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► To cite this version:

Thierry Bouwmans. Recent Advanced Statistical Background Modeling for Foreground Detection - A Systematic Survey. Recent Patents on Computer Science, 2011, 4 (3), pp.147-176. hal-00644746

HAL Id: hal-00644746

<https://hal.science/hal-00644746>

Submitted on 19 Nov 2015

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Recent Advanced Statistical Background Modeling for Foreground Detection - A Systematic Survey

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Short Running Title: Advanced Background Modeling: A Systematic Survey

Abstract: Background modeling is currently used to detect moving objects in video acquired from static cameras. Numerous statistical methods have been developed over the recent years. The aim of this paper is firstly to provide an extended and updated survey of the recent researches and patents which concern statistical background modeling and secondly to achieve a comparative evaluation. For this, we firstly classified the statistical methods in term of category. Then, the original methods are reminded and discussed following the challenges met in video sequences. We classified their respective improvements in term of strategies used. Furthermore, we discussed them in term of the critical situations they claim to handle. Finally, we conclude with several promising directions for future research. The survey also discussed relevant patents.

Keywords: Background modeling, Kernel Density Estimation, Mixture of Gaussians, Single Gaussian, Subspace Learning

1. INTRODUCTION

Different applications such as video surveillance [1], optical motion capture [2-4] and multimedia [5-7] need firstly to model the background and then to detect the moving objects. One way to obtain the background is to acquire a background image which doesn't include any moving object but in some environment the background is not available. Furthermore, it can always be changed under critical situations like illumination changes, objects being introduced or removed from the scene. To take into account these problems, many background modeling methods have been developed [8, 9] and these methods can be classified in the following categories:

- **Basic Background Modeling:** In this case, the background is modeled using the average [10] or the median [11] or the histogram analysis over time [12].
- **Statistical Background Modeling:** The background is modeled using a single Gaussian [13] or a Mixture of Gaussians [14] or a Kernel Density Estimation [15]. Statistical variables are used to classify the pixels as foreground or background.
- **Fuzzy Background Modeling:** The background is modeled using a fuzzy running average [16] or Type-2 fuzzy mixture of Gaussians [17]. Foreground detection is made using the Sugeno integral [18] or the Choquet integral [19]. The foreground detection can be performed by fuzzy inferences [335].

- **Background Clustering:** The background model supposes that each pixel in the frame can be represented temporally by clusters. Incoming pixels are matched against the corresponding cluster group and are classified according to whether the matching cluster is considered part of the background. The clustering approach consists in using K-mean algorithm [361] or using Codebook [362].
- **Neural Network Background Modeling:** The background is represented by mean of the weights of a neural network suitably trained on N clean frames. The network learns how to classify each pixel as background or foreground [332][333].
- **Wavelet Background Modeling:** The background model is defined in the temporal domain, utilizing the coefficients of discrete wavelet transform (DWT) [336].
- **Background Estimation:** The background is estimated using a filter. Any pixel of the current image that deviates significantly from its predicted value is declared foreground. This filter may be a Wiener filter [20], a Kalman filter [21] or a Tchebychev filter [22].

Table 1 shows an overview of this classification. The first column indicates the category and the second column the name of each method. The number of papers counted for each method is indicated in the parenthesis. The third column gives the name of the authors who have made the main publication for the corresponding method and the date of the related publication. Other classifications can be found in term of prediction [23], recursion [1], adaptation [24], or modality [25].

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Table 1. Background Modeling Methods: An Overview

Category	Methods	Authors - Dates
Basic Background Modeling	Mean (11) Median (13) Histogram over time (13)	Lee <i>et al.</i> (2002) [10] Mac Farlane <i>et al.</i> (1995) [11] Zheng <i>et al.</i> (2006) [12]
Statistical Background Modeling	Single Gaussian (33) Mixture of Gaussians (217) Kernel Density Estimation (5)	Wren <i>et al.</i> (1997) [13] Stauffer and Grimson (1999) [14] Elgammal <i>et al.</i> (2000) [15]
Fuzzy Background Modeling	Fuzzy Running Average (5) Type-2 Fuzzy Mixture of Gaussians (3)	Sigari <i>et al.</i> (2008) [16] El Baf <i>et al.</i> (2008) [17]
Background Clustering	K-Means (11) Codebook (35)	Butler <i>et al.</i> (2003) [361] Kim <i>et al.</i> (2005) [362]
Neural Network Background Modeling	General Regression Neural Network (1) Self Organizing Neural Network (9)	Culibrk <i>et al.</i> (2006) [332] Maddalena and Petrosino (2007) [333]
Wavelet Background Modeling	Discrete Wavelet Transform	Biswas <i>et al.</i> [336]
Background Estimation	Wiener Filter (1) Kalman Filter (19) Tchebychev Filter (3)	Toyama <i>et al.</i> (1999) [20] Messelodi <i>et al.</i> (2005) [21] Chang <i>et al.</i> (2004) [22]

All these modeling approaches are used in background subtraction context which presents the following steps and issues: background modeling, background initialization, background maintenance, foreground detection, choice of the feature size (pixel, a block or a cluster), choice of the feature type (color features, edge features, stereo features, motion features and texture features). Developing a background subtraction method, all these choices determine the robustness of the method to the critical situations met in video sequence [5, 20]: Noise image due to a poor quality image source (NI), Camera jitter (CJ), Camera automatic adjustments (CA), Time of the day (TD), Light switch (LS), Bootstrapping (B), Camouflage (C), Foreground aperture (FA), Moved background objects (MO), Inserted background (IB), Waking foreground object (WFO), Sleeping foreground object (SFO) and Shadows (S). The main difficulties come from the dynamic backgrounds and illumination changes:

- **Dynamic backgrounds** often appear in outdoor scenes. Fig. (1). presents four typical examples: Camera jitter, waving trees, water rippling and water surface. The left column shows the original images and the right the foreground mask obtained by the MOG [14]. In each case, there is a big amount of false detections.
- **Illumination changes** appear in indoor and outdoor scenes. Fig. (2). shows an indoor scene in which we can observe a gradual illumination change. This causes false detections in several parts of the foreground mask obtained by the MOG [14]. Fig. (3). illustrates the case of sudden illumination change due to a light on/off. Every pixel in the images is affected by this change which generates a large amount of false detections (see Fig. 3c).

Fig. (1). The first column presents original scenes containing dynamic backgrounds. The second column shows the foreground masks obtained by the MOG [14].



a) Sequence Camera jitter from [229]



b) Sequence Campus from [34]



c) Sequence Water rippling from [34]

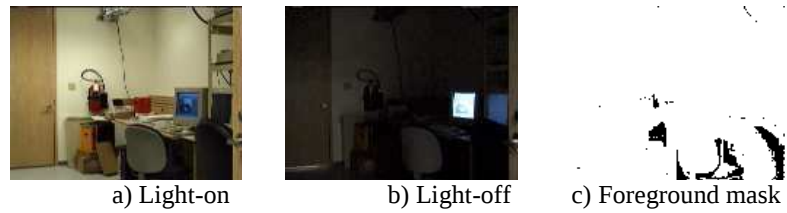


d) Sequence Water surface from [34]

Fig. (2). From left to right: The first image presents an indoor scene with low illumination. The second image presents the same scene with a moderate illumination while the third image shows the scene with a high illumination. The fourth image shows the foreground mask obtained with MOG [14]. This sequence called “Time of Day” comes from the Wallflower dataset [20].



Fig. (3). From left to right: The first image presents an indoor scene with light-on. The second image shows the same scene with light-off. The third image shows the foreground mask obtained with MOG [14]. This sequence called “Light Switch” comes from the Wallflower dataset [20].



Different datasets benchmarks are available [26-31] to evaluate the robustness of the background subtraction methods against these critical situations which have different spatial and temporal characteristics which must be taken into account to obtain a good segmentation. This challenge must be made in the context of real-time application which runs on common PC and so two constraints are introduced: less computation time (CT) and less memory requirement (MR) as possible. The performance is evaluated using the ROC analysis [32] or the PDR Analysis [33] or the similarity measure [34]. Others performance evaluation methods are proposed and compared in [35, 36]. Reading the literature, two main remarks can be made: (1) The most frequently used models are the statistical ones due to their robustness to the critical situations. (2) There are many recent developments regarding statistical models as can be seen for the MOG model with the acronyms found like GMM [37], TLGMM [38], STGMM [39], SKMGM [40], TAPPMOG [41] and S-TAPPMOG [42]. The objective is then to categorize the statistical models in one paper and classify their recent improvements following the strategies used. We also discuss them following the challenges met in video sequences and evaluate some of them in terms of false alarms using the Wallflower dataset [20].

This paper is an extended and updated paper of the surveys on Mixture of Gaussians for background modeling [48] and Subspace Learning for background modeling [334].

The rest of this paper is organized as follows: In Section 2, we firstly provide a background on the statistical background models and a classification of these models. In Section 3, we survey the first generation models and their respective improvements. In Section 4, we classified the second generation models. In Section 5, the third generation models are reviewed. In Section 6, we firstly investigated the performance in terms of robustness on dynamic backgrounds

and illumination changes and secondly in terms of per-pixel complexity. Then, a comparative evaluation is provided in Section 7. Finally, conclusion and future developments are given.

2. STATISTICAL BACKGROUND MODELING: AN OVERVIEW

The statistical tools provide a good framework to model the background and so many methods have been developed. We classified them in terms of category as follows:

- **First category:** The first way to represent statistically the background is to assume that the history over time of intensity values of a pixel can be modeled by a single Gaussian (SG) [13]. However, a unimodal model cannot handle dynamic backgrounds when there are waving trees, water rippling or moving algae. To solve this problem, the Mixture of Gaussians (MOG) has been used to model dynamic backgrounds [14]. This model has some disadvantages. Background having fast variations cannot be accurately modeled with just a few Gaussians (usually 3 to 5), causing problems for sensitive detection. So, a non-parametric technique was developed for estimating background probabilities at each pixel from many recent samples over time using Kernel density estimation (KDE) [15] but it is time consuming. In [165], Subspace Learning using Principal Component Analysis (SL-PCA) is applied on N images to construct a background model, which is represented by the mean image and the projection matrix comprising the first p significant eigenvectors of PCA. In this way, foreground segmentation is accomplished by computing the difference between the input image and its reconstruction.

Table 2. Advanced Statistical Background Modeling: An Overview

Category	Methods	Authors - Dates
First Category	Single Gaussian (SG) (33) Mixture of Gaussians (MOG) (217) Kernel Density Estimation (KDE) (55) Principal Components Analysis (SL-PCA) (25)	Wren <i>et al.</i> (1997) [13] Stauffer and Grimson (1999) [14] Elgammal <i>et al.</i> (2000) [15] Oliver <i>et al.</i> (1999) [165]
Second Category	Support Vector Machine (SVM) (9) Support Vector Regression (SVR) (3) Support Vector Data Description (SVDD) (6)	Lin <i>et al.</i> (2002) [180] Wang <i>et al.</i> (2006) [183] Tavakkoli <i>et al.</i> (2006) [186]
Third Category	Single General Gaussian (SGG) (3) Mixture of General Gaussians (MOGG) (3) Independent Component Analysis (SL-ICA) (3) Incremental Non Negative Matrix Factorization (SL-INMF) (3) Incremental Rank-(R_1, R_2, R_3) Tensor (SL-IRT) (2)	Kim <i>et al.</i> (2007) [190] Allili <i>et al.</i> (2007) [194] Yamazaki <i>et al.</i> (2006) [198] Bucak <i>et al.</i> (2007) [202] Li <i>et al.</i> (2008) [204]

- **Second category:** This second category uses support vector models. The objective is different following the models used. Lin *et al.* [180] used a SVM algorithm to initialize the background in outdoor scene. Wang *et al.* [183, 184] modeled the background by using SVR in the case of traffic surveillance scene where illumination changes (TD) appear. Tavakkoli *et al.* [186-189] applied SVDD to deal with dynamic backgrounds (MB).
- **Third category:** These models generalize the first generation model as the single general Gaussian (SGG) [190-192], the mixture of general Gaussians (MOGG) [193-195] and subspace learning using Independent Component Analysis (SL-ICA) [198, 200], Incremental Non-negative Matrix Factorization (SL-INMF) [202, 203] or Incremental Rank-(R_1, R_2, R_3) Tensor (SL-IRT) [204, 205]. The single general Gaussian (SGG) alleviates the constraint of a strict Gaussian and then shows better performance in the case of illumination changes (TD) and shadow (S). The MOGG have been developed to be more robust to dynamic backgrounds (MB). Subspace learning methods are more robust to illumination changes (LS).

