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HAL Id: hal-00684252
https://hal.archives-ouvertes.fr/hal-00684252
Submitted on 31 Mar 2012

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Performance Evaluation of Threshold-Based TOA Estimation Techniques Using IR-UWB Indoor Measurements

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Abstract—Ultra-wide bandwidth (UWB) technology is a viable candidate for enabling accurate localization through time of arrival (TOA) based ranging techniques. These ranging techniques exploit the high time resolution of the UWB signals to estimate the TOA of the first signal path. Nevertheless, these techniques are facing the problem of proper multipath mitigation especially in harsh propagation environments in which the first path may not exist or it may not be the strongest. This paper presents a realistic comparison between the ranging performances of four threshold-based TOA estimation techniques using experimental data collected from an IR-UWB indoor propagation measurement campaign performed in an office building.

Index Terms—TOA, Ranging techniques, Channel impulse response, IR-UWB, Measurements, Indoor positioning

I. INTRODUCTION

Ultra wide-band (UWB) is a viable technology for short-range wireless indoor communication with a number of attractive features: high-rate transmission, low complexity, low cost, and low-power consumption [1], [2]. This technology has generated considerable and increasing interest by many manufacturers since February 2002, when the Federal Communication Commission (FCC) opened up 7.5 GHz of spectrum (from 3.1 GHz to 10.6 GHz) for use by UWB devices. The traditional design approach for an UWB communication system uses narrow time-domain pulses of very short duration, typically on the order of a nanosecond, thereby spreading the energy of the radio signal quite uniformly over a wide frequency band ranging from extremely low frequencies to a few gigahertz [3], [4]. This method is usually called impulse radio UWB (IR-UWB). A great advantage of the short pulse modulation is the possibility to estimate the TOA with a fine resolution, which translates in ranging estimation with a less than one meter accuracy allowing for many location and tracking applications. The two main ranging techniques defined for IR-UWB are One Way Ranging (OWR) and Two Way Ranging (TWR) [4], [5], [6].

Using channel (impulse) responses -C(I)R-, different techniques have been proposed for estimating TOA. The simplest and easiest technique estimates the TOA as the time of arrival of this strongest path [6], [7]. However, this assumption is not usually true in multipath conditions. In such conditions, we distinguish two cases: the Line-of-Sight (LOS) in which no obstacle separates the Tx and the Rx and the Non-Line-of-Sight (NLOS) if the obstacle exists. In the LOS case, the strongest path is usually the first path while in the NLOS case the first path may be more attenuated than indirect paths [8]. Hence, we need more advanced techniques to extract this first path and estimate the TOA. The reader can refer to [3], [9] and references therein for more details about the techniques already proposed for TOA ranging within IR-UWB signals.

In that direction, this paper presents a contribution to the TOA estimation techniques based on IR-UWB channel responses. Four techniques are presented and studied using an IR-UWB measurements campaign. The first technique is typical and widely used. It is based on the setting of a threshold above the noise floor to detect the first ray. Based on this first technique, we derive three different techniques. The second technique is a modified version of the first one and uses the cumulative CR instead of the CR. The third technique is based on the detection of the first strongest paths using a dichotomous search approach. The fourth and last technique is a combination of the first and third techniques.

The rest of the paper is organized as follows. We start in section II by giving the assumed channel model. Then, we detail in section III the different techniques of TOA estimation. In section IV, the UWB measurement campaign is presented. This measurement campaign is used to tune, evaluate, and compare the different presented techniques. Finally, the results are discussed in section V and our concluding remarks are given in section VI.

II. UWB CHANNEL IMPULSE RESPONSE MODEL

For all the rest of the paper, we consider a multipath channel with a CIR modeled as the sum of all received pulses as follows:

\[ c(t) = \sum_{n=1}^{N} a_n \delta(t - \tau_n) \] (1)

where \( a_n \) and \( \tau_n \) are, respectively, the amplitude and time-delay of the \( n \)th propagation path; \( \tau_1 \) is the time of arrival of
the first path (i.e. The TOA between the Tx and the Rx) which we seek to find out.

