Atomic force microscopy-based single-cell indentation: Experimentation and finite element simulation
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Abstract—In order to understand and characterize the mechanical property and response of the mouse embryonic stem cells (mESC), we used the atomic force microscope (AFM) combined with the a PHANToM haptic feedback device. Atomic force microscopy has rapidly become a valuable tool for quantifying the biophysical properties of single cells or a collection of cells through force measurements. We report herein the mechanical characterization of single mESC indentation-relaxation measurements using micro-sphere AFM probes for fixed and live undifferentiated mESC. During cell indentation for both live cells and fixed cells undifferentiated, we provided force feedback to the user in real-time through the PHANToM haptic feedback device as the AFM tip was deforming the cell. The interface allowed the user to feel the cell indentation force in real time. The force was amplified for the human operator to perceive the change in force during cell indentation by the AFM cantilever. This information can be used as a mechanical marker to characterize state of the cell(live and fixed). As the interpretation of atomic force microscopy-based indentation tests is highly dependent on the use of an appropriate theoretical model of the testing configuration, a variety of contact models are presented to predict the mechanical behavior of an individual mouse embryonic stem cell (mESC) in different states. A comparison study with finite element simulations (FEM) of spherical tip indentation demonstrates the effectiveness of our computational model to predict the mESC deformation during indentation and relaxation nanomanipulation tasks.

I. INTRODUCTION

The realization of promising potential of stem cells for engineering bone, cartilage, muscle and other connective tissues requires a proper characterization of their unique biological, biochemical, proteomic, and biomechanical properties that are yet to be fully elucidated. The mechanical properties such as elasticity, membrane tension, cell shape, and adhesion strength may play an important role in the cell fate and differentiation [1],[2],[3]. The mechanical properties of biological cells have been studied with different techniques [4], the most popular are optical tweezers [5], magnetic beads [6], and micropipette aspiration [7]. However, those methods cannot compete with the precision that can be attained with Atomic force microscopy (AFM) method [8]. AFM has been widely used in the study of micro- and nanostructures including living cells. Modern AFM techniques allow solving a number of problems of cell biomechanics by simultaneous evaluation of the local mechanical properties and the topography of the living cells, at a high spatial resolution and force sensitivity [9]. In these experiments AFM cantilever serves as a microindenter to probe the cell, and further analysis of force-indentation data yields the local Young’s modulus. In addition, AFM indentation technique can be used to characterize the viscoelastic behavior of the cell cytoskeleton [10], including viscosity [11], loss and storage moduli [12], and stress relaxation times. AFM-based indentation techniques with force feedback have been applied here to characterize single-cell mouse embryonic stem cells (mESCs) [13]. We report herein the mechanical characterization of single mESC indentation-relaxation for different colonies of fixed and live undifferentiated mESCs. The proposed indentation tests use microsphere-modified AFM probes in order to estimate global elastic modulus for the cell to reflect the true global response of a mESCs [14], [15]. Distribution of the indenting load over several \( \mu \text{m}^2 \) area, averages the contribution of multiple cytoskeleton fibers and makes the contact analysis more accurate. Indeed, the use of \( 5 \mu \text{m} \) diameter spherical indenter allows to reduce experimental elastic data dispersion several-fold compared to regular pyramidal sharp SiNi AFM tips [16], [17]. As the interpretation of AFM-based indentation tests is highly dependent on the use of an appropriate theoretical model of the testing configuration, our results demonstrate the applicability of the Hertz contact model as the most appropriate model compared to the capsule model or the JKR and DMT models. We have used the Hertzian contact model for the spherical tip indenter to compute the Young’s modulus of the cells(live and fixed). We have demonstrated that even if the two dimensional mechanical models of mESCs are suitable...
for analytical studies, it gives a valuable understanding of the
principles governing mechanical interactions within a cell.
A numerical validation study of the Hertzian contact model
has been conducted through a realistic two-dimensional finite
element modeling (FEM). The numerical model is based
on viscoelastic approximation with large deformations of
cellular soft matter with material properties statically given
for the time span of cell micromanipulation. Finally, the FEM
simulations validate the mESC stress relaxation properties
(hysteresis was about 15-20 percent) indicating that energy
dissipation due to the material viscosity contribution is low
at this probe velocity and force measurements are dominated
by the cell elastic behavior. The proposed FEM model con-
stitutes a basis for simulation of micro/nano-injection tasks
using virtual haptic feedback model in tissue engineering
and cancer research [18]. The paper consists of five sections. In
Section II, we present the materials and methods used in
our work. In Section III, we present the results of mouse
embryonic stem cells characterization. In Section IV, we
made a comparative study between the different analytical
and numerical models. Finally, in Section V, we make some
concluding remarks and give the direction for future work.

