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A framework for the objective evaluation of segmentation algorithms using a ground-truth of human segmented 3D-models

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Abstract—In this paper, we present an evaluation method of 3D-mesh segmentation algorithms based on a ground-truth corpus. This corpus is composed of a set of 3D-models grouped in different classes (animals, furnitures, etc.) associated with several manual segmentations produced by human observers. We define a measure that quantifies the consistency between two segmentations of a 3D-model, whatever their granularity. Finally, we propose an objective quality score for the automatic evaluation of 3D-mesh segmentation algorithms based on these measures and on the ground-truth corpus. Thus the quality of segmentations obtained by automatic algorithms is evaluated in a quantitative way thanks to the quality score, and on an objective basis thanks to the ground-truth corpus. Our approach is illustrated through the evaluation of two recent 3D-mesh segmentation methods.

Keywords—3D-mesh; segmentation; evaluation; ground-truth

1. INTRODUCTION

Mesh segmentation consists in decomposing a polygonal surface into different regions (i.e. connected set of vertices or facets) of uniform properties, either from a geometric point of view or from a semantic point of view. This operation has become a necessary preprocessing step for many applications such as shape modeling [1], compression [1], deformation [2], texture mapping [3], etc.

According to recent states-of-the-art [4], [5], mesh segmentation techniques can be classified into two categories: surface-type (or geometric) methods and part-type (or semantic) methods. In the first case, the algorithms are based on low level geometric information (e.g. curvature [6]) in order to define segments (i.e. regions) with respect to geometric homogeneity, while in the latter case, the algorithms aim at distinguishing segments that correspond to relevant features of the shape, by following higher level notions such as defined in human perception theory [7]. This kind of approach is particularly suited for object animation / deformation and indexing applications, where the decomposition has to be meaningful.

In the literature, there exist a huge number of segmentation algorithms for both approaches (surface-type and part-type) allowing the processing of 3D-meshes [4], [5]. For the first approach (surface-type) some tools exist for quantifying the quality of the segmentation however they are linked to some specific applications like texture mapping [8] or medical imaging [9]. The fact is that no automatic tool has been proposed to evaluate segmentation algorithms (especially part-type ones) in a general purpose context, although, this task is not only necessary for researchers to compare a new algorithm to those already existing, but also for users so as to choose an algorithm and fix its parameters depending on the problem to solve.

The question of the evaluation of these part-type segmentation algorithms is quite critical, in order to produce better methods. Whereas compression or recognition algorithms are quite easy to evaluate thanks to compression ratio or misclassification probability, this task is far more difficult to handle for segmentation (and particularly semantic segmentation). Typically researchers exhibit some results for several models and just point out why their results look “good”.

Attene et al. [5] have proposed some criteria like the aspect of the boundaries (smoothness, length), the hierarchical / multi-scale properties, the robustness, the complexity and the number of parameters. However these criteria rather judge some technical points than the real quality of the techniques themselves. As it is raised by the authors, the main problem is that the objective quality of a segmentation of a given model is quite difficult to define, since it depends on the viewer’s point of view and knowledge. Moreover many authors argue that a segmentation quality is theoretically impossible to evaluate objectively because it depends only on the desired application. Indeed the desired task is of course of importance. For instance a structural recognition application does not need the same segmentation than a mesh simplification task. An alternative solution, which was also suggested by Attene et al. [5] is to compare the algorithm’s results with manual segmentations produced by human subjects (i.e. a ground-truth). The objective is thus to capture the semantic and cognitive behavior of the user regarding 3D graphics. It is obvious that this framework will not be suited for evaluating the segmentations within certain specific applications (medical, texture mapping, etc.). However for many applications (e.g. animation) researchers aim to obtain such semantic decomposition. Thus our objective
is rather to focus on the evaluation of such semantic (i.e. part based) methods. This kind of ground-truth-based evaluation was investigated in the field of 2D-image [10]. Of course, the ground-truth can depend also on the application.

This question of objective evaluation of segmentation is the main motivation of this paper, which introduces three main contributions. Firstly, we propose a ground-truth corpus, composed of a set of 3D-models associated with several manual segmentations produced by human observers. Secondly, we propose some objective dissimilarity measures which provide a quantitative comparison between two segmentations of a 3D-model. Thirdly, we define an automatic protocol for the calculation of an objective quality score for the evaluation of 3D-mesh segmentation algorithms based on these objective measures and on the ground-truth corpus.