The received signal can then be expressed as:

\[ r(t) = \sum_{n=1}^{N} a_n \omega(t - \tau_n) + n(t) = s(t - \tau_1) + n(t) \]  

(2)

where \( \omega(t) \) is the isolated ideal received pulse with duration \( T_p \) (i.e. in the absence of multipath and noise) and \( n(t) \) is the additive white Gaussian noise (AWGN) with zero mean and spectral density \( N_0/2 \) where \( N_0 \) is the noise power density. \( s(t) \) is the noise-free CIR defined as:

\[ s(t - \tau_1) = \sum_{n=1}^{N} a_n \omega(t - \tau_n) \]  

(3)

In all the rest of this paper, we use the sampled form of \( r(t) \) with a sample rate \( 1/T_s \) where \( T_s \) is the sample duration. Let \( M \) be the number of samples which compose \( r(t) \). Hence, if the received signal is observed in the interval \([0, T]\), we get \( T = MT_s \). The \( m \)th sample occurs at the time \( t_m = mT_s \) \((m \in [1, \ldots, M])\).

Given a channel response modeled by (2), the goal is to estimate \( \tau_1 \), i.e. the TOA of the first path. In the next section, four different techniques for estimating TOA will be described.

III. TECHNIQUES OF TOA ESTIMATION BASED ON UWB SIGNALS

This section presents the different techniques for estimating TOA from the UWB signals. These techniques are numerated from 1 to 4 as follows:

- **T1:** Setting a threshold above the noise floor
- **T2:** Setting a threshold above the cumulative noise floor
- **T3:** Dichotomous left interval selection
- **T4:** Thresholded dichotomous left interval selection

A. T1: Setting a threshold above the noise floor

This approach is the most typical and has been proposed by Lee and Scholtz in [10]. This technique starts by defining a threshold \( \gamma_{th} \) which must be above the noise level in order to limit as much as possible false alarm on noise peak while maintaining a sufficient level of detection. The implementation of this technique involves the following steps:

- Consider the squared channel response \( r^2(t) \);
- Compare the actual value of \( r^2(t) \) to the appropriate threshold \( \gamma_{th} \);
- Search the first crossing point and let \( m \) be the corresponding sample. The TOA estimate \( \hat{\tau}_1^{th} \) is then given by \( mT_s \).

The choice of the threshold is the most challenging task in such technique. As shown in Fig. 1, which plots an example of measured CR, the probability of detecting noise peaks (false alarm) is higher with an underestimated threshold. Whereas, with an overestimated threshold, it is the probability of skipping the direct path which is higher. In [11], different methods for choosing the threshold are described and compared. In this paper, we have chosen to statistically define the threshold relatively to the maximum value of the signal using the available UWB measurements (see section V below).

![Fig. 1. T1 - Setting a threshold above the noise floor: the threshold must be fairly chosen in order to avoid under- and over-estimation of the TOA.](image)

B. T2: Setting a threshold above the cumulative noise floor

In this technique, we propose to apply a threshold on the cumulative received signal instead of the simple received signal in technique T1. For this, the ecdf (energy cumulative density function) \( c_r(t) \) of the received signal \( r(t) \) is defined and it is given, at time \( \tau \) by:

\[ c_r(\tau) = \int_{0}^{\tau} r^2(t) dt = \int_{0}^{\tau} r^2(t - \tau_1) dt + \int_{0}^{\tau} n^2(t) dt + 2 \int_{0}^{\tau} s(t - \tau_1)n(t) dt \]  

(4)

where \( s(t) \) is defined in (3). Then, we obtain:

\[ c_r(\tau) = E_s(\tau_1, \tau) + c_n(\tau) + 2 \int_{0}^{\tau} s(t - \tau_1)n(t) dt \]  

(5)

where \( E_s(\tau_1, \tau) \) represents the integrated energy of the useful signal between \( \tau_1 \) and \( \tau \) and \( c_n(\tau) \) represents the integrated noise between 0 and \( \tau \). The last integral \( \int_{0}^{\tau} s(t - \tau_1)n(t) dt \) can be neglected assuming independence between signal and noise. This leads to the following expression:

\[ c_r(\tau) \approx E_s(\tau_1, \tau) + c_n(\tau) \]  

