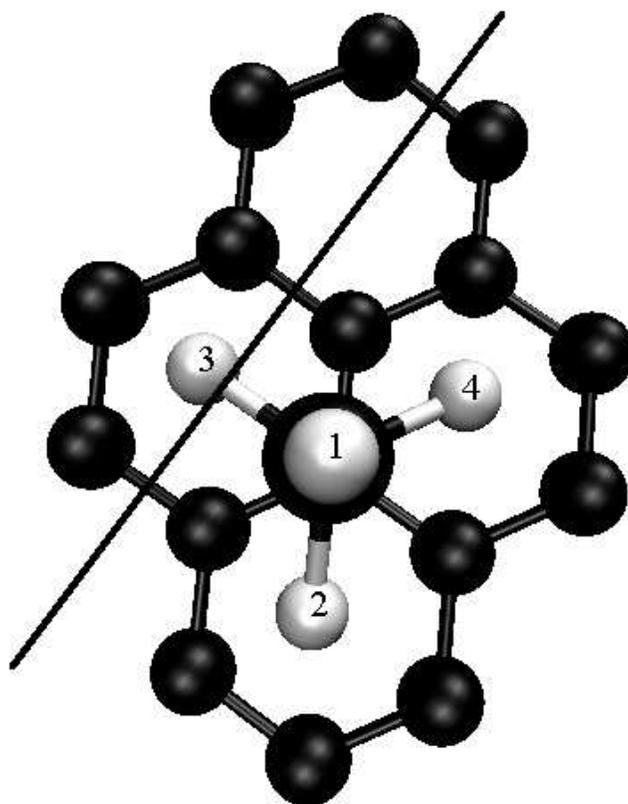
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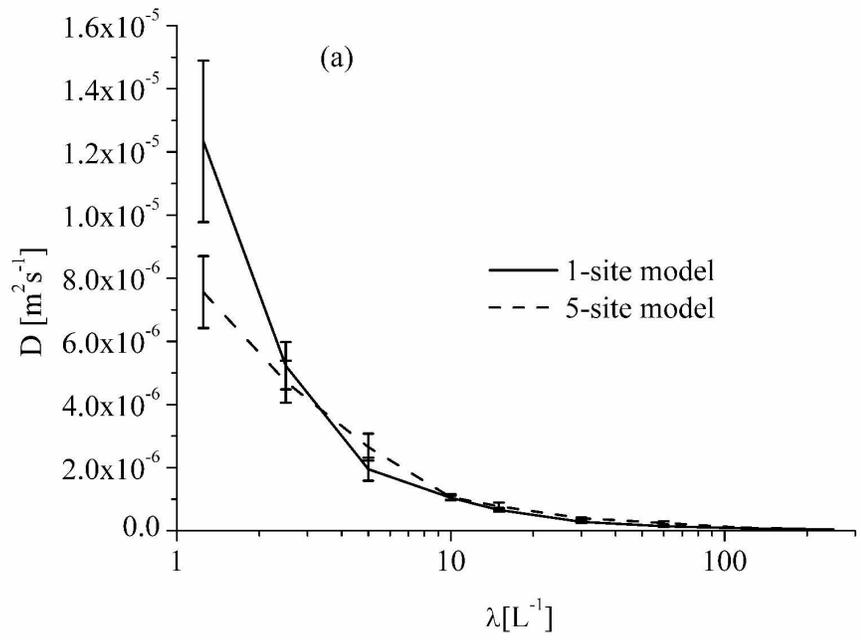
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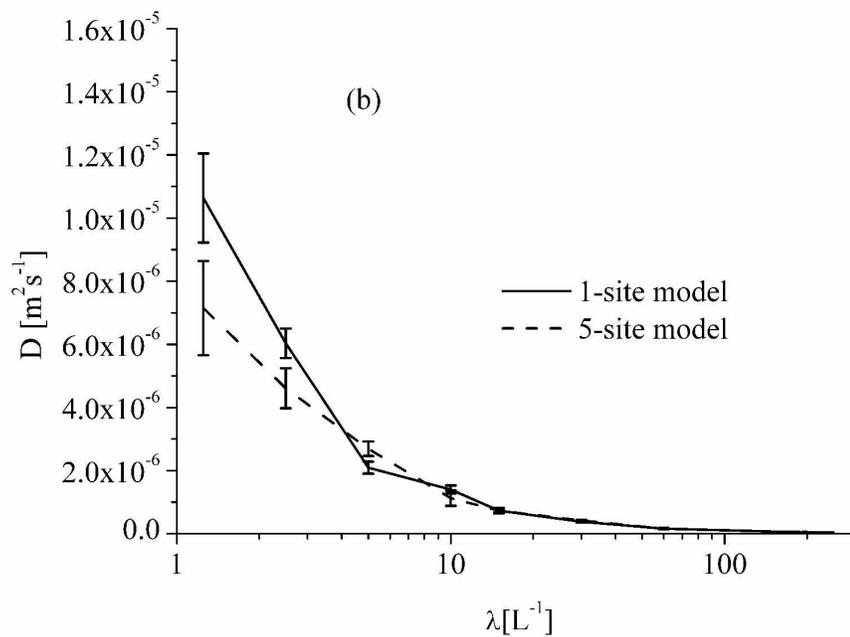