This work is done within the framework of the MADRAS project (3D Models And Dynamic models Representation And Segmentation) supported by the French Government Research Department. The ground-truth corpus is available for download for the scientific community, on the project website1.

This paper is organized as follows. In section 2, we provide a review of the state-of-the-art of segmentation evaluation. In section 3, we detail the construction of the ground-truth corpus. In section 4, we define two measures that compute the discrepancy (i.e. the dissimilarity) between two segmentations of a same object: a ground-truth segmentation and that obtained by an algorithm to evaluate, for instance, then we define an objective segmentation algorithm quality score. In section 5, our objective measures are firstly validated using the ground-truth corpus, then we demonstrate the usability of our whole evaluation protocol through the evaluation of two recent segmentation methods [6], [11]. Section 6 concludes the paper.

2. STATE-OF-THE-ART OF SEGMENTATION EVALUATION

Whereas almost nothing has been done by the scientific community regarding 3D-mesh segmentation evaluation, several advanced works exist for the quality assessment of 2D-image segmentation.

2.1 Evaluation of 2D-image segmentation

Zhang [12] offers a study on the different methods proposed so far for evaluation of 2D-image segmentation. According to Zhang, the different methods can be classified into three groups:

• Analytical methods: they directly treat the segmentation algorithms themselves by taking into account principles, requirements, utilities, complexity, etc., of algorithms. Using analytical methods to evaluate segmentation algorithm avoids a concrete implementation of the algorithm. However, the real quality of these algorithms cannot be obtained by a simple analytical study.

• Empirical goodness methods: they evaluate the performance of the algorithms by judging the quality of the segmented images themselves. To achieve this task, a set of quality criteria has to be defined. These criteria are established according to human intuition about what conditions should be satisfied by an ideal segmentation. However it seems difficult to establish quantitatively the quality of a segmentation only by using such a priori criteria.

• Empirical discrepancy methods: in this kind of methods, a set of reference images presenting the ideal segmentation is first of all built. This set of images which can be manually segmented by experts of the domain, constitutes a ground-truth. The purpose is to measure the discrepancy between the reference segmentation and that obtained by an algorithm to be evaluated. So, these methods try to determine how far a segmented image obtained by an algorithm is from one or several reference images. A large discrepancy involves a large segmentation error and thus this indicates a low performance of the considered segmentation algorithm.

The empirical discrepancy methods are the most popular for 2D-image segmentation evaluation [10], [13], indeed they seem to be the most suited for a quantitative evaluation as the measures of quality can be numerically computed, and for an objective evaluation thanks to the ground-truth.

Martin et al. [10] have proposed such a method to evaluate image segmentation algorithms. They built a public database containing ground-truth segmentations produced by human volunteers for images of a wide variety of natural scenes. They also defined a measure based on the computation of refinement error of a pixel between two segments (i.e. regions) containing this pixel.

2.2 Evaluation of 3D-mesh segmentation

In the literature there exist some works proposing the assessment of segmentation in a specific context. In the MRI (Magnetic Resonance Imaging) field for example, Gerig et al. [9] propose a tool that quantifies the segmentation quality of 3D-images (volumetric images) including different shape distance metrics such as maximum Hausdorff distance, and mean/median absolute distance between object surfaces. For texture mapping, Sander et al. [8] introduce a metric based on the texture stretch induced by the parametrization of the segmented regions and allowing the evaluation of the segmentation quality. More recently a set of technical criteria was proposed by Attene et al. [5] but they rather fall in the empirical goodness methods. Lastly, Berretti et al. [14] have presented some experimental results which are based on a ground-truth to validate their own segmentation

1http://www-rech.telecom-lille1.eu/madras/
algorithm. However, the ground-truth is not available online and according to the authors it contains very simple 3D-models (surfaces of revolution, vases, etc.). Their measure to compare two segmentations of a 3D-mesh is also a simple one. It is based on the area of regions and is not tolerant to refinement. Indeed the tolerance to refinement is an important property since it allows to distinguish between consistent and non-consistent segmentations. We can notice that the proposed solutions are either depending on the application context or do not reflect the real quality of the techniques themselves. Hence, the importance to propose a generic framework allowing an objective evaluation of segmentation algorithms.

3. Ground-truth corpus

We have created a ground-truth corpus available online for 3D-mesh segmentation evaluation. This corpus contains twenty 3D-models (as polygonal meshes) grouped in five classes, namely animal, furniture, hand, human and few-vertices. Each class contains four models as illustrated in figure 1.

