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Loading policies in cellular manufacturing systems with remainder cell

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Cellular manufacturing systems are used when both production volume and product variety are at medium level. The fluctuations of volume and mix can reduce drastically the performance of classical cellular manufacturing systems. Therefore, several configurations have been proposed in literature as virtual manufacturing cells, fractal cells and remainder cells. This paper investigates the cell loading approaches in a manufacturing system composed of dedicated cells and a remainder cell. The remainder cell consists of machines able to manufacture all part families. The loading decision concerns the allocation of the parts to the remainder cell, instead of the dedicated cell. A simulation environment based on Rockwell ARENA® has been developed to test the proposed approaches. The performance measures are evaluated in a very dynamic environment characterized by volume oscillations, mix fluctuations and machine failures. A classical cellular manufacturing system is used as a benchmark for the performance measures analyzed. The simulation results show that the proposed policies lead to better performance when market fluctuations occur.

Keywords Cellular manufacture, scheduling, dynamic environments, discrete event simulation, remainder cell

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Abstract

Cellular manufacturing systems are used when both production volume and product variety are at medium level. The fluctuations of volume and mix can reduce drastically the performance of classical cellular manufacturing systems. Therefore, several configurations have been proposed in literature as virtual manufacturing cells, fractal cells and remainder cells. This paper investigates the **cell loading approaches** in a manufacturing system **composed of dedicated** cells and a remainder cell. The remainder cell consists of machines able to manufacture all part families. The loading decision concerns the allocation of the parts to the remainder cell, instead of the dedicated cell. A simulation environment based on Rockwell ARENA® has been developed to test the proposed approaches. The performance measures are evaluated in a very dynamic environment characterized by volume oscillations, mix fluctuations and machine failures. A classical cellular manufacturing system is used as a benchmark for the performance measures analyzed. The **simulation results** show that the proposed policies lead to better performance when market fluctuations occur.

Keywords: cellular manufacture, scheduling, dynamic environments, discrete event simulation, remainder cell

1. Introduction and motivations

Cellular manufacturing systems (CMSs) are the more appropriate configuration to obtain the better performance when the production variety and volume are at medium level. The CMSs are characterized by the following benefits: simplification and reduction in material handling, decreasing the work in process, reduction in set-up time, increment in flexibility, better production control, and shorter lead time (Askin and Estrada, 1999). These benefits can be obtained when the demand volume and mix are rather constant respect to the design data of the manufacturing cells. **In order to remain efficient, the CMSs need to be reconfigured when the manufacturing conditions change** (Chen, 1998). Nowadays, competition is characterized by short life-cycle of the products, introduction of new products, demand and mix fluctuations. These issues lead to reduce drastically the "life cycle" of a CMS configuration with numerous re-configuration activities. Each reconfiguration activity causes costs of re-design of manufacturing cells and set-up times **that reduce** the availability of the manufacturing system. Tompkins et al. (2003) estimated that \$250 billion is annually spent in USA for planning and re-planning because of these changes, and this huge cost can be reduced by 10–30% via effective planning. In literature, several alternatives were proposed as: virtual manufacturing cells (McLean et al., 1982), fractal cells (Vektadari et al., 1997; Monteruil et al., 1999), holonic cells (Montreuil et al., 1993) and remainder cells introduction in the design of CMSs (Maddisetty, 2005). **The focus of this paper is on the operation management** of remainder cells in a CMS environment. The aim of the research concerns the development and analysis of loading approaches to integrate the remainder cell within the classical CMS. In particular, there are proposed three loading policies to decide when a generic part will be loaded in remainder cell instead of the manufacturing cell designed for the family of the part. A simulation environment has been developed in order to test the proposed policies when market fluctuations occur in terms of product mix and demand. Therefore, the benefits of the proposed approaches are tested in several dynamic conditions compared with a classical cellular manufacturing configuration. The rest of the paper is structured as follows: Section 2 provides an overview of the literature of remainder cells in CMSs, while in Section 3 the problem context is formulated. The loading approaches proposed are described in Section 4. Section 5 presents the simulation

environment and the case study. The numerical results are discussed in Section 6, while the conclusions and future research paths are drawn in Section 7.

2. Literature review

Several authors addressed the problem of adaptability of CMSs when some factors change such as: uncertain in demand, mix fluctuations and new product introduction.

Mak and Wong (2000) investigated the problem of resource allocation in a context of multiple production lines, each line is able to manufacture a range of products. A genetic algorithm was developed for product grouping and allocates the **group to a production line**. The uncertain considered is the volume of product and the demand.

Saad et al.(2002) discussed a multiple objective simulation optimization model for loading flexible cells. The approach developed is composed by three main modules: generic process planning module, a multi-objective algorithm based on *tabu search* method to generate and evaluate candidate part to cell scenarios; the performance**measures** are determined by simulation module.

Huang et al. (2003)developed an algorithm to optimize decision on capacity exchange between rush orders and prescheduled orders. Therefore, it can be considered as a mix production variation on the CMS.

Maddisetty (2005) integrated the design and operational control of CMS when the product demand is stochastic. The configurations investigated are: classical, shared and remainder cells. The performance measures evaluated are the work in process and average flow time.

Süer et al. (2009) proposed a new layered cellular manufacturing system to form dedicated, shared and remainder cells to deal with the probabilistic demand, and its performance is compared with the classical cellular manufacturing system.**The performance of work in process** and average flow time are betterthan the classical cellular system when high demand fluctuation was observed.

Safei et al. (2007) proposed a fuzzy programming based approach to design a cellular manufacturing system under dynamic and uncertain conditions. The dynamic conditions are characterized by multi-period planning horizon, in which the product mix and demand in each period can be different.

Bhandwale andKesavadas (2008) proposed a methodology to incorporate new parts, production mix changes and machines into an existing cellular manufacturing system. The objective is to fit the new parts and machines into an existing cellular manufacturing system thereby increasing machine utilizationand reducing investment in new equipment.

Viguier and Pierreval (2004) proposed an evolutionary programming algorithm to design a hybrid cellular manufacturing system. The hybrid cellular manufacturing system is composed by classical cells and functional cells (i.e. cells composed of machines of the same type). The proposed algorithm is illustrated on a test example with a known optimum.