**II. EXPERIMENTAL SETUP**

**A. Description**

The nanoindentation of the cells was performed using the
Atomic Force Microscope (Model: MFP-3D-BIO, Asylum
Research, Santa Barbara, CA) combined with PHANTom
haptic feedback device (Sensable Technologies, Inc.). The
AFM is integrated with a top view module and mounted on
a active vibration isolation table manufactured by Herzan
(Laguna Hills, CA) as shown in Fig. 2. The top view
module enables viewing of cells and easy alignment of the
laser beam on the AFM cantilever. The XY stage (manual)
allows the user to position the cell beneath the cantilever
tip of AFM. The entire AFM set up is enclosed in an
acoustic isolation chamber to prevent acoustic noise from
interfering with the AFM measurements. The x- and y-axes
range of the scan head is $90\mu m$. The z-axis scan range is
$40\mu m$. The Atomic Force Microscopy (AFM) system is used
to obtain force and cell deformation data from biological
samples. The cantilever is moved by the piezoelectric scanner
in the z direction towards the cell. The deflection of the
cantilever is detected by a photodiode when the tip comes in
contact with the cell. The difference between the cantilever
movement $z$, and the cantilever deflection $d$, represents
the cell indentation $\delta = z - d$. The stiffness depends not only
on Young’s modulus but also on the geometry of the tip-
surface contact. Therefore, the geometry and spring constant
of the cantilever are calibrated in the same way for the live
and fixed cells (see Fig.3). In the following experiments,
we used a spherical tip (sphere diameter: $5\mu m$) with spring
constants $0.006N/m$ and $1.75N/m$ for the live and fixed cells
respectively (our experience, we found that the fixed cells
were stiffer compared to the live cells).

![Fig. 2. Atomic Force Microscopy: The experimental set up for mESC indentation studies.](image)

**B. AFM calibration**

Before any experiment is done, it is necessary to perform
the calibration of the cantilever to determine its resonant
frequency. The resonant frequency measurement enables the
user to determine it lies within the specified range provided
by the manufacturer. If it does not, then it helps to determine
if the tip has been damaged. The determination of spring
constant, $K$, is a two step process:

- Determine the slope of contact region from a force curve
to determine the sensitivity of the cantilever, and
- Measure the Thermal Power Spectral Density (PSD)
to determine the resonant frequency of the cantilever and
to confirm that the cantilever and light source are
aligned. This confirms that the system is functioning
properly. The results are plotted as the deflection ampli-
tude data using Fourier transform in m/sqrt(Hz) vs. the
frequency in Hz (see Fig. 4). The spring constant of the
cantilever was determined experimentally for each tip
used in our studies using the IGOR software interface
supplied by Asylum Research.

**III. MOUSE EMBRYONIC STEM CELLS
CHARACTERIZATION**

**A. Cell culture preparation**

It is recommended to use specially coated dishes or
slides to facilitate adhesion. Such Petri dishes or slides are
available commercially, cells should be attached to some
rigid substrate, usually either a slide or the bottom of a
Petri dish. In our study, the mouse embryonic stem cells
(mESC) R1 (SCRC-1011, American Type Culture Collection (ATCC), Manassas, VA) were grown on 0.1(percent) gelatin coated plates in the absence of feeder cells. The ES medium consisted of 1000 U/ml leukemia inhibitory factor (LIF, ESGRO, Chemicon, Temecula, CA), 15(percent) fetal bovine serum (FBS)(Invitrogen), and basic medium that included Knockout Dulbecco’s modified Eagle’s medium (Invitrogen), 2 mM L-glutamine, 1x non-essential amino acids, and 0.1 mM mercaptoethanol. Differentiation was induced by removal of LIF from the medium. Prior to experiments, cells were dispersed using trypsin to obtain single cells and were plated on 60 mm tissue culture petri dish. Fixed mouse ES cells were obtained by treating the live mouse ES cells with 4 minutes and were stored in phosphate buffered saline (PBS).