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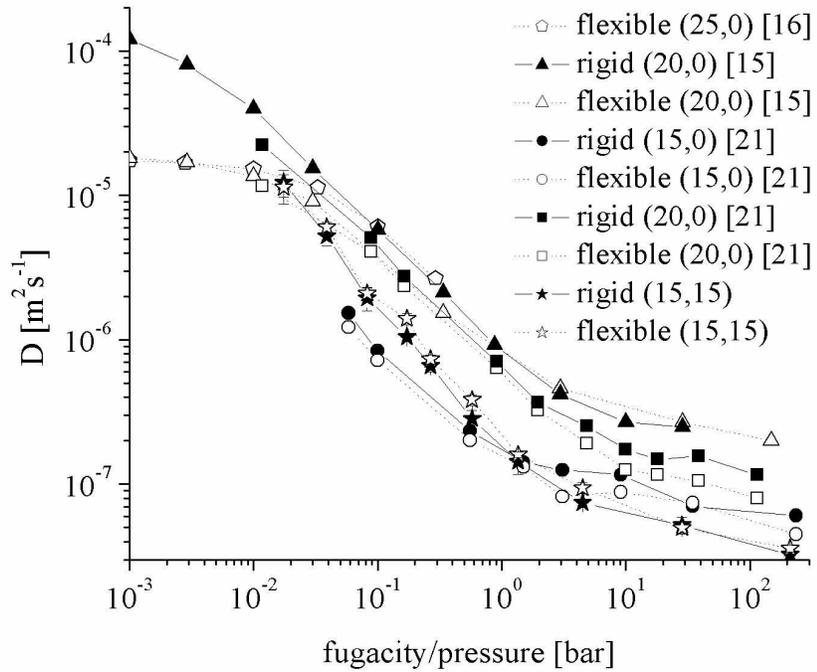
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Methane in carbon nanotube – molecular dynamics simulation

