Enhanced properties for ultrasonic transduction, phase transitions and thermal depoling in $0.96(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3$ - 0.04BaTiO_3 submicrometre-structured ceramics

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Enhanced properties for ultrasonic transduction, phase transitions and thermal depoling in $0.96(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3\text{-}0.04\text{BaTiO}_3$ submicron structured ceramic

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Abstract:

Submicron structured (grain size $\approx 500\text{nm}$), dense $(\text{Bi}_{0.5}\text{Na}_{0.5})_{0.96}\text{Ba}_{0.04}\text{TiO}_3$ ceramics were obtained from sol-gel autocombustion nanopowders by hot-pressing ($700\text{-}950^\circ\text{C}$) and subsequent recrystallization ($1000\text{-}1050^\circ\text{C}$). Electromechanical coefficients were obtained by analysis of the resonance spectra of thin disks using Alemany et al. software. The real part of the room temperature set of coefficients of the best performing materials ($\epsilon_{33}^0 = (416 - 16i)$, $d_{31} = (-22.68 + 0.55i) \text{pC/N}^{-1}$, $k_t = 44.5\%$, $k_p = 21.1\%$) can be compared with those of coarse-grained ceramics and d_{33} (95pC.N^{-1}) is higher. Shear related coefficients were obtained from thickness poled and length excited plates ($\epsilon_{11}^0 = (402 - 89i)$, $d_{15} = (108.3 - 21.4i) \text{pC.N}^{-1}$ and $k_{15} = 39.2\%$). At the depolarization temperature, $T_d = 153^\circ\text{C}$, the dielectric loss, $\tan\delta(T)$, of poled samples shows a maximum and the planar resonance virtually vanishes. Shear resonance of thickness-poled plates and weak planar electromechanical resonance are observed above T_d . The relaxor behaviour extends up to the isotropization point, $T_i = 238^\circ\text{C}$. This can be understood as due to the coexistence of the room temperature ferroelectric phase in the stability range of the low temperature non-polar phase at zero field, between T_d and T_i .

PACS: Dielectric materials, oxides, 77.84.Bw; piezoelectric materials, 77.84.-s; electromechanical resonance, 77.65.Fs; materials treatment effects on Microstructure, 81.40.-z; Structure of crystalline solids, 61.66.-f

Introduction

Within the expanding area of the study of lead-free piezoelectrics, the $(1-x)(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3-x\text{BaTiO}_3$ (BNT-BT) (BNBT100x) solid solution system [1] is being an area of high interest due to the peculiarities of its crystal structure [2]. Recently [3,4] it has been found that the phase diagram of unpoled ceramics differs from the one of poled ceramics, due to the electric-field induced phase transition observed for compositions near the MPB in BNT-based solid solution systems [5-8]. The nearly vertical Morphotropic Phase Boundary (MPB) composition, at $x \approx 0.06$ for unpoled ceramics, can be shifted towards lower x values by the action of an electric field [2,7], which induces a ferroelectric phase. Due to these peculiarities, the electromechanical properties at the MPB are not as high as expected by similitude with the $\text{Pb}(\text{Zr,Ti})\text{O}_3$ system. Another drawback of the MPB composition for some applications is that depoling temperature, at which most of the electromechanical activity vanishes by a mechanism still unclear, is low ($T_d \approx 100^\circ\text{C}$) [9].

When moving away from the MPB composition towards the $(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3$ side of the phase diagram, T_d increases approaching that of BNT ($T_d \approx 187^\circ\text{C}$) [10] and the electromechanical coupling factors show higher anisotropy, i.e., higher ratio k_t/k_p for the thickness and radial modes of thin disks, thickness poled [11]. In such a range of compositions, the reported electromechanical characterization in the ultrasonic range for $x=0.04$ (BNBT4) ceramics is incomplete, lacking parameters related to shear modes of resonance. Shear coefficients have a key importance for 3D modeling of piezoceramics by numerical methods [12] due to the increasing number of their applications that are based on shear modes.