B. Cantilever interaction with the surface

Prior to using the cantilever to measure the interaction force between the cell and the tip, it is important to observe the behavior of the cantilever, including instability and hysteresis resulting from adhesive forces. This measurement is called the Approach-Retract curve. Figure 5 represents the quantitative information of forces between the AFM probe tip and the sample as a function of the tip-sample distance.

C. Geometry of the cell

The cells were 10 and 15µm in diameter. The phase contrast module enabled imaging low contrast, transparent cells in fluid via an inverted microscope (Model: TE2000U, Nikon, Inc) as shown in figure 4.25. The cells were stained with Hoescht 33342 and were visualized by fluorescence microscopy (FM) as shown in figure (Fig.6). The three-dimensional geometry of mESC colony is visualized via the AFM contact mode imaging (Fig.8). The mESC colony size can be estimated through image analysis (ImagePro software from Asylum). To determine the cells height, two force indentation measurements are necessary, i.e, hard substrate and (ii) cell surface. First, initial height \( h_0 \) is measured by bringing the AFM tip in contact with the hard substrate and then bringing the AFM tip on the cell surface \( h_1 \). The cell’s height is the difference \( h = h_0 - h_1 \).

IV. MECHANICAL CHARACTERIZATION OF MESC: REVIEW OF ANALYTICAL MODELS

To estimate the mechanical properties of biological cells using the AFM, various analytical models can be used to estimate young’s modulus of mESC in live as well as fixed cells, we need to perform mechanical nanoindentation tests.

A. The Hertz contact

The Hertz contact model has been used extensively by the AFM community to quantify the mechanical property of biological samples using AFM [8],[9]. The Hertz contact model describes the simple case of elastic deformation of two perfectly homogeneous smooth surfaces touching under load. By collecting force-distance curves on a time scale where viscous contributions are small, the forces measured are dominated by the elastic properties. In our work, the geometry of the tip used for all experiments is spherical. The mechanical interaction between the spherical tip and mESC can be described by the Hertz contact model of two elastic bodies [20]. The model assumes that:

- The material properties of the tip and the cell are isotropic and homogeneous.
- The normal contact of the two bodies is adhesionless and frictionless.
- The contact geometry is assumed to be axisymmetric, smooth and continuous.

Furthermore, the theory has been experimentally shown to be valid at small deformations. The relationship between the indentation \( \delta \), and the loading force \( F \) is given by:

\[
F = \frac{4}{3} E^* R^{2/3} \delta^{2/3} \tag{1}
\]

where \( E^* \) is the combined modulus and the relative curvature of the tip and the cell respectively

\[
\frac{1}{E^*} = \frac{1 - \nu^2}{E} + \frac{1 - \nu'^2}{E'} \tag{2}
\]

\[
\frac{1}{R} = \frac{1}{R_1} + \frac{1}{R_2} \tag{3}
\]
where \((E, \nu, R_2)\) and \((E', \nu', R_1)\) represents the elastic modulus, Poisson’s ratio, and the radius of the cell and cantilever respectively. The elastic modulus of the silicon nitride cantilever (used for live cells) and silicon cantilever (used for fixed cells) were 222.22 GPa and 168.17 GPa respectively. The elastic modulus of the cells is in range of KPa [11]. Hence, our assumption that the tip used for probing is infinitely stiff compared to the cell and Hertz contact model is valid. Thus, Eq. 1 can be rewritten as:

\[
F = \frac{4E}{3(1-\nu^2)} R_1^2 \delta^2 
\]  

(4)

where \(E, \nu, h\) represent the elastic modulus, Poisson’s ration and the thickness of the capsule membrane respectively. \(R_0, R_s\) is the radius of the capsule and the spherical indenter respectively. \(\varepsilon\) is the relative deformation of the capsule given by \(\varepsilon = 1 - \frac{H}{2R_0}\) (\(H\) is the height of the capsule after indentation). The present model considers stretching as well as bending of the cell membrane, in our experiments the bending deformation term can be neglected for \(\varepsilon > 0.15\) [23].