Katarzyna Bartuś and Aleksander Bródka

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The behaviour of methane molecules inside carbon nanotube at room temperature is studied using classical molecular dynamics simulations. A methane molecule is represented either by a shapeless super-atom or by rigid set of 5 interaction centres localised on atoms. Different loadings of methane molecules ranging from the dense gas density to the liquid density, and the influence of flexibility of the CNT on structural and dynamic properties of confined molecules are considered. The simulation results show the decreases of the diffusion coefficient of methane molecules with density. At higher densities diffusion coefficient values are almost independent of molecular shape, but at low densities one observes faster motion of the super-atom molecule than that for the tetrahedral model of the molecule. For loadings of methane considered here the nanotube flexibility, introduced by the reactive empirical bond order (REBO) potential for interactions between carbon atoms of nanotube, does not have effect on diffusivity of methane molecules, and its impact on the molecular structure is weak. It is found that methane molecules in the vicinity of the nanotube wall show tripod orientation with respect to the nanotube surface.

Keywords: diffusion; carbon nanotube; methane molecule

1. Introduction

In last years carbon nanotubes (CNTs) have been subjected to intensive research because of their excellent combinations of mechanical, electrical and chemical properties. Furthermore, because of their nanometer-scale size, cylindrical shape, uniform porosity and high tensile strength CNTs have many potential applications such as molecular sieves, ultrafiltration membranes [1], sensors [2] and nanometer-sized pipes for the precise delivery of gases and liquids [3]. It is also of practical interest in connection with gas separation and purification, the development of storage media for natural gas and the behaviour of methane in underground reservoirs. The dynamics of fluids and gases in systems with restricted geometry is known to be very different from that in the bulk phase. Attempts to understand, and hence control the transport properties are well motivated by fundamental and applied

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3 interests. Recently, adsorption of methane in CNTs [4-7] and on them [8-13] have been
4 studied experimentally. To investigate behaviour of methane inside CNTs molecular
5 dynamics (MD) simulations [14-27] and Monte Carlo (MC) ones [28-32] have been used,
6 however, in most of the studies the CH₄ molecule was represented by a spherical super-atom,
7 i.e. the 1-site model, and only few of them modelled the methane molecule by 5 interaction
8 centres, i.e. the 5-site model [18,25-27]. For 1-site model molecular simulations of rigid CNT
9 have shown that the diffusion coefficient decreases with the increase of adsorbate
10 concentration [15-17,21]. The diffusion coefficient of methane molecules in a rigid (10,10)
11 CNT drops rapidly from value about $1 \cdot 10^{-4}$ m²/s in the limit of low concentration to about
12 10^{-7} m²/s at high pore loadings [17]. In the limit of low density, diffusion coefficient
13 of methane in the (20,0) CNT at room temperature was about $0.2 \cdot 10^{-4}$ m²/s in flexible
14 nanotube, whereas in a rigid one it was about $1.2 \cdot 10^{-4}$ m²/s [15]. It means, that at the lowest
15 density flexibility of the CNT reduces the diffusion coefficient of methane molecules
16 approximately by a factor of 6. For nondilute pore loadings, the difference between behaviour
17 of methane in the rigid nanotube and flexible one is very small, and for loadings resulting
18 in pressures greater than 0.1 bar the nanotube flexibility seems to be meaningless.
19 For the 5-site model of CH₄ in rigid nanotubes of various diameters and helical structure were
20 considered in the MD simulations performed at 300K for different densities of methane
21 molecules inside CNT [18,25,26], but influence of flexibility of CNT on the behaviour
22 of the CH₄ molecules was not studied. MD simulations of liquid methane with densities
23 from 0.353 to 0.17 g/cm³, confined in CNTs with diameters 0.7-1.4nm [18,25,26] showed that
24 flow of methane does not depend on the helicity of the CNT but it depends on the tube
25 diameter. For motion of methane molecules along the CNT the simulations predict normal-
26 mode diffusion, i.e. the mean square displacement function is proportional to time [18,25-27].
27 The MD simulation results gives also possibility to estimate the distance between
28 CH₄ molecule and inner wall of CNT, and for the (10,0) CNT the distance was 0.3nm and for
29 the (10,10) one it was 0.35nm [25]. Which is in accordance with the distance 0.348 nm
30 obtained for the 1-site model of CH₄ molecules in the rigid (10,10) CNT [24]. Adsorption
31 of methane molecules on the CNT surfaces was also studied using density functional theory
32 (DFT) method [33-38] and second order Möller-Plesset perturbation calculations [39].
33 Usually the studies considered few methane molecules and CNTs with small diameters,
34 and concentrated on binding energies of adsorbed molecules and their positions with respect
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3 A single wall CNT can be formed from a graphene sheet, and hence the nanotube
4 surface is closely related to that of graphite, which is considered as standard substrate
5 in experimental studies of 2D adsorbed phases [40-46] as well as theoretical ones [41,47-55].
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7 Therefore, results of studies of methane on graphite can be helpfull in understanding
8 behaviour of methane molecules in CNTs. Moreover, those studies were used to determine
9 parameters of the interaction potential between CH₄ molecule and carbon atoms of graphene
10 sheet [56].
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16 In this paper we present results of MD simulations of methane inside the (15,15) CNT
17 for two models of the CH₄ molecule are used: a usually applied united atom and tetrahedral
18 model taking into account atom positions in the molecule. We analyze the influence
19 of molecular model on structure and dynamics of the system. The MD simulations were
20 carried out for different loadings of methane in the CNT. We consider densities lower than
21 those for liquid methane used previously [18,24]. Distribution of methane molecules and their
22 orientations in the CNT are investigated and self-diffusion coefficient values are estimated
23 using the mean square displacements as well as velocity correlation functions. Moreover,
24 to study impact of flexibility of the CNT on behaviour of the confined methane we consider
25 rigid and elastic model of the nanotube.
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36 2. Computational Details