Mak et al. (2007) presented a methodology to solve the manufacturing cell creation and the production scheduling problems for designing virtual cellular manufacturing systems. The methodology is based on ant colony optimization algorithm and two simple heuristics are developed to assign workstations to the operations of the jobs, and to construct the final schedule. Numerical experiments showed that the proposed algorithm generates excellent final solutions in a much shorter computation time when compared with the genetic algorithm.

Kesen et al. (2009) developeda multi-objective mixed integer programming formulation for job scheduling in virtual manufacturing cells. The objective function is to minimize the sum of the makespanand total traveling distance/cost.

Balakrishnan and Cheng (2007) presented a review research that has been done to address cellular manufacturing of multi period planning horizons, with demand and resources uncertainties. The authors identify, among future areas for research the following: "*Comparison of dynamic cells (in which physical*

cells are reconfigured periodically) versus robust cells (in which cells stay static and uncertainties are managed through strategies such as VCMS) is needed to identify the conditions under which one would be favoured over the other"

Hoeck (2008) proposed an approach for order release and loading problem in a flexible manufacturing cell environment. The workload control approach involves three steps: lead orders are identified; transfer batches of the lead part types are calculated; workload of the machining centres is determined. A simulation environment was used to test the proposed approach.

Drolet et al. (2008) discussed the results of a simulation-based performance comparison between dynamic cellular manufacturing systems and two other well-known systems as classical cells and job shop systems. The experiments conducted regard 13 independent variables related to sources of turbulence and 17 independent variables related to performance measures. The research highlighted in what conditions one system is better than the others.

Renna and Padalino (2009) and Renna et al. (2008) proposed an innovative decision making strategy for autonomous agents in a cellular manufacturing environment by a budget assigned to each job in order to **purchase manufacturing cell services**. The budget manages as a market like approach among agents to coordinate the multi agent system. Moreover, a fuzzy tool has been proposed to assign the budget to each typology job. A simulation environment is developed in order to test the proposed approach. The simulations show that the proposed approach is robust and a scheduling approach able to select the jobs that have been the better performance.

From the analysis of the literature, the following issues can be drawn:

- few papers investigated the performance comparison between cellular manufacturing systems with remainder cells and other configurations. In these papers, the remainder cell is used as a secondary cell that can be used when the manufacturing cells are affected by machine breakdowns.
- most of the researches consider one uncertainty between mix and volume products. Moreover, a research on the rapidity change of volume and mix products was not discussed in literature. The discussion **in the literature** concerns the amplitude of variability of the uncertain (as the standard deviation of stochastic demand).

The aim of this paper is to overcome the above limitations, developing loading approaches in hybrid cellular manufacturing systems composed by classical cells and remainder cells. The use of an opportune loading approach allows **to response to market changes (volume and mix) avoiding the reconfiguration of the manufacturing cells**. Then, a simulation environment has been developed in order to test the proposed approaches introducing market fluctuations (mix and inter-arrival demand) and evaluate the effect of rapidity change of the conditions. A wide range of performance measures are investigated using a classical CMS as a benchmark. **The number of machines is the same for all configurations; therefore, the comparison is evaluated in a mid-term horizon in which only the different configuration is evaluated.**

3. Manufacturing system context

The configurations of the manufacturing system investigated are: classical cellular manufacturing and hybrid cellular with a remainder cell. The objective of this research is the comparison of the performance in **different conditions; therefore**, the composition of the manufacturing cells is known. It has been considered three part families that are manufactured by three manufacturing cells. Then, the configuration with remainder cell is composed by the same number of machines (N machines) re-arranged to include in the manufacturing system the remainder cell. Therefore, the comparison is performed with the same machines changing only the configuration. The demand is not known a priori, and **it follows an** exponential distribution. **Each cell is assumed to be independent, i.e. each family part performs all the operations in only**

one cell. Set-up times are assumed to be zero, because the machines of the manufacturing cells are configured for the particular part family (dedicated machines). The machines of the remainder cell are general purpose machines; therefore, they have a processing time greater than the machines in the manufacturing cells. This increment of processing time is due to the machines that are able to manufacture all part families. The processing time of machine i -th in remainder cell rpt_i is greater than the processing time of the machine i -th in the cell j -th (pt_{ij}). The processing times are correlated by the following expression:

$$\alpha = \frac{rpt_i}{pt_{ij}}, \alpha \geq 1 \quad (1)$$

The cellular manufacturing system has been designed for specific conditions; then, several disturbances have been introduced. These disturbances can be external (demand volatility) or internal (machine breakdowns). In this paper, it has been introduced the following disturbances:

- demand volatility; the volatility has been considered in term of mix fluctuation that changes the volume of each part family. Therefore, the workload of the manufacturing cells changes dynamically. Moreover, it has been considered volume fluctuations requested (inter-arrival time) by the market.
- machine breakdowns; each machine can breakdown randomly with a reduction of the productivity of the manufacturing cells.

Figure 1 shows the classical cellular manufacturing system, where each part family is assigned to the related manufacturing cell designed.

[Insert figure 1 here]

Figure 2 shows the hybrid configuration with the remainder cell. In this case, each part of a family has two possible routings: the manufacturing cell assigned and the remainder cell (the arrows of the figure 2 show the possible routing). The "cell loading policy" controller implements the strategy in order to decide the routing between the two possibilities when a part enters in the manufacturing system. The machines assigned to the remainder cell are able to perform any manufacturing operations required by all part families. The proposed strategies are deeply described in the following paragraph.

[Insert figure 2 here]

4. Loading approaches

The loading approach regards the hybrid manufacturing system with remainder cell; the problem is to decide when a part of a generic family can be manufactured by the remainder cell instead of the manufacturing cell. In literature, the remainder cell is used when an exception occurs such as machine breakdowns. In this paper, three methodologies are proposed to use the remainder cell to keep a high performance level of the entire manufacturing system. The loading approaches proposed are based on the evaluation of the Work InProcess (WIP) of the manufacturing cells: local approach, global and global exclusive approaches.

