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ACCEPTED MANUSCRIPT

Muon Production Height Studies with the Air Shower Experiment KASCADE-Grande

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Abstract

A large area (128 m²) muon tracking detector, located within the KASCADE experiment, has been built with the aim to identify muons ($E_\mu > 0.8$ GeV) and their angular correlation in extensive air showers by track measurements under 18 r.l. shielding. Orientation of the muon track with respect to the shower axis is expressed in terms of the radial and tangential angles, which are the basic tools for all muon investigations with the tracking detector. By means of triangulation the muon production height is determined. Distributions of measured production heights are compared to CORSIKA shower simulations. Analysis of these heights reveals a transition from light to heavy cosmic ray primary particles with increasing shower energy in the energy region of the 'Knee' of the cosmic ray spectrum.

Key words: Cosmic rays, Air shower, Muons, Muon production height

1. Introduction

Ultra High Energy (UHE) astrophysics includes, as one of its topics, the investigation of UHE Cosmic Ray (CR) particles interacting with the nuclei of the atmosphere and creating Extensive Air Showers (EAS) which are studied by means of ground based experiments of large detection area. To understand the nature of UHE particles it is necessary to measure as many components of the EAS cascade as possible. Particularly important is the measurement of the muon component, because muons, being a result of decays of mesons - the most numerous products of hadronic interactions in an air shower - carry information about those interactions to the observation level. In turn, knowledge of UHE hadronic interactions is a necessary condition for answering many questions formulated in CR research. The angular correlation information on EAS muons measured with the tracking detector is especially closely correlated to the parameters of the interactions in question. A recent compilation of muon study results is given in Ref. [1].

In the past, various tracking detectors for measuring CR particles have been put into operation either on the surface of Earth [2]-[8] or deep under-

ground [9]. Currently active installations for muon and neutrino studies are IceCube [10], ANTARES [11] and MINOS [12]. Tracking detectors provide the possibility to study the muon production height which is the subject of this work.

Muon information has usually been integrated over a large sample of showers and over the whole longitudinal profile. However, muons have some advantage compared with optical photons [13]-[15]: they reflect the development of the nuclear cascade with no mediation from electromagnetic cascades and, similar to the radio emission [16], they can be measured 24 hours a day - not only on clear moonless nights. Their evident disadvantage is that muons are less numerous than photons and are, therefore, subject to large fluctuations. In addition, they are charged particles and are subject to deflection in the geomagnetic field and also suffer from multiple Coulomb scattering in the atmosphere and detector shielding.

Muon tracking allows to measure the composition sensitive profile of a shower in the 'Knee' region, where it is not possible by the fluorescence technique used, e.g. by Fly's Eye [17] and Auger [18] experiments. It enables as well the study of hadron interactions [19, 20]. Muons have never been used up to now, with sufficient accuracy and large statistics, for the reconstruction of the longitudinal development of the EAS hadron component of individual showers due to the difficulty of building large area, ground-based muon telescopes. The reconstruction of the longitudinal development of the muon component by means of triangulation [21]-[24] provides a powerful tool for primary mass estimation and for study of high-energy hadron interactions with atmospheric nuclei.

The KASCADE-Grande air-shower experiment [25], set-up in Karlsruhe, Germany provides information on individual EAS up to primary energy 10^{18} eV. Complex analyses of KASCADE data [26] resulted in CR flux spectra for five groups of primary masses over the 'Knee' region. However, these spectra exhibit a strong dependence on the hadronic interaction models used in the data analysis. Therefore, an independent investigation of additional shower observables like muon angular correlations with respect to the shower direction is of a great importance. To address this task a Muon Tracking Detector (MTD) [27] was constructed providing additional information on muons for the measured EAS.

In this work we present the experimental investigation of the hadronic cascade in EAS using tracks of muons measured at the KASCADE-Grande experiment. Precise angular information on those tracks is used to determine

muon production heights. The sensitivity of this quantity to the mass and energy of CR primary particles is shown. The validity of hadronic interaction models used in Monte Carlo simulations is discussed. Due to the energy dependence of muon production height a transformation to muon production depth is used to investigate, in a model independent way, the CR composition. An estimate of the composition covering two decades of primary energy around the 'Knee' is given.

2. Muon Tracking Detector (MTD) in KASCADE-Grande

The original KASCADE experiment [28], with its array of scintillation counters registering the electron and muon components in EAS has been enlarged into KASCADE-Grande in 2001 - 2003 by adding the extended 'Grande' array of scintillation counters. The MTD was put into operation and started regular data taking in the beginning of 2003. It provides additional information on muons for the two parts of the experiment: KASCADE and Grande. Both arrays trigger the MTD.

The MTD utilizes streamer tube (ST) gas detectors grouped in modules. Four modules, three positioned on horizontal planes (top, middle, bottom) and one arranged vertically (wall), form a muon telescope, called a detector tower. The whole MTD comprises 16 towers arranged in two rows of a total detection area of 128 m². A multi-layer filter of six 3 cm thick iron plates, separated each by 5 cm of sand, covered with soil and resting on 30 cm of steel-concrete roof, absorbs a large fraction of accompanying low-energy particles, thus enhancing the identification of muons with an energy exceeding 0.8 GeV. The details of the design and performance of the MTD can be found elsewhere [27, 29].

The MTD shows a good stability of operation. Hereby, the stability of the gas composition on the sub-percent level is of great importance. However, the open gas system is influenced by the atmospheric pressure and temperature (internal in the detector T_{int} and atmospheric T_{atm}), which is observed in the measured free monitor muon count rate. After applying corrections, the free monitor rate (R) has a remaining variation of about 1%. The resulting temperature and pressure coefficients of the rate, together with the gas composition stability parameters, are given in Table 1. They provide the parameters for the MTD track efficiency determination and correction for temperature and pressure, i.e. for varying atmospheric conditions at KASCADE-Grande.

Figure 1: Anode wire amplitude spectra for individual odd/even numbered wire cells.