C. JKR and DMT contact

The JKR and DMT contact models modify the Hertz theory by taken into account the adhesion between two elastic spheres. The model assumes that the adhesion force operates over a short distance within the contact region. According to this theory [25], contact radius \(a\), indentation \(\delta\) and pull-off force \(P_{off}\) are represented by the following equations:

\[
\begin{align*}
\alpha^3 &= \frac{3R}{4\pi E'} (F + 3\pi R_w) + \sqrt{6\pi R_w F + (3\pi R_w)^2} \\
\delta &= \frac{\alpha^2}{\pi} - \sqrt{\frac{2\pi w}{E'}} \\
P_{off} &= \frac{3}{\pi} R_w
\end{align*}
\]

(6)

The DMT theory assumes the adhesion force operates just outside the contact zone where the surfaces are small distance apart. According to the DMT model, contact radius \(a\), indentation \(\delta\) and pull-off force \(P_{off}\) are represented by the following equations:

\[
\begin{align*}
\alpha^3 &= \frac{3R}{4\pi E'} (F + 3\pi R_w + 2\pi R_w) \\
\delta &= \frac{\alpha^2}{\pi} \\
P_{off} &= \frac{3}{2\pi} R_w
\end{align*}
\]

(7)
D. Comparison between experimental data and analytical models

We performed single indentation studies with a spherical tip on 20 mESC; 10 fixed and 10 live cells with spherical tip. We evaluate and compare between the different analytical models to determine whether it appropriately predicts the force-indentation relationship of mESC. We also present the force (loading and unloading) versus time profiles and determine whether force of adhesion exists between the tip and the cells. The figures (Fig.11, Fig.14) show the force versus cell indentation for live and fixed undifferentiated mESC using the capsule and the Hertz model respectively with corresponding $R^2$ value. Based on the experimental data, we performed a least square fit on the data set and the corresponding $R^2$ value was found to be 0.91 and 0.98 for the fixed and live undifferentiated mESC respectively. The figures (Fig.13, Fig.16) present the force (loading and unloading) versus time of fixed and live undifferentiated mESC, in our experiments, we observed that the adhesion force exists for only one of live undifferentiated but does not exist for the fixed cells. This could be due to the wear of the spherical tip [25] as there are no adhesion forces. The equation(4) was used to determine the global elastic modulus of the mESC. The average elastic modulus was 17.87 KPa and 0.217 KPa for the fixed and live undiff respectively (see Fig.17). The standard deviation for both of them was 3.37 KPa and 0.05 KPa for the fixed and live undiff cells. Finally, for our experiments, we infer that Hertz model appropriately describes the mechanical behavior of the live and fixed undifferentiated mESC.

FEM simulations may help us to answer the unsolved question: in which indentation range can we use the Hertz model to determine the cell global equivalent Young modulus since the Hertz theory was shown to be valid at small deformations?

V. FINITE ELEMENT MODEL (FEM) SIMULATION OF CELL INDENTATION RESULTS

A. Finite Element Simulations of spherical tip indentation for live and fixed mESC

The Fig.18 presents our approach for deducing the Young’s modulus from spherical-indentation tests. In a first time, the geometrical characteristics and the mechanical properties for different cells are determined with AFM indentation and analytical Hertz contact model. These properties are injected in the finite element simulation. The indentation depth versus force indentation are measured using the AFM.
and compared to the FEM predicted results. The finite element simulations are performed using an industrial research and development finite element code Cast3M. The FE model of the mESC is based on the following hypothesis:

- The mechanical problem is axisymmetric.
- The spherical tip is undeformable.
- The cell is supposed to have homogeneous, isotropic (visco)hyperelastic and nearly incompressible material properties.