37 We performed the MD simulations of methane in single-walled (15,15) CNT with
38 diameter $d=2.034$ nm and length $L=11.068$ nm. The CNT was generated using
39 two-dimensional perfectly hexagonal graphene sheet with the carbon-carbon bond length
40 of 0.142 nm, and the sheet was wrapped into seamless cylinder. To simulate different
41 loadings, we usually change the number of methane molecules, however, to obtain low
42 densities we increase length of the CNT two or four times, and systems considered here
43 are defined in Table 1. Assuming smooth wall of the nanotube we estimated densities
44 of methane inside the CNT, which are in the range from 0.178 g/cm³ to 0.9 mg/cm³.
45 The density estimated for the smallest system is larger than the density of methane at room
46 temperature and ambient pressure. For each system size the MD simulations are performed
47 for two models of CNT: rigid where carbon atoms are frozen and flexible, in which the carbon
48 atoms undergo thermal motions resulting from interactions with atoms of the CNT
49 and methane molecules. Interatomic interactions of carbon atoms in flexible CNT
50 are described by REBO potential [57], which was originally parameterized to examine
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3 the growth of diamond thin films by chemical vapour deposition. The REBO potential has
4 also been successfully used to study the structure of carbon nanotubes [58] and their
5 mechanical properties [59,60]. Moreover, the interaction potential was used to investigate
6 structural properties of activated carbons [61] as well as nanodiamonds and carbon ions
7 [62]. We considered two models of the CH₄ molecule. The first is the usually applied
8 the 1-site model [14-17,19-24], and the second one called the 5-site model is a rigid
9 tetrahedron with a central carbon atom and four hydrogen atoms [56]. Intermolecular
10 interactions are modelled by Lennard-Jones (LJ) potential, and its parameters for both models
11 are collected in Table 2. For the 1-site model the LJ potential parameters for unlike interacting
12 centres presented in Table 2 were calculated using the Lorentz-Berthelot mixing rules [63],
13 and $\sigma_{CNT}=0.34$ nm and $\epsilon_{CNT}/k_B=28$ K the values usually accepted and applied for carbon atoms
14 in graphite [64]. The LJ potential parameters for the 5-site model were adjusted by Severin
15 and Tildesley considering methane molecule over graphite plane [56]. Comparison of the two
16 interaction models of the methane molecules is presented in Figure 1. Both models of the CH₄
17 molecule describe interaction of methane molecule with a carbon atom of nanotube very
18 similarly. However, interactions between the methane molecules are slightly different,
19 especially for intermediate distances. In the MD simulations orientations of the methane
20 molecules modelled by 5 interaction centres are described by quaternions. For the highest
21 density of methane randomly oriented CH₄ molecules are placed in the fcc lattice nodes inside
22 the CNT and small displacements from the crystalline positions are applied. Translational
23 and angular velocities are chosen randomly and they are scaled to be consistent with
24 the required temperature. Periodic boundary conditions along the CNT axis, together with
25 the minimum image convention and spherical truncation of potential with cut-off radius r_c
26 (see Table 2) are applied to the centres of mass of the molecules. To obtain lower densities
27 part of the methane molecules are removed.