92 The analysis is based on 3-hit tracks, which are derived from x and y
 93 (wire and strip) hits in the 3 horizontal modules for each tower. Using 3-hit
 94 tracks only, together with the track quality parameter discussed in Ref. [27],
 95 makes the amount of tracks uncorrelated with a shower being below 1 %.
 96 The modules show, after correction for geometry, pressure and temperature
 97 variations, a hit efficiency close to 100%, varying on average by less than 1%.
 98 The track efficiency (ϵ) stability parameter is given in Table 1. The cluster
 99 sizes are limited to 10 cm at the wires and to 16 cm at the strips to control
 100 punch-through effects and to achieve tracks of a good quality. More details on
 101 track quality and its influence on the direction determination and comparison
 102 with shower and detector simulations can be found in Refs. [27], [30] and [31].
 103 Previously, the anode wire readout in the MTD was operated by combin-
 104 ing two neighboring wire cells. To improve the angular resolution a mod-
 105 ification was introduced [32], enabling to identify even and odd numbered
 106 wires, using the same common readout electronic channel. The individual
 107 wire cells are identified by means of the pulse shape, as illustrated in Fig. 1.
 108 This procedure improves the angular resolution by 30%.

109 3. Tangential and Radial Angles

110 The KASCADE-Grande data, both from the KASCADE and 'Grande'
 111 detector arrays, allow us, after detailed analysis steps [33], [34], [35] to
 112 determine the direction (θ and ϕ), the shower core position, the total number
 113 of electrons - electron size $\lg(N_e)$, and the total number of muons - muon
 114 size $\lg(N_\mu)$, for each shower. In KASCADE the so-called 'truncated' muon

Table 1: Variation of track efficiency (ϵ), Monitor Rate (R) and Gas Composition Stability Parameters of the MTD

$d\epsilon/dT_{int}$	$+(0.16\pm0.02) \text{ } \%/^{\circ}\text{C}$
$d\epsilon/dp_{int}$	$-(0.12\pm0.04) \text{ } \%/mb$
dR/dT_{atm}	$-(0.31\pm0.02) \text{ } \%/^{\circ}\text{C}$
dR/dp_{atm}	$-(0.12\pm0.04) \text{ } \%/mb$
Argon	$13.8\pm0.1\%$
CO ₂	$54.0\pm0.1\%$
Isobutane	$30.2\pm0.1\%$
Ethanol	$2.0\pm0.2\%$

number $\lg(N_{\mu}^{tr})$, is evaluated in the distance range 40-200 m from the shower core. In 'Grande' the muon size is determined in a different way [35]. The 'truncated' muon number is approximately related to the total muon number in the following way: $\lg(N_{\mu}) \approx \lg(N_{\mu}^{tr}) + 0.5$ [36]. This relation, obtained by simulations, results for the same showers reconstructed with KASCADE and Grande separately in similar muon shower size $\lg(N_{\mu})$ values within 10-15 %.

Determination of primary cosmic ray energy from the parameters of registered air showers is of primary interest for all EAS experiments. In KASCADE-Grande total energy E_0 of the primary CR particle, in GeV, can be expressed in an almost mass independent manner through $\lg(N_e)$ and $\lg(N_{\mu})$. Based on extensive simulation studies [37] with CORSIKA [38], using QGSJet01 [39] the following formula is found

$$\lg(E_0) = a \cdot \lg(N_e) + b \cdot \lg(N_{\mu}) + c \quad , \quad (1)$$

where the parameters have the following values. For the KASCADE array data analysis $a = 0.19$, $b = 0.79$ and $c = 2.33$, and in addition, $\lg(N_{\mu}^{tr})$ is used instead of $\lg(N_{\mu})$. For the Grande array analysis, following Ref. [40], we have $a = 0.31$, $b = 0.67$ and $c = 1.85$. Note, that because of the large coefficient for $\lg(N_{\mu})$ this parameter is sometimes used to demonstrate the behavior of various shower quantities as a function of primary energy, where an increase in $\lg(N_{\mu})$ means increase in E_0 . Formula (1) gives ≈ 10 -20 % (depending on the primary energy range) uncertainty in energy determination which is sufficient for this study. Investigation of an improved determination of E_0 in KASCADE-Grande is in progress and first results can be found in [41] and

137 references therein.

Figure 2: Illustration of the angular correlations in EAS and the definition of the radial (ρ) and tangential (τ) angles. The differences between the true and the reconstructed h_μ values for the two reconstruction approaches - see text - are also shown.

138 For the determination of the muon production height h_μ in EAS, orien-
 139 tation of the muon track with respect to the shower axis has to be investi-
 140 gated. Due to their transverse momentum parent mesons travel away from
 141 the shower axis. To investigate angular correlation of the muon track with
 142 respect to the shower axis, the angle in space between both directions is de-
 143 composed into two components: the radial (ρ) and the tangential (τ) angles
 144 [27], [42], shown in Fig. 2. The ρ angle is defined in the radial plane, sub-
 145 tended by the shower axis, the shower core position and the point where the
 146 muon hits the MTD detector plane. The τ angle is defined in the tangential
 147 plane which is perpendicular to the radial plane and parallel to the shower
 148 axis, and goes also through the point where the muon hits the detector plane.

149 The value of τ reflects predominantly the amount of muon scattering in
 150 the atmosphere and in any relevant absorber/detector material, and to some
 151 extent also the fact that muons can be produced off the shower axis. A
 152 contribution from the deflection of high-energy muons in the geomagnetic
 153 field (locally $< 0.1^\circ$ [31]) is also included there. The τ angle distribution,
 154 when averaged over all azimuth angles, is symmetrical around zero and gets

Figure 3: An example of radial angle distributions from Ref. [31] shows the behavior of this quantity in a wide range of $\lg(N_\mu^{tr})$, i.e. of primary energy. The selection used comprises a radial distance range 40-120 m, shower zenith angles $\theta < 30^\circ$ and $|\tau| < 0.7^\circ$. Relative yields reflect the CR flux in different $\lg(N_\mu^{tr})$ intervals. Lines connect the data points to guide the eyes.