An issue in the preparation of BNBT ceramics is the loss of volatiles (Bi, Na) at the high sintering temperatures required ($T > 1100^\circ\text{C}$), which leads to a.c. losses and d.c. conductivity that limits the poling and, consequently, the piezoelectric performance of the ceramics [10]. Sol-gel combustion synthesis [13] provides highly reactive nanopowder at moderate synthesis temperature (500°C). Dense, submicron structured BNBT6 ceramics with good stoichiometry and properties that can be compared with those of coarse grain ceramics have been obtained by hot-pressing powder produced by sol-gel combustion and further recrystallization at $T \leq 1050^\circ\text{C}$ [14,15]. Processing of ceramics from nanopowders allows nowadays to obtain fine grain ceramics. These are of interest for both the basic studies of size-effects in ferroelectrics and for their use as high frequency ultrasonic transducer materials, since they allow the miniaturization of the components.

Submicron structured BNBT4 ceramics from nanopowder, prepared by hot-pressing and recrystallization, are studied in this work as candidates for ultrasonic transducer materials. Electromechanical characterization in the ultrasonic range is carried out from the resonances of thin disks, thickness poled and excited, and thickness-poled shear plates, length excited. Alemany et al. software [16,17,18] is here used to analyze the impedance spectra at resonance and to calculate complex material coefficients. The thermal evolution of the dielectric permittivity and losses, as well as the one of the planar and shear modes of resonance, is also determined to evaluate the working range of the material.

Experimental method

$(1-x)(\text{Bi}_{0.5}\text{Na}_{0.5})\text{TiO}_3\text{-}x\text{BaTiO}_3$ with $x=0.04$ (BNBT4) nanometric powder was synthesized by a citrate, nitrate sol-gel auto-combustion method, as explained elsewhere [13]. In this process, the pure perovskite phase is directly obtained by heating the gel at 500°C. Pellets of the powder of 15 mm diameter and 1 mm thickness were obtained by uniaxial pressure forming followed by cold isostatic pressing at 200 MPa. A combination of hot-pressing at low temperature (700-950°C for 2h, at 20MPa in air, using heating and cooling rates of 3°C.min⁻¹) and subsequent recrystallization at higher temperature (1000 and 1050°C for 1-2h in air) has been applied to sinter the green pellets. The BNBT4-1 to 3 ceramics studied were obtained with variable grain size and density to determine the microstructure leading to the optimum properties. Ceramics were characterized using X-ray diffraction (XRD, Siemens D500) and scanning electron microscopy (FEG-SEM, NOVA NANOSEM 230 with beam deceleration module) and their density was obtained by Archimedes method. Computer assisted quantitative microstructural characterization (MIP45 Digital Image System) was carried out by analysis and measurements of images of SEM and optical microscopy (OM, Leitz Laborlux 12 MES/ST). Both mean grain and pore size ($\langle G \rangle$ and $\langle P \rangle$) of the ceramics were determined as the equivalent diameter to a circular shape ($D_{\text{eq}}=4(S/\pi)^{1/2}$, where S =grain or pore surface area) and from the analysis of the measured lognormal distributions of equivalent diameter [19] that also provides the corresponding standard deviations (σ_G and σ_P).

Sintered disks were ground to a thickness (t) to diameter (D) ratio below 1/20 (typically $t=0.7$ mm and $D=15$ mm) and Ag electrodes were attached at their major faces for the electric poling and for the impedance measurements at the radial and thickness resonance modes. Rectangular plates of lateral dimensions (L,w) to thickness (t) aspect ratio below 1/10 (typically $t=0.7$ mm and $L,w=8-9$ mm) were also cut from the sintered ceramic disks, electroded and

thickness poled. Poling electrodes were mechanically removed and a new pair of electrodes was applied on two of their perpendicular faces for the impedance measurements.

Owing to the reduced d.c. ceramic conductivity, it was possible to carry out poling of disks and plates in a silicone oil bath at $T_p=150-180^\circ\text{C}$ up to fields of 45 kV.cm^{-1} . Hot-poling took place for 30 minutes and the samples were cooled to room temperature with the field applied. The d_{33} piezoelectric coefficient was measured in a Berlincourt-meter.

Piezoelectric coefficients of ferroelectric ceramics are currently calculated using standard methods [20,21] from the measurements of complex impedance data at the electromechanical resonances. To overcome the well-known limitations of standard methods when dealing with material losses, alternative methods have been developed and will be used in this work. Fine-tuning of the thickness of the shear plates was carried out to minimize the coupling of the fundamental shear mode with other plate modes [12].

