Electrokinetic techniques for the determination of hydraulic conductivity
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1. Introduction

In a porous medium the fluid flux and the electric current density are coupled, so that the streaming potentials are generated by fluids moving through porous media and fractures. These electrokinetic phenomena are induced by the relative motion between the fluid and the rock because of the presence of ions within water. Both steady-state and transient fluid flow can induce electrokinetics phenomena. It has been proposed to use this electrokinetic coupling to detect preferential flow paths, to detect faults and contrast in permeabilities within the crust, and to deduce hydraulic conductivity. This chapter proposes a comprehensive review of the electrokinetic coupling in rocks and sediments and a comprehensive review of the different approaches to deduce hydraulic properties in various contexts.

Electrical methods are sensitive to the fluid content because of the relative high conductivity of water compared to the one of the rock matrix. The electrical resistivity can be related to the permeability and to the deformation, in full-saturated or in partially-saturated conditions (Doussan & Ruy, 2009; Henry et al., 2003; Jouniaux et al., 1994; 2006). The electrokinetic phenomena are induced by the relative motion between the fluid and the rock matrix. In a porous medium the electric current density, linked to the ions within the fluid, is coupled to the fluid flow (Overbeek, 1952) so that the streaming potentials are generated by fluids moving through porous media (Jouniaux et al., 2009). The classical interpretation of the self-potential (SP) observations is that they originate from electrokinetic effect as water flows through aquifer or fractures. Therefore some formula have been proposed to predict the permeability of porous medium or fault using the electrokinetic properties. The SP method consists in measuring the natural electric field on the Earth’s surface. Usually the electric field is measured by a high-input impedance multimeter, using impolarizable electrodes (Petiau, 2000; Petiau & Dupis, 1980) and its interpretation needs filtering techniques (Moreau et al., 1996). Moreover, for long-term observations the monitoring of the magnetic field is also needed for a good interpretation (Perrier et al., 1997). Some studies have proposed to use SP observations to infer water-table variations, to estimate hydraulic properties (Glover & Walker, 2009), and to deduce where to make a borehole for water-catchment. These studies involve surface or borehole measurements (Aubert & Atangana, 1996; Fagerlund & Heison, 2003; Finizola et al., 2003; Perrier et al., 1998; Pinettes et al., 2002), some of them have monitored self-potentials during hydraulic tests in boreholes (Darnet et al., 2006; Darnet & Marquis, 2004; Ishido et al., 1983; Maineult et al., 2008). Direct models
(Ishido & Pritchett, 1999; Jouniaux et al., 1999; Sheffer & Oldenburg, 2007) and inverse problems (El-kaliouby & Al-Garni, 2009; Fernandez-Martinez et al., 2010; Gibert & Pessl, 2001; Gibert & Sailhac, 2008; Minsley et al., 2007; Naudet et al., 2008; Sailhac et al., 2004; Saracco et al., 2004) have been developed to locate the source of self-potential. Because of similarity between the electrical potential with pressure behavior, it has been proposed also to use SP measurements as an electrical flow-meter (Pezard et al., 2009). However, inferring a firm link between SP intensity and water flux is still difficult. Recent modeling has shown that SP observations could detect at distance the propagation of a water front in a reservoir (Saunders et al., 2008).

We distinguish 1) The steady-state and passive observations which consist in measuring the electrical self-potential (SP). 2) The transient and active observations which consist in measuring the electrical potential induced by the propagation of a seismic wave. These observations are called seismo-electric conversion. The reverse can also be observed: the detection of a seismic wave induced by injection of electrical current and is called electro-seismic conversion.

2. Streaming potential coefficient in rocks and sediments

2.1 Theoretical background
The fluid flow in porous media or in fractures can induce electrokinetic effect because of the presence of ions within the fluid which can induce electric currents when water flows. The general equation coupling the different flows is,

\[ J_i = \sum_{j=1}^{N} L_{ij} X_j \]  

(1)

which links the forces \( X_j \) to the macroscopic fluxes \( J_i \), through transport coupling coefficients \( L_{ij} \) (Onsager, 1931).