The assumption of homogeneity, which may seem to be wrong, implies that we study a global equivalent elastic model of the cell. Furthermore, as already mentioned, the microsphere AFM-indentation test averages the contribution of multiple cytoskeleton fibres and smoothes the area contact geometry as needed for the use of the Hertz contact model. We used the Saint-Venant Kirchhoff hyperelastic model for which the elastic potential is given by:

\[ W(E) = \frac{\lambda}{2} (tr E)^2 + \mu (tr E^2) \]  

(8)

Since the strain energy function \( W \) is quadratic in terms of strain invariants, we obtain a linear relation between the second Piola-Kirchhoff stress tensor and the Green-Lagrange strain tensor and it is given by:

\[ S = \lambda (tr E) I + 2 \mu E \quad \text{or} \quad S_{ij} = \lambda E_{kk} \delta_{ij} + 2 \mu E_{ij} \]  

(9)

The Saint-Venant Kirchhoff law extends the Hooke’s law for large deformations. The main difference is that the stress field, which was a linear function of the gradient of the displacement field \( \text{grad} U \), is now a quadratic function of \( \text{grad} U \). Since a rate sensitivity effect and hysteresis may be observed in the force vs. indentation loading-unloading curves, a first attempt was made to describe this viscoelastic dissipative behavior with a classical Kelvin-Voigt viscoelastic model.

The relation between the second Piola-Kirchhoff stress tensor, the Green-Lagrange strain tensor and the the rate effect leads to:

\[ S = (\lambda (tr E) I + 2 \mu E) + \eta \left( \lambda (tr \dot{E}) I + 2 \mu \dot{E} \right) \]

\[ S_{ij} = (\lambda E_{kk} \delta_{ij} + 2 \mu E_{ij}) + \eta \left( \lambda \dot{E}_{kk} \delta_{ij} + 2 \mu \dot{E}_{ij} \right) \]  

(10)

<table>
<thead>
<tr>
<th>Mechanical and geometrical properties used in the FEM</th>
<th>Fixed Undiff</th>
<th>Live Undiff</th>
</tr>
</thead>
<tbody>
<tr>
<td>Diameter of the cell((\mu m))</td>
<td>12</td>
<td>10</td>
</tr>
<tr>
<td>height of the cell((\mu m))</td>
<td>8</td>
<td>7.2</td>
</tr>
<tr>
<td>Elastic modulus (KPa)</td>
<td>23.3</td>
<td>26.7</td>
</tr>
<tr>
<td>Indentation range ((\mu m))</td>
<td>2</td>
<td>0.5</td>
</tr>
<tr>
<td>Poisson ratio</td>
<td>0.49</td>
<td>0.49</td>
</tr>
<tr>
<td>Diameter of the Tip((\mu m))</td>
<td>5</td>
<td>5</td>
</tr>
</tbody>
</table>

The geometrical characteristics were obtained from experimental data, namely the diameter and height of the cell(Tab.I). The main difficulty of identifying material properties from the non linear force-displacement curve is that this geometrical non-linearity can come from both large strains and contact non-linearities. Indeed, the cells are indented \( \approx 2 \mu m \) which is not infinitesimal compared to the height of the cells \( \approx 8 \mu m \). If the non-linearity is attributed only to the contact geometry, the Young’s modulus values deduced from the classical Hertz equations may be unreliable[26]. A classical solution, but computationally very expensive, is to perform an inverse finite element solution to determine the optimum values of (visco)hyperelastic material properties. We chose a different strategy, computationally more efficient: we limited the fitting to data points that do not exceed 0.5\( \mu m \) (\( \approx 5\% \) of relative nominal strain). The viscosity coefficient was roughly estimated by successive simulations.