Complex impedance measurements at resonance were carried on using a HP4192A impedance analyzer controlled via a GPIB-PCIIA (National Instruments) interface board. Alemany et al. software [16,17,18] was used here for the calculation of the complex piezoelectric, elastic and dielectric coefficients in each mode of resonance, as well as for the determination of the corresponding electromechanical coupling factors and frequency numbers. After the calculation of the complex parameters, the resonance spectrum is reconstructed as an accuracy test of the final set of calculated coefficients, quantified by the regression factor (R^2) of such reconstruction.

Impedance measurements as a function of the temperature were carried out at various frequencies in the range between 1kHz and 1MHz with a HP4194A analyzer. The heating and cooling rates were 2°C/min . From these experimental data and the geometric factor thickness/area, the relative dielectric permittivity $\epsilon^* = \epsilon' - i\epsilon''$, and dielectric losses, $\tan\delta = \epsilon''/\epsilon'$ were obtained. This experimental set-up was also used for determination of the resonance spectra as a function of temperature.

Experimental results

Fig.1 shows the XRD patterns of the unpoled ceramics. All of them have a single phase distorted perovskite type structure to the resolution of the technique. Peaks are indexed for a $R3c$ rhombohedral symmetry, BNT-like, in hexagonal description (JCPDS file #70-9850). However, due to proximity to the MPB, signs of mixed phases [7] are observed in the unpoled samples. Fig. 2 shows, as an example, two selected 2θ ranges in the XRD patterns of the BNBT4-

1 ceramic, around $40^\circ 2\theta$ the doublet (006),(202) and around $46.5^\circ 2\theta$ the (024) peak, before and after poling. A clear field-induced phase transition with change of crystal symmetry is not observed in any of the ceramics, but the (024) peak becomes sharper, i.e., the rhombohedral character is enhanced. The texture change due to domain orientation during poling is observed by the change in relative intensity in the (006),(202) doublet. These changes are in agreement with recently reported results [7].

The results of the quantitative characterization of the microstructure of the samples (relative density and number of objects measured in the micrographs, average values and standard deviation of the distributions) are reported in Table I. Fig. 3 shows the SEM images from which the values of average grain size, shown in Table I, were calculated. Fig. 4 shows an example of the intermediate steps in the quantitative microstructural analysis and size distributions of grain (from SEM images) and pore (from OM images).

Fig. 5 shows the resonance spectra (resistance and conductance peaks, real parts of the complex impedance, $Z^* = R + iX$, and admittance, $Y^* = G + iB$, respectively) of the radial or planar (Fig. 5(a)) and thickness (Fig. 5(b)) modes of, thickness poled and excited, thin disk and the shear mode of, thickness-poled and length excited, shear plate (Fig. 5(c)) of BNBT4-2 ceramic. Both the experimental (symbols) and reconstructed spectrum (lines) are shown for each resonance.

Table II summarizes the relative density, range of grain size, d_{33} from Berlincourt-meter and the piezoelectric (h_{33} , e_{33} , d_{31} , g_{31}), elastic (C_{33}^D , C_{11}^D , S_{11}^E , S_{12}^E , S_{66}^E) and dielectric (ϵ_{33}^S , ϵ_{33}^σ) linear coefficients, including all losses, which are calculated from the measured radial and thickness resonances of thin disks. The Poisson ratio, electromechanical coupling factors (k_p , k_t) and frequency numbers (N_p , N_t) are shown in Table II. Similarly, Table III summarizes the material data (e_{15} , d_{15} , h_{15} , g_{15} , C_{11}^D , S_{55}^E , ϵ_{11}^S , ϵ_{11}^σ , k_{15} , N_{15}) obtained from the shear resonance of thickness poled plates. Tables II and III show also published data for dense BNBT6 and BNBT4 ceramics obtained by different processing routes [11, 22, 23] and for BNT ceramics [10].

Fig. 6 shows the real part of the relative dielectric permittivity and the dielectric loss as a function of the temperature for the BNBT4-1 sample. Results are shown for the unpoled ceramic, both measuring on heating and cooling, as well as for the poled ceramic measured on heating and for the thermally depoled ceramic measured on cooling. The observed differences can be discussed in terms of the structural changes induced by the poling field.

Fig. 7 shows for BNBT4-2 the evolution with the temperature of conductance peak, characteristic frequencies and electromechanical coupling factors of the planar resonance of a thin disk and the shear resonance of a thickness-poled plate.