Table 2 shows an overview of the statistical background modeling. The first column indicates the generation and the second column the name of each method. Their corresponding acronym is indicated in the first parenthesis and the number of papers counted for each method in the second parenthesis. The third column gives the name of the authors who have made the main publication for the corresponding method and the date of the related publication. We can see that the MOG with 217 papers is the most modified and improved because it is the most used due to a good compromise between robustness.

In the following sections, we remind the original methods for each generation and we have classify their related improvements in the following way: intrinsic improvements which concern the modification made in the initialization, the maintenance and the foreground detection steps, and

extrinsic improvements which consist in using external tools to perform the results.

3. FIRST CATEGORY

3.1 Single Gaussian (SG)

Wren *et al.* [13] proposed to model the background independently at each pixel location (i, j). The model is based on ideally fitting a Gaussian probability density function on the last n pixel's values. In order to avoid fitting the pdf from scratch at each new frame time $t+1$, the mean and the variance are updated as follows:

$$\mu_{t+1} = (1 - \alpha)\mu_t + \alpha X_{t+1}$$

$$\sigma_{t+1}^2 = (1 - \alpha)\sigma_t^2 + \alpha(X_{t+1} - \mu_{t+1})(X_{t+1} - \mu_{t+1})^T$$

where X_{t+1} is the pixel's current value, μ_t is the previous average, σ_t is the previous variance and α is the learning rate. The foreground detection is made as follows:

if $|\mu_{t+1} - X_{t+1}| < T$, the pixel is classified as background otherwise the pixel is classified as foreground.

Improvements: Medioni *et al.* [43] operated in the Hue-Saturation-Value (HSV) color space instead of the RGB one. The advantage is that the HSV color model is more robust to gradual illumination changes (TD) because it separates the intensity and chromatic information. Furthermore, HSV permits to eliminate partially camouflage. Zhao *et al.* [44] used HSV too remarking that the respective distributions of H and S vary naturally a lot and that the distribution of V is the most stable. So, the component H and S are only used when they are stable. Results [44] show better performance in presence of gradual illumination changes (TD) and shadows (S).

Discussion: The single Gaussian (SG) is suited for indoor scenes where there are moderate illumination changes.

3.2 Mixture of Gaussians (MOG)

In the context of a traffic surveillance system, Friedman and Russel [45] proposed to model each background pixel using a mixture of three Gaussians corresponding to road, vehicle and shadows. This model is initialized using an EM algorithm. Then, the Gaussians are manually labeled in a heuristic manner as follows: the darkest component is labeled as shadow; in the remaining two components, the one with the largest variance is labeled as vehicle and the other one as road. This remains fixed for all the process giving lack of adaptation to changes over time. For the foreground detection, each pixel is compared with each Gaussian and is classified according to it corresponding Gaussian. The maintenance is made using an incremental EM algorithm for real time consideration. Stauffer and Grimson [14] generalized this idea by modeling the recent history of the color features of each pixel $\{X_1, \dots, X_t\}$ by a mixture of K Gaussians. We remind below the algorithm.

Principle

First, each pixel is characterized by its intensity in the RGB color space. Then, the probability of observing the current pixel value is considered given by the following formula in the multidimensional case:

$$P(X_t) = \sum_{i=1}^K \omega_{i,t} \cdot \eta(X_t, \mu_{i,t}, \Sigma_{i,t}) \quad (1)$$

where the parameters are K is the number of distributions, $\omega_{i,t}$ is a weight associated to the i^{th} Gaussian at time t with mean $\mu_{i,t}$ and standard deviation $\Sigma_{i,t}$. η is a Gaussian probability density function:

$$\eta(X_t, \mu, \Sigma) = \frac{1}{(2\pi)^{n/2} |\Sigma|^{1/2}} e^{-\frac{1}{2}(X_t - \mu)^T \Sigma^{-1} (X_t - \mu)} \quad (2)$$

For computational reasons, Stauffer and Grimson [14] assumed that the RGB color components are independent and have the same variances. So, the covariance matrix is of the form:

$$\Sigma_{i,t} = \sigma_{i,t}^2 I \quad (3)$$

So, each pixel is characterized by a mixture of K Gaussians. Once the background model is defined, the different parameters of the mixture of Gaussians must be initialized. The parameters of the MOG's model are the number of Gaussians K, the weight $\omega_{i,t}$ associated to the i^{th} Gaussian at time t, the mean $\mu_{i,t}$ and the covariance matrix $\Sigma_{i,t}$.

Remarks:

- K determined the multimodality of the background and by the available memory and computational power. Stauffer and Grimson [14] proposed to set K from 3 to 5.
- The initialization of the weight, the mean and the covariance matrix is made using an EM algorithm. Stauffer and Grimson [14] used the K-mean algorithm for real time consideration.

Once the parameters initialization is made, a first foreground detection can be made and then the parameters are updated. Firstly, Stauffer and Grimson [14] used as criterion the ratio $r_j = \omega_j / \sigma_j$ and ordered the K Gaussians following this ratio. This ordering supposes that a background pixel corresponds to a high weight with a weak variance due to the fact that the background is more present than moving objects and that its value is practically constant. The first B Gaussian distributions which exceed certain threshold T are retained for a background distribution:

$$B = \text{argmin}_b \left(\sum_{i=1}^b \omega_{i,t} > T \right) \quad (4)$$

The other distributions are considered to represent a foreground distribution. Then, when the new frame incomes at times t+1, a match test is made for each pixel. A pixel matches a Gaussian distribution if:

$$\text{sqr}t\left((X_{t+1} - \mu_{i,t})^T \cdot \Sigma_{i,t}^{-1} \cdot (X_{t+1} - \mu_{i,t})\right) < k \sigma_{i,t} \quad (5) \text{ where}$$

k is a constant threshold equal to 2.5. Then, two cases can occur:

- Case 1: A match is found with one of the K Gaussians. In this case, if the Gaussian distribution is identified as a background one, the pixel is classified as background else the pixel is classified as foreground.
- Case 2: No match is found with any of the K Gaussians. In this case, the pixel is classified as foreground.

At this step, a binary mask is obtained. Then, to make the next foreground detection, the parameters must be updated. Using the match test (5), two cases can occur like in the foreground detection:

Case 1: A match is found with one of the K Gaussians.

- For the matched component, the update is done as follows:

$$\omega_{i,t+1} = (1 - \alpha) \omega_{i,t} + \alpha \quad (6)$$

where α is a constant learning rate.

$$\mu_{i,t+1} = (1 - \rho) \mu_{i,t} + \rho X_{t+1} \quad (7)$$

$$\sigma_{i,t+1}^2 = (1-\rho)\sigma_{i,t}^2 + \rho(X_{t+1} - \mu_{i,t+1}).(X_{t+1} - \mu_{i,t+1})^T \quad (8)$$

where $\rho = \alpha\eta(X_{t+1}, \mu_i, \Sigma_i)$

- For the unmatched components, μ and Σ are unchanged, only the weight is replaced by:

$$\omega_{j,t+1} = (1-\alpha)\omega_{j,t} \quad (9)$$

Case 2: No match is found with any of the K Gaussians. In this case, the least probable distribution k is replaced with a new one with parameters:

$$\omega_{k,t+1} = \text{Low Prior Weight} \quad (10)$$

$$\mu_{k,t+1} = X_{t+1} \quad (11)$$

$$\sigma_{k,t+1}^2 = \text{Large Initial Variance} \quad (12)$$

Once the parameters maintenance is made, foreground detection can be made and so on. Complete studies on the signification and the setting of the parameters can be found in [46, 47][218][289].

Improvements: The original MOG presents several advantages. Indeed, it can work without having to store an important set of input data in the running process. The multimodality of the model allows dealing with multimodal backgrounds and gradual illumination changes. Despite it, this model present some disadvantages: the number of Gaussians must be predetermined, the need for good initializations, the dependence of the results on the true distribution law which can be non-Gaussian and slow recovery from failures. Others limitations are the needs for a series of training frames absent of moving objects and the amount of memory required in this step. To alleviate these limitations, numerous improvements (217 papers) have been proposed over the recent years. All the developed improvements can be classified following the strategies and a complete survey over 100 papers in the period 1999-2007 can be found in [48]. We have summarized and updated them in the following classification:

- **Intrinsic improvements:** These strategies (Table 3) consist to be more rigorous in the statistical sense or to introduce spatial and/or temporal constraint in the different step of the model. For example, some authors [49-53] propose to determine automatically and dynamically the number of Gaussians to be more robust to dynamic backgrounds. Other approaches use another algorithm for the initialization [54, 55] and allow presence of foreground objects in the training sequence [56, 57, 58]. For the maintenance, the learning rates are better set [66, 67] or adapt over time [60-62, 68-78]. For the foreground detection, the improvement found in the literature are made using a different measure for the matching test [53, 79-82], using a Pixel Persistence Map

(PPM) [75, 76, 83], using the probabilities [84, 85], using a foreground model [61, 63, 86], using some matching tests [39, 60] and using the most dominant background model [87, 88, 89]. For the feature size, block wise [90, 91] or cluster wise [92] approaches are more robust than the pixel one. For the feature type, several features are used instead of the RGB space like different color features [93-99], edge features [100, 101], texture features [102], stereo feature [103, 104], spatial features [105], motion features [40] and video features [106]. Zheng *et al.* [267, 268] combined multiple features such as brightness, chromaticity and neighborhood information. Recent patents concern block wise approaches [352], texture features [353], motion features [354] and spatial features [355]. An overview of the different features used in the literature is shown in Table 5.

- **Extrinsic improvements:** Another way to improve the efficiency and robustness of the original GMM consist in using external strategies (Table 4). Some authors used Markov Random Fields [107-109], hierarchical approaches [110-113], multi-level approaches [100, 114-118], multiple backgrounds [119, 121], graph cuts [81], multi-layer approaches [122, 123], tracking feedback [128, 129] or specific post-processing [130-131]. Recent patents concern graph cuts approaches [3576, 357].
- **Reducing the computation time:** All the intrinsic and extrinsic improvements concern the quality of the foreground detection but there is another manner to improve the original MOG which consists in reducing the computation time. It achieved by using region of interest [132] [287], by using a variable adaption rate [133], by switching the background model [134] [271], by using space sampling strategies [135][216][238][272] or by using hardware implementation [136, 137] [271].
- **Enhancing the foreground detection:** All the previous improvements concern directly the original MOG and the foreground detection results only from it. Another way to improve this method is to enhance the results of the foreground detection by using cooperation with another segmentation method. It achieved by cooperation with a statistical background disturbance technique [138], with color segmentation [139], and with a region based motion detection [140]. Other authors used a cooperation with optical flow [217], block matching [247-248], predictive models [249], texture models [251][303], consecutive frame difference [258][261-262][279-280][282] and basic background subtraction [304-305][330]. A recent patent concern the cooperation with histogram statistics [358].