(6)

After the construction of this cumulative signal, the same steps presented for technique T1 are applied (see Fig. 2). That is to say:

- Compute the cumulative received signal \( c_r \);
- Compare the actual value of \( c_r \) to the appropriate threshold \( \gamma_{cum} \);
- Search the first crossing point and let \( m \) be the corresponding sample. The TOA estimate \( \hat{\tau}_1^{cum} \) is then given by \( mT_s \).

C. T3: Dichotomous left interval selection

This technique seeks to estimate properly TOA values associated with situations where the strongest path is not the first path (but it is still valid in LOS situations). This technique
proposes to consider the largest $N_{\text{max}}$ peaks of the received signal. A receiver can easily search these strongest paths. The TOA is then estimated as the time delay of the peak with the smallest index (see Fig. 3). In this technique, the key parameter is $N_{\text{max}}$ which is the number of the largest signal peaks. In this work, $N_{\text{max}}$ is chosen statistically using the UWB measurement campaign. The pseudo-code of this technique is given by Algorithm 1.

**Algorithm 1** Dichotomous left interval selection

$\gamma_0 \leftarrow \max \{r^2(\tau)\}$: compute the peak energy  
set $N_{\text{max}}$: the key parameter  
$\gamma \leftarrow \gamma_0$: initialize the threshold  
$N_{\text{int}} \leftarrow 1$: initialize the number of current intervals  
$\epsilon \leftarrow 10^{-2}$: set the the decreasing factor  
while $N_{\text{int}} < N_{\text{max}}$ do  
\hspace{1em} $T_\gamma \leftarrow \text{GetIntervals}(r^2(\tau), \gamma)$: compute the valid time support  
\hspace{1em} $N_{\text{int}} \leftarrow \text{NumberOfIntervals}(T_\gamma)$: update the number of intervals (strongest peaks)  
\hspace{1em} $\gamma \leftarrow \gamma(1 - \epsilon)$: decrease the threshold by $\epsilon$  
end while  
$\hat{T}_{\gamma_{\text{max}}} \leftarrow \min \{T_\gamma\}$: estimate the TOA

$T_\gamma$ is a union of intervals which corresponds to the delay values where the squared received signal is above a threshold $\gamma$. This set of intervals is determined via a dichotomous algorithm which stops when the preassigned value of interval $N_{\text{max}}$ has been reached. The estimated delay is then chosen as the minimum value of this interval. This pseudo-code defines two elementary function GetIntervals and NumberOfIntervals which respectively return the time support where $r^2(\tau) > \gamma$ and the number of disjoint intervals from a union of intervals given as an input. This approach is different in nature from both jump back and search forward (JBSF) and seek backward scheme (SBS) described in [3] and [12]. There is no threshold to be defined from a-priori knowledge of the channel parameters.

**Algorithm 2** Thresholded dichotomous left interval selection

set $\alpha$: the key parameter  
$\gamma_{\text{noise}} \leftarrow \max \{r^2(\tau)\}$, $\tau \in [0, 5\text{ns}]$  
$\gamma_0 \leftarrow \max \{r^2(\tau)\}$  
compute $\tau_0$: TOA of the strongest path  
$\text{win} \leftarrow [0, \tau_0]$; define the search-back window  
$\gamma \leftarrow \gamma_0$  
$\epsilon \leftarrow 10^{-2}$: decreasing factor  
while $\frac{\gamma - \gamma_{\text{noise}}}{\gamma_0} > \alpha$ do  
\hspace{1em} $T_{\gamma, \text{win}} \leftarrow \text{GetIntervals}(r^2(\tau), \gamma, \text{win})$  
\hspace{1em} $\gamma \leftarrow \gamma(1 - \epsilon)$: decrease the threshold by $\epsilon$  
end while  
$\hat{T}_{\gamma_{\text{win}}} \leftarrow \min \{T_{\gamma, \text{win}}\}$

**IV. UWB Measurement Campaign**

The measurements campaign has been carried out, within the framework of the FP7-WHERE project, by CEA-LETI.
in the SIRADEL headquarter building in Rennes, France. The goal was to collect UWB channel responses in a same local area. In order to assess small-scale fading, channel response measurements are made on several square grids. This measurements campaign is dedicated for the evaluation and validation of localization techniques and algorithms.