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48 The Newtonian and orientational equations of motions are solved with the six-
49 and five-value predictor-corrector integration scheme [63], respectively. The MD simulations
50 are carried out in the canonical ensemble (NVT) at temperature T=293 K. At the beginning
51 the system is far from the equilibrium state and distances between the interacting sites may be
52 very small. Therefore, in the first stage (10000 steps) of each simulation the equations
53 of motion are solved with a very short time step of about $0.15 \cdot 10^{-7}$ fs and after each 400 steps
54 the time interval is doubled until it reaches the maximum value of 0.5 fs, which was applied
55 through out the following 5000 time steps and in the next simulation stages. In the first two
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3 stages we used the velocity scaling when deviation of the instantaneous temperature from
4 the required one is larger than 3K. Then, 100000 time steps were performed to allow
5 the system to achieve equilibrium configuration. Afterwards, the MD production runs were
6 performed, where the configurations of the methane molecules, i.e. positions, orientations,
7 and velocities are recorded. Simulation length of each MD production run depends
8 on the density of methane molecules inside the CNT (see Table 1). In the last two stages
9 temperature is generally maintained by the constraint method [63]. For the 5-site model
10 the translational and rotational kinetic energies are constrained separately, and the equations
11 of motions are following:
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$$20 \frac{d}{dt} \mathbf{p}_i = \mathbf{F}_i - \xi_T \mathbf{p}_i, \quad \xi_T = \frac{\sum_{i=1}^N \mathbf{F}_i \cdot \mathbf{p}_i}{\sum_{i=1}^N \mathbf{p}_i \cdot \mathbf{p}_i}, \quad (1)$$

$$22 \hat{I}^M \frac{d}{dt} \boldsymbol{\omega}_i^M = \mathbf{G}_i^M + [\boldsymbol{\omega}_i^M \times (\hat{I}^M \boldsymbol{\omega}_i^M)] - \xi_R \hat{I}^M \boldsymbol{\omega}_i^M, \quad \xi_R = \frac{\sum_{i=1}^N \mathbf{G}_i^M \cdot \boldsymbol{\omega}_i^M}{\sum_{i=1}^N (\boldsymbol{\omega}_i^M)^T \hat{I}^M \boldsymbol{\omega}_i^M}. \quad (2)$$

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34 In the above equations \mathbf{p}_i and $\boldsymbol{\omega}_i$ are momentum and angular velocity of the i th molecule,
35 respectively. \mathbf{F}_i and \mathbf{G}_i indicate force and torque, respectively, acting on the i th molecule. \hat{I}
36 is the tensor of inertia moment, ξ_T and ξ_R are dumping constants that fix the translational and
37 rotational temperature, respectively, and the superscript M indicates a quantity
38 in the molecular system. It must be noted that in the constraint method temperature tends
39 to drift from its initial value [63]. Therefore, when the system temperature deviates from
40 the required value by more than 3K the velocity scaling was applied. It must be noted that
41 the velocity scaling is related to the constrained method, and for the leapfrog algorithm this
42 method reduces to simple scaling of the velocities [65]. In the presented simulations
43 the velocity scaling make small corrections of temperature. It was needed for the translational
44 motion only and it was used once per about 10000 time steps for the highest density and 1000
45 time steps for the lowest one. To verify this approach some simulations were performed
46 in the microcanonical ensemble (NVE), and their results for higher densities are in accordance
47 with results of the NVT simulations described above, but for low densities temperature
48 fluctuations are very high, up to 90K for the smallest system.
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Structure of methane in CNT is characterized by a distribution of the CH₄ centres of mass across the CNT calculated as follows

$$\rho^R(r) = \frac{\langle N^R(r, r + \Delta r) \rangle}{Nd\Gamma}, \quad (3)$$

where $N^R(r, r + \Delta r)$ means number of molecules in a cylindrical shell with inner and outer radii r and $r + \Delta r$ ($\Delta r = 0.01$ nm), respectively, and length L_z , $d\Gamma$ is the shell volume and angular brackets indicate averaging over time and the MD simulation runs. To investigate orientations of the methane molecules from the contact layer we calculate distribution of angles between C-H bonds and the normal to the CNT surface. The angle distribution is defined by