4.1 Local approach

The loading policy is based on evaluation of the state of each manufacturing cell compared to the state of the remainder cell. The controller of the generic cell j -th (WIP_j) computes the work in process as **the sum of the parts waiting in queues** of the machines that compose the cell.

$$WIP_j = \sum_{i \in j} NQ_i \quad (2)$$

where NQ_i is the **number of parts waiting in the machine's queue** i -th computed for the machines of the cell j -th.

When a part **arrives in the manufacturing** system, the controller will decide if the part enters to the manufacturing cell **designed for its family** or the part enters to the remainder cell (r subscript). The decision is based on the following conditions computed for all manufacturing cells.

$$WIP_j \geq WIP_r \quad (3)$$

$$WIP_j < WIP_r \quad (4)$$

The manufacturing cells that verified the condition (3) re-route the parts to the remainder cell. While, the manufacturing cells that verify the condition (4) don't re-route the parts. Therefore, the generic part of a family **is loaded** in j -th manufacturing cell (**designed for the part family**), if the condition (4) is verified, otherwise **it is loaded** in remainder cell.

This approach allows to limit the level of **the work in process** in the manufacturing cells and, therefore, reducing throughput time and delay of the parts. The main drawback is the possibility **to increase the work** in process in the remainder cell reducing the performance of the parts worked in this cell. This increment is due to the decision strategy; the expressions 3 and 4 don't take into account the global state of the manufacturing system. **Each manufacturing cell decides the re-routing of the parts independently**. The advantage of this approach is the reduction of communication; each manufacturing cell to take the decision needs to know only the state of the remainder cell.

4.2 Global approach

This approach is proposed to avoid the drawback of the local approach evaluating the global state of the manufacturing system. **In this case, each manufacturing cell computes** a congestion level ($cong_j$) related to the WIP of the manufacturing system by the following expression:

$$cong_j = \frac{WIP_j}{\sum_{i=1}^M NQ_i} \in [0,1] \quad (5)$$

where WIP_j is **the same value computed** in expression (2) and the denominator is the sum of the parts **in the queue** for all machines (M) of the manufacturing system (**the work in process of the entire manufacturing system is the global information**).

The part **assigned to the** generic j -th manufacturing cell has to be re-routed to the remainder cell, if two conditions are verified. The first is the following:

$$cong_j = MAX [cong_1, cong_2, \dots, cong_N] \quad (6)$$

The expression (6) means that the manufacturing cell j -th is the cell with maximum value **of the work** in process **compared to other** manufacturing cells (N is the number of manufacturing cells).

The second condition is the following:

$$WIP_j - WIP_r > 1 \quad (7)$$

Expression (7) means that the work in process of the manufacturing cell (j) has to be greater than the remainder cell (r). The difference between the two cells has to be two parts. It is chosen this strategy in order to obtain a work in process of the remainder cell always lower than other manufacturing cells. In fact, if the second part of the expression (7) is zero, when the part enters the remainder cell the two cells have the same work in process. Applying this methodology, the remainder cell plays a role in supporting the main manufacturing cells.

Following this policy, only, the manufacturing cell with higher WIP re-route the parts. However, if the WIP of some manufacturing cells are equal, many parts can be re-route to the remainder cell. For this reason, a modification of this approach is proposed in the following sub-section.

4.3 Global approach exclusive

This approach is simply an adjustment of the previous approach. In some cases, the conditions (6) and (7) can be verified for more than one manufacturing cell. In this approach only one manufacturing cell can re-route the part, if more cells can re-route the part at the same time. In particular, the first manufacturing cell that verifies the expressions (6) and (7) can re-route the part. This approach leads to reduce the utilization of the remainder cell.

5. Simulation environment

The objective of the simulation experiments is to measure the performance of proposed approaches benchmarked to a classical cellular manufacturing system in a very dynamic environment. The authors selected the Arena® discrete event simulation platform by Rockwell Software Inc. it was used to develop the simulation model of the presented approaches. Discrete event simulation – in many commercial tools and simulation packages, nowadays the simulation model is automatically created from high level modeling languages and notations – allows to validate and optimize dynamic and discrete systems such as production systems, but also workflows such as negotiation mechanisms. These models facilitate evaluating different coordination scenarios and maximizing their potential output and benefits. Arena® – based on the known SIMAN simulation language - is well suited for modeling shop floors of production systems in which each entity (part) follows a manufacturing route through production resources (servers, material handling systems, buffers, and so forth), (Kelton and Sadowski, 2009). The manufacturing system consists of ten machines ($M=10$), and it has been considered three part families. The configurations of the manufacturing system have to implement three manufacturing cells ($N=3$). Table 1 reports the mix for each part family.

[Insert table1 here]

In the case of the cellular manufacturing system (used as a benchmark), it has been designed two manufacturing cells with four machines for the part 1 and 2 (the two families have the same part mix); the third manufacturing cell is composed by two machines for the part 3 (lower value of mix). The configuration with the remainder cell consists of three manufacturing cells, but some machines need to be used in the remainder cell and subtracted from the manufacturing cells of the cellular manufacturing system. In this case, the configuration is the following: three machines are assigned for each manufacturing cell dedicated to part 1 and 2; two machines are assigned for the manufacturing cell dedicated to the part 3; two machines are assigned to the remainder cell. The machines assigned to the remainder cell perform the manufacturing operations with higher processing time (see equation 1), because these machines are general

purpose in order to perform any kind of operations. Figure 3 shows the cellular manufacturing system used for the simulation experiments with the assignment of the machines to the cells.

[Insert figure 3 here]

Figure 4 shows the re-configuration of the machines 4 and 8 to form the remainder cell. These machines are configured to perform any kind of operations required by the three part families.

[Insert figure 4 here]

Table 2 reports the processing time of the machines in the two configurations investigated.