Discussion

1. Electromechanical properties at room temperature

As shown in Tables I to III, the properties of dense and submicron structured BNBT4-2 and 3 ceramics are in good agreement with previously reported values for coarser grained BNBT4 ceramics prepared at higher temperatures [11]. BNBT4-1 ceramic shows similar grain size, but lower relative density (Table I) and, therefore, higher porosity, than BNBT4-2 and 3. This results in higher compliance and mechanical and dielectric losses, as well as lower coupling coefficients (Table II). The optimum set of properties is found for the combination of submicron grain size and low porosity of BNBT4-2 (Tables II and III). This can be understood as a consequence of a good stoichiometry, arising from the low processing temperatures, and homogeneous microstructure (Figs. 1 and 3) that reduces conductivity and losses and allows efficient poling at relatively high temperature.

BNBT4-2 and 3 ceramics show values of the properties in between those of BNBT6 and BNT composition. The dielectric permittivity (ϵ_{33}^0) is lower than in BNBT6 and higher than in BNT; the thickness coupling factor and electromechanical anisotropy are higher ($k_t/k_p = 2.2$) than in BNBT6 ($k_t/k_p = 1.5$), approaching the value of BNT, whereas d_{33} piezoelectric coefficient is higher than in BNT, approaching the value of BNBT6 (Table II).

The comparison of the data obtained in submicron structured ceramics from nanopowder evidences that the dielectric losses, as well as the piezoelectric e_{33} , d_{31} , g_{31} are lower for the BNBT4 composition than for the BNBT6. Also, when comparing real values of all elastic s_{ij}^E coefficients and the frequency numbers it is observed that BNBT4 ceramic is similar to BNBT6 from the mechanical point of view, but the losses are also lower.

Table III shows the characterization for the shear mode in which, again, we found that values of BNBT4 properties are intermediate from those of BNBT6 and BNT. The free permittivity (ϵ_{11}^0), the shear coupling factor and the d_{15} piezoelectric coefficient of BNBT4 are higher than those of BNT, approaching the values of BNBT6.

Besides these interesting properties and just as an example among the many studies on doping BNBT ceramics to enhance electromechanical performance, CaO/MnO co-doping [24] has shown efficiency in increasing d_{33} , k_p and k_t . At the same time the depolarization temperature is almost unchanged, the sinterability increases and the grain size of the ceramics is reduced. Therefore, routes for further improvement of the properties of pure BNBT4 ceramics for ultrasonic transduction purpose by doping are available.

II. Temperature evolution of the permittivity and electromechanical properties

The curves of the real part of the dielectric permittivity as a function of temperature have a maximum at $T_m = 275^\circ\text{C}$ and are dispersive up to $\sim 238^\circ\text{C}$ on heating and $\sim 225^\circ\text{C}$ on cooling (Fig. 6). This upper limit temperature for the dispersive region is often ascribed in BNT-based compositions [1] to T_{R-T} , the transition temperature from the room temperature ferroelectric (rhombohedral) (FE(R)) phase to the antiferroelectric (tetragonal) (AFE(T)) phase by similitude with BNT. However, it resembles more to the isotropization point (T_i) of the optical properties of BNT ($T_{R-T} < T_i < T_m$), which is associated to a local maximum in the first derivative of the real part of the dielectric permittivity vs. temperature curve $d\epsilon'/dT$ [25]. Early interpretation of T_i on cooling involved the percolation phenomena of the AFE regions that begin to form at T_m within the ferroelastic twins formed in the paraelectric-ferroelastic (PE-Felas) phase, stable above T_m . This ferroelastic twins originates on cooling from the paraelectric-paraelastic (PE-Pelast) cubic phase, stable above 540°C for pure BNT. The percolation of the AFE regions creates long-range AFE order in the crystal. On heating, the complete separation of AFE regions at T_i can only take place when a critical density of PE-Felast interlayer takes place. This requires a higher temperature, thus the observed thermal hysteresis of T_i . It is clear that the temperature of formation on cooling and destruction on heating of the long range ordered AFE phase will correspond to the most unstable state of the crystal and thus to a $d\epsilon'/dT$ local maximum. The AFE character of the BNT-based compositions is under discussion. The term Low Temperature Non-Polar at Zero Field phase (LTNPZF), which would account with the pinched hysteresis loops characteristic of the phase taking place above T_{R-T} , seems more appropriated [26]. The depolarization temperature for BNBT4 is the temperature at which the ferroelectric long-range order and macroscopic ferroelectric properties disappear, T_{R-T} or, more properly, $T_{FE-LTNPZF}$. A recent work [3] has coined the term antiferroelectric-relaxor, which will account with the dielectric dispersion found in the range of stability of this phase, between $T_{FE-LTNPZF}$ and T_i .