![Fig. 1. From top to bottom line: animal, human, furniture, few-vertices and hand classes.](image)

The models come from the GAMMA database from INRIA and from the Princeton Shape Benchmark [15], which are both public 3D-model databases.

Note that it was crucial for our corpus, to present a high variety of models so as to be able to study properly the different segmentation algorithm’s behaviors while avoiding to privilege certain algorithms over others.

We have then conducted a large campaign of manual segmentation with human subjects.

3.1 Tool for manual segmentation

In order to easily collect manual segmentations from a wide range of people, we have used the MeshLab application; this software allows the processing of 3D-meshes, providing a set of tools for editing, filtering, inspecting, rendering and converting them. In particular it allows an explicit segmentation of models using colors.

Indeed, a virtual brush allows a human observer to colorize each vertex of the mesh to segment. Each segment (a set of vertices) is then distinguished from others by its associated color. Using this application, anyone can segment models without having any prior skills in computer graphics. Moreover to accelerate the coloring process (which could be fastidious for complex models) and to make it easier, we have developed a color propagation algorithm allowing the user to only indicate the different boundaries between the different segments; the whole segments are then automatically filled by colors (see figure 2). Basically with this tool, between 5 and 10 minutes are necessary for an observer to segment a 3D-model.

![Fig. 2. Automatic propagation of colors on the baby model. The user just need to color the boundaries of the regions that he wants to separate (left), our algorithm then automatically complete the coloring (right).](image)

3.2 Segmentation protocol

In order to obtain a lot of ground-truth segmentations for the model corpus, we have made a large call to volunteers. They have freely segmented the models and no condition was imposed on the manner with which they had to do this task. The models were randomly assigned to each volunteer with a bias towards models that had been already segmented several times. Figure 3 illustrates some models with one of their associated ground-truth segmentation.

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This ground-truth corpus is in a constant evolution in terms of number of models and number of segmentations per model. Having more than one segmentation per mesh is very important since two observers do not necessarily share the same opinion on the segmentation of a model. This is due to the lack of rules that define how to decompose an object into sub-objects: thus each observer can segment at different granularities for instance. Figure 4 illustrates an example of a 3D-model segmented by two different persons. One can notice that the first segmentation (on the left side) is nearly a refinement of the second one (on the right side).

The results presented in this paper have been generated using our current version of the ground-truth corpus including 60 segmentations, 3 per model, done by 25 different subjects (staff members and PhD students from University of Lille and Insa-Lyon).

4. FROM DISSIMILARITY MEASURES TO OBJECTIVE QUALITY SCORE

The objective of such measures is to evaluate existing and future segmentation algorithms in a quantitative way and on an objective basis. This objective can be achieved by measuring the dissimilarity between the segmentations obtained by algorithms to evaluate and those of the associated ground-truth.

4.1 Segmentation dissimilarity measures

As mentioned in the state-of-the-art section, in the field of 2D-image, Martin et al. [10] have defined two measures based on the computation of refinement error of a pixel between two segments containing this pixel; they have then applied them to evaluate the performance of 2D-segmentation algorithms and have shown the relevance of the obtained results.

Hence we have generalized their dissimilarity measures for 3D-mesh segmentation evaluation.

First of all, we formally define what is a segmentation of a 3D-mesh.

According to Shamir [4], let $M$ be a 3D-mesh, and $\mathcal{R}$ the set of mesh elements; in our case these elements are the vertices $v_i$ of $M$. A segmentation $\mathcal{S}$ of $M$ is the set of sub-meshes $\mathcal{S} = \{M_0, ..., M_{k-1}\}$ induced by the partitioning of $\mathcal{R}$ into $k$ disjoint sub-sets of vertices.

Similarly to the 2D measure from Martin et al. [10], we define the 3D local refinement error $L_{3D}$. Let $\mathcal{S}_1$ and $\mathcal{S}_2$ be two segmentations of a 3D-mesh $M$. $L_{3D}(\mathcal{S}_1, \mathcal{S}_2, v_i)$ is the local refinement error of a vertex $v_i$ between $\mathcal{S}_1$ and $\mathcal{S}_2$ defined as:

$$L_{3D}(\mathcal{S}_1, \mathcal{S}_2, v_i) = \frac{|R(\mathcal{S}_1, v_i) \setminus R(\mathcal{S}_2, v_i)|}{|R(\mathcal{S}_1, v_i)|}$$

(1)

Where the operator $\setminus$ denotes the set differencing, $|x|$ the cardinality of the set $x$, and $R(\mathcal{S}, v_i)$ the region in segmentation $\mathcal{S}$ that contains the vertex $v_i$, i.e. the subset of vertices corresponding to a sub-mesh $M_j$ of $\mathcal{S}$ containing $v_i$.