[Insert table2 here]

The total time to manufacture the parts is 40 equal for all part families; in this way, the performance comparison is due only to the different configurations. The total processing time is distributed to the machines uniformly. In the case of cellular manufacturing configuration, the machines from 1 to 4 (cell 1) have a processing time of 10 unit times in order to perform all the processing time required (40 unit times); the same processing times are assigned to the machines from 5 to 8 (cell 2); while the machines 9 and 10 (cell 3) have 20 unit times. In case of remainder cell introduction, the cells 1 and 2 have three machines with a processing time of 13.33 unit times. The machines 4 and 8 assigned to the remainder cell have a processing time of 24 unit times. It is assigned a value of $\alpha=1.2$ (see equation 1); the processing time of general purpose machines of remainder cell is greater of 20% than the machines of a cell that are specifically configured for a part family. This choice overestimates the difference of processing time between dedicated and general purpose machines. However, the focus of this paper is the evaluation of the behavior of loading approaches; the study of α will be associated with the economic evaluation of the investment in machines. Parts enter the system following an exponential arrival stream whose inter-arrival times are reported in table 3. The simulations are performed for four congestion levels of the manufacturing system.

[Insert table3 here]

Several experiments have been conducted in order to set the inter-arrival time; the values reported in table 3 allow to obtain an order of magnitude of average utilization of the manufacturing system. These inter-arrival times allow to investigate several degrees of congestion of the manufacturing system.

A due date is assigned to the parts by the following expression:

$$\text{due date} = 40 \bullet \text{duedate}_{\text{index}} \quad (8)$$

The due date is obtained by the technological processing time (40 unit times) multiplied with an index; this index is 1.5 for parts 1 and 2, while it is one for part 3 (part 3 has a low part mix). However, the objective of the research is the comparison of the performance; therefore, the choice of the due date index does not affect the analysis.

Concerning the machine breakdowns, it has been assumed that all the manufacturing machines are subject to faults; Mean Time Between Failures (MTBF) is distributed according to the normal distribution, with mean 2000 unit times and variance 200 unit times. Mean Time To Repair (MTTR) follows a normal distribution with mean 40 unit times and variance 6 unit times (equal for all machines).

6. Simulation results

The proposed approaches are tested in static and dynamic situations; the dynamicity of the manufacturing system is characterized by the stage length and the simulation length is fixed to 43200 time units. In order to emulate a market dynamic environment the demand characteristics (inter-arrival time and product mix) changing during the production run consisting of several alternating stages. Four stage lengths have been considered; table 4 reports the stage length and the number of changes (demand characteristics) that occur over the entire simulation horizon.

[Insert table4 here]

Table 5 describes the design of the simulation experiments conducted for the two configurations of the manufacturing system. Combining the four inter-arrival times, four stage length and the two demand changes (mix and inter-arrival) and the static condition (without any changes) it has been obtained 28 experimental classes.

[Insert table5 here]

The two demand changes are obtained by the following expressions:

$$\text{mix product}_p^* = \text{mix product}_p \bullet \text{UNIFORM}[0.9,1.1], \text{ for product } p=1,2,3; \quad (9)$$

Expression (9) means that the mix of the products (for which the cellular manufacturing systems were designed, mix product_p) is affected by a variation of 20% (1.1-0.9) extracted by a uniform distribution.

$$\text{inter-arrival}^* = 5.5 \bullet \text{UNIFORM}[0.9,1.1] \quad (10)$$

Expression (10) computes the inter-arrival time of the parts starting from 5.5 multiplied for an uncertain of 20% extracted by a uniform distribution. The value 5.5 of inter-arrival time assures a medium level of average utilization of the manufacturing system about 70%. The inter-arrival and mix changes are computed for each alternation between two consequently stages. The uniform distribution is used to simulate demand and mix random fluctuations. For each experiment class, a number of replications able to assure a 5% confidence interval and 95 % of confidence level for each performance measure have been conducted.

The performance measures investigated are the following:

- Throughput time for each part j (*thr. Time j*);
- Average throughput time (*average thr. Time*);
- Throughput (*thr.*);
- Work In Process (WIP);
- Average utilization of the manufacturing system (*av. utilization*);
- Total tardiness time of the parts (*tardiness*).

The results reported in the following tables and figures are an elaboration of the simulation results reported in the appendix. Table 6 reports the percentage difference among the proposed approaches and cellular manufacturing system (used as the base for percentage computation), when the environmental conditions are static and without machine breakdowns. Table 6 reports the average value and the standard deviation of the performance over the congestion levels. The average values show the difference among the approaches if the congestion levels have the same probability to occur. The standard deviation (*dev.st*) is an index of the performance variation when the congestion level changes (robustness).

[Insert table6 here]

The results of the table 6 show that in a static condition and without machine breakdowns, the cellular manufacturing system leads to the better performance level. Only, the throughput time of the part 3

improves, because the remainder cell can support the related manufacturing cell when the peak of WIP_3 occurs. The influence of congestion levels is very low except for tardiness and throughput time of the part 3 (see dev.st of table 6). Table 7 reports the same analysis of table 6 with machine breakdowns.

[Insert table7 here]

From the analysis of table 7 the following issues can be drawn:

- The local approach leads to performance very close to the cellular manufacturing system, except for the tardiness performance. In fact, the main benefit of this approach is the reduction of the tardiness (average of 16%).
- The global approach leads to worst performance for all measures, except the throughput time of the part 3. However, the average throughput time gets worse than the cellular manufacturing system. The global approach exclusive reduces the deterioration of the performance, but the performance measures are worse than the cellular manufacturing system.
- Generally, the performance measures that are influenced by the congestion level are the tardiness and the throughput time of the part 3 (for these performance measures the standard deviation is relevant).

Table 8 reports the percentage difference among the proposed approaches and the cellular manufacturing system for different congestion levels, when mix fluctuations are present. The values reported are the average over the different stage lengths; the performance measures have a low dependence on stage length (as showed in appendix with the numerical results).

[Insert table8 here]

In these environmental conditions, the proposed approaches lead to better results for all performance measures of the manufacturing system: reduction of average throughput time, reduction of work in process and reduction of tardiness. The global approach and global approach exclusive increase the benefit compared to the cellular manufacturing system. It can be noticed that the reduction of throughput time is obtained for all family parts, while the local approach reduces only the throughput time of the part 3. Moreover, the performance measures of the global and global exclusive have a greater dependence on the congestion levels than the local (see dev.st). In particular, the benefits of two global approaches are relevant in cases of medium and high congestion levels (inter-arrival 4.5 and 5), while in case of low congestion level (inter arrival 7) the performance measures are worse than the cellular manufacturing system.

Table 9 reports the simulation results when the inter-arrival fluctuation is present. Also, in this case the values are the average over the stage lengths.

