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A spatio-temporal model to describe the spread of *Salmonella* within a laying flock

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Abstract

Salmonella is one of the major sources of toxi-infection in humans, most often because of consumption of poultry products. The main reason for this association is the presence in hen flocks of silent carriers, i.e. animals harbouring *Salmonella* without expressing any visible symptoms. Many prophylactic means have been developed to reduce the prevalence of *Salmonella* carrier-state. While none allows a total reduction of the risk, synergy could result in a drastic reduction of it. Evaluating the risk by modeling would be very useful to estimate such gain in food safety. Here, we propose an individual-based model which describes the spatio-temporal spread of *Salmonella* within a laying flock and takes into account the host response to bacterial infection. The model includes the individual bacterial load and the animals' ability to reduce it thanks to the immune response, i.e. maximum bacterial dose that the animals may resist without long term carriage and, when carriers, length of bacterial clearance. For model validation, we simulated the *Salmonella* spread under published experimental conditions. There was a good agreement between simulated and observed published data. This model will thus allow studying the effects, on the spatiotemporal distribution of the bacteria, of both mean and variability of different elements of host response.

Keywords:

Salmonella; Individual-based model; bacterial transmission; individual heterogeneity

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1. Introduction

Salmonella is a major cause of human toxi-infection and poultry products, eggs and egg products, are the most common source of human *salmonellosis*. *Salmonella* enterica serovar Enteritidis is the strain most often associated with salmonellosis caused by poultry products (EFSA, 2009; Humphrey, 1990). *Salmonella* enteritidis can colonize the gastrointestinal tract of fowls as well as their systemic organs, such as spleen or liver, for long periods. This colonization does not cause clinical signs. This silent carrier-state will in turn lead to between animals transmission. Horizontal transmission within the flock may occur either directly from one infected animal to another fowl, especially in the same cage, through aerosols (Gast et al., 2002; Lever and Williams, 1996) or indirectly because of environmental contamination, mainly through water and feed, as observed in Nakamura et al., 1994. Vertical transmission though trans-ovarian route may also occur (Humphrey and Lanning, 1988). Moreover, once the animal is infected, there is an individual variation in the duration and level of bacteria excretion (Beaumont et al., 2003; Ishola, 2009).

Because of the importance for food safety of poultry contamination by *Salmonella*, prevention of animal infection is an important research area. Many experiments have been conducted to evaluate control methods to prevent animal colonization: vaccination (Barrow, 2007; Zhang-Barber et al., 1999), competitive exclusion (Rantala and Nurmi, 1973), acidification of food, selection for increased animal genetic resistance (Beaumont et al., 2009).

While none of these control measures results in a zero risk, their relative efficacy and possibility of synergy still remains to be estimated. This may be investigated through modeling of bacteria spread within a hen house including horizontal and vertical transmission and animals heterogeneity once infected (level and duration of excretion).

Models have already been proposed to study *Salmonella* spread within various animal species: hens (Leslie, 1996; Prévost et al., 2006; Thomas et al., 2009), pigs (Hill et al., 2008; Lurette et al., 2008) and dairy herds (Xiao et al., 2005, 2006, 2007; Lanzas et al., 2008). But no model considered, at least until now, both the bacterial transmission and heterogeneity of hens's response to infection. Individual variability of the immune response may be introduced into stochastic individual-based models. Such model patterns are largely used in ecology (Grimm et al., 2006) and were already used to model the growth and migration of *Salmonella* enteritidis in hens' eggs (Grijnspeerdt et al., 2005).

The objective of this paper is to present a stochastic individual-based model for the spread of *Salmonella* within a hen house. It allows us to consider individual levels of bacterial infection as well as variability of the host response, i.e. maximal

dose an animal may eliminate without long term infection as well as duration of bacterial clearance. The paper is organized as follows: in Section 2 we describe our individual-based model; validation and exploration of the model behaviour are presented in section 3; they are followed by a discussion and a conclusion in section 4 and 5 respectively.

2. Model

The model description hereafter follows the ODD (Overview, Design concepts, Details) protocol for describing individual and agent-based models (Grimm et al., 2006).