$$\rho^\phi(\phi) = \frac{\langle N^\phi(\phi, \phi + \Delta\phi) \rangle}{4N_C}, \quad (4)$$

where $N^\phi(\phi, \phi + \Delta\phi)$ is number of the C-H bonds, whose angle with respect to the normal to the CNT surface is in the interval $(\phi, \phi + \Delta\phi)$ with $\Delta\phi = 1^\circ$, and N_C is number of the CH₄ molecules which were taken into account. The angle is defined as follows

$$\phi = \arccos \left[\frac{\mathbf{n} \cdot (\mathbf{r}_H - \mathbf{r}_C)}{|\mathbf{n}| |\mathbf{r}_H - \mathbf{r}_C|} \right], \quad (5)$$

where \mathbf{r}_H and \mathbf{r}_C describe positions of the hydrogen atom and carbon one, respectively, in the CH₄ molecule, and the surface normal $\mathbf{n} = (x_C, y_C, 0) / \sqrt{(x_C^2 + y_C^2)}$ lays in the plane perpendicular to the pore axis and it is defined by coordinates of the carbon atom in the methane molecule.

To study dynamics of the systems we estimate self-diffusion coefficient, and two methods have been used to calculate the coefficient: one resulting from the linear response theory and the fluctuation-dissipation theorem, and the other from the Einstein formula [63]. For motion parallel to the pore axis the diffusion coefficient is defined by the following equations:

$$D = \int_0^\infty \langle v_z(t) v_z(0) \rangle dt, \quad (6)$$

$$D = \lim_{t \rightarrow \infty} \frac{1}{2t} \langle (z(t) - z(0))^2 \rangle \quad (7)$$

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3 where $v_z(t)$ and $z(t)$ are components of the velocity and position of the centre of mass
4 of methane molecule at time t , respectively. In Equations (6) and (7) angular brackets mean
5 averaging over molecules, the initial time and MD simulation runs, and the correlation
6 functions appearing in those equations are calculated up to half of the MD simulation length.
7 For long times the velocity autocorrelation functions approach zero, and the integral
8 in Equation (6) is calculated for the whole time range. The mean-squared displacement
9 (MSD) function change linearly with time except short times where ballistic motion
10 is observed, and using Equation (7) to calculate the diffusion coefficient about 10%
11 of the initial data in the MSD functions were ignored.
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22 3. Results and Discussion