When dealing with the coupling between the hydraulic flow and the electric flow, assuming a constant temperature, and no concentration gradients, the electric current density \( J_e \) [A.m\(^{-2}\)] and the flow of fluid \( J_f \) [m.s\(^{-1}\)] can be written as the following coupled equation:

\[ J_e = -\sigma_0 \nabla V - L_{ek} \nabla P. \]

(2)

\[ J_f = -L_{ek} \nabla V - \frac{k_0}{\eta_f} \nabla P. \]

(3)

where \( P \) is the pressure that drives the flow [Pa], \( V \) is the electrical potential [V], \( \sigma_0 \) is the bulk electrical conductivity [S.m\(^{-1}\)], \( k_0 \) the bulk permeability [m\(^2\)], \( \eta_f \) the dynamic viscosity of the fluid [Pa.s], \( L_{ek} \) the electrokinetic coupling [A Pa\(^{-1}\) m\(^{-1}\)]. Thus the first term in equation 2 is the Ohm’s law and the second term in equation 3 is the Darcy’s law. The coupling coefficients must satisfy the Onsager’s reciprocal relation in the steady state: the coupling coefficient is therefore the same in equation 2 and equation 3. This reciprocity has been verified on porous materials (Auriault & Strzelecki, 1981; Miller, 1960) and on natural materials (Beddiar et al., 2002).

The streaming potential coefficient \( C_{s0} \) [V.Pa\(^{-1}\)] is defined when the electric current density \( J_e \) is zero, leading to
\[
\frac{\Delta V}{\Delta P} = -\frac{C_{ek}}{\sigma_0} = C_{s0}
\]

This coefficient can be measured by applying a driving pore pressure \(\Delta P\) to a porous medium and by detecting the induced electric potential difference \(\Delta V\). The driving pore pressure induces a streaming current (second term in eq. 2) which is balanced by the conduction current (first term in eq.2) which leads to the electric potential difference \(\Delta V\) that can be measured. We detail here what we know about this streaming potential coefficient (SPC) on sands and rocks because we will see that it can be used with the electro-osmosis coefficient to deduce the permeability. In the case of a unidirectional flow through a cylindrical saturated porous capillary, this coefficient can be expressed as (Jouniaux et al., 2000; Jouniaux & Pozzi, 1995b):

\[
C_{s0} = \frac{\varepsilon_f \zeta}{\eta_f \sigma_{eff}}
\]

with the fluid electrical permittivity \(\varepsilon_f\) [F.m\(^{-1}\)], the effective electrical conductivity \(\sigma_{eff}\) [S.m\(^{-1}\)] defined as \(\sigma_{eff} = F\sigma_0\) with \(F\) the formation factor and \(\sigma_0\) the rock conductivity which can include a surface conductivity. The potential \(\zeta\) [V] is the zeta potential described as the electrical potential inside the EDL at the slipping plane or shear plane (i.e., the potential within the double-layer at the zero-velocity surface). Minerals forming the rock develop an electric double-layer when in contact with an electrolyte, usually resulting from a negatively charged mineral surface. An electric field is created perpendicular to the surface of the mineral which attracts counterions (usually cations) and repulses anions in the vicinity of the pore matrix interface. The electric double layer (Fig. 1) is made up of the Stern layer, where cations are adsorbed on the surface, and the Gouy diffuse layer, where the number of counterions exceeds the number of anions (Adamson, 1976; Davis et al., 1978; Hunter, 1981). The streaming current is due to the motion of the diffuse layer induced by a fluid pressure difference along the interface. This streaming current is then balanced by the conduction current, leading to the streaming potential. When the surface conductivity can be neglected compared to the fluid conductivity \(F\sigma_0 = \sigma_f\) and the streaming coefficient is described by the well-known Helmholtz-Smoluchowski equation (Dukhin & Derjaguin, 1974):

\[
C_{s0} = \frac{\varepsilon_f \zeta}{\eta_f \sigma_f}
\]