2.1. Purpose

An individual-based model was used to represent the spatial spread of *Salmonella* within a flock of laying hens reared in cages. We assumed that all animals in a cage are infected at the same time (through contaminated food, water, rodents...) so that the individual unit of interest here is a cage. In this model, the risk of long term infection is dependant on both individual bacterial load and a stochastic threshold, corresponding to individuals' capacities of resistance to infection. When the latter are overwhelmed, persistent infection occurs. Its length and duration of immune protection after recovery are stochastic.

2.2. Entities, state variables, and scales

In this model, individuals are cages harboring hens (all of them harbor the same number of hens). Individuals are aligned in rows and each group of two rows are separated from each other by an interval allowing the farmer to take care of animals. As we are interested in the transmission via the environment, the flock is divided in grid cells, allowing us to describe the contamination in each location of the hen house. Each individual is then identified in the hen house by its position $x = (x_1, x_2)$ (i.e x_1 -abscissa and x_2 -ordinate).

An individual is characterized by its bacterial load denoted by $B(t_n, x)$ and its health status denoted by $\mathcal{H}(t_n, x)$ at time t_n and position x . In our model, we assume that there exists an individual bacterial threshold within an individual denoted by $D(x)$ so that the individual bacterial load decreases over the time when the initial bacterial load is lower than $D(x)$, increases when the initial bacterial load is higher than $D(x)$ and remains constant when it is equal to $D(x)$ (see Figure 2(a)). An individual infection beyond the threshold results in systemic infection (because of overwhelming of individuals capacities to reduce bacterial load).

Table 1: State variables given for each location $x = (x_1, x_2)$ in the hen house at a time t_n .

$C(t_n, x)$	Density of bacterial environmental infection
$B(t_n, x)$	Level of bacterial load within an individual
$\mathcal{H}(t_n, x)$	Health status of the individual
$D(x)$	Bacterial threshold within the individual

At the same time t_n and position x , the level of contamination in environment is represented by $C(t_n, x)$. Note that, for positions that do not contain individuals, variables $B(t_n, x)$, $\mathcal{H}(t_n, x)$ and $D(x)$ are not defined while $C(t_n, x)$ is defined.

The full set of variables for the individual-based model are described in Table 1. Time step for the model is one day.

2.3. Process overview and scheduling

The flowchart in Figure 1 outlines the events occurring during each time step for one given replication. Details are given by submodels in section 2.7.

2.4. Design concepts

Interaction: we consider interaction between one individual and those located in the neighborhood through inhalation or ingestion of bacteria excreted in the environment.

Stochasticity: two components are stochastic: threshold for bacterial load and time interval before change to next health status.

Observation: the model outputs are the health status of each individual and the density of bacteria in environment at each time step for all positions. From these outputs, we compute the percentage of individuals over time in the house and over row for each health status which are determinant for practical issues and for comparison to experimental data.

2.5. Initialization

Initialization consists in defining the size of the house, the number of rows of individuals, the number of individuals by rows and following state variables for each location. Health status ($\mathcal{H}(t_n, x)$), bacterial load ($B(t_n, x)$) and density of bacteria in the environment ($C(t_n, x)$) are initialized by the user. The threshold $D(x)$ is initialized stochastically for each replication and each individual and kept constant during the whole replication.

Figure 1: Flowchart showing a time step iteration. For each time step, **Rule 1** considers individual infection (ingestion or inhalation in environment) to update individual bacterial load (as described in Section 2.7.1), **Rule 2** considers the bacterial load to update health status (as described in Section 2.7.2), **Rule 3** computes the number of excreted bacteria to update the contamination level in environment (as described in Section 2.7.3).

2.6. Input for time varying process

The model does not use input data to represent time-varying process.

2.7. Submodels

Further notations are needed to describe the submodels: the time interval $(0, T_{max})$ is partitioned into subintervals (t_n, t_{n+1}) , with a time step $\delta t = t_{n+1} - t_n = 1$ day.

Let $\Omega \subset \mathbb{R}^2$ be the area covered by the hen house and denote by $x = (x_1, x_2) \in \Omega$ a point of hen house. Assume that $x_1 \in (0, L_1)$ and $x_2 \in (0, L_2)$ where L_1 and L_2 is the length and width of hen house respectively. We use a uniform Cartesian grid consisting of grid points (x_{1i}, x_{2j}) to partition the x_1 -component and x_2 -component interval of x where $x_{1i} = i\delta x_1$ and $x_{2j} = j\delta x_2$, $i = 0, 1, 2, \dots, N_1$, $j = 0, 1, 2, \dots, N_2$ and we simplify the writing of the point (x_{1i}, x_{2j}) by $x_{i,j}$.