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24 The distributions of methane across the CNT are similar for two models of methane
25 molecule, and in Figure 2 we show the results of methane for the 5-site model only. For low
26 densities methane form monolayer, with thickness of about 0.25 nm, near the nanotube wall,
27 and maximum of the monolayer peak is observed at about 0.65 nm. For higher densities some
28 of the particles are localised in the inner part of the CNT. The distribution peaks for the rigid
29 CNT are narrower than those for the flexible one, when thermal fluctuations of the wall atoms
30 make roughness of the surface more evident and increase frequency of collisions of methane
31 molecules with nanotube atoms. The layered structure of methane in CNT is also
32 demonstrated in Figure 3, which presents projection of positions of the methane molecules
33 on the plane perpendicular to the CNT axis for selected loadings of methane.
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42 Additional information about structure of methane in the CNT is given by the angle
43 distribution of bonds of the CH_4 molecules from the contact layer $\rho^0(\phi)$. The distributions
44 presented in Figure 4 were calculated for molecules for which a distance from the CNT axis
45 is larger than 0.65 nm, i.e. the position of the monolayer peak maximum (compare Figure 2).
46 For all densities the functions are similar, and hence in Figure 4 we show results for two
47 systems only: the highest loading of methane considered here and the lowest one.
48 In the functions there are two broad peaks: the first peak with maximum at about 65°
49 and the other one with maximum at about 160° , which is approximately three times weaker
50 than the first one. The distribution functions suggest that a tripod orientation of the methane
51 molecule with respect to the CNT surface is preferred. For both models of the CNT the angle
52 distributions are almost the same. This observation indicates weak impact of the CNT
53 flexibility on orientation of the methane molecules in the vicinity of the CNT wall. Similar
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3 shapes of the distribution function were observed considering thicker layer when distance
4 of a molecule from the CNT axis is larger than 0.5 nm, but the peaks of the distribution
5 functions are less pronounced than those presented in Figure 4. These results suggest that
6 the tripod orientation is characteristic for molecules near the CNT wall, but molecules
7 localised further from the nanotube surface do not show any preferred orientation. One must
8 note that for ideal tripod orientation the angles, which C-H bonds form with the normal
9 to the CNT surface are following: one of 180° and three ones of 70.5° , and such orientation
10 is suggested by studies of methane adsorbed on a graphite surface using the classical MD
11 simulation [47,54] and DFT method [49,55]. In other words the methane molecules in CNT
12 are tilted with respect to the ideal tripod orientation. The tilted tripod position of a molecule
13 lying nearby the CNT surface is confirmed by energy minimization of single methane
14 molecule in the CNT. The conjugate gradient method gave minimum of the interaction energy
15 for the CH_4 molecule localised 0.337 nm above a carbon atom in the nanotube with the tripod
16 legs oriented toward the centres of the three adjacent carbon hexagons as it is shown in Figure
17 5. This distance is found to be similar to results predicted for methane molecules inside
18 the (10,10) CNT [24,25] and the (10,0) one [25]. The observed distance between the methane
19 molecule and the nanotube surface is in good agreement with the experimental results
20 for methane adsorbed on a graphite sheet, which changes from 0.33 nm [40] when methane
21 molecules form an adlayer with the $\sqrt{3} \times \sqrt{3}$ structure [41] to 0.345 nm estimated at low
22 coverage [48]. The energy minimalization gives also angles between the methane bonds
23 and the surface normal, and they are following: for C-H_1 it is 178.3° , for C-H_3 72.2°
24 and for C-H_2 and C-H_4 69.7° (see Figure 5). The angles indicate that the tilt appears
25 in the plane perpendicular to the nanotube axis, and one may suspect that the tilt results from
26 curvature of the nanotube. To confirm this suggestion similar calculations were performed
27 for single CH_4 molecule in the (10,10) CNT and (60,60) one with diameters 1.354 nm
28 and 8.124 nm, respectively. For the small nanotube an angle between the C-H_1 bond
29 and surface normal is 175.4° , which is smaller than that for the (15,15) CNT, whereas for
30 the large CNT the angle is 179.9° and this value is very close to that for graphene sheet.

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The diffusion coefficient values for CH_4 in the rigid CNT and flexible one for both
methane models are presented in Figure 6. In all cases under consideration the diffusion
coefficients obtained from Equations (6) and (7) are very similar, and hence we show only
results obtained from velocity autocorrelation function, and the coefficient errors were
estimated using results obtained from the consecutive MD simulation runs. The value

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3 of diffusion coefficient for both methane models drops dramatically with density due
4 to the increase of frequency of intermolecular collisions. This observation is in accordance
5 with previous simulations [15-17,21,23] and it is due to dominated methane-methane
6 collisions over the methane-carbon ones. However, for low densities the values
7 of the diffusion coefficient for the 1-site model are higher than those for the 5-site one.
8 In other words, the realistic model of the methane molecule becomes important at low
9 densities. Moreover, comparing results presented in Figure 6(a) and Figure 6(b) one may
10 conclude that the diffusivity of methane molecules in a flexible nanotube differ very little
11 from that for a rigid one suggesting that the vibration of the nanotube carbon atoms which
12 interact through the REBO potential has a little influence on translational motion of methane
13 molecules.
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23 To compare the diffusion coefficients obtained here with accessible data [15,16,21]
24 we estimated adsorptive pressures of methane in the (15,15) CNT using isotherms reported
25 by Nicholson [66]. Dependence of the diffusion coefficient on pressure obtained
26 by Jakobtorweihen et al. [15,16] and Chen et al. [21] together with our results when
27 the methane molecule is represented by one LJ interaction centre are shown in Fig. 7.
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32 In all cases diffusion coefficient depends on pressure similarly, however its values obtained
33 here are slightly smaller than those published earlier [15, 16, 21] that may be result of
34 different simulation methods. Moreover, it is seen that our smallest system 5/4L is out of the
35 low-density region for which the earlier studies [15, 16, 21] show faster translational motion
36 of methane in the rigid CNT than that in the flexible one. In other words, our results for the
37 REBO potential, support a conclusion of the previous works that impact of the nanotube
38 flexibility on methane behaviour in the CNT is small at high and intermediate densities.
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50 4. Conclusions