The assumptions are a laminar fluid flow and identical hydraulic and electric tortuosity. The influencing parameters on this streaming potential coefficient are therefore the dielectric constant of the fluid, the viscosity of the fluid, the fluid conductivity and the zeta potential, itself depending on rock, fluid composition, and \(pH\) (Guichet et al., 2006; Ishido & Mizutani, 1981; Jaafar et al., 2009; Jouniaux et al., 2000; Jouniaux & Pozzi, 1995a; Lorne et al., 1999a; Vinogradov et al., 2010). There exists a \(pH\) for which the zeta potential is zero: this is the isoelectric point and \(pH\) is called \(pH_{IEP}\) (Davis & Kent, 1990; Sposito, 1989). At a given \(pH\) the most influencing parameter is the fluid conductivity (Fig.2). When collecting data from literature on sands and sandstones we can propose that \(C_{s0} = -1.2 \times 10^{-8} \sigma_f^{-1}\) which leads to a zeta potential equal to \(-17\) mV assuming eq. 6 and that zeta potential and dielectric constant do not depend on fluid conductivity. These assumptions are not exact, but the value of zeta is needed for numerous modellings which usually assume the dielectric constant not dependent on the fluid conductivity. Therefore an average value of \(-17\) mV for such
modellings is rather exact, at least for medium with no clay nor calcite. Another formula is often used (Pride & Morgan, 1991) based on quartz minerals rather than on sands and sandstones, which may be less appropriate for field applications. When the medium is not fully saturated Perrier & Morat (2000) suggested a model in which the streaming potential coefficient is dependent on a relative permeability model $k_r$.

$$C(S_w) = C_{s0} \frac{k_r}{S_w^n}$$

assuming that the relative electrical conductivity is equal to $S_w^{\frac{m}{n}}$. The parameter $n$ is the Archie saturation exponent (Archie, 1942). This exponent has been observed to be about 2 for consolidated rocks and in the range $1.3 < n < 2$ for coarse-texture sand (Guichet et al., 2003; Lesmes & Friedman, 2005; Schön, 1996). Note that the use of Archie’s law is valid in the absence of surface electrical conductivity. Recently Allègre et al. (2010) (and Allègre et al. (2011)) proposed original streaming potential measurements performed during a drainage experiment and measured the first continuous recordings of the streaming potential coefficient as a function of water saturation. These authors observed that the streaming potential coefficient exhibits two different behaviours as the water saturation decreases. Values of $C_{s0}$ first increase for decreasing saturation in the range $0.55 - 0.8 < S_w < 1$, and then decrease from $S_w = 0.55 - 0.8$ to residual water saturation. This behaviour was never reported before and still needs further interpretation. Jackson (2010) used a bundle capillary model to compute the streaming potential coefficient as a function of water-saturation. He showed that the behaviour of the SPC depends on the capillary size distribution, the wetting behaviour of the capillaries, and whether we invoke the thin or thick electrical double layer assumption. Depending upon the chosen value of the saturation exponent and the irreducible water-saturation, the relative SPC may increase at partial saturation, before decreasing to zero at the irreducible saturation. Up to now permeability predictions using electrokinetic techniques use theoretical developments in full saturated conditions.

Similarly the electro-osmosis coefficient is defined when the flow of fluid $J_f$ is zero, leading to

$$\frac{\Delta P}{\Delta V} = - \frac{L_{ek} \eta}{k_0} = C_{e0}$$

This coefficient can be measured by applying an electric potential difference $\Delta V$ and by detecting the induced electro-osmotic flow [m.s$^{-1}$] corresponding to the first term of equation 3, by controlling the hydraulic gradient, usually maintaining identical water heads. Assuming the Helmholtz-Smoluchowski equation (eq. 6) the electro-osmosis coefficient can be written as:

$$C_{e0} = \frac{\epsilon \zeta}{k_0 F}$$

and then depends also on pH (Beddiar et al., 2005) through the zeta potential. Since the permeability and the formation factor are not independent, but can be related by $k_0 = CR^2/F$ (Paterson, 1983) with $C$ a geometrical constant usually in the range 0.3-0.5 and $R$ the hydraulic radius, the electro-osmosis coefficient can be written as:

$$C_{e0} = \frac{\epsilon \zeta}{CR^2}$$
As we can see from this section, the streaming potential coefficient and the electro-osmosis coefficient are directly proportional to the zeta potential, which can not be directly measured and which is difficult to model at a rock-water interface. Therefore the zeta potential is usually deduced from streaming potential measurements. Moreover the streaming potential coefficient is inversely proportional to the fluid conductivity, whereas the electro-osmosis coefficient is inversely proportional to the hydraulic radius.