[Insert table9 here]

The results show how the proposed approaches lead to better results when the inter-arrival fluctuation occurs. The improvement of the performance is better for the global and global exclusive approaches (very similar between them). The stage length has a low influence on the results' comparison, because the standard deviation values are very low. The above comments are valid when the inter-arrival and mix fluctuations are present together (see table 10). In this case, the improvements are greater than the case of only inter-arrival fluctuations.

[Insert table10 here]

In summary, the three performance measures with higher improvement are: average throughput time, work in process and tardiness. Figures 5a, 5b and 5c show the percentage difference among the proposed

approaches and the cellular manufacturing system over the different unforeseen events considered. As the reader can notice, when the conditions are static the approach with remainder cell leads to worst performance while, the loading approaches with remainder cell lead to better performance measures with the introduction of exceptions (mix and inter-arrival fluctuations and machine breakdowns).

[Insert figure 5 here]

7. Conclusions and future development

The paper proposes loading policies for cellular manufacturing systems with a general purpose cell defined in literature remainder cell. A simulation environment has been developed to test the proposed approaches compared to a classical cellular manufacturing system. The simulations have been conducted in static conditions and in a very dynamic environment with market changes (mix and inter-arrival time fluctuations) and machine breakdowns. The results of this research can be summarized as it follows:

- The cellular manufacturing configuration is better when the market conditions are static, this validates the benchmark developed;
- The proposed loading policies allow to obtain relevant improvements of the performance when mix fluctuations occur. The benefits are reduced when the inter-arrival fluctuations occur, but however, the proposed approaches are better than the cellular manufacturing configuration. The performance measure with better improvement is the due date (tardiness). The performance of work in process and average throughput time are also improved.
- The two approaches with the better performance (global and global exclusive) have higher dependence on the congestion levels, while the local approach is more robust.
- The better performance of the global approaches than the local approach underlines that the decision taken on global information can lead to relevant improvements of the performance measures.
- Finally, the low values of standard deviation when external and internal exceptions occur (see table 10) show that the proposed approaches are robust to the rapidity change of the manufacturing system conditions.

In briefly, the remainder cell was used in literature as a cell to support the manufacturing cells when machine breakdowns occur; the loading policies proposed show how the remainder cell can be used to keep a high level of performance when market fluctuations happen. The benefits of the remainder cell are evaluated when the processing time of the remainder cell is greater than the dedicated cell. This assumption is made to introduce the effect of the efficiency; general purpose machines can be less efficient than task-specific dedicated machines.

This strategy can avoid the re-configuration of cellular manufacturing systems when market conditions change, reducing costs and set-up times.

Future research paths concern the following issues. The performance measures of the hybrid cellular manufacturing system for different amplitude of market fluctuations. Another future research path is the evaluation of the increment of processing time for the machines assigned to the remainder cell. This analysis needs to be conducted with the related investment cost in machines, because the parameter α is strength related to the cost of machines.

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Figure 1. Cellular manufacturing system

Figure 2. Cellular manufacturing system with remainder cell

Figure 3. Cellular manufacturing system

Figure 4. Cellular manufacturing system with remainder cell

Figure 5a. Average throughput time

Figure 5b. Tardiness

Figure 5c. Work In Process

Legend

1	Local approach
2	Global approach
3	Global approach exclusive

	Part 1	Part 2	Part 3
Part mix	40%	40%	20%

Table 1. Partmix

For Peer Review Only

	machine 1	machine 2	machine 3	machine 4	machine 5
Processing time (cellular)	10	10	10	10	10
Processing time (remainder)	13.33	13.33	13.33	24	13.33
	machine 6	machine 7	machine8	machine 9	machine 10
Processing time (cellular)	10	10	10	20	20
Processing time (remainder)	13.33	13.33	24	20	20

Table 2. Processing times

For Peer Review Only

	int 1	int 2	int 3	Int 4
Inter arrival time parameter [unit times]	4.5	5	6	7
Average utilization [order of magnitude]	0.9	0.8	0.65	0.55

Table 3. Inter-arrival time

For Peer Review Only

Stage length	Number of changes
8640	5
4320	10
2880	15
2160	20

Table 4. Stage length

For Peer Review Only

Exp. no.	Inter-arrival	Stage length	Mix changes	Inter-arrival changes
1	4.5	Static	no	no
2	5	Static	no	no
3	6	Static	no	no
4	7	Static	no	no
5	4.5	8640	yes	no
6	5	8640	yes	no
7	6	8640	yes	no
8	7	8640	yes	no
9	4.5	4320	yes	no
10	5	4320	yes	no
11	6	4320	yes	no
12	7	4320	yes	no
13	4.5	2880	yes	no
14	5	2880	yes	no
15	6	2880	yes	no
16	7	2880	yes	no
17	4.5	2160	yes	no
18	5	2160	yes	no
19	6	2160	yes	no
20	7	2160	yes	no
21	5.5	8640	no	yes
22	5.5	4320	no	yes
23	5.5	2880	no	yes
24	5.5	2160	no	yes
25	5.5	8640	yes	yes
26	5.5	4320	yes	yes
27	5.5	2880	yes	yes
28	5.5	2160	yes	yes

Table 5. Experimental plan

	Thr. Time 1	Thr. Time 2	Thr. Time 3	Average Thr. time	Thr.	WIP	Av. utilization	tardiness
Local approach								
Average	8.69%	8.71%	-22.87%	0.66%	-0.13%	0.57%	3.27%	-9.48%
Dev.st	5.02%	4.88%	12.65%	1.79%	0.28%	1.71%	1.78%	6.89%
Global approach								
Average	23.83%	23.73%	-19.07%	13.04%	-0.05%	13.02%	3.47%	77.87%
Dev.st	2.78%	2.84%	12.54%	3.13%	0.23%	3.18%	1.95%	65.74%
Global approach exclusive								
Average	15.80%	15.78%	-20.55%	6.62%	-0.08%	6.57%	3.01%	27.94%
Dev.st	4.28%	4.50%	12.30%	2.17%	0.18%	2.21%	1.60%	27.36%