155 narrower with increasing muon momentum [43], which is expected from the
 156 momentum dependence of multiple scattering and from geomagnetic bending.
 157 The ρ angle value, being defined in the shower coordinate system, is
 158 dominantly correlated with the transverse momentum of the parent meson.
 159 It is also substantially larger than the corresponding τ values. The multiple
 160 scattering of the muon in the atmosphere and muon filter above the MTD
 161 contributes also to the value of ρ , but has a relatively minor effect on it.
 162 An example of ρ distributions are shown in Fig. 3 [31]. They exhibit an
 163 asymmetric shape, being shifted with increasing $\lg(N_\mu^{tr})$ towards larger ρ
 164 values. This shift is due to the deeper penetration of higher energy showers,

but it is not so strongly pronounced because of the wide range of shower core distances selected for Fig. 3. Negative ρ values are due to a finite resolution of the ρ angle ($\approx 0.2^\circ$) and due to the possible muon scattering towards the shower axis.

4. Muon Production Height

In previous theoretical studies [44] the longitudinal development of the muon component in EAS was investigated by an integral transformation from lateral particle densities to a more shower development related observable like the muon production heights. Due to the very different shower development for light and heavy primary CR particles, their corresponding mean production heights are expected to be different, and thus to be indicative for the primary mass (see Fig. 4).

Conditions of the experiment and the response of the MTD were extensively studied with experimental data and simulations ([27], [30], [31]) to ensure the best tracking resolution and to clean the sample from non-shower-muon tracks. The effects of the non-central location of the MTD within KASCADE were also taken into account.

In order to decrease the effect of multiple muon scattering on their path to the detector $|\tau|$ angles smaller than 0.7° are considered. This cut enriches the sample with high energy muons, above a few GeV [30], having smaller multiple scattering angles ($\sigma_\tau \approx 0.2^\circ$) and smaller bending in the geomagnetic field, which improves considerably the determination of the correct production height.

Elimination of tracks not belonging to shower muons or originating in the absorber above the MTD (in addition to the cuts ensuring good track quality, mentioned in Section 2) is achieved by limiting the radial angle value to $\rho < 8^\circ$. For muon production height analysis in this work only positive radial angles are considered.

To ensure a nearly full azimuthal symmetry of the measured muons, events with 40 m - 80 m core distance to the MTD are selected (the location of the MTD is shifted by 54.65 m to the north from the KASCADE center **because this detector was not considered from the beginning**). In addition, this selection lowers the influence of the geomagnetic field on the mean muon directions. Below 40 m the punch-through effects forbid a valuable muon tracking and above 80 m the highly asymmetric azimuthal event

distribution (see Fig. 6.3 in Ref. [31]) is difficult to correct. For Grande reconstructed high-energy events the distance range 250 m - 360 m was chosen to avoid extended punch-through and trigger efficiency problems for large distances. For KASCADE (Grande) selections a combined Array-MTD analysis is only reliable above shower size $\lg(N_e) \geq 4.8$ (6.0) and $\lg(N_\mu) \geq 4.1$ (5.5).

In this work the experimental data on showers with zenith angles $\theta < 18^\circ$ were analyzed. The mean height values $\langle h_\mu \rangle$ were calculated in the altitude range up to 12 km along the shower axis, where the majority of muons with energy exceeding 0.8 GeV at ground are produced. For example, as CORSIKA simulations show, in a 10^{16} eV proton induced shower about 90% of such muons are produced in this altitude range. Despite of the fact that the first encounters with nuclei of the atmosphere occur at even higher altitudes, they are not considered in this work, both in data and simulations, because of their large uncertainty. The value of 12 km was chosen because at this altitude, and for the selected distance range of investigated muons to the shower core, the uncertainties in the ρ angle values become comparable to the values themselves.

Figure 4: Mean muon production heights observed at different distances from the shower core in CORSIKA simulated vertical showers for proton and iron primaries and two fixed primary energy values [47].

Employing the ρ and τ angles to define the orientation of muon track with respect to the shower axis together with the relative distance R_μ from the muon hit to the shower core position, the height h_μ can be calculated. This can be done along the muon track, which is the appropriate way to consider absorption or interaction of muons in showers [45, 46].

Another approach, used in the present work, is the determination of the height h_μ along the shower axis. One way is to use the relation $h_\mu = R_\mu / \tan \rho$

in the shower coordinate system. We could also employ, for angles much smaller than one radian, instead of ρ , the angle $\zeta = \sqrt{(\rho^2 + \tau^2)}$ [43], which is the angle in space between muon track and the shower direction.

As shown in Fig. 2 both reconstruction methods lead to muon production heights different from the true one by Δh_μ^ρ in case of the calculation with ρ , and by Δh_μ^ζ when using the angle ζ . In the former case the muons are assumed to be produced on the shower axis (which is not always the case) while in the latter, the muon production point is reconstructed on a cylindrical surface around the shower axis. The actual value of this difference in both reconstruction methods (being one of the sources of systematic errors) varies slightly with the type of primary and its energy, leading in most cases to an underestimation of the mean production height by a few percent.

In Table 2 a comparison of these differences is given for two fixed primary energies and two primary species. The results for muons with $E_\mu > 0.8$ GeV are obtained with CORSIKA simulated vertical showers (500 showers for 10^{15} eV and 158 for 10^{16} eV primary energy) using the QGSJet01 [39] and GHEISHA [48] interaction models. As seen in columns 3 and 4 the uncertainties range from $\approx 2\%$ to $\approx 8\%$, showing slightly better results for the ' ρ -method'.

One can expect smaller errors if a correction for multiple scattering in the atmosphere was made in the calculations. The actual amount of scattering is, of course, not known. However, for the selection used in the analysis ($0 < \rho < 8^\circ$ and $|\tau| < 0.7^\circ$) the simulations predict an average scattering angle at the level of 0.2° . It was checked with Monte Carlo simulations that up to 12 km altitude and a distance range of 40-80 m between a muon and the shower core, a subtraction of the absolute value of τ from ρ or ζ when calculating h_μ provides an improvement of the accuracy. Reconstructed negative h_μ values are below 5-7 %. The difference between the reconstructed mean value of the positive h_μ and the true mean muon production height is illustrated in columns 5 and 6 of Table 2. The investigation of h_μ in this work was done using the following relation

$$h_\mu = \frac{R_\mu}{\tan(\rho - |\tau|)} \quad . \quad (2)$$

The mean muon production height reconstructed with the relation (2) differs at most by $\pm 4\%$ from the true value.