This local refinement error produces a positive real valued output that presents the ratio of the number of vertices not shared between the first segment and the second one.

The $L_{3D}$ is asymmetrically tolerant to refinement since the error is null when segment $\mathcal{S}_1$ is a subset (refinement) of segment $\mathcal{S}_2$.

We have to precise here that our measure consider that a segmented region is a set of vertices. We could have considered a segmented region as a set of facets (indeed, both definitions exist). We have chosen this kind of partitioning since it seems preponderant in the literature [4]. However, our measure could be easily adapted to face-based methods; in that case the set differencing operator (equation 1) should take into account some kind of surfacic difference.

Given this $L_{3D}$, there exist two ways to combine it for all vertices into a global measure for the entire 3D-mesh [10]: the Global Consistency Error (GCE) and the Local Consistency Error (LCE).

The Global Consistency Error (GCE) forces all local refinements to be in the same direction and is defined as:
\[ GCE(S_1, S_2) = \frac{1}{N} \min \left\{ \sum_i L_{AD}(S_1, S_2, v_i), \sum_i L_{AD}(S_2, S_1, v_i) \right\} \]  

The Local Consistency Error (LCE) allows for different directions of refinement in different segments of the 3D-mesh:

\[ LCE(S_1, S_2) = \frac{1}{N} \sum_i \min\{L_{AD}(S_1, S_2, v_i), L_{AD}(S_2, S_1, v_i)\} \]  

Where \( N \) is the number of vertices. For both the GCE and the LCE, a value of 0 indicates a complete similarity, whereas a value of 1 indicates a maximum deviation between the two segmentations being compared. It is clear that the GCE is a tougher measure than LCE since \( LCE \leq GCE \).

It is important to note that these measures are based on vertices and thus depend on the surface sampling. Indeed, the regions that have a high number of vertices will have a high effect on the consistency error whatever their area. However we do not consider this surface sampling dependence as a drawback since we suppose that in a correctly modelized object, the number of vertices well reflects the significance of the region.

Another important point to note is that there are two degenerative segmentations that achieve a GCE and a LCE score of zero: one vertex per segment, and one segment for the entire mesh. This is due to the tolerance of the measure toward refinement. However in practice, as further experiments demonstrate, this measure has a quite good behavior, since we never meet such degenerate cases in standard 3D-mesh segmentation algorithms. Actually, the segmentations to be compared must have numbers of segments sharing the same orders of magnitude.

### 4.2 Quality score of a segmentation algorithm

GCE and LCE are dissimilarity measures between two segmentation results of a same object. Using these two measures, together with the ground-truth corpus, we now define two quality measures for automatically rating segmentation algorithms. These two metrics reflect the global quality of the considered segmentation algorithm when comparing its segmentation results to the whole ground-truth corpus.

Let \( GCE_M(g_i, S) \) be the Global Consistency Error applied to a model \( M \) between a ground-truth segmentation \( g_i \) and the corresponding segmentation \( S \) obtained by an automatic algorithm to evaluate. The per-model Global Consistency Error of a model \( M \) regarding a certain segmentation algorithm is then:

\[ GCE_M = \frac{1}{n} \sum_i GCE_M(g_i, S) \]  

Where \( n \) is the number of ground-truth segmentations associated to the model \( M \).

Similarly, the per-model Local Consistency Error of a model \( M \) is:

\[ LCE_M = \frac{1}{n} \sum_i LCE_M(g_i, S) \]  

Given these two measures \( (GCE_M \text{ and } LCE_M) \), we define the Global Consistency Score (GCS) for the algorithm to evaluate, that takes into account the \( N \) models from the ground-truth:

\[ GCS = 1 - \left( \frac{1}{N} \sum_i GCE_M \right) \]  

And the Local Consistency Score (LCS):

\[ LCS = 1 - \left( \frac{1}{N} \sum_i LCE_M \right) \]  

Both of these Scores quantify the global similarity between the results of the segmentation algorithm to evaluate and the ground-truth rather than dissimilarity. Hence they quantify the quality of the segmentation algorithms. They lie in the range \([0, 1]\) with value of 1 indicating a perfect quality and a value of 0 indicating no correlation with the ground-truth.