Table 6. Simulation results - static environment without machine breakdowns

Inter-arrival	Thr. Time 1	Thr. Time 2	Thr. Time 3	Average Thr. time	Thr.	WIP	Av. utilization	tardiness
Local approach								
Average	5.08%	4.60%	-24.04%	-2.04%	-0.08%	-2.12%	4.25%	-16.00%
Dev.st	6.43%	5.53%	12.16%	3.16%	0.05%	3.19%	0.44%	10.27%
Global approach								
Average	17.79%	18.96%	-20.17%	9.96%	-0.16%	9.86%	4.26%	44.88%
Dev.st	2.69%	3.47%	12.32%	3.67%	0.10%	3.63%	0.38%	41.22%
Global approach exclusive								
Average	12.69%	12.11%	-21.45%	4.40%	-0.14%	4.27%	0.85%	12.97%
Dev.st	5.69%	4.66%	11.84%	2.94%	0.23%	2.78%	4.84%	15.00%

Table 7. Simulation results - static environment with machine breakdowns

Inter-arrival	Thr. Time 1	Thr. Time 2	Thr. Time 3	Average Thr. time	Thr.	WIP	Av. utilization	tardiness
Local approach								
4.5	5.88%	5.52%	-43.67%	-6.83%	-0.02%	-6.87%	3.66%	-13.08%
5	-0.25%	-0.78%	-31.34%	-7.91%	0.04%	-7.88%	4.14%	-25.73%
6	1.18%	1.46%	-18.11%	-3.09%	-0.10%	-3.16%	4.43%	-25.26%
7	2.80%	2.87%	-12.21%	-0.48%	-0.32%	-0.82%	4.14%	-21.83%
Average	2.40%	2.27%	-26.33%	-4.58%	-0.10%	-4.68%	4.09%	-21.48%
Dev.st	2.63%	2.64%	14.06%	3.42%	0.16%	3.28%	0.32%	5.86%
Global approach								
4.5	-18.20%	-18.61%	-51.97%	-26.96%	0.00%	-27.05%	4.09%	-46.21%
5	-6.82%	-7.30%	-34.29%	-13.60%	-0.04%	-13.67%	3.76%	-39.39%
6	2.98%	2.86%	-18.57%	-1.94%	-0.05%	-2.00%	3.63%	-18.02%
7	6.34%	6.42%	-12.13%	2.32%	-0.06%	2.23%	2.91%	1.35%
Average	-3.93%	-4.16%	-29.24%	-10.05%	-0.04%	-10.12%	3.60%	-25.57%
Dev.st	11.03%	11.25%	17.78%	13.13%	0.03%	13.14%	0.50%	21.59%
Global approach exclusive								
4.5	-18.51%	-18.84%	-51.81%	-27.12%	0.06%	-27.17%	4.09%	-46.50%
5	-7.36%	-8.38%	-34.32%	-14.23%	-0.08%	-14.33%	3.79%	-41.23%
6	2.83%	2.78%	-18.55%	-2.03%	-0.02%	-2.08%	3.63%	-18.77%
7	6.47%	6.31%	-12.02%	2.35%	-0.03%	2.26%	3.21%	1.29%
Average	-4.14%	-4.53%	-29.18%	-10.26%	-0.02%	-10.33%	3.68%	-26.30%
Dev.st	11.23%	11.41%	17.76%	13.25%	0.06%	13.24%	0.37%	21.98%

Table 8. Simulation results - mix changes

Exp. no.	Thr. Time 1	Thr. Time 2	Thr. Time 3	Average Thr. time	Thr.	WIP	Av. utilization	tardiness
Local approach								
Average	1.31%	1.10%	-23.05%	-4.36%	-0.02%	-4.42%	4.61%	-22.70%
Dev.st	0.16%	0.17%	0.39%	0.22%	0.14%	0.37%	0.22%	0.90%
Global approach								
Average	-0.79%	-1.01%	-24.59%	-6.34%	0.07%	-6.36%	4.09%	-28.56%
Dev.st	0.34%	0.40%	0.23%	0.25%	0.50%	0.69%	0.14%	1.18%
Global approach exclusive								
Average	-0.95%	-1.05%	-24.37%	-6.36%	0.00%	-6.42%	3.85%	-28.85%
Dev.st	0.08%	0.17%	0.39%	0.15%	0.22%	0.36%	0.29%	0.74%

Table 9. Simulation results - inter-arrival changes

Exp. no.	Thr. Time 1	Thr. Time 2	Thr. Time 3	Average Thr. time	Thr.	WIP	Av. utilization	tardiness
Local approach								
Average	0.18%	-0.11%	-24.33%	-5.61%	-0.14%	-5.76%	3.73%	-26.18%
Dev.st	0.25%	0.12%	0.52%	0.22%	0.26%	0.39%	1.03%	0.77%
Global approach								
Average	-1.63%	-2.17%	-26.04%	-7.50%	-0.32%	-7.81%	3.63%	-31.50%
Dev.st	0.85%	0.66%	0.38%	0.58%	0.26%	0.74%	0.29%	1.73%
Global approach exclusive								
Average	-1.71%	-2.20%	-25.78%	-7.49%	-0.09%	-7.56%	3.63%	-31.52%
Dev.st	0.57%	0.43%	0.25%	0.38%	0.17%	0.40%	0.35%	1.18%

Table 10. Simulation results - inter-arrival and mix changes

APPENDIX

WIP [parts]

Thr. Time [unit time]

Average Thr. Time [unit time]

Tardiness [unit time]