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52 Properties of methane in CNT are studied using the MD simulation method.
53 The results obtained for methane densities considered here, i.e. for states from the dense gas
54 phase to the liquid one, show that impact of the CNT flexibility, introduced by the REBO
55 interaction potential, on translational motion and structure of methane molecules is weak.
56 Values of the diffusion coefficient of methane molecules in the rigid CNT and flexible one are
57 almost the same. Similarly, shapes of the distribution functions of angles between the C-H
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3 bonds in the methane molecule and the CNT surface normal are alike for both nanotubes.
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5 A slight difference is observed in density profiles across the CNT. For both models of CNT
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7 one observes layered structure of methane by nanotube wall, but methane molecules
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9 in the rigid CNT show better localisation near the nanotube wall than those in the flexible
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11 CNT.

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13 Distribution of methane molecules in the CNT is almost independent on the methane
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15 molecule model. The simulation results show that the diffusion coefficients for the two
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17 models of CH₄ considered here are comparable only for higher densities, whereas for low
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19 densities atomic structure of methane molecule leads to reduction of the diffusion
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21 coefficient. One may conclude that approximation of the methane molecules by spherical
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23 super-atoms is reasonable for higher densities. Moreover, one may suspect that atomic
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25 structure of the molecule may be important at temperatures lower than that considered here.

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27 Distribution of the methane molecule orientation suggests tilted tripod position
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29 of the molecules from monolayer with respect to the CNT. This conclusion is confirmed
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31 by the energy minimization of one CH₄ molecule in the CNTs, and the tilt of the molecule
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33 results from curvature of the nanotube.
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Table 1. Systems under consideration and lengths of the MD production runs.

System symbol (number of CH ₄ molecules/ the CNT length)	240/L	180/L	120/L	60/L	60/2L	60/4L	40/4L	20/4L	10/4L	5/4L
MD simulation length [ps]	50	50	50	50	50	50	300	400	500	600
Number of simulation runs	4	4	4	4	4	4	6	8	10	12

Table 2. Parameters of the LJ interactions.

INTERACTIONS	5-site model			1-site model		
	ε/k_B [K]	σ [nm]	r_c [nm]	ε/k_B [K]	σ [nm]	r_c [nm]
CH ₄ -CH ₄			1.06	148.1	0.381	1.00
C _{MOL} -C _{MOL}	51.198	0.335				
C _{MOL} -H _{MOL}	23.798	0.299				
H _{MOL} -H _{MOL}	4.87	0.261				
CNT-CH ₄			1.04	64.4	0.361	0.95
C _{CNT} -C _{MOL}	47.68	0.330				
C _{CNT} -H _{MOL}	17.00	0.298				

Figure captions

Figure 1. The LJ potential for 1-site model and 5-site one averaged over orientations of the methane molecules.

Figure 2. Density distribution of methane molecules (5-site model) across the CNT for (a) rigid and (b) flexible nanotube.

Figure 3. Projection of centres of methane molecule (5-site model) in the rigid CNT on a plane perpendicular to the nanotube axis for the systems marked (see Table1).

Figure 4. Distribution of angles between C-H bonds of methane molecule and the normal to the CNT wall for (a) rigid and (b) flexible nanotube.

Figure 5. Position of the CH₄ molecule with respect to the carbon atoms of the nanotube. Grey circles represent the hydrogen atoms, black circles the carbon ones. Solid line is parallel to the nanotube axis.

Figure 6. Diffusion coefficient D as a function of linear density of methane, λ , for (a) rigid and (b) flexible nanotube.

Figure 7. Comparison of diffusion coefficients obtained here (stars) with data reported in [15,16,21].