In Fig. 5 an example of muon production height distributions h_μ (from Ref. [31]), obtained with KASCADE data, shows the behavior of this quantity

Table 2: Dependence of the systematic mean muon production height errors (in % of the true value) on the reconstruction method

1	2	3	4	5	6
Primary	E_0 [eV]	Δh_μ^ρ	Δh_μ^ζ	$\Delta h_\mu^\rho(\text{cor})$	$\Delta h_\mu^\zeta(\text{cor})$
H	10^{15}	-3.1%	-4.0%	+2.1%	+2.4%
Fe	10^{15}	-7.3%	-8.4%	-3.5%	-3.1%
H	10^{16}	-1.8%	-2.7%	+4.2%	+4.3%
Fe	10^{16}	-5.0%	-5.7%	-0.5%	+0.02%

in a wide range of primary energy (expressed by $\lg(N_\mu^{tr})$). Event selection differs from the one used for the analysis in this work in order to show some general features of the distributions. These distributions indicate that the production heights may extend to very large values. For large $\lg(N_\mu^{tr})$ values (large primary energies) the deeper shower development is mostly demonstrated by relatively fewer muons from large h_μ .

Further systematic effects are to be considered. In the region of small $\lg(N_\mu^{tr})$ in Fig. 5, the measured h_μ values can have a bias. For a successful reconstruction of the shower parameters on the KASCADE array level, the showers must have a certain electron particle number N_e at ground. At small energies only showers which fluctuate to lower production heights have enough particles and are fully reconstructed. Those showers are very likely proton induced showers, and hence a bias may be present in the analysis for small $\lg(N_\mu^{tr})$ due to the smaller trigger efficiency for iron, being of about 80% at the lowest $\lg(N_\mu^{tr})$ bin.

With increasing shower zenith angle θ , $\langle h_\mu \rangle$ is shifting somewhat towards larger values, but the change amounts to less than hundred meters in the whole range of θ . Similar shifts are observed for an analysis using full simulation, only. This effect is small compared to the difference of $\langle h_\mu \rangle$ for proton and iron induced showers, which amounts to about 1000 m (see Fig. 4), when using the cuts employed in our analysis.

5. Muon Production Heights in Showers Induced by Light and Heavy Primary Masses

The electron size $\lg(N_e)$ and muon size $\lg(N_\mu^{tr})$ provide an opportunity to separate light from heavy primary CR initiated showers. The size parameters

Figure 5: An example of muon production height distributions from Ref. [31] shows the behavior of this quantity in a wide range of $\lg(N_\mu^{tr})$, i.e. primary energy. The selection used comprises a radial distance range of 40-120 m and shower zenith angles $\theta < 30^\circ$. Radial and tangential angle cuts are the same as used in this article ($\rho=0-8^\circ$ and $|\tau| < 0.7^\circ$). Relative yields reflect the CR flux in different $\lg(N_\mu^{tr})$ intervals. Lines connect the data points to guide the eyes.

284 $\lg(N_e)$ and $\lg(N_\mu^{tr})$, as determined from the KASCADE array, are for the
 285 following studies corrected for their shower angle dependent attenuation, see
 286 Ref. [49], employing the formula $\lg(N_i^0) = \lg(N_i(\theta)) + 0.43 \cdot (1022/\Lambda_i) \cdot (\sec \theta -$
 287 $1)$, where $\Lambda_e = 175 \text{ g} \cdot \text{cm}^{-2}$, $\Lambda_\mu = 823 \text{ g} \cdot \text{cm}^{-2}$, and i stands for e or μ ,
 288 respectively. The ratio of the corrected parameters, namely $\lg(N_\mu^{tr,0})/\lg(N_e^0)$,
 289 turned out to be sensitive to the mass composition of primary CR [33, 37].

290 A ratio $\lg(N_\mu^{tr,0})/\lg(N_e^0)$ of 0.74, which corresponds roughly to Nitro-
 291 gen, is used to divide the experimental shower data into samples enriched
 292 with light and heavy primaries [37, 31]. Grouping the showers in the two-
 293 parameter space $\lg(N_e^0)$ vs. $\lg(N_\mu^{tr,0})$, according to $\lg(N_\mu^{tr,0}) > 0.74 \lg(N_e^0)$
 294 or $\lg(N_\mu^{tr,0}) \leq 0.74 \lg(N_e^0)$, heavy or light primary CR particles are selected,
 295 respectively. Using this coarse selection of the showers their muon tracks can

296 be used to calculate the muon production height h_μ along the shower axis.

Figure 6: Radial angle distributions (left panel) and muon production height distributions h_μ along the shower axis (right panel) for light and heavy CR primary mass enriched showers and for different $\lg(N_\mu^{tr,0})$ intervals. Shower core distances range is 40-80 m, and shower angles $\theta < 18^\circ$. Lines connect the data points to guide the eyes.

297 Fig. 6 shows the distributions of the radial angle and muon production
 298 height (left and right panel, respectively) for the selected distance range 40-
 299 80 m for different primary energies (expressed in terms of the muon number).
 300 Besides the dynamical shift of the radial angle distributions with increasing
 301 muon number, the figures show an increasing sensitivity to the mass of the
 302 CR particle. The drop to zero yield at small h_μ relates to the cuts on ρ and
 303 τ angles and the μ -hit shower core distance range employed in the analysis.

304 At high energies large muon production altitudes are predominantly cre-
 305 ated by heavy primaries. Narrower distributions, differently for light and
 306 heavy CR primaries, indicate a decrease of fluctuations in the $\langle h_\mu \rangle$ para-
 307 meter with increasing primary energy. Fig. 7 compares the muon production
 308 height distributions of Fig. 6 to simulation results for proton (triangles) and

Figure 7: Muon production height distributions along the shower axis h_μ for light (open circles) and heavy (full circles) enriched shower samples and a shower core distance range 40-80 m, and shower zenith angles $\theta < 18^\circ$ compared to CORSIKA simulations employing QGSjetII + FLUKA models for proton (H) and iron (Fe) primaries. Here $\lg(N_\mu) \approx \lg(N_\mu^{tr,0}) + 0.5$ (see Section 3). Lines connect the data points to guide the eyes.

iron (squares) primaries. The CORSIKA simulations were performed with ver. 6.307 of the code using the QGSJetII and, for interaction energies below 200 GeV, FLUKA2002.4 models [50].