From now, an individual will be identified by the coordinates of its center $x_{a,b}$ where a and b are chosen from $\{0, 1, 2, \dots, N_1\}$ and $\{0, 1, 2, \dots, N_2\}$ respectively.

(a)

(b)

Figure 2: (a) Example of evolution of Bacterial load, $B(\tau, \cdot)$ on one day, $\tau \in (t_n, t_{n+1})$. Curves with three different initial sizes of dose: $B(t_n, \cdot) = 4.5 \log_{10}$ (the bottom solid line), $B(t_n, \cdot) = 5 \log_{10} = D(\cdot)$ (the dotted line) and $B(t_n, \cdot) = 5.5 \log_{10}$ (the upper solid line). (b) Growth rate of bacterial load $g(B)$. Here, individual threshold, $D = D(\cdot)$ is set at $5 \log_{10}$, carrying capacity, M at $10 \log_{10}$ and the density of bacteria that an individual acquires by ingestion or inhalation at zero.

Figure 3: Evolution of health status for an individual and its interaction with the contaminant in environment at time t_n and position $x_{a,b}$: S_0 (susceptible) I_{D-} , (infected with a digestible low dose of infection), I_{D+} , (suffering from a long term digestive infection), I_S (systemic infection) and R (recovered). The force of infection $g + I_p$ is defined in Section 2.7.2. The parameters $\gamma, \eta(B_{1x}), \mu, \beta_{I_{D+}}, \beta_{I_S}$ and λ are described in Table 2.

2.7.1. Model for individual bacterial load within each day

An individual must initially be exposed to a sufficient density of bacteria to become infected (Humphrey et al., 1991; Gast, 1993; Lever and Williams, 1996). At very low dose of infection, the bacterial load within an individual will decrease over time due to the ability of the organism to overcome this infection. At the opposite, it will multiply over time when this initial dose of infection exceeds a threshold until saturation value due to the limitation of resources. We denote by M , the carrying capacity of bacterial load within an individual (i.e. maximal number of bacteria that an individual may carry) and $D(x_{a,b})$ ($0 < D(x_{a,b}) < M$), the threshold of bacteria load for which an individual at position $x_{a,b}$ is able to overcome an infection and reduce the number of bacteria over the time. We use the *strong allee effet* (Jiang and Shi, 2009; Wang and Kot, 2001) to model the growth of bacteria within an individual in the following way. Let $B(\tau, x_{a,b})$, $f(B(\tau, x_{a,b}))$ and $g(B(\tau, x_{a,b}))$ be the level of bacterial load, the per capita growth rate and the growth rate of bacteria load within an individual at time $\tau \in (t_n, t_{n+1})$ and position $x_{a,b}$ respectively. We assume that the functions f and g depend on bacterial load $B(\tau, x_{a,b})$ so that f is negative when density of bacteria $B(\tau, x_{a,b})$ is small. Consequently $B(\cdot, x_{a,b})$ decreases when $B(t_n, x_{a,b}) < D(x_{a,b})$, increases when the initial condition $B(t_n, x_{a,b}) > D(x_{a,b})$ and is constant when $B(t_n, x_{a,b}) = D(x_{a,b})$ (see Figure 2(a)).

From (Jiang and Shi, 2009; Wang and Kot, 2001), g is written as function of f

(see Figure 2(b)) as:

$$g(B(\tau, x_{a,b})) = B(\tau, x_{a,b})f(B(\tau, x_{a,b}))$$

where

$$f(B(\tau, x_{a,b})) = \theta \left(\frac{B(\tau, x_{a,b})}{D(x_{a,b})} - 1 \right) \left(1 - \frac{B(\tau, x_{a,b})}{M} \right)$$

for all $\tau \in (t_n, t_{n+1})$, θ is the net growth rate of bacteria within an individual.