On heating of the poled sample, $T_d = T_{FE-LTNPZF}$ is revealed by the sharp jump in the real part of the permittivity and the maxima of the losses at $\sim 153^\circ\text{C}$ for BNBT4 (Fig. 6), in good agreement with previous results from depolarization current [11]. Whereas there are not differences in the curves of the real part of the permittivity versus temperature measured on cooling, the difference between measurements on heating of the samples before and after poling is clear, being $\epsilon'_{33}(\text{poled}) > \epsilon'(\text{unpoled})$ in the interval between $T_d = T_{FE-LTNPZF}$ and T_i (Fig. 6).

As shown in Fig. 7, for $T_d \approx 150^\circ\text{C}$ we found $f_s \approx f_p$ in the resonance spectrum of the planar mode as a function of the temperature. The electromechanical coupling factor calculated using standard methods vanishes at T_d . However, a weak resonance spectrum was observed up to higher temperatures and it is possible to obtain $k_p \neq 0$ up to $T \approx 230^\circ\text{C}$ using Alemany et al. software (Fig. 7). This residual macroscopic piezoelectricity indicates that, although the long-range FE order disappear at T_d , it may exist a medium-range order [27] by coexistence of FE clusters in the LTNPZF phase above T_d , also reflected in the differences of the permittivity before and after poling between $T_{\text{FE-LTNPZF}}$ and T_i . Such a medium-range order progressively disappears as the temperature increases towards T_i . For BNT [28] and BNT-BKT-BT [5] ceramics a weak piezoelectric activity above $T_{\text{FE-LTNPZF}} = 200^\circ\text{C}$ and 177°C , respectively, was also previously reported.

When the shear resonance is studied in a similar manner, the observed depolarization temperature, as defined by the point in which $f_s \approx f_p$, is found at a higher temperature ($T_d^{\text{SH}} \approx 175^\circ\text{C}$) (Fig. 7). The electromechanical anisotropy here observed reveals the complexity of the depolarization process of these samples. This anisotropy could arise from a texture developed during hot-pressing or by a mechanism of progressive disappearance of the FE clusters that reduces first the polarization extension mechanisms and, at higher temperature, the polarization rotation mechanisms associated to the shear mode. Dielectric anisotropy has been reported for BNT ceramics [10]. The full explanation of the mechanism underlying these effects exceeds the purpose of this work and demands additional structural information. It is clear, however, from the results in Fig. 7 that the working range of BNBT4 ceramics extends to higher temperatures than the currently reported T_d when the applications are based on shear resonances.

Conclusions

Submicron structured, dense $(\text{Bi}_{0.5}\text{Na}_{0.5})_{1-x}\text{Ba}_x\text{TiO}_3$ ceramics with $x=0.04$ were obtained and studied as candidates for lead-free ultrasonic transducer materials. For BNBT4 ceramics, the free permittivity ($\epsilon_{33}^\sigma, \epsilon_{11}^\sigma$), the k_t and k_{15} coupling factors and electromechanical anisotropy (k_t/k_p) are higher than for BNBT6. The d_{33} , d_{31} and d_{15} piezoelectric coefficient are higher in BNBT4 than in BNT, approaching the values for BNT6. The comparison of ceramics from sol-gel auto-combustion nanopowder also evidences that BNBT4 ceramics have lower dielectric, mechanical and piezoelectric losses than BNBT6 ceramics. BNBT4 has higher depolarization temperature than BNBT6, which is $T_d \approx 150^\circ\text{C}$ when determined from dielectric

loss measurements in poled samples and thermal evolution of the radial mode spectrum. Finally, an electromechanical anisotropy was observed during the thermal depolarization. The depolarization temperature from the evolution of the shear mode spectrum is found to be $T_d^{SH} \approx 175^\circ\text{C}$.

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Figure captions

Fig. 1. XRD pattern of BNBT4 ceramics.