### 5. Experiments

We begin this section by validating our objective measures using the ground-truth corpus, then we present two segmentation algorithms \([6], [11]\) and evaluate them using our whole evaluation protocol.

#### 5.1 Validation of segmentation dissimilarity measures

One way to attest the validity of our 3D segmentation dissimilarity measures, is to show that they provide low values when comparing ground-truth segmentations of a same object – namely \textit{consistent} segmentations – and high values when comparing \textit{random} segmentations of a same object. Hence we have compared the \( GCE_M \) and the \( LCE_M \) distributions between these two kinds of segmentation pairs, \textit{consistent} and \textit{random}.

For each model of the corpus, two random segmentations were generated by a simple and automatic algorithm: \( n \) seed vertices were randomly chosen on the object, then \( n \) connected regions were obtained by a simple region growing mechanism. Figure 5 shows some 3D-models of the corpus on which the random segmentation algorithm was applied.

Figure 6 illustrates the \( GCE_M \) and the \( LCE_M \) distributions of each model of the corpus for both kinds of segmentation (\textit{consistent} and \textit{random}). To compute the \( GCE_M \) and the \( LCE_M \) for the \textit{consistent} segmentations and, in order to be in agreement with our definitions of the \( GCE_M \) and the \( LCE_M \), we considered the first ground-truth associated to a given model as an automatic segmentation. Similarly, for the \textit{random} segmentations,
we therefore considered, the first random segmentation as an automatic segmentation and the second one as a ground-truth segmentation.

Fig. 5. Random segmentations of some 3D-models of the corpus.

Fig. 6. Distributions of the $GCE_M$ (a) and the $LCE_M$ (b) for both segmentation pairs (consistent in red color and random in blue color) over all 3D-models corpus (20 3D-models).

We can notice that for the $GCE_M$ (figure 6(a)), the distances between consistent segmentations are close to zero. However, the random segmentation distances are localized around 0.4. Thus the error between segmentations produced by volunteers for a same 3D-model is significatively lower than the ones obtained between random segmentations. More precisely, the $GCE_M$ mean for the consistent segmentations is 0.081 against 0.43 for the random segmentations. These results clearly validate the accuracy of the GCE measure for assessing segmentation dissimilarity, since they provide results agreeing with the human opinion (the ground-truth). However, figure 6(b) shows that the LCE measure fails to distinguish clearly between random and consistent segmentations as some models share the same values of $LCE_M$ for both types (consistent and random).

5.2 Evaluation of two segmentation algorithms

We apply here the quality metrics defined in section 4 to evaluate two recent segmentation algorithms [6], [11] of the state-of-the-art.

Tierny et al. [11] have proposed a part-type hierarchical segmentation method based on the extraction of an enhanced topological skeleton. Globally, the skeleton is used to delimit the object core and to identify the junction surfaces. The result of this operation is a coarse segmentation which is refined following a hierarchical scheme defined with regard to the topology of the model.

In figure 7(a), each node of the skeleton denotes a segment of the mesh. Each segment is distinguished by a color resulting in an over-segmentation of the object (figure 7(b)). A region merging algorithm based on the notions of core and junction areas is then applied to provide a hierarchical segmentation as illustrated in figure 7(c, d).

Fig. 7. Hierarchical segmentation process proposed by Tierny et al. [11]: original skeleton graph (a), over-segmentation (b), coarse segmentation (c) and fine segmentation (d) (from [11]).

Lavoué et al. [6] have rather proposed a surface-type segmentation method using a region growing algorithm. The curvature is first calculated for all vertices of the mesh, and classified into several clusters. A region growing mechanism then extracts connected regions (associated with similar curvature), starting from several seed-facets. Figure 8 illustrates some typical examples of results from this algorithm which is rather dedicated to CAD models.

To ensure a relevant comparison between these algorithms, we compute the $GCE_M$ and the $LCE_M$ for every 3D-model of the corpus and each segmentation algorithm, and then their GCS and LCS.

The first experiment for the evaluation of the algorithms is illustrated in figure 9 that shows the $GCE_M$
and the $LCE_M$ for each model of the corpus for each algorithm and also for random segmentations. The values are sorted in increasing order for each algorithm, hence the $j^{th}$ model may not be the same across algorithms. This kind of graph was already applied for segmentation evaluation in the field of 2D-image [13].