2.2 Permeability prediction

These electrokinetic properties have been used to predict the permeability. Li et al. (1995) defined an electrokinetic permeability $k_e$ by the following relation:

$$k_e = \eta \sigma_r \frac{C_s}{C_o}$$

with $\sigma_r$ the rock conductivity (measured when $J_f$ is zero).

These authors verified on 12 samples of sandstones, limestones and fused glass beads that the electrokinetic permeability $k_e$ successfully predicts the rock permeability $k_r$ (measured when $J_e$ is zero) over a range of about four decades from $10^{-15}$ to $10^{-11}$ m². Pengra et al. (1999) verified also this relation on eight samples of sandstone and limestone, and four fused glass beads, in the permeability range $10^{-15}$ to $10^{-11}$ m² (Fig. 3). This approach has been used to propose the permeability measurement (Wong, 1995) within boreholes (Fig. 4). The advantage was that we only needed to apply or to measure the pressure and the electric field.

A simplest way to measure the permeability in borehole, was performed using only the streaming potential coefficient (eq. 4). Although this coefficient does not depend directly on permeability, Hunt & Worthington (2000) showed that the borehole streaming potential response could detect fractures and cracks. A pressure pulse is generated by a nylon block which displaces water as it moves upwards (Fig. 5). This mechanical system avoids spurious electrical noise induced by electro-mechanical systems. The electrode response is normalized to the peak pressure recorded by the hydrophone. The authors showed that the maximum electrical signal was clearly associated with the highest fracture density and the widest aperture (few cm). The recorded amplitudes were in the range $4 \times 10^{-7}$ to $1.5 \times 10^{-6}$ V/Pa. It was proposed that the fluid flow in the cracks causing the streaming potential was predominantly caused by the seismic wave within the rock that distorts crack aperture as it passes, rather than by the source directly forcing fluid into cracks. In this case the permeability dependence of the streaming potential coefficient may be linked to the indirect effect of surface conductivity which may not be negligible: the effective conductivity can decrease with increasing permeability, leading to an increase in the streaming potential coefficient (eq. 5) (Jouniaux & Pozzi, 1995a).

Recently, Glover et al. (2006) proposed a new prediction for the permeability by comparing an electrical model derived from the effective medium theory to an electrical model for granular medium. These authors derived the RGPZ model defined as:

$$k_{RGPZ} = \frac{d^2 \phi^{3m}}{4a m^2}$$

where $\phi$ is the porosity, $m$ the cementation exponent from the Archie’s law, $a$ is a parameter thought to be equal to $8/3$ for samples composed of quasi-spherical grains, and $d$ is the relevant grain size. They showed that the relevant grain size is the geometric mean, which can be deduced from Mercury Injection Capillary Pressure (MICP). The relevant grain size
can also be inferred from borehole NMR data, and then must be deduced from an empirical procedure relating grain size to the $T_2$ relaxation time. This new model was shown to match data over 348 samples over a 500 m thick sand-shale succession in the North Sea. Since the porosity can also be derived from NMR data, the advantage of this approach is to provide a log of permeability along the studied borehole, at the scale which is investigated by the NMR tool.