Fig. 2. Selected peaks of the XRD pattern of the BNBT4-1 (HP700°C-2h+1050°C-1h) ceramic before and after poling : (a) around $40^{\circ}2\theta$ the doublet (006),(202) and (b) around $46.5^{\circ}2\theta$ the (024) peak.

Fig. 3. SEM micrographs of ceramic surfaces polished and quenched from 800°C to room temperature: (a) BNBT4-1 (HP700°C-2h+1050°C-1h), (b) BNBT4-2 (HP800°C-2h+1050°C-1h) and (c) BNBT4-3 (HP950°C-2h+1000°C-2h).

Fig. 4. Steps of the process of quantitative microstructural characterization of the BNBT4-2 (HP800°C-2h+1050°C-1h) ceramics: original grey level images from microscopy, objects identified in the corresponding digital images for the measurement of their areas and lognormal distributions of grain (Figs. (a)-(c)) and pore (Figs. (d)-(f)) equivalent diameters.

Fig. 5. Resonance spectra of BNBT4-2 ceramic thin disk (Figs. (a) and (b)) and shear plate (Fig. (c)). Experimental (symbols) and reconstructed (lines) spectra after calculation of coefficients by Alemany et al. software are shown for all resonances.

Fig. 6. BNBT4-1 ceramic: dielectric permittivity, real part and losses, of unpoled samples on heating and cooling (Figs. (a) and (b)) and after poling (Figs. (c) and (d)) on heating and on cooling of the thermally depoled sample. Arrows indicate the increasing measurement frequency (1, 2, 5, 10, 50, 100, 200, 500 and 1000 kHz).

Fig. 7. Thermal dependence of the conductance peaks (Figs. (a) and (b)) and of the characteristic frequencies and electromechanical coupling factors for the radial mode of a thickness poled and excited thin disk (Fig. (c)) and the shear mode of a thickness-poled and length excited shear plate (Fig. (d)) of BNBT4-2.

Table captions

Table I. Results of the quantitative characterization of the ceramic microstructure: density and characteristics of the lognormal distributions of equivalent diameters of grains (from SEM images) and pores (from OM images).

Table II. Piezoelectric, elastic and dielectric parameters, electromechanical coupling factors and frequency numbers, obtained from measurement of the planar (P) and thickness (T) resonances of thin disks of BNBT4 ceramics, poled and excited in thickness. Data from the literature are also shown for comparison.

Table III. Piezoelectric, elastic and dielectric parameters, as well as electromechanical coupling factors and frequency numbers, obtained from the shear resonance of plates of BNBT4 ceramics, thickness poled and length excited. Data from the literature are also shown for comparison.

Table I.

Composition, Synthesis route, Processing conditions	BNBT4 sol-gel autocombustion HP + recrystallization		
	BNBT4-1 700°C-2h/ 1050°C-1h	BNBT4-2 800°C-2h/ 1050°C-1h	BNBT4-3 950°C-2h/ 1000°C-2h
relative density (%)	93%	95%	98%
mean size <G> (nm) SEM	(520 ± 10)	(560 ± 10)	(510 ± 10)
σ_G (nm) SEM	(550 ± 20)	(600 ± 20)	(500 ± 20)
Number of measured grains SEM	722	695	789
mean size <P> (nm) OM	(2600 ± 40)	(3850 ± 30)	(630 ± 40) (1830 ± 9)
σ_P (nm) OM	(400 ± 10)	(470 ± 6)	(600 ± 60) (250 ± 4)
Number of measured pores OM	2022	842	633

Table II.