Table 6 and Table 7 show respectively an overview of the critical situations and the real-time constraints for the different MOG versions that can tackle them better than the original one.

Table 3. Intrinsic improvements of the MOG

Background Step	Parameters	Authors - References
Background Initialization	Variable K	Zivkovic [49], Cheng <i>et al.</i> [50], Shimada <i>et al.</i> [51], Tan <i>et al.</i> [52], Carminati <i>et al.</i> [53], Klare and Sarka [230], Shimada <i>et al.</i> [237], Shahid <i>et al.</i> [240], Singh and Mitra [248], Wang <i>et al.</i> [278], Huang <i>et al.</i> [288], Wang <i>et al.</i> [307], Zhou <i>et al.</i> [317]
	Variables μ, σ, ω	<i>Another algorithm:</i> Morellas <i>et al.</i> [54], Lee [55], Ju <i>et al.</i> [241], Singh <i>et al.</i> [245], Singh <i>et al.</i> [246], Wang and Dai [252], Hu <i>et al.</i> [259], Guo <i>et al.</i> [270], Molin [285], Qin <i>et al.</i> [286], Li <i>et al.</i> [315], Wang and Miller [331] <i>Allowing presence of moving objects:</i> Zhang <i>et al.</i> [56], Amintoosi <i>et al.</i> [57], Lepisk [58], Lee <i>et al.</i> [273], Wang <i>et al.</i> [307]
Background Maintenance	Variable K	Zivkovic [49], Cheng <i>et al.</i> [50], Shimada <i>et al.</i> [51], Tan <i>et al.</i> [52], Klare and Sarka [230], Shimada <i>et al.</i> [237], Singh and Mitra [248], Wang <i>et al.</i> [278], Zhou <i>et al.</i> [317]
	Variables μ, σ, ω	<i>Maintenance rules:</i> Han and Li [59], Park and Buyn [266] <i>Maintenance mechanisms:</i> Zhang <i>et al.</i> [56], Wang and Suter [60], Lindstrom <i>et al.</i> [61], Li <i>et al.</i> [269], Lee <i>et al.</i> [273] <i>Selective maintenance:</i> Stauffer and Grimson [62], Landabaso and Pardas [63], Park <i>et al.</i> [64], Mittal and Huttenlocher [65], Salas <i>et al.</i> [215], Wang and Dai [252], Hu <i>et al.</i> [259], Li <i>et al.</i> [265], Liu and Zhang [276], Yu <i>et al.</i> [290]
	Learning rates α, ρ	<i>Better settings:</i> Zang and Klette [66], White and Shah [67] <i>Adaptive learning rates:</i> Wang and Suter [60], Lindstrom <i>et al.</i> [61], Stauffer and Grimson [62], KaewTraKulPong and Bowden [68-70] Lee [71], Harville <i>et al.</i> [72], Porikli [73], Liu <i>et al.</i> [74], Pnevmatikakis <i>et al.</i> [75, 76], Power <i>et al.</i> [77], Leotta <i>et al.</i> [78], Sheng and Cui [272], Quast <i>et al.</i> [284], Molin [285], Qin <i>et al.</i> [286], Shah <i>et al.</i> [298], Kan <i>et al.</i> [302], Quast <i>et al.</i> [308], Lin <i>et al.</i> [309], Bin and Liu [320], Zhao and He [322], Li <i>et al.</i> [323]
Foreground Detection	Different measure for the matching test	Carminati <i>et al.</i> [53], Ren <i>et al.</i> [79], Lee [80], Sun [81], Morellas <i>et al.</i> [82], Xuehua <i>et al.</i> [261], Rui <i>et al.</i> [262]
	Pixel Persistence Map (PPM)	Pnevmatikakis <i>et al.</i> [75, 76], Landabaso and Pardas [83]
	Probabilities	Yang and Hsu [84], Lee [85], Lien <i>et al.</i> [251], Zhang and Zhou [21]
	Foreground model	Lindstrom <i>et al.</i> [61], Landabaso <i>et al.</i> [63], Withagen <i>et al.</i> [86], Landabaso <i>et al.</i> [263], Feldman <i>et al.</i> [313], Feldman [314], Tian and Wang [318]
	Some matching tests	Zhang <i>et al.</i> [39], Wang and Suter [60]
	Fusion rules	Lien <i>et al.</i> [251]
	Most dominant background	Haque <i>et al.</i> [87, 88, 89]

Table 4. Extrinsic improvements of the MOG

Methods	Authors - References
Markov Random Fields	Kumar and Sengupta [107], Zhou and Zhang [108], Schindler and Wang [109], Landabaso <i>et al.</i> [263], Li <i>et al.</i> [291], Dickinson <i>et al.</i> [316], Zhang and Zhou [327], Wang <i>et al.</i> [328]
Hierarchical approaches	Sun and Yuan [110], Park <i>et al.</i> [111], Chen <i>et al.</i> [112], Zhou <i>et al.</i> [113], Zhong <i>et al.</i> [242], Zhong <i>et al.</i> [264], Li <i>et al.</i> [265]
Multi-level approaches	Javed <i>et al.</i> [100], Zang and Klette [114], Zhong <i>et al.</i> [115], Cristani <i>et al.</i> [116-118], Yang <i>et al.</i> [325]
Multiple backgrounds	Su and Hu [119, 120], Porikli [121], Qi <i>et al.</i> [310], Qi <i>et al.</i> [311]
Graph cuts	Sun [81], Chang and Hsu [257], Li <i>et al.</i> [269], Li <i>et al.</i> [291]
Multi-layer approaches	Yang <i>et al.</i> [122], Porikli and Tuzel [123], Park and Buyn [266], Huang and Wu [292]
Features-Cameras strategies	Xu and Ellis [124], Nadimi and Bhanu [125, 126], Conaire <i>et al.</i> [127]
Tracking feedback	Harville [128], Taycher <i>et al.</i> [129], Wang <i>et al.</i> [275], He <i>et al.</i> [301], Yuan <i>et al.</i> [344], Shao <i>et al.</i> [326]
Post-processing	Turdu and Erdogan [130], Parks and Fels [131], Fazli <i>et al.</i> [306]

Table 5. Features improvements of the MOG

	Size/Type	Authors - References
Feature Size	Block	Fang <i>et al.</i> [90], Pokrajac and Latecki [91], Wang <i>et al.</i> [275], Zhong <i>et al.</i> [281], Zhang <i>et al.</i> [294], Wang <i>et al.</i> [329]
	Cluster	Bhaskar <i>et al.</i> [92], Cai <i>et al.</i> [243]
Feature Type	Color features Normalized RGB YUV	Stijman <i>et al.</i> [93], Xu et Ellis [94] Harville et al.[72], Sun [81], Fang <i>et al.</i> [90] , Guo <i>et al.</i> [270], Feldman <i>et al.</i> [313] , Feldman [314]
	HSV	Sun [81], Xuehua <i>et al.</i> [261], Rui <i>et al.</i> [262], Wang and Tang [274]
	HSI	Wang and Wu [95]
	Luv	Yang and Hsu [96]
	Improved HLS	Setiawan <i>et al.</i> [97]
	YCrCb	Kristensen <i>et al.</i> [98], Ribeiro <i>et al.</i> [99]
	Edge features	Javed <i>et al.</i> [100], Jain <i>et al.</i> [101], Klare and Sarka [203], Li <i>et al.</i> [253]
	Texture features	Tian and Hampapur [102], Shimada and Taniguchi [250], Huang <i>et al.</i> [255]
	Stereo features Disparity Depth	Gordon <i>et al.</i> [103] Harville <i>et al.</i> [72], Silvestre [104]
	Spatial features	Yang and Hsu [84], Dickinson <i>et al.</i> [105], Klare and Sarka [230], Wei <i>et al.</i> [231]
	Motion features	Tang <i>et al.</i> [40]
	Phase features	Xue <i>et al.</i> [312]
	Video features	Wang <i>et al.</i> [106], Wang <i>et al.</i> [239]
	Entropy features	Park <i>et al.</i> [295], Park <i>et al.</i> [296]
	Bayer features	Suhr <i>et al.</i> [297]
	HOG features	Fabian [299], Hu <i>et al.</i> [300]

Table 6. Challenges and MOG Versions

Critical Situations	Authors - References
CS 1 - Noise Image	Xu [221], Teixeira <i>et al.</i> [222], Li <i>et al.</i> [265]
CS 2-1 - Camera jitter	Campbell-West <i>et al.</i> [219], Xu [221], Achkar and Amer [223], Rao <i>et al.</i> [224], Li <i>et al.</i> [265]
CS 2- 2 - Camera Adjustements	Zen and Lai [225], Molin [285]
CS 3 - Gradual Illumination Changes	Tian <i>et al.</i> [234], Huang <i>et al.</i> [254], Wang <i>et al.</i> [277], Baloch [283], Huang <i>et al.</i> [288], Lin <i>et al.</i> [309]
CS 4 - Sudden Illumination Changes	Tian <i>et al.</i> [234], Li <i>et al.</i> [253], Baloch [283], Lin <i>et al.</i> [309], Xue <i>et al.</i> [312], Li <i>et al.</i> [323]
CS 5-1 - Bootstrapping during initialization	Gao <i>et al.</i> [220]
CS 5-2 - Bootstrapping during maintenance	Lindstrom <i>et al.</i> [61]
CS 6 - Camouflage	Guo <i>et al.</i> [270]
CS7 - Foreground Aperture	Utasi and Czúni [226]
CS 8 - Moved background objects	Teixeira <i>et al.</i> [222]
CS 9 - Inserted background objects	Teixeira <i>et al.</i> [222]
CS 10 - Multimodal background	Dalley <i>et al.</i> [227], Li <i>et al.</i> [265]
CS 11 - Waking foreground object	Su and Hu [119], Hu and Su [120]
CS 12 - Sleeping foreground objects	Cheng <i>et al.</i> [229], Cai <i>et al.</i> [256], Hu <i>et al.</i> [259]
CS 13 - Shadows Detection	Xu [221], Huang and Chen [232], Zhang <i>et al.</i> [233], Tian <i>et al.</i> [234], Izadi <i>et al.</i> [235], Rahman [236], Chen <i>et al.</i> [260], Landabaso <i>et al.</i> [263], Li <i>et al.</i> [265], Quast <i>et al.</i> [284], Molin [285], Huang <i>et al.</i> [288], Forczmanski and Seweryn [293], Tian and Wang [318], Li and Xu [319], Bin and Liu [320], Liu and Bin [321], Lai <i>et al.</i> [324], Wang <i>et al.</i> [328]

Table 7. Real Time Constraints and MOG Versions

Real-Time Constraints	Authors - References
Computation Time	Cuevas <i>et al.</i> [228], Chang and Hsu [257], Krishna <i>et al.</i> [271]
Memory Requirement	Krishna <i>et al.</i> [271]

Discussion: The Mixture of Gaussians (MOG) is adapted for outdoor scene where there are slow multimodal variations in the backgrounds. For the dynamic backgrounds like camera jitter, waving trees and water rippling, this model causes false detections.