We assume the dynamics of individual bacterial load satisfies the following differential equation:

$$\frac{dB(\tau, x_{a,b})}{d\tau} = g(B(\tau, x_{a,b})) + I_p(t_n, x_{a,b}), \quad \tau \in (t_n, t_{n+1}). \quad (1)$$

where initial condition of Eq. (1) is denoted by $B(t_n, x_{a,b})$. $I_p(t_n, x_{a,b})$ is interpreted as the density of bacteria that an individual (i.e. all hens forming one individual) acquires by ingestion or inhalation at time t_n and position $x_{a,b}$. We model the latter in the form

$$I_p(t_n, x_{a,b}) = k \sum_{y_{i,j} \in \omega(r)} C(t_n, y_{ij}). \quad (2)$$

where $\omega(r) \subset \Omega$ is the area of contamination around the individual at position $x_{a,b}$, k is the transmission probability of infection of an individual after inhalation or ingestion of bacteria in environment. We have denoted by r the radius of contamination around the individual of center x so that $\omega(r) := \{y \in \Omega : \|x - y\|_2 \leq r\}$ and $\|\cdot\|_2$ is the Euclidean norm.

The immune response is strongly dependant on many individual factors, e. g. genetics (see for example Barrow, 2007; Bumstead and Barrow, 1988; Beaumont et al., 2003). Therefore the individual threshold for bacterial load $D(x_{a,b})$, was assumed to vary from an individual to another resulting in a variability between individuals in the dynamics of Eq. (1) for the same initial condition $B(t_n, x_{a,b})$. Thus we assume that the thresholds $D(\cdot)$ are triggered according to a random variable Y_D defined by $Y_D = Z \times 10 \log_{10}$ where Z is beta distributed, $\mathcal{B}(p, q)$ ($p, q > 0$), with mean $p/(p+q)$. Y_D takes on values in interval $(0, 10 \log_{10})$. For an individual at position $x_{a,b}$, the threshold $D(x_{a,b})$ was drawn from distribution of Y_D at the beginning of each replication and is kept constant during the replication.

2.7.2. Epidemiologic model

An individual located in position $x_{a,b}$ and at time step $\delta t = t_{n+1} - t_n$ is in one of the five disease-states (see Figure 3): S_0 : susceptible individual without bacterial load.

Table 2: Baseline values for the parameters

	Description	Dimension	values
p, q	Parameters of beta distribution	Dimensionless	$p = 35, q = 45$
M	Carrying capacity of bacteria within an individual	cfu	$10 \log_{10}$
γ	Rate of transition from I_{D+} to I_S	Day^{-1}	$1/2$
$\eta(B_{1x})$	Recovery rate	Day^{-1}	Table 3
μ	Rate of return of individual from R to S_0 status	Day^{-1}	$1/200$
$\beta_{I_{D+}}$	Excretion rate of individual at I_{D+} status.	Day^{-1}	$4 \log_{10}$
β_{I_S}	Excretion rate of individual at I_S status.	Day^{-1}	$4.5 \log_{10}$
λ	Natural death rate of <i>Salmonella</i> in environment.	Day^{-1}	0.1
α^2	Diffusion coefficient of <i>Salmonella</i> in environment.	$\text{m}^2 \times \text{Day}^{-1}$	0.01
k	Transmission probability of infection	Dimensionless	0.08
r	Radius of contamination around the individual	m	2
θ	Net growth rate of bacteria within an individual.	h^{-1}	0.0007

185 I_{D-} : individual suffering from digestive infection at a dose lower than its threshold
186 $D(x_{a,b})$ (i.e. with a transient infection). I_{D+} : individual suffering from digestive
187 infection at a dose higher than its threshold $D(x_{a,b})$. I_S : individual systemically
188 infected after the long term digestive infection. R : recovered individual. We denote
189 by $\mathcal{H}(t_n, x_{a,b})$ the health state of an individual, $\mathcal{H}(t_n, x_{a,b}) \in \{S_0, I_{D-}, I_{D+}, I_S, R\}$.