Detector simulations were based on GEANT [51]. Identical cuts for data and simulations were used and the slope of the simulated energy spectrum was weighted to -2.7 below and to -3.1 above the 'Knee'. In Fig. 7 (as well as in Fig. 6) the plots of h_μ are normalized to integral yield equal one in the full range up to 12 km, but they are shown to 9 km only in order to expand the low production height region. However, the following discussion of the features seen at high values of h_μ is also true for the production heights

above 9 km. In this expanded region we see up to ≈ 3.5 km that data are embraced by the simulation results. Muons observed there, up to $\lg(N_\mu) \approx 5.0$, stem from hadronic interactions of energies below 200 GeV, modeled in simulations with FLUKA2002.4 code. At higher $\lg(N_\mu)$ - the lowest panel in Fig. 7 - contribution from higher interaction energies in this region increases. This **suggests** that low-energy interaction model FLUKA describes the data well. Muons produced above ≈ 3.5 km have parent mesons predominantly created at interaction energies larger than 200 GeV, which are modeled in simulations by the QGSJetII code. We observe here that the high-energy model has problems in describing the data.

The comparison reveals more muons at high production heights in the simulations (the distributions are shifted to the right). This excess of muons in the simulations at high altitudes with respect to the data may indicate that muons produced higher up have too high an energy and do not decay, surviving to the observation level, what is not observed in the measurements. The same effect will occur when the simulated mesons have too small an energy in the region of the first or second interaction, and would decay earlier than in reality. Shifting the maximum of shower development in the models deeper in the atmosphere will act in the direction of reducing the observed discrepancy with the data.

Figure 8: Experimental values of the mean muon production height along the shower axis $\langle h_\mu \rangle$ vs. $\lg(N_\mu^{tr,0})$ for light and heavy primary mass enriched showers and a shower core distance range 40-80 m, and shower angles $\theta < 18^\circ$. The bands bracketing the data points represent variations for the $\lg(N_\mu^{tr,0})/\lg(N_e^0)$ ratio from 0.73 to 0.75.

Simulation results shown in Fig. 7 are similar to the ones obtained with the older QGSJet01 model, which predicted the mean h_μ values shifted

slightly up by ≈ 150 m.

In Fig. 8 experimental values of the mean muon production height $\langle h_\mu \rangle$ as a function of $\lg(N_\mu^{tr,0})$ are shown. A good separation between light and heavy enriched primary CR particles is seen. The dependence on $\lg(N_\mu^{tr,0})$ suggests that production heights corrected for an appropriate elongation rate will exhibit a clear remaining dependence on the CR particle mass. Mean muon production heights for light and heavy mass enriched showers exhibit a height difference of about 12%, which is 3-4 times the systematic error quoted in Table 2.

Shaded bands show how $\langle h_\mu \rangle$ changes when the boundary between 'heavy' and 'light' is moved by ± 0.01 in the $\lg(N_\mu^{tr,0})/\lg(N_e^0)$ ratio, which is 10-20 % of the peak position difference in the distributions of this ratio for proton and iron primary induced showers [31]. One observes that the light sample is more sensitive to such a change giving a broader band, what can be explained by larger fluctuations in the shower development than in case of showers initiated by heavy CR primaries.

6. Mean Muon Production Depth vs. Electron and Muon Shower Sizes

In the previous section (Figs. 6, 7 and 8) the muon production height was shown to depend on the mass of the CR primary and its energy. In the following we will study this mass dependence of the muon production height in more detail. For this purpose we will use production height values referenced to the top of the atmosphere, called muon production depth, denoted as H_μ , and expressed in units of atmospheric depth ($\text{g}\cdot\text{cm}^{-2}$) using the US-Standard atmosphere [38] in data - corrected for temperature and pressure - and simulations. Seasonal differences between local atmospheric conditions near the KASCADE site and the US Standard are smaller than ± 2 % (see Fig.2.1 in Ref. [38]) having little influence on our final results.

Usually, shower development is described by the evolution of its electromagnetic component, where X_{max} is understood as the atmospheric depth at which the number of electrons and photons of the air shower reaches its maximum. X_{max} is considered to be a primary mass sensitive parameter. Concerning muons which stem dominantly from $\pi^\pm$ decays, the corresponding production height at which most muons are created may also provide a mass sensitive observable.

376 To reveal the primary mass sensitivity of the H_μ parameter one has to
 377 subtract the energy dependence expressed in terms of the elongation rate,
 378 taking into account the shower size observables.

379 Subtracting from the production depth H_μ for each track in a shower
 380 the energy dependent penetration depth we use the following relation for the
 381 mass dependent H_μ^A

$$H_\mu^A = H_\mu - D_\mu(\lg(N_\mu^{tr,0}) - 3.6) + D_e(\lg(N_e) - 4.8), \quad (3)$$

382 where the parameter offsets originate from the analysis thresholds.

383 For the following analysis the elongation rate components (the coeffi-
 384 cients in equation (3)), similar to the energy dependence of X_{max} observed
 385 in EAS simulations, were assigned the following values: $D_\mu=70 \text{ g}\cdot\text{cm}^{-2}$ and
 386 $D_e=20 \text{ g}\cdot\text{cm}^{-2}$ per decade. These values have been varied iteratively by up
 387 to $\pm 20 \text{ g}\cdot\text{cm}^{-2}$ to obtain the slope of the middle H_μ^A ridge in the param-
 388 eter $\lg(N_e^0)$ vs. $\lg(N_\mu)$ representation reproducing the $\lg(N_\mu)/\lg(N_e^0)$ ratio of
 389 heavy-light separation (Section 5). We assume that the elongation rates D_μ
 390 and D_e are independent of the primary mass.