3.3 Kernel Density Estimation (KDE)

To deal with dynamic backgrounds like camera jitter, waving trees and water rippling, Elgammal *et al.* [15] proposed to estimate the probability density function for each pixel using the kernel estimator K for N recent sample of intensity values $\{x_1, x_2, \dots, x_N\}$ taken consecutively in a time size window W as follows:

$$P(x_t) = \frac{1}{N} \sum_{i=1}^N K(x_t - x_i) \quad (13)$$

where $K()$ is the kernel estimator function which is taken as a Normal Gaussian function $N(0, \Sigma)$. So, the probability density function is determined as follows:

$$P(x_t) = \frac{1}{N} \sum_{i=1}^N \frac{1}{(2\pi)^{d/2} |\Sigma|^{1/2}} e^{-1/2 * (x_t - x_i)^T \Sigma^{-1} (x_t - x_i)} \quad (14)$$

Elgammal *et al.* [15] assumed that the different color channels are independent with different kernel bandwidths, then the kernel function bandwidth is as follows:

$$\Sigma = \begin{pmatrix} \sigma_1^2 & 0 & 0 \\ 0 & \sigma_2^2 & 0 \\ 0 & 0 & \sigma_3^2 \end{pmatrix} \quad (15)$$

So, the probability density function can be written as follows:

$$P(x_t) = \frac{1}{N} \sum_{i=1}^N \prod_{j=1}^d \frac{1}{\sqrt{2\pi\sigma_j^2}} e^{-1/2 * (x_{t_j} - x_{i_j})^T / \sigma_j^2} \quad (16)$$

Elgammal *et al.* [15] detected the foreground using the probabilities and a threshold T as follows:

If $P(x_t) < T$ then the pixel classified as foreground
else the pixel is classified as background (17)

At this step, a binary mask is obtained. Then, to make the next foreground detection, the parameters must be updated. For this, Elgammal *et al.* [15] used two background models: a short term one and a long term one. These two models achieve different objectives:

- The short term model adapts quickly to allow very sensitive detection. This model consists of the most recent N background sample values. The sample is updated using a selective maintenance mechanism, where the decision is based on the foreground classification.
- The long term model captures a more stable representation of the scene background and adapts to changes slowly. This model consists of N sample pixels taken from a much larger window in time. The sample is updated using a non selective maintenance mechanism.

So, to combine the advantage of each model and to eliminate their disadvantages, the next foreground detection is obtained by taking the intersection of the two foreground detection coming from the short term model and the long term model. This intersection eliminates the persistence false positives detection from the short term model and extra false positives detection that occur in the long term model results. The only false positives detection that will remain will be rare events not represented in either model. If this rare event persists over time in the scene then the long term model will adapt to it, and it will be suppressed from the result later. Taking the intersection will, unfortunately, suppress true positives in the first model result that are false negatives in the second, because the long term model adapts to foreground as well if they are stationary or moving slowly. To address this problem, all pixels detected by the short term model that are adjacent to pixels detected by the combination are included in the final foreground detection.

Improvements: The original KDE present several advantages. The multimodality of the model allows dealing with multimodal backgrounds particularly in fast changes (waving trees, water rippling, etc...). Despite it, this model

present some disadvantages: N frames need to be kept in memory during the entire detection process which is costly memory wise when N is large. The algorithm is time consuming too due the complexity in $O(N*N)$. To solve these problems, different improvements have been proposed:

- **Intrinsic improvements:** These strategies consist in changing the kernel function [141-149] as shown in Table 8. For the training, some authors propose to decrease the number of samples by determining a proper size of the frame buffer [143], by using a diversity sampling scheme [150,151] or by using a sequential Monte Carlo sampling scheme [152]. A recent patent concern the sequential kernel density approximation through mode propagation [359]. Furthermore, recursive maintenance [143-145,153, 154, 159] can be adopted to reduce the computation time. For the foreground detection, different scheme can be used as in [143, 146, 147, 153-155]. For the feature type, several features are used instead of the RGB space like the edge features [156] and motion features [157]. To choose which features to use, Parag *et al.* [158] proposed a framework for feature selection.

- **Extrinsic improvements:** Some authors (Table 9) used Markov Random Fields [155, 159], hierarchical approaches [160], multiple backgrounds [161] and graph cuts [162].

- **Enhancing the foreground detection:** Another way to improve this method is to enhance the results of the foreground detection by using cooperation with another segmentation method. It achieved by cooperation with the consecutive frame difference [163] or using a subspace learning approach using PCA [164].

The Table 8 and 9 give respectively an overview of the intrinsic and extrinsic improvements. Table 10 and Table 11 show respectively an overview of the critical situations and the real-time constraints for the different KDE versions that can tackle them better than the original one.

Table 8. Intrinsic improvements of the KDE

Background Step	Improvements	Authors - References
Background Model	Gaussian Kernel Function	<i>Automatic selection of kernel band width:</i> Tavakkoli <i>et al.</i> [141, 142]
	Rectangular Kernel Function	<i>Constant kernel band width:</i> Ianasi <i>et al.</i> [143], Tanaka <i>et al.</i> [144, 145] <i>Variable kernel band width:</i> Zivkovic [146]
	Derivative Kernel Function	Cvetkovic <i>et al.</i> [147]
	Negative coefficient polynomial kernel function	Witherspoon and Zhang [148]
	Cauchy Kernel Function	Ramezani <i>et al.</i> [149]
Background Initialization	Decreasing the number of samples	<i>Adopting the proper size of frame buffer:</i> Ianasi <i>et al.</i> [143] <i>Diversity samples scheme:</i> Mao and Shi [150, 151] <i>Sequential Monte Carlo sampling:</i> Tang <i>et al.</i> [152]
Background Maintenance	Background image	Ianasi <i>et al.</i> [143]
	Recursive Maintenance	<i>Recursive maintenance of the PDF:</i> Tavakkoli <i>et al.</i> [153], Tanaka <i>et al.</i> [144, 145], Ramezani <i>et al.</i> [149] <i>Recursive maintenance of the background PDF and foreground PDF:</i> Tavakkoli <i>et al.</i> [154] <i>Recursive maintenance of the PDF and the background image:</i> Ianasi <i>et al.</i> [143]
	Number of samples	Zivkovic [146]
	Selective Maintenance	Tavakkoli <i>et al.</i> [141, 142], Mao and Shi [151]
Foreground Detection	Dissimilarity measure	Ianasi <i>et al.</i> [143]
	Probability	Zivkovic [146], Tavakkoli <i>et al.</i> [153]
	Foreground model	Tavakkoli <i>et al.</i> [153, 154]
	Two thresholds	Cvetkovic <i>et al.</i> [147]

Table 9. Extrinsic improvements of the KDE

Methods	Authors - References
Markov Random Fields	Pahalawatta <i>et al.</i> [159]
Hierarchical approaches	Orten <i>et al.</i> [160]
Multiples backgrounds	Tanaka <i>et al.</i> [161]
Graph cuts	Mahamud [162]

Table 10. Challenges and KDE Versions

Critical Situations	Authors - References
CS 1 - Noise Image	Mao and Shi [150 , 151]
CS 2-1 - Camera jitter	Sheihk and Shah [155]
CS 2- 2 - Camera Adjustements	Cvetkovic <i>et al.</i> [147], Sung <i>et al.</i> [347], Hwang <i>et al.</i> [348]
CS 3 - Gradual Illumination Changes	Sheihk and Shah [155]
CS 4 - Sudden Illumination Changes	Sung <i>et al.</i> [48], Hwang <i>et al.</i> [49]
CS 5-1 - Bootstrapping during initialization	Martel-Brisson and Zaccarin [346]
CS 5-2 - Bootstrapping during maintenance	Sheihk and Shah [155]
CS 6 - Camouflage	Tavakkoli <i>et al.</i> [142], Gu <i>et al.</i> [345]
CS7 - Foreground Aperture	
CS 8 - Moved background objects	Elgammal <i>et al.</i> [15], Cvetkovic <i>et al.</i> [147]
CS 9 - Inserted background objects	
CS 10 - Multimodal background	
CS 11 - Waking foreground object	
CS 12 - Sleeping foreground objects	
CS 13 - Shadows Detection	Elgammal <i>et al.</i> [15], Cvetkovic <i>et al.</i> [147], Mao and Shi [150 , 151]

Table 11. Real Time Constraints and KDE Versions

Real-Time Constraints	Authors - References
Computation Time	Elgammal [349], Sadeghi <i>et al.</i> [350]
Memory Requirement	Elgammal [349], Sadeghi <i>et al.</i> [350]

Discussion: The KDE is more adapted for outdoor scene where dynamic backgrounds appear but less suited for illumination changes.

3.4 Subspace Learning using PCA (SL-PCA)

Subspace learning offer a good framework to deal with illumination changes as it allows taking into account spatial information. Oliver *et al.* [165] proposed to model each background pixel using an eigenbackground model.

This model consists in taking a sample of N images $\{I_1, I_2, ..., I_N\}$ and computing the mean background image μ_B and its covariance matrix C_B .

This covariance matrix is then diagonalized using an eigenvalue decomposition as follows:

$$L_B = \Phi_B C_B \Phi_B^T \quad (18)$$

where Φ_B is the eigenvector matrix of the covariance of the data and L_B is the corresponding diagonal matrix of its eigenvalues.

In order to reduce, the dimensionality of the space, only M eigenvectors ($M < N$) are kept in a principal component analysis (PCA). The M largest eigenvalues are contained in the matrix L_M and the M vectors correspond to these M largest eigenvalues in the matrix Φ_M .

Once the eigenbackground images stored in the matrix Φ_M are obtained and the mean μ_B too, the input image I_t can be approximated by the mean background and weighted sum of the eigenbackgrounds. Φ_M .

The coordinate in eigenbackground space of input image I_t can be computed as follows:

$$w_t = (I_t - \mu_B)^T \Phi_M \quad (19)$$

When w is back projected onto the image space, a reconstructed background image is created as follows:

$$B_t = \Phi_M w_t^T + \mu_B \quad (20)$$

Then, the foreground object detection is made as follows:

$$|I_t - B_t| > T \quad (21)$$

where T is a constant threshold.

Improvements: The eigenbackground model which we have called SL-PCA provides a robust model of the probability distribution function of the background, but not of the moving objects while they do not have a significant contribution to the model. So, the first limitation of this model is that the size of the foreground object must be small and don't appear in the same location during a long period in the training sequence. The second limitation appears for the background maintenance. Indeed, it is computationally intensive to perform model updating using the batch mode

PCA. Moreover without a mechanism of robust analysis, the outliers or foreground objects may be absorbed into the background model. The third limitation is that the application of this model is mostly limited to the gray-scale images since the integration of multi-channel data is not straightforward. It involves much higher dimensional space and causes additional difficulty to manage data in general. Another limitation is that the representation is not multimodal so various illumination changes cannot be handled correctly. To alleviate these limitations, numerous improvements (25 papers) have been proposed over the recent years. A survey over 15 papers in the period 1999-2009 can be found in [334]. Thus, the different improvements which attempt to solve these four limitations are summarized in the following classification with the recent advances:

- **Alleviate the limitation of the size of the foreground object:** Xu *et al.* [166, 167] proposed to apply recursively an error compensation process which reduces the influence of foreground moving objects on the eigenbackground model. An adaptive threshold method is also introduced for background subtraction, where the threshold is determined by combining a fixed global threshold and a variable local threshold. Results show more robustness in presence of moving objects. Another approach developed by Kawabata *et al.* [168] consists in an iterative optimal projection method to estimate a varied background in real time from a dynamic scene with foreground. Firstly, background images are collected for a while and then the background images are compressed using eigenspace method to form a database. After this initialization, a new image is taken and projected onto the eigenspace to estimate the background. As the estimated image is much affected by the foreground, the foreground region is calculated by using background subtraction with former estimated background to exclude the region from the projection. Thus the image whose foreground region is replaced by the former background is projected to eigenspace and then the background is updated. Kawabata *et al.* [25] proved that the cycle converges to a correct background image. Recently, Quivy and Kumazawa [351] proposed to generate the background images using the Nelder-Mead Simplex algorithm and a dynamic masking procedure. This paper presents an original method that replaces the projection/reconstruction step of the SL-PCA by a direct background image generation. The experiments proved that the proposed method performs better than the SL-PCA [165], SL-REC [166, 167], and SL-IOP [168] for large and fast moving objects.
- **Dealing with the time requirement and the robustness:** For the maintenance, some authors [169-177] proposed different algorithms of incremental PCA. The incremental PCA proposed by [169] need less computation but the background image is contaminated by the foreground object. To solve this, Li *et al.* [170, 171]

proposed an incremental PCA which is robust in presence of outliers. However, when keeping the background model updated incrementally, it assigned the same weights to the different frames. Thus, clean frames and frames which contain foreground objects have the same contribution. The consequence is a relative pollution of the background model. In this context, Skocaj *et al.* [172, 173] used a weighted incremental and robust. The weights are different following the frame and this method achieved a better background model. However, the weights were applied to the whole frame without considering the contribution of different image parts to building the background model. To achieve a pixel-wise precision for the weights, Zhang and Zhuang [174] proposed an adaptive weighted selection for an incremental PCA. This method performs a better model by assigning a weight to each pixel at each new frame during the update. Experiments [174] show that this method achieves better results than the SL-IRPCA [170, 171]. Wang *et al.* [175, 176] used a similar approach using the sequential Karhunen-Loeve algorithm. Recently, Zhang *et al.* [209] improved this approach with an adaptive scheme. All these incremental methods avoid the eigen-decomposition of the high dimensional covariance matrix using approximation of it and so a low decomposition is allowed at the maintenance step with less computational load. However, these incremental methods maintain the whole eigenstructure including both the eigenvalues and the exact matrix Φ_M . To address this problem, Li *et al.* [177] proposed a fast recursive and robust eigenbackground maintenance avoiding eigen-decomposition. This method achieves similar results than the SL-IPCA [169] and the SL-IRPCA [170, 171] at better frames rates. Fig. (4). shows a classification of these algorithms following their robustness and their adaptivity.