The time-domain channel sounder is mainly composed of a pulse pattern generator, a wide band digital oscilloscope, and UWB antennas. The whole measurement setup is illustrated in Fig. 5 [13]. On the transmitter side, a Pulse Generator (Picosecond Pulse Lab 4050B) with two additional impulse forming networks and a power amplifier fit the desired UWB impulse shape in the $3−7$ GHz bandwidth (see Fig. 6). On the receiver side, a wide-band Digital Oscilloscope (Tektronix TDS 6124C) is used with a sampling rate of 20 Gsps in real-time. In order to improve the time precision, a sinc interpolation is used in order to get a final time step of 5ps. Moreover, the signal is averaged over 16 snapshots for increasing the signal-to-noise ratio (SNR). For dynamic range consideration, it is also necessary to use Low Noise Amplifiers in front of oscilloscope input channels. On both Tx and Rx sides the same kind of antenna is used. The radiation pattern is omni-directional in azimuth with a bipolar radiation pattern in elevation [14].

During the campaign, four fixed receiver positions were defined and 302 measurement points were selected for the transmitter positions [14] with the transmitter and the four receivers at the same height (120cm between the floor and the antenna ground plan). Fig. 7 shows the different positions of transmitters and receivers. The most important pieces of furniture (metallic cupboards and tables) should be taken into consideration when modeling the channel propagation and estimating TOA in order to better understand the effects of radio propagation, channel characteristics, and environment components on extracted TOA. These furniture pieces are presented in Fig. 8. Nevertheless, many other small pieces of furniture (chairs, printers, refrigerator, etc) are present when performing measurements. Taken into consideration all these small furnitures in channel modeling is a hazardous task. Hence, the choice was been made not to consider these small furnitures.

When performing channel sounding, it is necessary to extract exclusively the channel behavior (with or without antennas) by using appropriate calibration procedures based on deconvolution tools [15]. These calibration procedures aim to eliminate the effects of all the elements involved in the
link like PA, cable, and LNAs. For each Tx-Rx pair, we store the CR measured by the sounder. In addition to the CR, different parameters are saved in each profile mainly Tx and Rx positions accurately measured, date, and time [14]. We define also the link quality indicator (LQI) as the ratio between the maximum signal amplitude and the maximum noise amplitude estimated during the first five nanoseconds corresponding to a common time slot without any signal [14]. The LQI gives an indication about the SNR of the received signal. The ranging techniques will hence be evaluated for different values of the LQI (i.e. the SNR).

V. Results and Discussions

The four presented techniques in section III are dependent on key-parameters which have to be adequately chosen in order for the technique to perform higher ranging accuracy. The determination of optimal key-parameters is not the object of this paper. In order to make a fair comparison between the four techniques, we set the key-parameters to the values which fit the best the available measurements. Nevertheless, these key parameters can be fixed in a more optimal way in order to guarantee more enhanced performances. These parameters can be chosen for example with respect to the SNR values or based on received signal statistics [3].

A. Tuning of different techniques using the measurement campaign

The figures (a) to (d) in Fig. 9 represent the average absolute ranging error as a function of key parameter values respectively for the four techniques. In each figure, the key-parameter which gives the best average ranging accuracy is chosen. These figures give a parametric evaluation of the different techniques and highlight the importance of choosing the best value for the key parameter in order to reach the highest ranging accuracy.