3. Fault and hydraulic fracturing

3.1 Permeability prediction within fault

It has also been proposed to deduce the permeability of the Nojima fault (Japan) using the self-potential observations in surface when water is injected into a well of 1800 m depth (Murakami et al., 2001). Water flow is induced at about 1600 m depth when crossing the fracture zone, and the change in voltage in the aquifer is conducted to the whole part of the well through the iron casing pipe (Fig. 6). Therefore the electrokinetic source occurring at depth can be detected at the surface. Self-potential variations of 10-35 mV in response to water pressure of 35-38x10$^5$ Pa were observed. The magnitude of self-potential variations decreases with increasing distance from the injection well. An amplitude of $-20$ mV was detected near the well, about $-10$ mV at 40 m, and within the noise at one hundred meters. The electrokinetic source is the dragging current expressed by the second term in eq. 2. Assuming the Helmholtz-Smoluchowski equation (eq. 6) and the Darcy’s law (second term in eq. 3), and using the definition of the formation factor $F$, we can write the dragging current:

$$J_{\text{drag}} = -\frac{\varepsilon_f \zeta}{F_k} J_f$$

(13)

This dragging current is balanced by the conduction current (the first term in eq. 2). Assuming a line source model with $L$ the length of the casing pipe, the potential difference $\Delta V$ between two electrodes at the surface is related to the total conduction current $I_{\text{cond-tot}}$ [A] by (Murakami et al., 2001):

$$\Delta V = \frac{I_{\text{cond-tot}}}{2\pi \sigma_f L} \log(a/b)$$

(14)

where $a$ and $b$ are the distances from the borehole to the electrodes. Then the permeability of the fault is deduced by:

$$k_{\text{fault}} = -\frac{\varepsilon_f \zeta}{F} \frac{Q_{f-tot}}{I_{\text{cond-tot}}}$$

(15)

The total conduction current $I_{\text{cond-tot}}$ is deduced from surface potential measurements $\Delta V$ (eq. 14). The total water injection (usually several liters/min) provides the value of $Q_{f-tot}$ [m$^3$s$^{-1}$]. The formation factor $F$ of the fault can be deduced from resistivity well-logging assuming Archie’s law and knowing the fluid conductivity. The value of zeta potential has to be deduced from laboratory experiments published in the literature, possibly using figure 2. Murakami et al. (2001) deduced that the permeability of the fault was higher at the end of the water injection than at the beginning. Assuming different hypotheses for the zeta potential to $-1$ to $-10$ mV they deduced a permeability in the range $10^{-16}$ to $10^{-15}$ m$^2$. The chemical properties of the injected water is important since it can decrease dramatically the zeta potential if species such as Ca$^{2+}$ or Al$^{3+}$ are present in high quantity. The advantage of this method is to be able to deduce the permeability at depth of the fault.
3.2 Self-potentials related to hydraulic fracturing

Since fluid flow can create streaming potentials, the hydraulic fracturing can induce streaming potentials as the fracture propagates, if the fracture remains full-filled with water. Laboratory experiments on hydraulic fracturing on granite samples showed that the streaming potential varies linearly with the injection pressure (Moore & Glaser, 2007). However the SPC increases in an exponential trend when approaching the breakdown pressure. Since the permeability also shows an exponential increase with injection pressure, the authors concluded that the SPC is varying as $k^{1.5}$. The explanation was not an effect due to the surface conductivity, but a difference in the hydraulic tortuosity (David, 1993) and electric tortuosity (as suggested by Lorne et al. (1999b)) induced by dilatancy of microcracks.

The streaming potential induced by an advancing crack has been modeled by Cuevas et al. (2009). The authors modeled the streaming electric current density by defining a source-time function from the pressure profile in the propagating direction of the opening crack. The streaming electric current is maximum at the tip of the fracture and decays exponentially in front of the tip. The decay constant linearly increases with the propagation speed of the fracture. As the fractures progresses, the streaming potential observed at a distant point results from a superposition of delayed sources arising at the position of the advancing fluid front. The results show that the energy is focused in the vicinity of the advancing fracture’s tip, however a tail can also be distinguished as the source behind the tip does not vanish instantaneously. Cuevas et al. (2009) could model the streaming electrical spike recorded by Moore & Glaser (2007) during hydraulic fracturing by modeling the propagation of two cracks and adjusting the propagation velocity, the direction of propagation and the initial fracture volume. The authors concluded that direct information of the hydraulic fracture propagation can be provided by measuring the electrical field at distant.