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|c|}
\hline
\textbf{Class} & \textbf{Tierny, coarse} & \textbf{Tierny, fine} & \textbf{Lavoué} & \textbf{Random} \\
\hline
Animal & 0.80 & 0.79 & 0.76 & 0.60 \\
Human & 0.82 & 0.75 & 0.75 & 0.60 \\
Furniture & 0.89 & 0.88 & 0.88 & 0.59 \\
Few-vertices & 0.86 & 0.85 & 0.83 & 0.50 \\
Hand & 0.81 & 0.80 & 0.75 & 0.53 \\
\hline
\end{tabular}
\caption{Summary of the per-class GCS of each algorithm.}
\end{table}

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|c|c|}
\hline
\textbf{Class} & \textbf{Tierny, coarse} & \textbf{Tierny, fine} & \textbf{Lavoué} & \textbf{Random} \\
\hline
Animal & 0.85 & 0.84 & 0.84 & 0.69 \\
Human & 0.86 & 0.84 & 0.87 & 0.69 \\
Furniture & 0.92 & 0.92 & 0.93 & 0.69 \\
Few-vertices & 0.88 & 0.89 & 0.86 & 0.62 \\
Hand & 0.87 & 0.86 & 0.83 & 0.67 \\
\hline
\end{tabular}
\caption{Summary of the per-class LCS of each algorithm.}
\end{table}

\begin{table}[h]
\centering
\begin{tabular}{|c|c|c|}
\hline
\textbf{Algorithm} & \textbf{GCS} & \textbf{LCS} \\
\hline
Tierny [11], coarse & 0.83 & 0.88 \\
Tierny [11], fine & 0.81 & 0.87 \\
Lavoué [6] & 0.79 & 0.87 \\
Random & 0.57 & 0.68 \\
\hline
\end{tabular}
\caption{Summary of the global GCS and LCS.}
\end{table}

To explain the difference between Tierny et al. [11] and Lavoué et al. [6] algorithms, we present in figure 10 two models of the corpus with their segmentations obtained by both algorithms and one of their associated ground-truth.

From a global point of view, the obtained segmentations are correct for both algorithms since they basically follow the ground-truth. However, it is clear that if we take into account the detail of each segment and the continuity of its boundaries, then Tierny et al. [11] algorithm gives the best segmentation for the hand model while Lavoué et al. [6] algorithm is better for the table model. This segmentation difference is straight since the algorithms belong to different segmentation classes: part-type for Tierny and surface-type for Lavoué. It is interesting to observe that this class difference appears on the per-class GCS results (see table 1): segmentation
results from Lavoué et al. [6] algorithm are very good for the furniture and few-vertices classes which contain mechanical or non-organic pieces which are rather segmented in a geometric manner (i.e. surface-type) by the human observers. On the other hand, results from Tierny et al. [11] algorithm are significatively better for human, hand and animal classes which are rather segmented in a semantic way by the observers.

6. CONCLUSION AND FUTURE WORK

In this paper, we presented a fully automatic protocol for the quantitative evaluation of 3D-mesh segmentation algorithms. The protocol is based on a ground-truth corpus, allowing an objective evaluation. We made the following contributions: (1) We built a ground-truth corpus available on-line. This corpus is composed of a set of 3D-models associated with several manual segmentations produced by human observers. (2) We proposed two measures that quantify the consistency between two segmentations of a 3D-model. These measures are based on the computing of the refinement error of a vertex between two segments containing this vertex, similarly to the work of Martin et al. [10] for 2D segmentation evaluation. (3) Based on these measures and on the ground-truth corpus, we proposed an objective score that reflects the global quality of an automatic segmentation algorithm.

To demonstrate the usability of this evaluation framework, we performed a detailed comparison between two recent segmentation algorithms: Tierny et al. [11] algorithm and Lavoué et al. [6] algorithm.

Currently, we are still working on the enlargement of the corpus in terms of number of models and ground-truth. We also plan to integrate the results of other segmentation algorithms applied to this corpus to offer a wealthier comparison and a more relevant analysis. Our objective is that the corpus and the evaluation methods become a valuable tool for the scientific community.

We also would like to define new measures according to the family of shapes (CAD-CAM shapes or natural shapes) and for a given application context such as segmenting for partial indexing for instance. Moreover, an interesting property that such measures would possess is the robustness to surface sampling in order to allow a valid comparison between segmentations of a same object with different sampling.

An other interesting point will be to integrate the user’s opinion to judge which segmentation is the best, then compare this subjective evaluation of the observer to our evaluation protocol.

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