190 Transitions from S_0 -state to I_{D-} -state and from I_{D-} -state to I_{D+} -state are only
191 regulated by the density of bacteria within the individual. For each time-step δt , for
192 each individual in S_0 -state or I_{D-} -state, we solve Eq. (1) via Runge Kutta methods
193 (Butcher, 2003) and we obtain a unique solution denoted by $B(t_{n+1}, x_{a,b})$ for each
194 initial condition $B(t_n, x_{a,b})$. We assume that for $B(t_{n+1}, x_{a,b}) = 0$, individual is in
195 S_0 -state, when $B(t_{n+1}, x_{a,b}) \in]0, D(x_{a,b})$, individual is in I_{D-} -state and can go back
196 to the S_0 -state. When the bacterial load $B(t_{n+1}, x_{a,b})$ becomes higher than the
197 threshold $D(x_{a,b})$, then the individual changes its status from I_{D-} to I_{D+} state.
198 The first occurrence of a bacterial load verifying, for an individual at position $x_{a,b}$,
199 $B(t_{n+1}, x_{a,b}) > D(x_{a,b})$ is denoted by B_{1x} .

200 The transitions from I_{D+} -state to I_S -state, from I_S -state to I_R -state and from R -
201 state to S_0 -state are stochastic. We denote by $T(x_{a,b}/I_{D+})$, $T(x_{a,b}/I_S)$ and $T(x_{a,b}/R)$,
202 the residence time of an individual in the I_{D+} , I_S and R -state respectively. We
203 assume that at time, t_n , an individual newly reaches the I_{D+} -state, $T(x_{a,b}/I_{D+})$ is

204 triggered according to an exponential distribution with an average duration equal to
 205 $1/\gamma$ and the individual will change its status from I_{D+} to I_S at time, $t_{n+\ell}$, where ℓ
 206 equal to the integer part of $T(x_{a,b}/I_{D+})/\delta t$. In the same way, successively $T(x_{a,b}/I_S)$
 207 and $T(x_{a,b}/R)$ are triggered according to an exponential distribution with an average
 208 duration equal to $1/\eta(B_{1x})$ and $1/\mu$. We denote by $P_{I_{D+}}$, P_{I_S} and P_R respectively,
 209 the transition probabilities for I_{D+} to become I_S , I_S to become R , R to become S_0
 210 per unit of time. Then $(P_{I_{D+}}, P_{I_S}, P_R) = (1 - \exp(-1/\gamma), 1 - \exp(-1/\eta(B_{1x})), 1 -$
 211 $\exp(-1/\mu))$.

212 2.7.3. Model for diffusion of bacteria in the hen house

213 Bacterial environmental contamination within an industrial hen house is mod-
 214 eled assuming that *Salmonella* is dispersed in the environment via a diffusion process
 215 through dust particles and contaminated aerosols (Gast et al., 2002; Nakamura et al.,
 216 1994; Lever and Williams, 1996). Let $C_{i,j}^n = C(t_n, x_{i,j})$ be the density of bacteria
 217 at time t_n and position $x_{i,j}$. $C_{i,j}^n$ is a approximated solution of a continuous reac-
 218 tion diffusion equation describing the dispersion of bacteria in hen house (Appendix
 219 Eq. (A.1)). It was approximated by a forward finite difference scheme in time and
 220 centered finite difference scheme in space, which gives

$$\begin{aligned} \frac{C_{i,j}^{n+1} - C_{i,j}^n}{\delta t} &= \frac{\alpha^2}{(\delta x_1)^2} (C_{i+1,j}^{n+1} - 2C_{i,j}^{n+1} + C_{i-1,j}^{n+1}) \\ &\quad + \frac{\alpha^2}{(\delta x_2)^2} (C_{i,j+1}^{n+1} - 2C_{i,j}^{n+1} + C_{i,j-1}^{n+1}) \\ &\quad - \lambda C_{i,j}^{n+1} + (\beta_{I_S})_{i,j}^{n+1} + (\beta_{I_{D+}})_{i,j}^{n+1} \end{aligned} \quad (3)$$

with boundary conditions

$$C_{0,j}^{n+1} = C_{1,j}^{n+1}, C_{N_1-1,j}^{n+1} = C_{N_1,j}^{n+1},$$

$$C_{i,0}^{n+1} = C_{i,1}^{n+1}, C_{i,N_2-1}^{n+1} = C_{i,N_2}^{n+1},$$

221 and initial condition $C_{i,j}^0 \geq 0$. Convergence of numerical scheme in $\|\cdot\|_\infty$ norm
 222 is obtained by the following condition $\delta t \alpha^2 / (\delta x_1)^2 < 1/4$ and $\delta t \alpha^2 / (\delta x_2)^2 < 1/4$
 223 (Lucquin and Pironneau, 1996, Page 281).