Hydraulic stimulation is often used to stimulate fluid flow in geothermal reservoirs. Surface electrical potentials were measured when water was injected (during about 7 days) in granite at 5 km depth at the Soultz Hot Dry Rock site (France) (Marquis et al., 2002). An anomalous potential of about 5 mV was interpreted as an electrokinetic effect a depth and measured at the surface because of the conductive well casing. The question of the exact origin between electrokinetic and electrochemical (Maineult, Bernabé & Ackerer, 2006; Maineult, Jouiaux & Bernabé, 2006) effects was raised by Darnet et al. (2004). Finally it has been shown that whatever the injection rate was, the electrochemical contribution was almost negligible (Maineult, Darnet & Marquis, 2006): the SP anomaly was mainly related to the temperature contrast between the in-situ brine and the injected fresh water only at the earliest stage of injection, and was essentially related to water-flows afterwards. Further investigations showed that a slow SP decay is observed after shut-in : its was interpreted as related to large fluid-flow persisting after the end of stimulation and correlated to the microseismic activity (Darnet et al., 2006). The fluid flow was not detected on hydraulic data because it took place in a zone hydraulically disconnected from the openhole. The authors concluded that the SP observations could monitor the fluid flow at the reservoir scale and revealed that the fluid flow plays a major role in the mechanical response of the reservoir to hydraulic stimulation. Another field experiment was performed with periodic pumping tests (injection/production) in a borehole penetrating a sandy aquifer (Maineult et al., 2008). The attenuation of SP amplitude with distance was roughly similar to the pressure attenuation. Therefore the authors proposed that hydraulic diffusivity could be inferred from SP observations. Moreover the comparaison between surface and borehole
measurements suggested that nonlinear phenomena are present, probably related to the saturation and desaturation processes occurring in the vadose zone (Maineult et al., 2008).

4. Seismo-electromagnetic conversions to detect hydraulic property contrasts

4.1 Theoretical background

The electrokinetic effect can also be induced by seismic wave propagation, which leads to a relative motion between the fluid and the rock matrix. In this case the electrokinetic coefficient depends on the frequency \( \omega \) as the dynamic permeability \( k(\omega) \) (Smeulders et al., 1992). Pride (1994) developed the theory for the coupled electromagnetics and acoustics of porous media. The transport relations [(Pride, 1994) equations (250) and (251)] are:

\[
J_e = \sigma(\omega) E + L_{ek}(\omega) \left( -\nabla p + \omega^2 \rho_f u_s \right)
\]

\[
- i \omega J_f = L_{ek}(\omega) E + \frac{k(\omega)}{\eta} \left( -\nabla p + \omega^2 \rho_f u_s \right)
\]

The electrical fields and mechanical forces which induce the electric current density \( J_e \) and the fluid flow \( J_f \) are, respectively, \( E \) and \( -\nabla p + i\omega^2 \rho_f u_s \), where \( p \) is the pore-fluid pressure, \( u_s \) is the solid displacement, \( E \) is the electric field, \( \rho_f \) is the pore-fluid density, and \( \omega \) is the angular frequency. The electrokinetic coupling \( L_{ek}(\omega) \) is now complex and frequency-dependent and describes the coupling between the seismic and electromagnetic fields (Pride, 1994; Reppert et al., 2001):

\[
L_{ek}(\omega) = L_{ek} \left[ 1 - \frac{i \omega m}{\omega_c} \left( 1 - \frac{2 d}{\Lambda} \right)^2 \left( 1 - i \frac{3/2}{d} \sqrt{\frac{\omega \rho_f}{\eta}} \right)^2 \right]^{-\frac{1}{2}}
\]

where \( m \) and \( \Lambda \) are geometrical parameters of the pores (\( \Lambda \) is defined in Johnson et al. (1987) and \( m \) is in the range 4 – 8), \( d \) the Debye length. The transition frequency \( \omega_c \) defined in the Biot’s theory separates the viscous and inertial flow domains and depends on the permeability \( k_0 \). The frequency-dependence of the streaming potential coefficient has been studied (Chandler, 1981; Cooke, 1955; Groves & Sears, 1975; Packard, 1953; Reppert et al., 2001; Schoemaker et al., 2007; 2008; Sears & Groves, 1978) mainly on synthetic samples. Both models (Gao & Hu, 2010; Garambois & Dietrich, 2001, 2002; Haartsen et al., 1998; Haartes & Pride, 1997; Pain et al., 2005; Schakel & Smeulders, 2010) and laboratory experiments (Block & Harris, 2006; Bordes et al., 2006, 2008; Chen & Mu, 2005; Zhu et al., 1999) have been developed on these seismoelectromagnetic conversions.