Numerical FEM used two structure meshing; first the coarse mesh size composed of 398 nodes and 724 triangles and second with 1628 nodes and 3108 triangles(Fig.20). The results of mESC deformations are visualized in (Fig.21) and (Fig.22) for a fixed mESC. The FEM analysis shows that moderate to large deformations are observed around the contact region (\( \approx 20\% \) for 0.34\( \mu m \) and \( \approx 40\% \) for 1\( \mu m \)). As a validation, the Hertz contact model and FEM simulations have been compared with force-displacement curves obtained from AFM indentation experiments on both undifferentiated fixed (Fig.24) and live undifferentiated (Fig.23) single mESC. These comparisons show clearly that the Hertz contact model cannot be used for the whole indentation range:

- if the Young modulus is deduced from the full datasets, the finite element simulation show good agreement to experimental results but only until moderate deformations (\( <\approx 10\% \)).
- if the Young modulus is deduced from a truncated dataset, the finite element simulation show good agree-

---

1 The FE code Cast3M is developed by the Department of Mechanics and Technology (DMT) of the French Atomic Energy Agency (CEA - DEN/DM2S/SEMT).
ment to experimental results for the whole simulation and differ significantly from Hertz contact model for large deformations ($>10\%$).

Finally, hysteresis was quantified experimentally and numerically by subtracting the area under indentation and retraction curves, which represents the viscous dissipation of energy into the cell. The FEM simulations and experimental data are shown in Fig.25. Calculated in this manner, hysteresis was about 15-20 percent, indicating that energy dissipation due to the material viscosity contribution is low at this probe velocity and force measurements are dominated by the cell elastic behavior.

\begin{equation}
F = K d
\end{equation}

Where $K$ is the spring constant of the cantilever and $d$ the cantilever deflection. Thus, our haptics-enabled AFM system obtains the relationship between the force exerted on the cell and the corresponding deformation. The force detected by the AFM during cell contact is acquired by a data acquisition board in real-time (model: dSPACE DS1103). The interface allowed the user to feel the cell indentation force in real time. The force was amplified by a factor of $10^7$ for the human operator to perceive the change in force during cell indentation by the AFM cantilever between the fixed and live cells. This tool can be used as a mechanical marker to characterize the biological state of the cell. The haptic feedback was rendered in real time to the operator during cell indentation by the AFM tip. The operator was able to feel the change in the stiffness during cell deformation between the fixed and live cells.

\section*{C. Analysis and Discussion}

Despite variations between cells of the same population, the experimental data show that fixed cells are more stiffer than live cells ($10^2$ to $10^3$ magnitude of order). Nevertheless, fixed and live mESC present common mechanical nonlinear responses. The finite element simulations show good agreement with both Hertz contact model and experimental indentation for low to moderate deformations (around 10\% of relative nominal strain (see Fig.22, Fig.23). Furthermore, as expected, the finite element simulations show perfect adequation with Hertz contact model for low deformation. The differences between our experimental results and nu-
Numerical simulations for large deformations can be explained by the fact that Hertz contact model is only valid for small deformations ([21], [22]). A first attempt has been made to approach observed experimental hysteresis with a simple Kelvin-Voigt model. Preliminary simulations show quantitatively good agreement with experimental data (Fig. 24).

VI. CONCLUSIONS AND FUTURE WORK

Atomic force microscopy has rapidly become a valuable tool for quantifying the biophysical properties of single cells. We have presented the mechanical characterization of single mESC indentation-relaxation studies using microsphere-modified AFM probes for different fixed and live undifferentiated mESCs. As the interpretation of atomic force microscopy-based indentation tests is highly dependent on the use of an appropriate contact model, we have used Hertz contact model based on our recent work on analyzing the various contact models appropriate for the AFM tip and mESC interaction. Finite element simulations (FEM) of spherical tip indentation proves the effectiveness of computational model to predict the mESC deformation behavior during mESC indentation and relaxation tests. As a perspective, the proposed FEM model constitutes a basis for simulation of nanoinjection tasks using virtual haptic feedback model for tissue engineering applications and development of new therapies for regenerative medicine. In our ongoing and future work, we are developing a real-time force-feedback simulator dedicated to AFM indentation for various living cells. To achieve these goals, the proposed finite element model (FEM) takes into account the nonlinear elasticity cell model, the geometry and properties of AFM-tip indenters (spherical and pyramidal probes).

REFERENCES