- **Dealing with the grey scale and the pixel-wise limitations:** Recently, Wu *et al.* [207] proposed to combine the PCA model with single gaussian model. PCA allow the robustness to illumination changes and the single gaussian to describe color information for each pixel. So, it can detect the chroma changes and remove shadow pixels. An adaptively strategy is used to integrate the two models. A binary graph cut is then used to perform the foreground/background segmentation. In another way, Han and Jain [178] proposed an efficient algorithm using a weighted incremental 2-Dimensional Principal Component Analysis. It is shown that the principal components in 2DPCA are computed efficiently by transformation to standard PCA. To perform the computational time, Han and Jain [178] used an incremental algorithm to update eigenvectors to handle temporal variations of background. The proposed algorithm was applied to 3-channel (RGB) and 4-channel (RGB+IR) data.

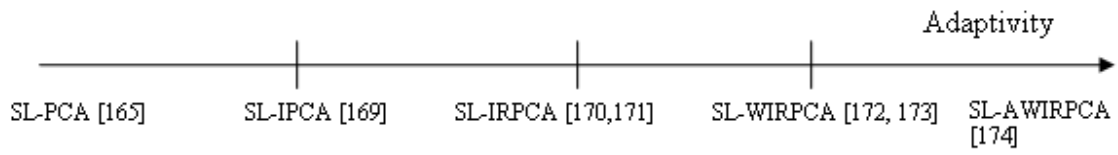


Fig. (4): Adaptivity of the SL-PCA Algorithms

Results show noticeable improvements in presence of multimodal background (MB) and shadows (S). To solve the pixel-wise limitation, Zhao *et al.* [206] used spatio-temporal block instead of pixel. Furthermore, their method consist in applying the candid covariance free incremental principal components analysis algorithm (CCIPCA) which is fast in convergence rate and low in computational complexity than classical IPCA algorithms. Results show more robustness robust to noise and fast lighting changes.

- **Dealing with multimodal illumination changes:** Recently, Dong *et al.* [211] proposed to use a multi-subspace learning to handle different illumination changes. The feature space is organized into clusters which represent the different lighting conditions. A Local Principle Component Analysis (LPCA) transformation is used to learn separately an eigen-subspace for each cluster. When a current image arrives, the algorithm selects the learned subspace which shares the nearest lighting condition. The results [211] show that the LPCA algorithm outperforms the original PCA [165] algorithm and MOG [14] especially under sudden illumination changes. In a similar way, Kawanishi *et al.* [213-214] generated the background image which well expresses the weather and the lighting condition of the scene. This method collects a huge number of images by super long term surveillance, classifies them according to their time in the day, and applies the PCA so as to reconstruct the background image.

A recent patent concern a method based on space-time video block and online subspace learning [360]. This method allows a robust incremental update and alleviates the pixel-wise limitations.

The Table 12, Table 13, Table 14 and Table 15 group by type the different improvements of the SL-PCA.

Table 12. Influence of the foreground objects

Methods	Authors - Dates
Recursive Error Compensation (SL-REC)	Xu <i>et al.</i> (2006) [166, 167]
Iterative Optimal Projection (SL-IOP)	Kawabata <i>et al.</i> (2006) [168]
Simplex Algorithm (SL-SA)	Quivy and Kumazawa (2011) [351]

Table 13. Time requirement and the robustness

Methods	Authors - Dates
Incremental PCA (SL-IPCA)	Rymel <i>et al.</i> (2004) [169]
Incremental and robust PCA (SL-IRPCA)	Li <i>et al.</i> (2003) [170, 171]
Weighted Incremental and Robust PCA (SL-WIRPCA)	Skocaj <i>et al.</i> (2003) [172, 173]
Adaptive Weight Selection for Incremental PCA (SL-AWIPCA)	Zhang and Zhuang (2007) [174]
Sequential Karhunen-Loeve algorithm (SL-SKL)	Wang <i>et al.</i> (2006) [175, 176]
Adaptive Sequential Karhunen-Loeve algorithm (SL-ASKL)	Zhang <i>et al.</i> [209]
Fast Recursive Maintenance (SL-FRM)	Li <i>et al.</i> (2006) [177]

Table 14. Dealing with the grey scale and the pixel-wise limitations

Methods	Authors - Dates
PCA - Single Gaussian (SL-PCA-SG)	Wu <i>et al.</i> (2009) [207, 208]
Weighted Incremental 2PCA (SL-WI2DPCA)	Han and Jain (2007) [178]
Candid Covariance Incremental PCA (SL-CCIPCA)	Zhao <i>et al.</i> (2008) [206]

Table 15. Dealing with multimodal illumination changes

Methods	Authors - Dates
Local Principle Component Analysis on Clusters (LPCA-C)	Dong <i>et al.</i> (2010) [211, 212]
Local Principle Component Analysis on Separated Sequences (LPCA-SS)	Kawanishi <i>et al.</i> (2009) [213-214]

3.5. Discussion

In Section 3, we surveyed the models of the first category and their related improvements. These improvements perform each original algorithm for specified critical situations. However, some authors have recently proposed to use more advanced statistical models as Support Vector models to deal more accurately with dynamics background.

4. SECOND CATEGORY

The second category models use more sophisticated statistical model as support vector machine (SVM), support vector regression (SVR) and support vector data description (SVDD).

4.1 Support Vector Machine (SVM)

Support Vector Machines were introduced by Vapnik *et al.* [179]. For classification, SVMs work by determining a hyperplane in a high dimensional feature space to separate the training data into two classes. The best hyperplane can be derived by minimizing the margin which represents the least distance from the hyperplane to the data. Using this classification aspect, Lin *et al.* [180] proposed to use the SVMs for background modeling. Particularly, Lin *et al.* [180] used a PSVM with probabilistic outputs because the SVM gives only binary outputs. A sigmoid model is used to convert binary SVM scores into posterior probabilities:

$$p(y=1|f) = \frac{1}{1 + \exp(Af + B)} \quad (22)$$

where y is binary class label and f is an output score of the SVM decision function. The two parameters A and B are fitted using maximum likelihood estimation from a training set (f_i, y_i) , and derived by minimizing the negative log-likelihood function:

$$\min - \sum_i t_i \log(p_i) + (1 - t_i) \log(1 - p_i) \quad (23)$$

where

$$t_i = \frac{y_i + 1}{2} \text{ and } p_i = \frac{1}{1 + \exp(Af_i + B)} \quad (24)$$

To avoid overfitting and to derive unbiased training for the minimization, a hold-out set is generated from the data by dividing each training set of 80% and 20% respectively. The large subset is used for SVM training, and the smaller one is used for the two parameter minimization. In this context, Lin *et al.* [180] used 100 images of size 160*120 with known background. Each image is divided into blocks of size 4*4 and considering two features for each block: optical flow value and consecutive image difference. For each block, its label is defined as +1 for background and -1 otherwise. The background initialization starts with the first image and each block are tested by the PSVM. An image block is classified as background if its probability output is larger than a threshold T :

$$p(b_i) > T \quad (25)$$

When an image block $p(b_i) > T$ is classified as background for M consecutive times, the Fisher linear distance is used:

$$d(b_i, b_{back}) = \frac{(\mu_i - \mu_{back})^2}{(\sigma_i^2 - \sigma_{back}^2)} \quad (26)$$

where μ and σ^2 are the mean and the variance of the intensity distribution of a block.

When the distance between the two blocks is large, two possible conditions appear. The current block can be either part of a uniform region of a moving object or a new background just revealed. The averaging PSVM probability for the current block over the past M frames is compared with the PSVM probability of the background. If the new average PSVM probability is larger, then the background is replaced by the current block.

Continuing this way, the initialization process will be terminated when replacement events do not occur for a consecutive M frames. When the initialization is finished, the foreground detection is made by thresholding the difference between the background model and the current image.

4.2 Support Vector Regression (SVR)

Given a set of training data, SVR fits a function by specifying an upper bound on a fraction of training data allowed to lie outside of a distance ε from the regression estimate. This type of SVR is usually referred to as ε -insensitive SVR [181]. For each pixel belonging to the background, a separate SVR is used to model it as a function of intensity. To classify a given pixel as background or not, Wang *et al.* [183] [184] feed its intensity value to the SVR associated it and threshold the output of the SVR. Let assume a set of training data for some pixel p obtained from several frames $\{(x_1, y_1), \dots, (x_N, y_N)\}$, where x_i corresponds to the intensity value of pixel p at frame i , and y_i corresponds to the confidence of pixel p being a background pixel. Once the SVR has been trained, the confidence of the pixel p in a new frame i , $f(x_i)$, is computed using the following linear regression function:

$$f(x_i) = \sum_{j=1}^N (a_i - a_j^*) k(x_i, x_j) + \xi \quad (27)$$

where $k(x_i, x_j)$ is a kernel function. The parameters a , a^* and ξ , called Lagrange multipliers, are obtained by solving an optimization problem using the method of the Lagrange multipliers. Given the SVR-based background model, the intensity of each pixel in a new frame forms the input to the SVR. The output of the SVR represents the confidence that a given pixel belongs to the background. Eventually, a pixel is labelled as background if its

confidence is between a low threshold S_l and a high threshold S_h . Specifically, a binary foreground detection map is formed at frame t as follows:

$$\begin{aligned} M_{x_i}^t &= 0 \text{ if } S_l < f(x_i) < S_h \\ M_{x_i}^t &= 1 \text{ otherwise} \end{aligned} \quad (28)$$

where $f(x_i)$ is the SVR output and $S = \{S_l, S_h\}$ are the initial thresholds. Then, for each region in the binary map, the SVR-based background model is update using an online SVR learning algorithm [182].