Note that assuming the Helmholtz-Smoluchowski equation for the streaming potential coefficient leads to the electrokinetic coupling inversely dependent on the formation factor \( F \) as:

\[
L_{ek} = \epsilon_f \zeta \frac{\eta_f}{\eta_f F}
\]

The formation factor is inversely related to the permeability and proportional to the hydraulic radius \( F = CR^2/k_0 \) (Paterson, 1983). Since the permeability can vary of about fifteen orders of magnitude, whereas this is not the case of the hydraulic radius, the static electrokinetic coupling \( L_{ek} \) will increase with increasing permeability.
4.2 Detection of permeability contrasts

Two kinds of mechanical to electromagnetic conversions exist: 1) The electrokinetic signal which travels with the acoustic wave; 2) The interfacial conversion occuring at contrasts of physical properties such as permeability.

The first kind of conversion has been used to show that a reliable permeability log can be derived from electrokinetic measurements (Singer et al., 2005), using an acoustic source within a borehole (Fig. 7). Singer et al. (2005) showed by a finite element model and by laboratory experiments that the normalized coefficient defined by the electric field divided by the pressure depends \([V \text{ Pa}^{-1} \text{ m}^{-1}]\) on the permeability. This coefficient is coherent with the electrokinetic coefficient \(L_{ek}\) (eq. 19) per unit of conductance [S] and then should increase with increasing permeability. At low permeability the oscillating source will induce a larger solid displacement because the fluid is not easily displaced. However the relative movement between solid and fluid is limited, leading to a decrease of the electric field even if pressure increases, so that this normalized coefficient is decreased. The investigated depth of such a permeability is of the order of centimeters. The source was a short steel tube near the top of the borehole and hit on top with a hammer. The main wave propagation is a Stoneley wave which induces the electric field. The logging tool is moved step-by-step within the borehole (Fig. 7). This model showed that the normalized coefficient could detect a 0.5 m-thick bed of permeability \(10^{-13} \text{ m}^2\) within a formation of permeability \(10^{-15} \text{ m}^2\). The measured amplitude of the normalized coefficient on sandstones is in the range \(1.6 \times 10^{-7}\) to \(2.5 \times 10^{-6} [V \text{ Pa}^{-1} \text{ m}^{-1}]\) increasing with increasing permeabilities from \(6.2 \times 10^{-15} \text{ m}^2\) to \(2.2 \times 10^{-12} \text{ m}^2\).

The second kind of conversion can be used to detect contrasts in permeability in the crust. The seismic source induces a seismic wave propagation downward up to the interface (Fig. 8). Because of the difference in the physical properties there is a charge imbalance that causes a charge separation on both sides of the interface. This acts as an electric dipole which emits an electromagnetic wave that travels with the speed of the light in the medium and that can be detected at the surface (Fig. 9). The velocity of the seismic wave propagation is deduced by surface measurements of the soil velocity. Then the depth of the interface can be deduced by picking the time arrival of the electromagnetic wave. Usually the seismoelectric signals show low amplitude from 100 μV to mV. Then signal processing needs filtering techniques such as Butler & Russell (1993). The advantage of this method is to detect the contrasts of permeability at depth from few meters to few hundreds of meters (Dupuis & Butler, 2006; Dupuis et al., 2007; Dupuis et al., 2009; Haines, Guitton & Biondi, 2007; Haines, Pride, Klemperer & Biondi, 2007; Strahser et al., 2007, 2011; Thompson et al., 2005).