Inter-arrival	WIP	Thr. Time 1	Thr. Time 2	Thr. Time 3	Average Thr. time	Tardiness	Thr.	Av. utilization
Cellular manufacturing system								
4.5	19.350	79.250	79.150	118.560	87.160	339000	13.294	0.880
5	12.800	60.040	59.840	80.040	64.000	128000	11.980	0.790
6	8.690	49.890	50.130	60.320	52.090	42335	10.010	0.660
7	6.820	46.570	46.630	53.158	47.920	20479	8.530	0.566
Local approach								
4.5	19.580	92.080	91.770	72.970	88.160	333000	13.300	0.916
5	12.60	64.070	64.150	58.250	62.940	108000	11.990	0.827
6	8.700	52.770	52.810	50.610	52.350	36006	9.960	0.686
7	6.990	49.400	49.580	47.990	49.190	19339	8.520	0.592
Global approach								
4.5	21.400	101.260	101.170	77.170	96.430	411000	13.280	0.914
5	14.120	72.950	72.590	61.800	70.580	170000	11.980	0.828
6	9.920	61.030	61.470	53.040	59.610	81686	9.980	0.692
7	7.980	57.610	57.430	49.700	55.960	54160	8.550	0.596
Global approach exclusive								
4.5	20.621	96.850	96.980	76.340	92.830	376000	13.290	0.915
5	13.270	68.100	67.910	60.070	66.430	134000	11.970	0.822
6	9.290	56.730	56.810	51.960	55.810	55324	9.980	0.684
7	7.440	53.020	53.060	49.020	52.250	33884	8.540	0.588

Table A1. Numerical results - Static environment without machine breakdowns

Inter-arrival	WIP	Thr. Time 1	Thr. Time 2	Thr. Time 3	Average Thr. time	tardiness	Thr.	Av. utilization
Cellular manufacturing system								
4.5	26.000	108.790	110.910	144.650	116.980	609000	13.300	0.880
5	15.100	72.300	72.300	88.340	75.570	213000	11.970	0.790
6	9.440	54.950	55.100	63.100	56.660	66439	9.990	0.660
7	7.280	49.700	49.850	55.430	50.910	32775	8.570	0.570
Local approach								
4.5	26.158	124.640	125.040	88.550	117.620	604000	13.290	0.915
5	14.120	72.670	72.700	62.900	70.730	165000	11.970	0.824
6	9.210	55.980	56.150	52.470	55.350	51813	9.980	0.692
7	7.270	51.370	51.440	48.940	50.910	26673	8.560	0.592
Global approach								
4.5	28.290	135.750	135.930	93.170	127.330	697000	13.280	0.913
5	15.960	83.280	82.940	67.030	79.900	242000	11.960	0.823
6	10.430	64.630	64.860	54.800	62.760	99858	9.960	0.690
7	8.330	59.920	60.240	51.100	58.290	65920	8.560	0.596
Global approach exclusive								
4.5	27.540	131.590	131.800	92.48	123.890	664000	13.290	0.912
5	15.132	78.100	78.230	65.65	75.680	205000	11.980	0.824
6	9.890	60.700	60.710	54.04	59.380	75866	9.980	0.684
7	7.730	55.330	55.440	50.07	54.330	43396	8.530	0.584

Table A2. Numerical results - Static environment

Inter-arrival	WIP	Thr. Time 1	Thr. Time 2	Thr. Time 3	Average Thr. time	tardiness	Thr.	Av. utilization
Cellular manufacturing system								
4.5	29.750	123.450	124.840	168.680	133.760	769000	13.290	0.880
5	15.660	74.220	74.440	93.480	78.330	237000	11.980	0.790
6	9.530	55.230	55.420	64.230	57.160	69743	9.990	0.662
7	7.320	50.130	49.970	55.650	51.190	34091	8.570	0.570
Local approach								
4.5	26.590	126.990	127.120	89.930	119.720	624000	13.280	0.910
5	14.300	73.490	73.700	63.180	71.540	172000	11.980	0.824
6	9.180	55.900	55.980	52.350	55.240	51233	9.970	0.689
7	7.200	51.460	51.240	48.750	50.840	26054	8.490	0.590
Global approach								
4.5	20.840	98.280	97.990	76.410	93.870	386000	13.290	0.916
5	13.370	68.430	68.820	60.320	67.000	139000	11.960	0.820
6	9.310	57.020	56.920	51.960	56.000	56732	9.960	0.684
7	7.460	53.040	53.240	49.020	52.330	34375	8.550	0.583
Global approach exclusive								
4.5	20.830	98.100	98.000	76.230	93.780	385000	13.300	0.916
5	13.260	68.330	67.710	60.040	66.460	134000	11.950	0.822
6	9.290	56.730	56.790	52.090	55.840	55651	9.980	0.684
7	7.470	53.120	53.050	49.140	52.310	34345	8.570	0.587

Table A3. Numerical results - Mix changes (stage length: 8640)

Inter-arrival	WIP	Thr. Time 1	Thr. Time 2	Thr. Time 3	Average Thr. time	tardiness	Thr.	Av. utilization
Cellular manufacturing system								
4.5	28.713	120.480	120.660	161.370	129.150	725000	13.290	0.880
5	15.610	73.680	73.940	94.410	78.040	234000	11.980	0.792
6	9.4700	55.230	55.310	63.860	57.030	68844	9.960	0.660
7	7.2900	49.810	50.060	55.690	51.110	33848	8.550	0.569
Local approach								
4.5	26.640	127.250	127.430	89.450	119.840	625000	13.290	0.913
5	14.290	73.690	73.620	62.720	71.500	171000	11.970	0.823
6	9.2100	55.880	56.250	52.460	55.350	51827	9.970	0.690
7	7.2500	51.210	51.420	49.020	50.860	26573	8.540	0.592
Global approach								
4.5	20.900	98.520	98.300	76.410	94.070	388000	13.300	0.916
5	13.400	68.730	68.930	60.210	67.130	140000	11.960	0.820
6	9.300	56.920	56.640	52.180	55.870	56155	9.980	0.686
7	7.470	53.110	53.340	48.920	52.380	34736	8.550	0.583
Global approach exclusive								
4.5	21.020	98.780	98.720	77.380	94.520	393000	13.310	0.916
5	13.310	68.080	68.380	60.450	66.690	136000	11.960	0.822
6	9.300	56.860	56.840	52.060	55.910	56135	9.970	0.684
7	7.440	53.070	53.150	48.930	52.290	34081	8.530	0.584

Table A4. Numerical results - Mix changes (stage length: 4320)