4.3 Support Vector Data Description (SVDD)

Tavakkoli *et al.* [186] proposed to model the background using support vector data description (SVDD) in videos with quasi-stationary backgrounds. Data domain description concerns the characteristics of a data set [185]. The boundary of the dataset can be used to detect novel data or outliers. A normal data description gives a closed boundary around the data. The simplest boundary can be represented by a hyper-sphere. The volume of this hyper-sphere with center a and radius R should be minimized while containing all the training samples x_i . To allow the possibility of outliers in the training set, slack variables $\varepsilon_i \geq 0$ are introduced. The error function to be minimized is defined as:

$$F(R, a) = R^2 + C \sum_i \varepsilon_i \quad (29)$$

Subjects to the constraints:

$$\|x_i - a\|^2 \leq R^2 + \varepsilon_i \quad \forall i \quad (30)$$

In equation (1), C is a trade-off between simplicity of the system and its error and is called confidence parameter. After incorporating the constraints (30) into the error function (29) by Lagrange multipliers we have:

$$L(R, a, \alpha_i, \gamma_i, \varepsilon_i) = R^2 + C \sum_i \varepsilon_i - \sum_i \alpha_i (R^2 + \varepsilon_i - (\|x_i - a\|^2)) - \sum_i \gamma_i \varepsilon_i \quad (31)$$

L should be maximized with respect to Lagrange multipliers $\alpha_i \geq 0$ and $\gamma_i \geq 0$ and minimized with respect to R , a and ε_i . Lagrange multipliers γ_i can be removed if the constraint $0 \leq \alpha_i \leq C$ is imposed. After solving the optimization problem we have:

$$\begin{aligned} L &= \sum_i \alpha_i (x_i \cdot x_i) - \sum_{i,j} \alpha_i \alpha_j (x_i \cdot x_j) \\ \forall \alpha_i : 0 &\leq \alpha_i \leq C \end{aligned} \quad (32)$$

When a new sample satisfies the inequality in (30), then its corresponding Lagrange multipliers are $\alpha_i \geq 0$, otherwise they are zero.

Therefore we have:

$$\begin{aligned} \|x_i - a\|^2 < R^2 &\rightarrow \alpha_i = 0, \gamma_i = 0 \\ \|x_i - a\|^2 > R^2 &\rightarrow \alpha_i = C, \gamma_i > 0 \end{aligned} \quad (33)$$

From the above, we can remark that only samples with non-zero α_i are needed in the description of the data set, therefore they are called support vectors of the description. To test a new sample y , its distance to the center of the hyper-sphere is calculated and tested against R . Tavakkoli *et al.* [186] used this methodology to built a descriptive boundary for each pixel in the background training frames to generate its model for the background. Then, these boundaries are used to classify their corresponding pixels in new frames as background and foreground pixels. In practice, for each pixel in the scene a single class classifier is trained by using its values in the background training frames. This classifier consists of the description boundary and support vectors, as well as a threshold used to describe the data. For the foreground detection, each pixel in the new frames is classified as background or foreground using its value and its corresponding classifier from the training stage. Feature vectors x_{ij} used in the current implementation are $x_{ij} = [C_r; C_g]$, where C_r and C_g are the red and green chrominance values for pixel (i, j) .

Improvements: This model presents several advantages: The accuracy is not bounded to the accuracy of the estimated probability density functions and the memory requirement is less than non-parametric techniques. Because support vector data description explicitly models the decision boundary of the known class, it is suitable for novelty detection without the need to use thresholds. Furthermore, the classifier performance in terms of false positive is controlled explicitly. The main disadvantage is that the training of SVDD requires a Lagrange optimization which is computationally intensive. For the maintenance, all the SVDD must be recomputed. To perform the training, Tavakkoli *et al.* [187] proposed to use a genetic approach to solve the Lagrange optimization problem. The Genetic Algorithm (GA) starts with the initial guess and solves the optimization problem iteratively. In [188][189], Tavakkoli *et al.* proposed to use an incremental SVDD. In this way, the maintenance is performed too.

4.4 Discussion

Support vector models offer a nice framework for background modeling specifically in presence of illumination changes and dynamic backgrounds. Another way to model the background is to perform the first category by using a more adaptive model.

5. THIRD CATEGORY

The third category models generalize the first category model as the single general Gaussian (SGG), the mixture of general Gaussians (MOGG) and subspace learning using Incremental Component Analysis (SL-ICA), Incremental Non-negative Matrix Factorization (SL-INMF) or Incremental Rank-(R_1, R_2, R_3) Tensor (SL-IRT).

5.1 Single General Gaussian (SGG)

Kim *et al.* [190-192] proposed to model the background using a generalised Gaussian family (GGF) model of distributions to cope with problems from various changes in background and shadows. The idea is that pixel variance fitted sometimes a Laplace one or a Gaussian one. Indeed, pixel variance in a static scene over time in indoor scenes taken with the latest camera is closer to a Laplace distribution than a Gaussian, but the Laplace model has limitation for use in various environments. The pixel variation in a static scene over time is defined as:

$$P(X_t) = \frac{\rho\gamma}{2\Gamma(1/\rho)} e^{-(\gamma^\rho |x-\mu|^\rho)} \text{ with } \gamma = \frac{1}{\sigma} \left(\frac{\Gamma(3/\rho)}{\Gamma(1/\rho)} \right) \quad (34)$$

where $\Gamma(\bullet)$ is a gamma function and σ^2 is a variance of the distribution. In Equation (1), $\rho = 1$ represents a Laplace distribution while $\rho = 2$ represents a Gaussian distribution. The models are decided for each pixel by computing excess kurtosis g_2 of the first m frames. The excess kurtosis of Laplace and Gaussian distributions is respectively 3 and 0. The optimal parameters of the background model are estimated by the maximization of the likelihood of the observed value:

$$g_2 = \frac{N \sum_{i=1}^N (x_i - \mu)^4}{\left(\sum_{i=1}^N (x_i - \mu)^2 \right)^2} - 3 \quad (35)$$

In practice, Kim *et al.* [190-192] modelled the background in two parts: a luminance component obtained by a weighted mean of RGB channels and a hue component in HSI color space. The maintenance is made using a selective running average as in [13]. The foreground detection is firstly performed by subtracting the intensity components of the current frame from the background model:

$$D(x, y) = |I(x, y) - B(x, y)| \quad (36)$$

where $I(x, y)$ and $B(x, y)$ correspond respectively to the luminance of the current frame and the background model. Then, pixels are classified into three categories using two thresholds as follows:

$$\begin{aligned} &\text{background pixel if } D(x, y) < T_1 k(x, y) \\ &\text{suspicious pixel if } T_1 k(x, y) \leq D(x, y) \leq T_2 k(x, y) \\ &\text{foreground pixel if } T_2 k(x, y) < D(x, y) \end{aligned} \quad (37)$$

where $k(x, y)$ is a scale parameter. The thresholds T_1, T_2 and T_3 are determined using the training frames. The SGG shows better performance than the MOG and the KDE in indoor and outdoor scene.

5.2. Mixture of General Gaussians (MOGG)

Allili *et al.* [193-195] proposed a finite mixture model of general Gaussians for robust segmentation in the presence of noise and outliers. This model has more flexibility to adapt the shape of data and less sensibility for over-fitting the number of classes than the mixture of Gaussians. Each pixel is characterized by its intensity in the RGB color space. Then, the probability of observing the current pixel value is considered given by the following formula in the multidimensional case:

$$P(X_t) = \sum_{i=1}^K \omega_{i,t} \eta(X_t, \mu_{i,t}, \sigma_{i,t}, \lambda_i) \quad (38)$$

where the parameters are K is the number of distributions, $\omega_{i,t}$ is a weight associated to the i^{th} Gaussian at time t with mean $\mu_{i,t}$ and standard deviation $\sigma_{i,t}$. $\lambda_i = 0$ if the distribution is a Gaussian one and $\lambda_i = 3$ if the distribution is a Laplace one. η is a Gaussian probability density function:

$$\eta(X_t, \mu_{i,t}, \sigma_{i,t}, \lambda_i) = \prod_{j=1}^d A(\lambda_j) \exp \left(-B(\lambda_j) \left| \frac{X_j - \mu_j}{\sigma_j} \right|^{\lambda_j} \right)$$

where $A(\lambda) = \frac{(\Gamma(3/\lambda) / \Gamma(1/\lambda))^{1/\lambda}}{2\sigma\Gamma(1/\lambda)}$ and

$$B(\lambda) = \left(\frac{\Gamma(3/\lambda)}{\Gamma(1/\lambda)} \right). \quad (39)$$

The optimal number of Gaussians is computed at each time t by minimizing the criterion Minimum Message Length (MML). If the number of Gaussians at time $t+1$ is smaller than at time t , the parameters are updated in a similar way than in [14]. The same matching test as in [14] is used to check if a pixel matches a Gaussian. For the labeling, the same scheme that Stauffer and Grimson [14] is used. The MOGG show better performance than the MOG in the presence of shadows (S).

5.3 Subspace Learning

Subspace learning can be made using PCA as seen in the Section 3.4. In the literature [196], there are other methods to reduce the space and these different methods have been classified by Skocaj and Leonardis [197] as reconstructive methods and discriminative methods:

- **Reconstructive subspace learning:** The reconstructive methods allow a well approximation of data and so provide a good reconstruction. Another advantage is that reconstructive methods are unsupervised techniques. Furthermore, reconstructive methods enable incremental updating which is very suitable for real-time application. These methods are task-independents. The most common reconstructive methods are the following: Principal Components Analysis (PCA) [51], Independent Component Analysis (ICA) [52] and Non-negative Matrix Factorization (NMF) [53]. PCA transforms a number of possibly correlated data into a smaller number of uncorrelated data called principal components. ICA is a variant of PCA in which the components are assumed to be mutually statistically independent instead of merely uncorrelated. The stronger condition allows remove the rotational invariance of PCA, i.e. ICA provides a meaningful unique bilinear decomposition of two-way data that can be considered as a linear mixture of a number of independent source signals. Non-negative matrix factorization (NMF) finds linear representations of non-negative data. Given a non-negative data matrix V , NMF finds an approximate factorization $V = WH$ into non-negative factors W and H . The non-negativity constraints make the representation purely additive, i.e. allowing no subtractions, in contrast to principal component analysis (PCA) and independent component analysis (ICA).
- **Discriminative subspace learning:** The discriminative methods are supervised techniques and allow a well separation of data and so provide a good classification. Furthermore, discriminative methods are spatially and computationally efficient. These methods are task-dependents. The most common discriminative methods are the following: Linear Discriminant Analysis (LDA) [54] and Canonical Correlation Analysis (CCA) [55]. LDA projects the data onto a lower-dimensional vector space such that the ratio of the between-class distance to the within-class distance is maximized. The goal is to achieve maximum discrimination. Canonical correlation analysis (CCA) is a multivariate statistical model that facilitates the study of interrelationships among sets of multiple dependent variables and multiple independent variables. Canonical correlation simultaneously predicts multiple dependent variables from multiple independent variables.

All these methods are originally implemented with batch algorithms which require that the data must be available in

advance and be given once altogether. However, this type of batch algorithms is not adapted for the application of background modeling in which the data are incrementally received from the camera. Furthermore, when the dimension of the dataset is high, both the computation and storage complexity grow dramatically. Thus, incremental methods are highly needed to compute in real-time the adaptive subspace for the data arriving sequentially. Following these constraints, the reconstructive methods are the most adapted for background modeling. Furthermore, their unsupervised aspect allows avoid a manual intervention in the learning step. In the following paragraphs, we survey the subspace learning methods applied recently to background modeling: Independent Component Analysis (ICA), Non-negative Matrix Factorization (NMF) and Incremental Rank-(R_1, R_2, R_3) Tensor.