Composition, Synthesis route, Processing conditions	BNBT4 sol-gel autocombustion HP + recrystallization			BNBT6 sol-gel autocombustion HP 800°C-2h + recrystallization 1050°C-1h [22]	BNBT4 mixed oxides sintering 1160-1180°C/1h [11]	BNBT6 mixed oxides sintering 1160-1180°C/1h [11]	BNT mixed oxides sintering 1100°C/2h [10]
	BNBT4-1 700°C-2h/ 1050°C-1h	BNBT4-2 800°C-2h/ 1050°C-1h	BNBT4-3 950°C-2h/ 1000°C-2h				
Berlincourt d_{33} (10^{-12}C.N^{-1})	100	95	99	148	87	122	72.9
R^2	0.9997	0.9998	0.9996	0.9999	NA	NA	NA
R^2	0.9734	0.8987	0.8460	0.9548	NA	NA	NA
k_p (%)	19.6	21.1	21.1	26.8	21	29	16.8
N_p (kHz.mm)	2980	3054	3125	2933	3000	3000	3260
k_{31} (%)	11.8	12.6	12.6	15.74	---	---	10.2
k_t (%)	41.3	44.5	44.3	40.4	45	40	45.5
N_t (kHz.mm)	2268	2288	2348	2281	2570	2522	2780
ϵ_{33}^{σ}	435 – 18i	416 - 16 i	475 – 20i	641 – 31i	445 (1KHz)	601 (1KHz)	343 (1MHz)
$\tan \delta$ (ϵ_{33}^{σ})	0.041	0.037	0.042	0.048	0.021	0.018 (1KHz)	0.028 (1MHz)
ϵ_{33}^s	330 – 15i	318 - 10 i	360 – 15i	456-31 i	---	---	---
h_{33} (10^8 V/m)	27.8 + 26i	31.8 + 0.14 i	30.3 + 0.46i	23.4 - 0.07 i	---	---	---
e_{33} (C.m ²)	8.13 – 0.30i	8.95 - 0.25 i	9.68 – 0.25i	9.46-0.67i	---	---	---
d_{31} (10^{-12} C.N ⁻¹)	- 22.4 + 0.53i	- 22.7 + 0.55 i	- 23.7 + 0.54i	- 37.0 + 1.33i	---	---	-15.0
g_{31} (10^{-3} m.V.N ⁻¹)	- 5.82 – 0.10i	- 6.16 - 0.08 i	- 5.63 – 0.11i	- 6.51 – 0.08i	---	---	---
c_{33}^D (10^{10} N.m ²)	13.26 + 0.48i	12.77 + 0.39 i	14.98 + 0.73i	13.62 + 0.45i	---	---	---
c_{11}^D (10^{10} N.m ²)	11.87 + 0.06 i	13.16 + 0.06 i	13.30 + 0.07i	11.94 + 0.08i	---	---	---
Poisson ratio	0.28	0.29	0.30	0.31	0.25	0.25	0.263
s_{11}^E (10^{-12} m ² N ⁻¹)	9.36 – 0.05i	8.86 - 0.04 i	8.49 – 0.04i	9.73 – 0.07i	---	---	7.07
s_{12}^E (10^{-12} m ² N ⁻¹)	- 2.59 + 0.01i	- 2.59 + 0.01 i	- 2.51 + 0.01i	- 3.02 + 0.02i	---	---	---
s_{66}^E (10^{-12} m ² N ⁻¹)	23.90 – 0.12i	22.89 - 0.11 i	21.99 – 0.11i	25.52-0.19i	---	---	---

Table III.

Composition, Synthesis route, Processing conditions	BNT4 sol-gel autocombustion HP + recrystallization BNT4-2 800°C-2h/1050°C-1h	BNT6 sol-gel autocombustion HP + recrystallization 800°C-2h /1050°C-1h [22]	BNT6 mixed oxides sintering 1200°C 2h [23]	BNT mixed oxides sintering 1100°C 2h ref. [10]
R^2	0.7939	0.9847	NA	NA
$K_{15}(\%)$	39.2	40.2	49.8	36.2
$N_{15}(\text{kHz}.\text{mm})$	1423	1373	1568	1650
ϵ_{11}^s	343 - 67 i	609 - 29j	---	---
ϵ_{11}^o	402 - 89 i	726 - 40i	373 (1KHz)	367(1MHz)
$e_{15}(\text{C}.\text{m}^2)$	5.00 - 0.80 i	6.55 - 0.23i	---	---
$d_{15}(10^{-12} \text{ C}.\text{N}^{-1})$	108.3 - 21.4 i	158.3 - 8.31i	194	87.3
$h_{15}(10^8 \text{ V}.\text{m}^{-1})$	16.37 + 0.55 i	12.16 + 0.16i	---	---
$g_{15}(10^{-3} \text{ m}.\text{V}.\text{N}^{-1})$	30.30 + 0.66 i	24.64 + 0.05i	---	---
$s_{55}^E(10^{-12} \text{ m}^2.\text{N}^{-1})$	21.80 - 0.80 i	24.17 - 0.42i	23.3	17.9

Fig. 1.

Fig. 2.

Fig. 3.

Fig. 4.

Fig. 5

Fig. 6

Fig. 7.