391 This two-component correction on H_μ is similar to the one for $\lg(E_0)$ in
 392 equation (1). There, contributions from $\lg(N_e)$ and $\lg(N_\mu)$, reflecting the
 393 complementary information on shower development, are also employed. The
 394 shower development leads also to different fluctuations in those shower para-
 395 meters. It is known from earlier studies that the $\lg(N_e)$ parameter exhibits
 396 fluctuations to large values, in agreement with the simulations, while the
 397 $\lg(N_\mu^{tr})$ parameter shows little fluctuations. On the contrary, the H_μ para-
 398 meter (independent of shower angle) is fluctuating towards smaller values.
 399 Therefore, we may argue that in the corrections of H_μ for the elongation rate
 400 fluctuations will cancel to some extent and thus, the resulting mass depen-
 401 dent muon production depth H_μ^A represents a stable observable. In Fig. 9
 402 muon production depth distributions are compared for three N_μ size bins
 403 before (H_μ) and after (H_μ^A) correction for the elongation rate, according to
 404 equation (3).

405 Using equation (3) the presentation shown in Fig. 10 has been obtained.
 406 Here $\langle H_\mu^A \rangle$ represents the average mass dependent production depth H_μ^A
 407 per shower having at least one muon track in the MTD. Above the logarithmic
 408 muon number 5.5 an analysis from the Grande array data in a separate
 409 distance range is considered. As a result one can identify regions of different
 410 mass dependent mean muon production depths in the two-parameter space

Figure 9: Muon production depth distributions are compared for three $\lg(N_\mu)$ -size bins before (open symbols) H_μ and after (full symbols) H_μ^A correction for the elongation rate, according to the equation (3). The depth cut corresponds to 12 km.

411 $\lg(N_e^0)$ vs. $\lg(N_\mu)$ which themselves vary over almost 3 orders of magnitude.
 412 These regions of distinct $\langle H_\mu^A \rangle$ are 'color' coded with a $40 \text{ g}\cdot\text{cm}^{-2}$ step
 413 size. Based on the assumption that the $\langle H_\mu^A \rangle$ parameter is not prone to
 414 large fluctuations, the spread of the regions of the same 'color' is a measure
 415 of the correlations in the two other fluctuating shower parameters $\lg(N_e^0)$ and
 416 $\lg(N_\mu)$.

417 The borders between different regions are marked for some cases with
 418 solid or dashed lines with a certain slope in the $\lg(N_e^0)$ vs. $\lg(N_\mu)$ plane. In
 419 the middle ridge the solid line has the previously employed slope for selecting
 420 light or heavy primary particles, being now equal to 0.83 instead of 0.74, due
 421 to the transformation to $\lg(N_\mu)$. For regions away from the middle different
 422 slopes of the ridges may be observed, **as in the case of the dashed line**
 423 **which marks the ridge of one of the heavier groups of primaries.**
 424 Data boundaries are curved because of the limited statistics of showers and
 425 CR primary types, as shown in Fig. 22 in Ref. [26].

426 An integral number of muons for a nucleus A induced shower is

$$N_\mu^A \sim A(E_0/A)^\beta, \quad (4)$$

427 where $\beta \approx 0.85$ [53]. Taking into account that $X_{max} \sim \lg(E_0/A) + \text{const}$
 428 and assuming that $X_{max,\mu}^A$ exhibits a similar $\lg(E_0/A)$ dependence as X_{max} ,
 429 using equation (4), we obtain:

Figure 10: $\lg(N_e^0)$ vs. $\lg(N_\mu)$ matrix with effective mean muon production depth $\langle H_\mu^A \rangle$ along the z -axis. Borders between different regions are marked with solid or dashed lines (see text). Here, $\lg(N_\mu) \approx \lg(N_\mu^{tr,0}) + 0.5$ (see Section 3). Above $\lg(N_\mu)=5.5$ data from the Grande array in a distance range 250 - 360 m are considered and normalized to KASCADE data.

$$X_{max,\mu}^A \sim 1/\beta [\lg(N_\mu^A) - (1 - \beta) \lg(A)] \quad . \quad (5)$$

Fig. 9 shows that in the H_μ^A range of our analysis ($> 200 \text{ g}\cdot\text{cm}^{-2}$), $X_{max,\mu}^A$ (peak position) is larger than the $\langle H_\mu^A \rangle$ value, due to the tails in H_μ^A distributions towards the small values. However, this $X_{max,\mu}^A$ in Fig. 9 is close to the largest $\langle H_\mu^A \rangle$ value in Fig. 10.

A scale for $\langle H_\mu^A \rangle$ regions corresponding to 'iron' and 'proton' primaries can be estimated based on an analogy to the electromagnetic cascade, ignoring the difference between $X_{max,\mu}^A$ and $\langle H_\mu^A \rangle$. For a 10^{16} eV proton shower we obtain the number of hadronic cascade generations to be $n \approx 5.5$ from $X_{max,\mu}^p \approx 660 \text{ g}\cdot\text{cm}^{-2}$ in Fig. 10, having in mind that $X_{max,\mu}^p = n \cdot \lambda_{\pi\text{-air}} \approx 5.5 \cdot 120 \text{ g}\cdot\text{cm}^{-2} \approx 660 \text{ g}\cdot\text{cm}^{-2}$, and that a fraction of pions decay immediately into muons. For heavy CR particles we read from Fig. 10 a corresponding value $X_{max,\mu}^{Fe} \approx 540 \text{ g}\cdot\text{cm}^{-2} \approx 4.5 \cdot 120 \text{ g}\cdot\text{cm}^{-2}$, leading to 4.5 generations and providing the scale of equation (5). For proton primaries the normalization of equation (5) is achieved by setting $1/\beta \approx 138 \text{ g}\cdot\text{cm}^{-2}$. The other extreme value for equation (5) for iron would lead to $X_{max,\mu}^{Fe} \approx X_{max,\mu}^p - 29.5 \text{ g}\cdot\text{cm}^{-2} \cdot \ln(56) \approx 540 \text{ g}\cdot\text{cm}^{-2}$.

The slope of the lines in Fig. 10 can be also interpreted using the muon number vs. energy relation in equations (4) and (1). The exponent β can

be connected to the amount of inelasticity involved in the processes of A -air collisions [53]. A comparatively steeper slope observed in the dashed line may correspond to an increased inelasticity [53] with respect to the light CR primaries, which may be a subject of further studies.

Figure 11: Flux correction factors due to the acceptance and the geometry differences between the array and the MTD (see text for details). The curve represents a polynomial fit.