In the rest of this paper, the chosen key-parameters are:
- Technique $T_1$: $\gamma_{th}/\gamma_0 = 0.14$
- Technique $T_2$: $\gamma_{cum} = 0.04$
- Technique $T_3$: $N_{max} = 16$
- Technique $T_4$: $\alpha = 13$

B. Comparison of different techniques

In order to compare the four TOA ranging techniques, we consider the UWB measurement campaign described before and we apply the different techniques on the 302 Tx positions. In total, we got $302 \times 4 = 1208$ TOA estimates. First, we plot in Fig. 10 the evolution of the average ranging error with respect to the LQI values. This figure reveals that at higher SNR, the four techniques achieve close ranging accuracy which tends to 3cm. For lower SNR, the $T_4$ technique achieves the best performances while the typical $T_1$ technique is not reliable at all. The techniques $T_2$ and $T_3$ outperform the $T_1$ technique at lower and medium SNR. These results outperform the results proposed in [16] and approaches those presented in [12] where no real measurement campaign was used to evaluate the performances of ranging techniques. Indeed, these two papers used simulation models (CM1, ..., CM4), which are more or less simplified and do not accurately represent the reality of the radio channel. In our work, the goal was to evaluate the ranging techniques on a real measurements campaign in order to outcome the limits of such techniques.

In the rest of this section, we will present the performances for links with a LQI higher than 10dB.

\[
\begin{align*}
\text{Fig. 9. Tuning of different ranging techniques using UWB measurements:} \\
\text{the key-parameters are chosen to best fitting the measurements.}
\end{align*}
\]

\[
\begin{align*}
\text{Fig. 10. Average Ranging error wrt. LQI for different techniques.}
\end{align*}
\]
the Rx. If an obstacle exists, we have no visibility between the Tx and the Rx and we differ two cases: the NLOS case where a direct path crosses the obstacle and reach the Rx and the NLOS\(^2\) case where no direct path is crossing the obstacle. In each figure, we plot the cumulative density function (cdf) of the ranging error for the four different techniques. Fig. 11 shows that the \(T4\) technique outperforms the three other techniques. Table I shows that the lower mean ranging error and standard deviation are performed by the fourth technique (\(T4\)) which is based on the fusion of \(T1\) and \(T3\) techniques. It benefits thus from the advantages of these two techniques to give the best ranging accuracy. With a real measurement campaign, we believe that the obtained accuracy of 13cm as a mean value and 50cm as a deviation value is very promising compared to results presented in [6], [12], [16], [17]. Notice also that the choice of the key parameter of each technique should be done in a more optimal way in order to enhance the ranging accuracy.

In some NLOS and NLOS\(^2\) situations, it occurs that the signal is obstructed by a metallic cabinet which makes the detection of the first ray very difficult and the ranging accuracy very poor. This is shown in Fig. 12 where we plot the distribution of ranging error for the four receivers using the \(T4\) technique. In this figure, the positions obstructed by metallic cabinets show a low ranging accuracy. These metallic cabinets deeply affect the TOA ranging accuracy. In order to better model and exploit TOA within localization applications under the presence of such obstructing objects, TOA models should be spatially particularized as shown in [18].

### VI. Conclusion

This paper presented a study of four different ranging techniques applied to IR-UWB technology. Using an IR-UWB measurements campaign, these four techniques are tuned, evaluated, and compared. The paper presented the typical threshold-based TOA estimation technique and proposed a modified version using the cumulative channel impulse response. We proposed also a dichotomous based technique which outperforms the cumulative CIR based technique. The fourth and last technique is a fusion of the two techniques: threshold based and dichotomous based. This technique benefits from the advantages of these two techniques and outperforms hence all the studied techniques. The main outcome of this paper was to study the performances of ranging techniques on a real UWB measurement campaign unlike the most of existing works which are based on simplified simulation models. The paper shows that the reached accuracy with this real measurements campaign is very promising compared to the state of the art.

### ACKNOWLEDGMENT

This work has been performed in the framework of the ICT project ICT-248894 WHERE2, which is partly funded by the European Union.
Fig. 12. Mapping of ranging error obtained with the TH technique for the different receivers. The figure highlights the effect of metallic cupboards on the ranging accuracy.

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