224 2.8. Calibration

225 *Data for carrying capacity M*: we have no data to estimate the value of M .
 226 Noticing that in experimental infections, almost all individuals are infected with
 227 an inoculum dose ranging between $3 \log_{10}$ and $9.5 \log_{10}$ colony-forming units (cfu)

(a) Dose= 10^4 cfu

(b) Dose= 10^6 cfu

(c) Dose= $7.5 \cdot 10^7$ cfu

Figure 4: Evolution over time of the percentages of I_{D+} , I_S and $I_{D+} + I_S$ when all individuals were inoculated with the same bacterial dose a) $= 10^4$ cfu and b) $= 10^6$ cfu as in Gast (1993); c) $= 7.5 \cdot 10^7$ cfu as in Gast et al. (1997). Observed data (corresponding to percentage of individuals shedding *Salmonella* in feces) are shown by crosses. Median value of simulations are shown by solid lines. The 5th and 95th percentiles observed on the 300 replicates are shown by dotted curves.

(a)

(b)

Figure 5: Evolution over time of the percentages of I_{D+} , I_S and $I_{D+} + I_S$ after rearing infected individuals in the vicinity of healthy ones a) i.e inoculating (10^6 cfu) one single individual out of three as in Gast (1993) and b) letting 8 infected (10^5 cfu) as in Nakamura et al. (1994). In both cases, individuals are in two adjacent rows and inoculated individuals share water with not uninoculated ones. Observed data (corresponding to percentage of individuals shedding *Salmonella* in feces) are shown by crosses. Median value of simulations are shown by solid lines. The 5th and 95th percentiles observed on the 300 replicates are shown by dotted curves.

(a) Evolution of the percentage of $I_{D+} + I_S$ over time and row

(b) Evolution of the percentage of I_{D+} , I_S and $I_{D+} + I_S$ over time

Figure 6: Results of simulations achieved using data from Table 4 (column (g)) and inoculation of one individual at Day 0 with a high bacterial dose (10^9 cfu) in the midst of hen house, when rows are separated from each other by 2 meters. (a): only the median value on the 300 replicates are shown, (b): median value of simulations are shown by solid lines. The 5th and 95th percentiles observed on the 300 replicates are shown by dotted curves.

(a) Evolution of the percentage of $I_{D+} + I_S$ over time and row

(b) Evolution of the percentage of I_{D+} , I_S and $I_{D+} + I_S$ over time

Figure 7: Results of simulations achieved using data from Table 4 (column (g)) and inoculation of one individual at Day 0 with a high bacterial dose (10^9 cfu) at the corner of hen house, when rows are separated from each other by 2 meters. (a): only the median value on the 300 replicates are shown, (b): median value of simulations are shown by solid lines. The 5th and 95th percentiles observed on the 300 replicates are shown by dotted curves.

(a) Evolution of the percentage of $I_{D+} + I_S$ over time and row

(b) Evolution of the percentage of I_{D+} , I_S and $I_{D+} + I_S$ over time

Figure 8: Results of simulations achieved using data from Table 4 (column (f)) and inoculation of one individual at Day 0 with a high bacterial dose (10^9 cfu) at the corner of hen house, when rows are separated from each other by 1 meter. (a): only the median value on the 300 replicates are shown, (b): median value of simulations are shown by solid lines. The 5th and 95th percentiles observed on the 300 replicates are shown by dotted curves.

Table 3: Calibration of the average duration of the systemic period, $1/\eta(B_{1x})$ as a function of B_{1x} (the first value of $B(t_{n+1}, x_{a,b})$ satisfying $B(t_{n+1}, x_{a,b}) > D(x_{a,b})$).