Inter-arrival	WIP	Thr. Time 1	Thr. Time 2	Thr. Time 3	Average Thr. time	tardiness	Thr.	Av. utilization
Cellular manufacturing system								
4.5	28.130	118.970	119.020	155.050	126.510	699000	13.290	0.880
5	15.550	73.690	75.250	90.820	77.820	232000	11.970	0.794
6	9.500	55.580	55.220	63.600	57.070	68734	9.980	0.660
7	7.300	49.830	50.010	56.120	51.180	34309	8.550	0.566
Local approach								
4.5	26.630	127.210	127.470	89.460	119.820	625000	13.290	0.913
5	14.280	73.420	73.810	63.010	71.510	171000	11.970	0.823
6	9.240	56.190	56.220	52.410	55.450	52426	9.980	0.692
7	7.250	51.300	51.470	49.070	50.920	26794	8.540	0.592
Global approach								
4.5	20.870	98.370	98.290	76.400	93.980	388000	13.290	0.916
5	13.430	68.770	69.140	60.340	67.250	141000	11.970	0.822
6	9.320	56.890	57.240	52.060	56.080	57341	9.970	0.684
7	7.460	53.220	52.930	49.010	52.280	34236	8.550	0.586
Global approach exclusive								
4.5	20.760	97.710	97.580	76.720	93.500	383000	13.290	0.916
5	13.280	68.270	68.040	60.370	66.610	136000	11.950	0.820
6	9.290	56.840	56.870	52.140	55.920	56172	9.960	0.684
7	7.460	53.010	53.100	49.100	52.270	34139	8.560	0.588

Table A5. Numerical results - Mix changes (stage length: 2880)

Inter-arrival	WIP	Thr. Time 1	Thr. Time 2	Thr. Time 3	Average Thr. time	tardiness	Thr.	Av. utilization
Cellular manufacturing system								
4.5	27.680	117.170	117.420	152.450	124.590	681000	13.290	0.880
5	15.250	73.110	73.590	88.390	76.430	220000	11.950	0.790
6	9.500	55.200	55.390	64.140	57.100	69468	9.970	0.660
7	7.270	49.790	49.810	55.460	50.950	33092	8.550	0.567
Local approach								
4.5	26.490	126.660	126.300	89.760	119.180	619000	13.290	0.913
5	14.300	73.360	73.760	62.980	71.460	171000	11.980	0.827
6	9.170	55.870	56.130	52.280	55.260	51358	9.940	0.688
7	7.240	51.180	51.450	48.870	50.830	26352	8.540	0.592
Global approach								
4.5	20.700	97.400	97.480	76.500	93.280	381000	13.280	0.916
5	13.380	68.670	68.630	60.200	66.980	139000	11.970	0.823
6	9.310	57.010	56.880	52.110	55.990	56678	9.970	0.684
7	7.440	52.840	53.170	48.920	52.190	33801	8.550	0.586
Global approach exclusive								
4.5	20.560	96.500	96.700	76.420	92.600	374000	13.290	0.916
5	13.320	68.330	68.160	60.100	66.630	136000	11.980	0.822
6	9.330	57.070	57.000	52.070	56.060	56864	9.980	0.686
7	7.470	53.270	53.150	48.950	52.370	34494	8.550	0.586

Table A6. Numerical results - Mix changes (stage length: 2160)

Stage Length	WIP	Thr. Time 1	Thr. Time 2	Thr. Time 3	Average Thr. time	tardiness	Thr.	Av. utilization
Cellular manufacturing system								
8640	11.710	62.000	62.050	73.100	64.270	120000	10.910	0.720
4320	11.710	61.830	62.100	73.300	64.270	120000	10.910	0.720
2880	11.740	61.870	62.100	73.790	64.370	121000	10.920	0.723
2160	11.720	61.860	62.110	73.090	64.230	120000	10.930	0.720
Local approach								
8640	11.250	62.890	62.870	56.550	61.620	94149	10.930	0.754
4320	11.170	62.580	62.690	56.290	61.380	92256	10.900	0.754
2880	11.180	62.580	62.710	56.430	61.410	92398	10.910	0.754
2160	11.210	62.760	62.810	56.400	61.520	92984	10.920	0.754
Global approach								
8640	10.970	61.440	61.370	55.250	60.180	85759	10.920	0.748
4320	11.010	61.460	61.440	55.440	60.250	86338	10.950	0.750
2880	11.060	61.600	61.810	55.450	60.460	87777	10.970	0.753
2160	10.860	61.110	61.220	55.030	59.950	83760	10.860	0.750
Global approach exclusive								
8640	11.010	61.390	61.520	55.590	60.290	86458	10.940	0.750
4320	10.970	61.310	61.480	55.390	60.210	85675	10.920	0.748
2880	10.940	61.230	61.400	55.430	60.150	85101	10.900	0.748
2160	10.950	61.290	61.340	55.380	60.140	85009	10.910	0.748

Table A7. Numerical results - interarrival changes

Stage Length	WIP	Thr. Time 1	Thr. Time 2	Thr. Time 3	Average Thr. time	tardiness	Thr.	Av. utilization
Cellular manufacturing system								
8640	11.920	62.910	63.060	74.330	65.330	128000	10.920	0.724
4320	11.990	63.140	63.290	75.180	65.670	130000	10.940	0.723
2880	11.900	62.500	62.710	75.150	65.170	127000	10.940	0.725
2160	11.920	62.600	63.090	74.810	65.290	127000	10.940	0.722
Local approach								
8640	11.290	63.020	63.100	56.790	61.830	95598	10.940	0.740
4320	11.270	63.040	63.170	56.620	61.830	95425	10.920	0.754
2880	11.170	62.680	62.620	56.570	61.440	92676	10.890	0.754
2160	11.250	62.860	62.990	56.630	61.680	94243	10.930	0.754
Global approach								
8640	10.920	61.510	61.480	55.180	60.250	86315	10.850	0.748
4320	10.970	61.610	61.470	55.320	60.310	86632	10.900	0.748
2880	11.050	62.120	61.860	55.370	60.690	89043	10.910	0.753
2160	11.060	61.820	61.860	55.600	60.600	88684	10.940	0.750
Global approach exclusive								
8640	10.970	61.500	61.480	55.360	60.280	86289	10.900	0.750
4320	11.060	61.790	61.630	55.620	60.500	88044	10.950	0.752
2880	11.010	61.620	61.610	55.630	60.430	87314	10.910	0.748
2160	11.080	61.940	61.890	55.650	60.670	88933	10.940	0.749

Table A8. Numerical results - interarrival and mix changes