5. Limitations of this technique

The limitations of this technique arise from the low amplitude of the electrical signal. It needs good pre-amplifiers to be able to detect the signals. Then it needs an adapted signal processing to remove the anthropic noise, and further filtering techniques to extract the expected signal from the remaining records. The interpretation of self-potential observations may not be easy if the signals are induced not only by the electrokinetic effect, but also by a thermoelectric effect, and by an electrochemical effect. The interpretation of the seismo-electric conversion may not be easy if the contrast in the permeability is not high enough.
Fig. 1. Electric double layer, courtesy of P.W.J. Glover (Glover & Jackson, 2010). The solid mineral presented is the case of silica. At pH above the isoelectric point the cations are adsorbed within the Stern layer; there is an excess of cations in the diffuse layer. The zeta potential is defined at the shear plane. The fluid flow creates a streaming current which is balanced by the conduction current, leading to the streaming potential.

Fig. 2. Streaming potential coefficient from data collected (in absolute value) on sands and sandstones at pH 7-8 (when available) from Ahmad (1964); Guichet et al. (2006; 2003); Ishido & Mizutani (1981); Jaafar et al. (2009); Jouniaux & Pozzi (1997); Li et al. (1995); Lorne et al. (1999a); Pengra et al. (1999); Perrier & Froidefond (2003). The regression (black line) leads to \( C_s = -1.2 \times 10^{-8} \sigma_f^{-1} \). A zeta potential of \(-17\) mV can be inferred from these collected data (from Allègre et al. (2010)).
Fig. 3. Comparison between the permeability $k$ and the electrokinetic permeability $k_e$. The solid line is $k_e = k$ (modified from Pengra et al. (1999)).

Fig. 4. In-situ permeability measurement (from Wong (1995)) from streaming potential and electro-osmosis measurements using eq. 11. For the streaming potential measurement: an oscillating pressure is applied by electromechanical transducer (22) to the rock formation (20) through fluid chamber (21) with valve (42) open. The pressure differential in the rock between fluid chamber (21) and (21') is measured by a pressure sensor (25) and the induced voltage difference is measured by the voltage electrodes (32) and (32'). For the electro-osmosis measurements the valve (42) is closed, the pressure difference induced when a current is passed through the rock (by current electrodes 29 and 29') is measured by pressure sensor (25).
Fig. 5. Scheme of the principle of borehole electrokinetic response to detect fractures (modified from Hunt & Worthington (2000)). The source is a nylon block (N) pulled by the rope, which induces fluid flow near the wall of the rock formation, leading to an electrokinetic effect. The electrodes are 1 m apart. The hydrophone is 2.5 m below the source. The electrode response is normalized by the peak pressure.
Fig. 6. Measurement of the permeability of the Nojima fault (modified from Murakami et al. (2001)). The water injection inside the borehole of 1800 m depth crosses the fault inducing an electrokinetic source at depth within the fault. The conduction current is conducted by the iron pipe up to the surface. The difference of potential $V$ is measured by electrodes on the surface. The permeability is deduced from eq. 15.
Fig. 7. Scheme of the principle of electrokinetic logging to measure the permeability (modified from Singer et al. (2005)). The acoustic source induces a Stoneley wave propagation (detected by the hydrophones) leading to an electric field (measured by the electrodes). The experiment is repeated by moving the tool downward.
Fig. 8. The seismic waves propagates up to the interface where an electric dipole is generated because of the contrast in permeability. This electromagnetic wave can be detected at the surface by measuring the difference of the electrical potential $V$ between electrodes. Picking the time arrival allows to know the depth of the interface.
Fig. 9. Model of the seismoelectric response to a hammer strike on the surface at position zero (from Haines (2004)). The seismoelectric signal is shown as measured at the surface along a line centered on the seismic source. The interfacial signal is related to a contrast between properties of the media, such as the permeability.

6. Conclusion

The electrokinetic properties can be used to deduce permeability in the crust, possibly at depth, within fault, and along boreholes. Some conditions are needed to be able to use electrokinetic coupling to infer hydraulic properties. The electrical noise can prevent being able to detect small electric potentials, even using appropriate filtering techniques. When possible, the joint inversion with other observations can improve parameters such as electrical conductivity. The seismoelectric method could provide deeper investigations when using stronger seismic sources.

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8. References


Electrokinetic Techniques for the Determination of Hydraulic Conductivity