To derive the CR flux spectra from the $\langle H_\mu^A \rangle$ information in Fig. 10 one has to introduce correction factors. They are obtained from the ratio of all registered showers which trigger KASCADE in the 40-80 m distance range to all showers with at least one track inside the MTD which survive the analysis cuts. Flux correction factors are shown in Fig 11. Correction values take into account the efficiency of the registration and reconstruction of muon tracks, as well as the geometry of the MTD. The size of the clusters on wires and strips in the MTD becomes large for high particle densities. Therefore, due to the software limit on these sizes (see Section 2) large showers are only accepted further away within the 40-80 m interval. These corrections are almost independent of the selection of $\langle H_\mu^A \rangle$ bins where the statistics is sufficient.

Sorting the $\lg(N_e^0)$ vs. $\lg(N_\mu^{tr})$ events by regions of constant $\langle H_\mu^A \rangle$ in the matrix of Fig. 10, then multiplying their number by the flux correction factors, and applying the almost mass independent equation (1) for $\lg(E_0)$ the energy spectra of relative production depth abundances are obtained and shown in Fig. 12. So far, no explicit mass range assignment is given. The spectra are shown together with their systematic and statistical error combinations. The errors with wide boundary bars are statistical while the short

boundary bars indicate the systematic variation of the H_μ^A regions between $\pm 20 \text{ g}\cdot\text{cm}^{-2}$ multiplied by the correction factors from Fig. 11. In Fig. 12 the Grande data, analyzed in the separate distance range (see Fig. 10), are normalized to KASCADE flux in two bins below and above $\lg(E_0/\text{GeV}) = 7.7$, i.e. in the overlapping region. The spectra reveal distinct features. While the 'low mass' (H_μ^A large) spectra show a rapid drop with increasing shower energy, 'medium' and 'heavy mass' (H_μ^A small) spectra seem to overtake at large primary energy. This feature is model independent because only the experimental data are used for obtaining mean muon production depth abundances.

In the present analysis - due to the detection threshold of the MTD - a small fraction of tracks ($\approx 15 \%$) may be missing at small $\lg(N_\mu)$ (Fig. 11), leading to a bias in the light particle 'mass' interpretation. Unfortunately, our result cannot contribute to the discussion on the behavior of the total CR flux spectrum at higher energies, because the MTD detection area is too small and the amount of collected data limited. The required corrections from Fig. 11 would become prohibitively large. However, as indicated by the dashed line in Fig. 12, the total flux spectrum is in good agreement with the KASCADE spectrum obtained by an unfolding technique [26].

Table 3 provides a collection of the fluxes for different muon production depth H_μ^A windows showing results for every second bin in Fig. 12. The errors of the fluxes are dominated by systematic errors.

Figure 12: Energy spectra for primaries which produce muons at different effective muon production depth H_μ^A ; above $\lg(E_0/\text{GeV}) = 7.7$ the Grande array data analysed in a separate distance range are considered. The dashed line reproduces the CR spectrum as measured by KASCADE - Ref. [26].

Figure 13: Differential muon multiplicity spectra in the MTD for different effective muon production depth H_μ^A . Above $\lg(N_\mu) = 5.5$ Grande multiplicities are normalized to KASCADE multiplicities in the overlapping region.

Each shower event is also characterized by a multiplicity of muon tracks. These multiplicities help improving the statistical accuracy of the $\langle H_\mu^A \rangle$ determination having no influence on the systematic uncertainties of the analysis described above. However, one finds that the mean muon multiplicity depends on the primary CR energy in a different way for different $\langle H_\mu^A \rangle$ regions ($\approx$ different primary mass groups), what is shown in Fig. 13. Double-differential mean muon multiplicities $d^2 \langle M_\mu \rangle / d \lg(N_\mu) \times d \lg(N_e^0)$ detected by the MTD are selected for specific $\langle H_\mu^A \rangle$ regions (see Ref. [27] or Ref. [54] for comparable information). Data show variations due to the fluctuations in the $\lg(N_e^0)$ parameter. These multiplicities rise with $\lg(N_\mu)$ but with different slopes for different $\langle H_\mu^A \rangle$ regions. Therefore, the mean muon multiplicity rise with primary energy can be used for the primary CR mass estimation.

7. Summary and Outlook

The KASCADE-Grande experimental setup, where the electron and muon components of EAS are measured with high accuracy by arrays of scintillator detectors simultaneously with the precise measurement of muon directions in the tracking detector, allows us to approach the estimation of primary CR composition by means of investigation of the muon production heights in EAS.

Table 3: Fluxes Φ and systematic errors Δ for different "mass" groups (in $(\text{m}^2 \cdot \text{sr} \cdot \text{s} \cdot \text{GeV}^{-1.5})^{-1}$).

$\lg(E_0)[\text{GeV}]$	Φ_{620}	Δ_{620}	Φ_{600}	Δ_{600}	Φ_{560}	Δ_{560}	Φ_{540}	Δ_{540}
6.1	551.6	194.1	1641.4	130.5	510.4	324.6	0.0	0.0
6.3	576.9	133.8	1316.4	109.3	447.5	243.1	3.4	0.0
6.5	573.6	87.8	1124.7	83.3	375.6	164.9	22.2	11.4
6.7	312.3	67.1	980.4	106.1	465.7	169.7	6.8	3.6
6.9	211.7	70.8	669.7	34.7	458.4	105.5	63.5	0.0
7.1	86.8	22.7	457.7	143.9	471.3	86.4	119.9	80.1
7.3	72.8	78.6	489.4	10.4	308.5	39.4	157.2	107.6
7.5	47.7	72.3	131.8	34.2	139.6	72.2	502.8	110.3
7.7	< 8.7	5.0	< 45.8	31.8	< 47.1	19.1	717.6	194.8
7.9	< 7.3	16.7	< 48.9	2.2	< 30.9	8.4	496.3	246.0
8.1	< 4.8	14.6	< 13.2	6.9	< 14.0	14.5	424.1	305.0

It has been shown that certain muon production depth H_μ^A regions create bands in the two parameter $\lg(N_e)$ vs. $\lg(N_\mu)$ space, which can be transformed into CR energy spectra in the range from $\approx 10^{15}$ eV to $\approx 10^{17}$ eV (Fig. 12). These spectra have features similar to the energy spectra of primary mass groups from Ref. [26]. One can state that the behavior of larger production depths H_μ describes the 'lighter' masses and the smaller production depths correspond to 'heavier' ones. A coarse mass scale may be provided by $X_{max,\mu}^A \sim \ln(A)$.