5.3.1 Subspace learning using ICA (SL-ICA)

ICA generalizes the technique of PCA. When some mixtures of probabilistically independent source signals are observed, ICA recovers the original source signals from the observed mixtures without knowing how the sources are mixed. The assumption made is that the observation vectors $X = (x_1, x_2, \dots, x_M)^T$ can be represented in terms of a linear superposition of unknown independent vectors $S = (s_1, s_2, \dots, s_M)^T$:

$$X = AS \quad (40)$$

where A is an unknown mixing matrix ($M \times N$). ICA finds a matrix W , so that the resulting vectors:

$$Y = WX \quad (41)$$

recovers the independent vectors S , probabilistically permuted and rescaled. W is roughly the inverse matrix of A . Applying it to background modeling, the ICA model is given by:

$$Y = WX_t \quad (42)$$

$X_t = (x_B, x_F)^T$ is the mixture data matrix of size $2 \times K$ in which $K = M \times N$. $x_1 = (x_{11}, x_{12}, \dots, x_{1K})$ is the first frame which can contain or not foreground objects and $x_2 = (x_{21}, x_{22}, \dots, x_{2K})$ is the second frame which contain foreground objects. $W = (w_1, w_2)^T$ is the demixing matrix, in which $w_i = (w_{i1}, w_{i2})$ with $i=1,2$. $Y = (y_1, y_2)^T$ is the estimated source signals in which $y_i = (y_{i1}, y_{i2}, \dots, y_{ik})$. Several ICA algorithms can be used to determine W . Yamazaki *et al.* [198] used a neural learning algorithm [199]. In another way, Tsai and Lai [200] used a Particle Swarm Algorithm (PSO) [201]. Once W is

determined, there are two ways in the literature to generate the background and the foreground mask images:

- The first case which $\mathcal{X}_1$ contains foreground object like in Yamazaki *et al.* [198]. Then, the foreground mask for the frames $\mathcal{X}_1$ and $\mathcal{X}_2$ is obtained by thresholding respectively $\mathcal{Y}_1$ and $\mathcal{Y}_2$. The background image is obtained by replacing regions representing foreground objects in $\mathcal{X}_1$ by the corresponding regions representing background in $\mathcal{X}_2$.
- The second case which $\mathcal{X}_1$ contains no foreground object like in Tsai and Lai [200]. Then, the foreground mask for the frames $\mathcal{X}_2$ is obtained by thresholding $\mathcal{Y}_2$. The background image is $\mathcal{Y}_1$.

The ICA model was tested on traffic scenes by Yamazaki *et al.* [198] and show robustness in changing background like illumination changes. In [200], the algorithm was tested on indoor scenes where sudden illumination changes appear.

5.3.2 Subspace learning using INMF (SL-INMF)

The non-negative matrix factorization (NMF), with rank r , decomposes the data matrix $V \in R^{p \times q}$ into two matrices which are $W \in R^{p \times r}$ called the mixing matrix, and $H \in R^{r \times q}$ named as the encoding matrix:

$$V \approx WH \quad (43)$$

So, NMF aims to find an approximate factorization that minimizes the reconstruction error. Different cost functions based on the reconstruction error have been defined in the literature, but because of its simplicity and effectiveness, the squared error is the most used:

$$F = \|V - WH\|^2 = \sum_{i=1}^p \sum_{j=1}^q (V_{ij} - (WH)_{ij})^2 \quad (44)$$

where subscription ij stands for the ij^{th} matrix entity. Applying it to background modelling, Bucak *et al.* [202, 203] proposed an incremental NMF algorithm. The background initialization is made using N training frames. So, V is vector column corresponding to a matrix of size $(p \times q) \times N$. The matrices W and H are updated incrementally. The foreground detection is made by thresholding the residual error which correspond to the deviations between the background model and the projection of the current frame onto the background model. The INMF has similar performance to dynamic background and illumination changes than the IRPCA proposed by Li *et al.* [170].

5.3.3 Subspace learning using Incremental Rank-(R1,R2, R3) Tensor (SL-IRT)

The different previous subspace learning considered image as a vector. So, the local spatial information is almost lost. Li *et al.* [204, 205] proposed to use a high-order tensor learning algorithm called incremental rank-(R_1, R_2, R_3) tensor based subspace learning to take into account the spatial information. This online algorithm constructs a low-order tensor eigenspace model in which the sample mean and the eigenbasis are updated adaptively. Denote $G = \{BM_q \in R^{M \times N}\}_{q=1,2,\dots,t}$ as a scene's background

appearance sequence with the q -th frame being BM_q .

Denote p_{xy} as the x -th and the y -th pixel of the scene. The tensor-based eigenspace model for an existing $A = \{BM_q^{xy} \in R^{I_1 \times I_2 \times I_3}\}_{q=1,2,\dots,t}$ ($I_1=I_2=5$ corresponding to

a K neighborhood of p_{xy} with $K=I_1 I_2 - 1 = 24$) consists of the maintained eigenspace dimensions (R_1, R_2, R_3) corresponding to the three tensor unfolding modes, the mode- n column projection matrices $U^{(n)} \in R^{I_n \times R_n}$, the mode-3 row projection matrix $V^{(3)} \in R^{(I_1 \times I_2) \times R_3}$, the column means $\bar{L}^{(1)}$ and $\bar{L}^{(2)}$ of the mode-(1,2) unfolding matrices $A_{(1)}$

and $A_{(2)}$, and the row mean $\bar{L}^{(3)}$ of the mode-3 unfolding matrix $A_{(3)}$. Given the K -neighbor image region

$I_{t+1}^{xy} \in R^{I_1 \times I_2 \times I_3}$ centered at the x -th and y -th pixel p_{xy} of the current incoming frame $I_{t+1} \in R^{M \times N \times I}$, the distance

RM_{xy} (determined by the three reconstruction error norms of the three modes) between I_{t+1}^{xy} and the learned tensor-based eigenspace model is computed. Then, the foreground detection is defined as follows:

$$p_{xy} \text{ is classified as background if } \exp\left(-\frac{RM_{xy}^2}{2\sigma^2}\right) > T$$

$$p_{xy} \text{ is classified as foreground otherwise} \quad (45)$$

where σ is a scaling factor and T denotes a threshold. Thus, the new background model $BM_{t+1}(x, y)$ at time $t+1$ is defined as:

$$BM_{t+1}(x, y) = H_{xy} \quad \text{if } p_{xy} \text{ is classified as foreground} \\ BM_{t+1}(x, y) = I_{t+1}(x, y) \quad \text{otherwise} \quad (46)$$

where $H_{xy} = (1 - \alpha)MB_t(x, y) + \alpha I_{t+1}(x, y)$, MB_t is the mean matrix of $BM_{t:t}$ at time t and α is a learning rate factor. Then, the tensor eigenspace model is updated incrementally and so on. The IRT show more robustness to noise than the IRPCA proposed by Li *et al.* [170].

Table 16. Performance evaluation on dynamic backgrounds and illumination changes

Method	Dynamic backgrounds	Illumination changes	Indoor/outdoor scene	Applications
SG [13]	-	Slow changes	Indoor scene	Motion Capture
MOG [14]	Slow movement	Slow changes	Outdoor scene	Video Surveillance
KDE [15]	Yes	Slow changes	Outdoor scene	Video Surveillance
SL-PCA [165]	-	Yes	Outdoor scene (small objects)	Video Surveillance
SVM [180]	-	Slow changes	Outdoor scene	Video Surveillance
SVR [183]	Slow movement	Slow changes	Outdoor scene	Video Surveillance
SVDD [189]	Yes	Yes	Outdoor scene	Video Surveillance
SGG [190]	-	Slow changes	Indoor scene	Motion Capture
MOGG [194]	Slow movement	Slow changes	Outdoor scene	Video Surveillance
SL-ICA [200]	-	Yes	Outdoor scene (small objects)	Video Surveillance
SL-INMF [202]	-	Yes	Outdoor scene (small objects)	Video Surveillance
SL-IRT [205]	-	Yes	Outdoor scene (small objects)	Video Surveillance

Table 17. Computational complexity

Method	Background Initialization	Background Maintenance	Foreground Detection
SG [13]	$O(N)$	$O(1)$	$O(1)$
MOG [14]	$O(NK)$	$O(K)$	$O(K)$
KDE [15]	$O(N)$	$O(n)$	$O(1)$
SL-PCA [165]	$O(N)$	$O(N+M)$	$O(P)$
SVM [180]	$O(N)$	$O(N+t)$	$O(1)$
SVR [183]	$O(N)$	$O(1)$	$O(1)$
SVDD [189]	$O(N)$	$O(1)$	$O(1)$
SGG [190]	$O(N)$	$O(1)$	$O(1)$
MOGG [194]	$O(NK)$	$O(K)$	$O(K)$
SL-ICA [200]	$O(N)$	$O(M)$	$O(P)$
SL-INMF [202]	$O(N)$	$O(M)$	$O(P)$
SL-IRT [205]	$O(N)$	$O(M)$	$O(P)$

6. PERFORMANCE EVALUATION

We have firstly evaluated the ability of each method to deal with dynamics backgrounds and illumination changes. Then, the evaluation is conducted of per-pixel computational complexity and memory requirements.

6.1 Challenges

Table 16 groups the ability of each method to deal with dynamics backgrounds and illumination changes. The third column indicates in which type of scene the method is well suited. The related applications are indicated in the fourth column.

6.2 Computational complexity

The SG is the fastest method because the classification is just made using a threshold and the background maintenance just adapts the mean and the variance. Its complexity depends on N for the initialization. The MOG method has $O(NK)$ complexity with K the number of Gaussian distributions used, typically between 3 and 5. For maintenance, the KDE computes its value in the Gaussian kernels centered on the past n frames, thus raising $O(n)$ complexity, with n typically as high as 100. For the reconstructive subspace learning, their computational complexities are related to the operations needed to compute the elements stored and updated, i.e the

principal matrix or the eigenstructures. For example, the incremental tensor subspace learning requires $O(I_1 I_2 (R_1 + R_2 + R_3))$ operations [205]. For the foreground detection, the reconstructive subspace learning methods have an estimated complexity per pixel of $O(P)$, where P is the number of the best eigenvectors. For the background maintenance, their complexity is related to M which is the number of samples used to update the model. $M=1$ if the model is update every frame. Table 17 shows the per-pixel computational complexity of each algorithm at each stage. More details about the complexity of each algorithm can be found in their corresponding papers.

6.3 Memory requirements

For the statistical methods, the memory complexity per pixel is the same as the computational complexity. At classification time, reconstructive approaches require a memory complexity per pixel $O(P)$, with P the number of the best eigenvectors. However, at training time these methods require allocation of all the N training images, with an $O(N)$ complexity. For the reconstructive subspace learning, the memory requirements are related to the elements stored and updated, i.e the principal matrix or the eigenstructures. For example, the incremental tensor subspace learning requires $O(I_1 R_1 + I_2 R_2 + (I_1 I_2) R_3)$ memory units [205].

7. COMPARISON

We have chosen to compare different improvements of the MOG for dynamic backgrounds and the subspace learning models (SL-PCA, SL-ICA, SL-INMF and SL-IRT) for illumination changes. Results on the Wallflower dataset provided by Toyama *et al.* [20] are presented. We collected these results because of how frequent its use is in this field. This frequency is due to its faithful representation of real-life situations typical of scenes susceptible to video surveillance. Moreover, it consists of seven video sequences in which each sequence presenting one of the difficulties a practical task is likely to encounter (i.e illumination changes, dynamic backgrounds). The size of the images is 160*120 pixels. A brief description of the Wallflower image sequences can be made as follows:

- **Moved Object (MO):** A person enters into a room, makes a phone call, and leaves. The phone and the chair are left in a different position. This video contains 1747 images
- **Time of Day (TOD):** The light in a room gradually changes from dark to bright. Then, a person enters the room and sits down. This video contains 5890 images
- **Light Switch (LS):** A room scene begins with the lights on. Then a person enters the room and turns off the lights for a long period. Later, a person walks in the room, switches on the light, and moves the chair, while the door is closed. This video contains 2715 images.
- **Waving Trees (WT):** A tree is swaying and a person walks in front of the tree. This video contains 287 images.
- **Camouflage (C):** A person walks in front of a monitor, which has rolling interference bars on the screen. The bars include similar color to the person's clothing. This video contains 353 images.
- **Bootstrapping (B):** The image sequence shows a busy cafeteria and each frame contains people. This video contains 3055 images.
- **Foreground Aperture (FA):** A person with uniformly colored shirt wakes up and begins to move slowly. This video contains 2113 images.