Muon multiplicity distributions provide an extra parameter in determining the CR primary mass and future tests for high energy interaction models employed in EAS simulations.

Muons are direct messengers of hadronic interactions, and it is a common understanding that they are very well suited for testing the interaction models used in simulations and interpretations of the EAS data. The results obtained in this work are to some extent based on the QGSJet01 model (energy conversion formula (1)) and confirm the effect seen in the spectra in Ref. [26], namely, that the lightest masses (here the largest atmospheric depths) have a break in the spectrum at lower energies compared to the

heavier (smaller depths) ones. However, the obtained relative abundances of various production depth ranges (Fig. 12) are model independent.

In addition to the investigation of EAS development using triangulation of muons the mean pseudorapidity of muons in EAS [47, 52, 55] is a very promising tool for tests of the interaction models. This parameter is closely related to the rapidity of pions - the most abundant products of high energy interactions - and it is highly sensitive to the longitudinal development of the shower in the atmosphere. Simulations show [47] that muons produced at a certain height H_μ carry to the observation level a certain mean pseudorapidity $\langle \eta \rangle$, fairly independent from primary mass and energy. Therefore, H_μ provides an average measure of $\langle \eta \rangle$ and an excess of certain H_μ values can be related to the excess of certain pseudorapidity values in the production of mesons at given heights. KASCADE-Grande with its MTD offers the possibility of such investigation.

The discrepancy in the muon production height distributions between QGSJet simulations and measurements (Fig. 7) points to the necessity of further investigation of high energy interaction models.

Concerning the muon production height, shower zenith angle ranges larger than 18° will be investigated in the near future. Also very inclined muons studied using the wall modules of the MTD are subject of ongoing investigations.

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Figure captions for the article

Fig. 1. Anode wire amplitude spectra for individual odd/even numbered wire cells.

Fig. 2. Illustration of the angular correlations in EAS and the definition of the radial (ρ) and tangential (τ) angles. The differences between the true and the reconstructed h_μ values with the two reconstruction approaches - see text - are also shown.

Fig. 3. An example of radial angle distributions from Ref. [31] shows the behavior of this quantity in a wide range of $\lg(N_\mu^{tr})$, i.e. of primary energy. The selection used comprises a radial distance range 40-120 m, shower zenith angles $\theta < 30^\circ$ and $|\tau| < 0.7^\circ$. Relative yields reflect the CR flux in different $\lg(N_\mu^{tr})$ intervals. Lines connect the data points to guide the eyes.

Fig. 4. Mean muon production heights observed at different distances from the shower core in CORSIKA simulated vertical showers for proton and iron primaries and two fixed primary energy values [47].

Fig. 5. An example of muon production height distributions from Ref. [31] shows the behavior of this quantity in a wide range of $\lg(N_\mu^{tr})$, i.e. primary energy. The selection used comprises a radial distance range of 40-120 m and shower zenith angles $\theta < 30^\circ$. Radial and tangential angle cuts are the same as used in this article ($\rho=0-8^\circ$ and $|\tau| < 0.7^\circ$). Relative yields reflect the CR flux in different $\lg(N_\mu^{tr})$ intervals. Lines connect the data points to guide the eyes.

Fig. 6. Radial angle distributions (left panel) and muon production height distributions h_μ along the shower axis (right panel) for light and heavy CR primary mass enriched showers and for different $\lg(N_\mu^{tr,0})$ intervals. Shower core distances range is 40-80 m, and shower angles $\theta < 18^\circ$. Lines connect the data points to guide the eyes.

Fig. 7. Muon production height distributions along the shower axis h_μ for light (open circles) and heavy (full circles) enriched shower samples and a shower core distance range 40-80 m, and shower zenith angles $\theta < 18^\circ$ compared to CORSIKA simulations employing QGSjetII +FLUKA models for proton (H) and iron (Fe) primaries. Here $\lg(N_\mu) = \lg(N_\mu^{tr,0}) + 0.5$ (see Section

698 3). Lines connect the data points to guide the eyes.

699

700 Fig. 8. Experimental values of the mean muon production height along
701 the shower axis $\langle h_\mu \rangle$ vs. $\lg(N_\mu^{tr,0})$ for light and heavy primary mass en-
702 riched showers and a shower core distance range 40-80 m, and shower angles
703 $\theta < 18^\circ$. The bands bracketing the data points represent variations for the
704 $\lg(N_\mu^{tr,0})/\lg(N_e^0)$ ratio from 0.73 to 0.75.

705

706 Fig. 9. Muon production depth distributions are compared for three
707 $\lg(N_\mu)$ -size bins before (open symbols) H_μ and after (full symbols) H_μ^A cor-
708 rection for the elongation rate, according to the equation (3). The depth cut
709 corresponds to 12 km.

710

711 Fig. 10. $\lg(N_e^0)$ vs. $\lg(N_\mu)$ matrix with effective mean muon production
712 depth $\langle H_\mu^A \rangle$ along the z -axis. Borders between different regions are
713 marked with solid or dashed lines (see text). Here, $\lg(N_\mu) \approx \lg(N_\mu^{tr,0}) + 0.5$
714 (see Section 3). Above $\lg(N_\mu)=5.5$ data from the Grande array in a distance
715 range 250 - 360 m are considered and normalized to KASCADE data.

716

717 Fig. 11. Flux correction factors due to the acceptance and the geometry
718 differences between the array and the MTD (see text for details). The curve
719 represents a polynomial fit.

720

721 Fig. 12. Energy spectra for primaries which produce muons at different
722 effective muon production depth H_μ^A ; above $\lg(E_0) = 7.7$ the Grande array
723 data analysed in a separate distance range are considered. The dashed line
724 reproduces the CR spectrum as measured by KASCADE - Ref. [26].

725

726 Fig. 13. Differential muon multiplicity spectra in the MTD for different ef-
727 fective muon production depth H_μ^A . Above $\lg(N_\mu)=5.5$ Grande multiplicities
728 are normalized to KASCADE multiplicities in the overlapping region.