For each sequence, the ground truth is provided for one image when the algorithm has to show its robustness to a specific change in the scene. Thus, the performance is evaluated against hand-segmented ground truth. Three terms are used in the evaluation: False Positive (FP) is the number of background pixels that are wrongly marked as foreground; False Negative (FN) is the number of foreground pixels that are wrongly marked as background; Total Error (TE) is the sum of FP and FN.

7.1 MOG and its improvements

For the first category, we compare the MOG with its main improvements. Table 18 and Fig. (5) group the experimental results found in the literature for the algorithms chosen which are:

1. **The original algorithm:** Stauffer and Grimson [14].
2. **Three intrinsic improvements:** White *et al.* [67] which used a better setting for the learning rates using Particle Swarm Optimization, Wang *et al.* [60] which modified the foreground detection step using a mixed color space i.e a normalized RGB color space for pixels with high intensities and in RGB color space for pixels with low intensities and Setiawan *et al.* [97] which used the IHLS space.
3. **Three extrinsic improvements:** Schindler *et al.* [109] which used the MRFS to smooth the results spatially, Cristani *et al.* [117] which proposed the Spatial-Time Adaptive Per Pixel Mixture Of Gaussian called S-TAPPMOG and Cristani *et al.* [118] which used an adaptive spatio-temporal neighborhood analysis called ASTNA. For these two last algorithms, the authors don't give the result for the following image sequences: Moved Object, Time of Day and Light Switch. So, we have indicated for these the Total Error without these image sequences.

From Table 18, we can see that the original MOG gives the bigger total of error. A better setting of the learning rate and the threshold T using the PSO [67] divides approximately by 2 the number of total errors. The use of the IHLS color space [97] decreases a lot the number TE which becomes just under 10 000. The improvement proposed by Wang *et al.* [60] gives the better results for the intrinsic improvements. For the extrinsic improvements, the best results are obtained by MOG using MRF proposed by Schindler *et al.* [109] followed by S-TAPPMOG [117] and ASTNA [118]. For all the methods, the image sequences Light Switch (LS) gives the larger amount of false positive. Here, the best result is obtained by the method proposed by Schindler *et al.* [109]. The use of IHLS [97] gives it best improvement for the image sequences Camouflage (C) and for the method proposed by Wang *et al.* [30], it is the image sequences Waving Trees (WT). In conclusion, this performance evaluation shows that taking into account spatial and temporal consistency improves the results in a significant way. Fig. (6) presents the overall performance for the five first algorithms. It is not intended to be a definitive ranking of these algorithms. Such a ranking is necessarily task-, sequence-, and application dependent.

Fig. (5). Results on the Wallflower dataset [26] for the MOG and its improvements.

Sequence	MO	TD	LS	WT	C	B	FA
Test image							
Ground Truth							
MOG Stauffer <i>et al.</i> [14]							
MOG with PSO White <i>et al.</i> [67]							
MOG using IHLS Setiawan <i>et al.</i> [97]							
Improved MOG Wang <i>et al.</i> [60]							
MOG with MRF Schindler <i>et al.</i> [109]							
S-TAPMOG Cristani <i>et al.</i> [117]	-	-	-				
ASTNA Cristani <i>et al.</i> [118]	-	-	-				

Table 18. Comparison on the Wallflower dataset [26] for the MOG and its improvements.

Algorithm		Problem Type							TE
		MO	TD	LS	WT	C	B	FA	
MOG [14]	FN	0	1008	1633	1323	398	1874	2442	27053
	FP	0	20	14169	341	3098	217	530	
MOG with PSO [67]	FN	0	807	1716	43	2386	1551	2392	13916
	FP	0	6	772	1689	1463	519	572	
MOG-IHLS [97]	FN	0	379	1146	31	188	1647	2327	9739
	FP	0	99	2298	270	467	333	554	
Improved MOG – FD [60]	FN	0	597	1481	44	106	1176	1274	7081
	FP	0	358	669	288	413	134	541	
MOG with MRF [109]	FN	0	47	204	15	16	1060	34	3808
	FP	0	402	546	311	467	102	604	
S-TAPPMOG [117]	FN	-	-	-	153	643	1414	1912	7844
	FP	-	-	-	1152	1382	811	377	
ASTNA [118]	FN	-	-	-	253	823	2349	1900	7031
	FP	-	-	-	100	1173	73	360	

Fig. (7). Results on the Wallflower dataset [26] for the subspace learning models.

Sequence	MO	TD	LS	WT	C	B	FA
Test image							
Ground truth							
SL-PCA Oliver <i>et al.</i> [165]							
SL-ICA Tsai and Lai [200]							
SL-INMF Bucak <i>et al.</i> [202]							
SL-IRT Li <i>et al.</i> [204]							

Table 19. Comparison on the Wallflower dataset [26] for the subspace learning models.

Algorithm		Problem Type							TE
		MO	TD	LS	WT	C	B	FA	
SL-PCA [165]	FN	0	879	962	1027	350	304	2441	17677
	FP	1065	16	362	2057	1548	6129	537	
SL-ICA [200]	FN	0	1199	1557	3372	3054	2560	2721	15308
	FP	0	0	210	148	43	16	428	
SL-INMF [202]	FN	0	724	1593	3317	6626	1401	3412	19098
	FP	0	481	303	652	234	190	165	
SL-IRT [204]	FN	0	1282	2822	4525	1491	1734	2438	17053
	FP	0	159	389	7	114	2080	12	

7.2 Subspace learning models

SL-PCA which is from the first category is compared with the subspace learning models from the third category: SL-IRT, SL-PCA and SL-INMF. Table 19 and Fig. (7) group the experimental results found in the literature for the subspace learning algorithms. From Table 19, we can see that SL-ICA gives the smallest TE followed by SL-IRT, SL-PCA and SL-INMF. Fig. (8) shows the overall performance. This ranking has to be taken with precaution because a poor performance on one video influences the TE and then modifies the rank. The main interpretation is that all the models are robust to illumination changes as can be seen on the sequence called “Time of Day” (TD) and “Light Switch” (LS). Otherwise, the subspace learning algorithms are more or less adapted for specific situations. For example, only SL-PCA gives FP in the sequence called “Moved Objects” (MO) due the fact that the model is not update overtime. In the same way, SL-INMF gives the biggest total error due to its results on the sequence called “Camouflage” (C). This is confirmed by the Fig. (9). which shows the performance without this sequence. In this case, SL-INMF is the second in term of performance. SL-ICA has globally good performance except for the sequence called “Bootstrap” (B) by giving less true detection.

SL-IRT seems to be more efficient in the case of camouflage. SL-PCA gives less FN than FP. For SL-ICA, SL-INMF and SL-IRT, it is the contrary. We can remark that SL-ICA provides very less FP than FN. It is interesting in video-surveillance because it decreases false alarms.

Fig. (6). Overall performance on the Wallflower dataset [26] for the MOG and its improvements.

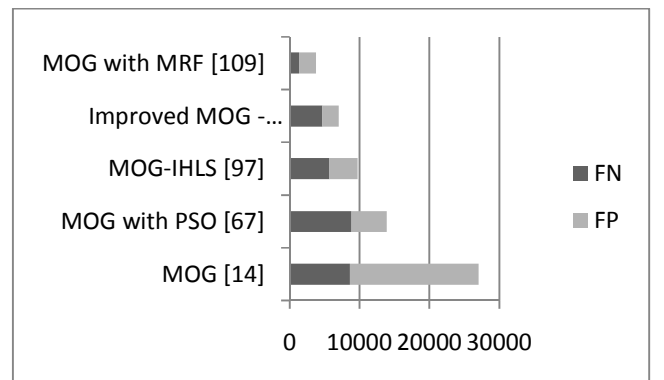


Fig. (8). Overall performance on the Wallflower dataset [26] for the subspace learning models.

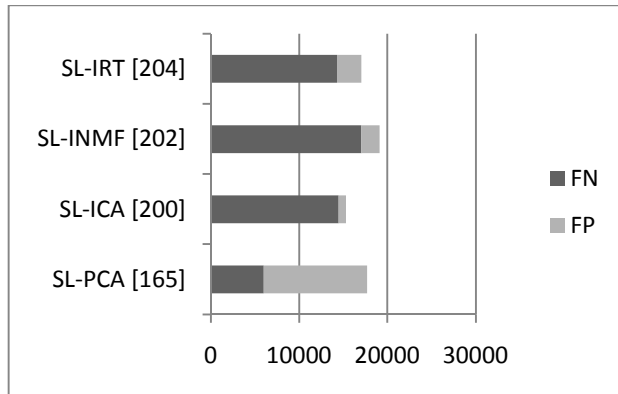
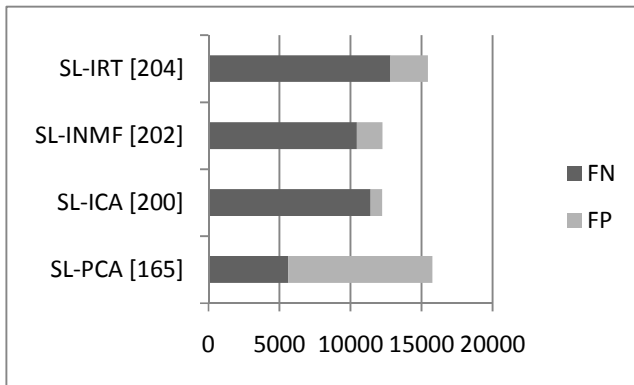


Fig. (9). Overall performance on the Wallflower dataset [26] without the sequence called “Camouflage” for the subspace learning models.



8. CURRENT & FUTURE DEVELOPMENTS

This paper attempts to provide a comprehensive survey on statistical background modeling for foreground detection and to provide some structural categories for the strategies developed in 300 papers and 10 recent patents. Thus, we proposed a classification in term of category. For the MOG and KDE, we proposed a classification for their related improvements in two classes respectively called intrinsic and extrinsic improvements. Strategies adding spatial and temporal information in the different steps or in added process proved their abilities to improve the robustness of the original model to the critical situations. Cooperation with other segmentations has shown their interests too. Methods which reduce the computation time permit to deal with the constraints of real-time application. Although significant progress has been made, there is still work to be done and we believe that a systematic comparative evaluation must be made and thus determine the best combination of strategies. In this context, we encourage the evaluation using the Wallflower dataset like in [60, 67, 97, 109].

Furthermore, two main investigations seem to be very promising:

- For dynamic backgrounds, combination between SG, MOG and KDE [337-339] which allows to gives more robustness when there are waving trees, water surfaces and water rippling in the scene.
- For illumination changes, robust PCA [340-344] in which the background is modeled by a low rank subspace that can gradually change over time, while the moving foreground objects are considered as the correlated sparse outliers.

In conclusion, this paper allows the reader to survey recent advances on statistical background modeling and it can effectively guide him to select the best improvement for his specific application. Particularly, this survey paper allows: 1) Developers to choose the appropriate improvement to tackle the critical situations met in their application. 2) Researchers to have a recent state-of-the-art and so easily identify new ideas. 3) Reviewers to verify quickly the originality of a paper.

9. ACKNOWLEDGMENTS

The authors would like to thanks Serhat Selcuk BUCAK (Pattern Recognition and Image Processing Lab, Michigan State University, USA) who provided the results obtained by his algorithm SL-INMF, Du-Ming TSAI and Shia-Chih LAI (Department of Industrial Engineering and Management, Yuan-Ze University, Taiwan) who provided the results obtained by their algorithm SL-ICA.

CONFLICT OF INTEREST

The author declared no conflict of interest

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