B_{1x} in cfu	$< 10^4$	$[10^4, 5 \cdot 10^4[$	$[5 \cdot 10^4, 10^5[$	$[10^5, 5 \cdot 10^5[$	$[5 \cdot 10^5, 10^6[$	$> 10^6$
$1/\eta(B_{1x})$ in day	1	4	7	10	13	16
$1/\eta(B_{1x}) + 1/\gamma$ in day	3	6	9	12	15	18

and that a saturation of bacteria within an individual seems to be observed beyond $9.5 \log_{10} cfu$ (Gast, 1993; Gast et al., 2004; Humphrey et al., 1991; Lever and Williams, 1996), M was set at $10 \log_{10} cfu$.

Data for recovery rate, η and rate of transition from I_{D+} to I_S , γ : Humphrey et al. (1991, Table 1) showed that the duration of faecal excretion is correlated with the size of inoculum dose and can vary from 3.4 to 36.8 days for dose varying from 10^3 to 10^6 while Gast et al. (2005) showed that the duration of faecal excretion can vary from 13.8 to 32.9 for an inoculum dose at 10^9 of different *Salmonella* strains. Since individuals excrete at digestive or systemic state, the sum of average durations of the digestive period, $1/\gamma$, and of the systemic period, $1/\eta$ is necessarily a function of the inoculum size and of the *Salmonella* strains. Setting $1/\gamma$ at 2 days as in (Prévost et al., 2006, 2008), then we generate some residence time in I_{D+} varying in about 95% of the simulation from 0.05 to 3 days. Assuming that $1/\eta(B_{1x})$ depends on the initial value of bacterial load in I_{D+} -status, mean $1/\eta(B_{1x})$ was calibrated as described in Table 3. This allowed to generate with exponential distribution residence time in I_S varying in 95% of the simulations from 0.6 to 47 days for doses ranging from 10^3 to 10^9 .

Data for parameters p and q of beta distribution to trigger the individual threshold $D(x_{a,b})$: we set $p = 35$ and $q = 45$ so that 5% of individuals have a bacterial threshold lower than $3.5 \log_{10}$ and higher than $5.8 \log_{10}$.

Data for net growth θ : the net growth rate is the key parameter influencing simultaneously the fast-growing (or slow-growing) and the fast-decreasing (or slow-decreasing) of the bacterial load over time when the initial bacterial load is higher and lower respectively than the threshold. Many factors such as the bacterial strain, host factors might affect this parameter. In the literature, no experimental data were available for laying hens. We assumed that θ is equal to $0.0007 h^{-1}$.

Data for mortality rate of bacteria λ : we assume that the mortality rate of bacteria in the environment is $\lambda = 0.1 day^{-1}$ as (Prévost et al., 2006, 2008).

Rate of bacterial excretion for I_{D+} and I_S states: as in Prévost et al. (2006, 2008),

we assumed that individuals excreted low levels of bacteria and that an individual in I_{D+} excreted less than an individual in I_S state. We set $\beta_{I_{D+}} = 4 \log_{10} \text{cfu} \times \text{Day}^{-1}$, and $\beta_{I_S} = 4.5 \log_{10} \text{cfu} \times \text{Day}^{-1}$.

Data for transmission probability of infection of an individual after inhalation or ingestion of bacteria, k , and radius of contamination around the individual, r : from Eq. (1), variation in parameters k or r will result in a similar trend in the density of bacteria that an individual (i.e. all hens forming one individual) acquires by ingestion or inhalation (I_P). To calibrate these data, we used the results for the inhalation dose of bacteria calculated by Lever and Williams (1996) in rearing conditions similar to that of flock of laying hens. These results showed that each individual would inhale every 24 h a bacterial load ranging between 0 and $2 \log_{10}$. We assumed that $r = 2$ m (maximal distance for aerosol transmission) and k was set at 0.08 so that I_P remains in the interval $(0, 2 \log_{10})$.

Data for diffusion coefficient α^2 : we assumed that α^2 is equal to 0.01.

3. Simulation experiments

3.1. Material and method

Three types of scenarios are considered, the first two for model validation and the third for model exploration. The width, L_2 and length, L_1 of hen house were always initialized to 15 m and 30 m respectively while the number of individuals varies following the scenarios and are summarized in Table 4. To quantify the level of agreement between predicted and simulated data, the Standard error of simulated and observed data was evaluated for the scenarios 1 and 2.

3.1.1. Scenario 1: validation of kinetics of infection

Experiments in which all individuals were initially inoculated with the same dose of bacteria were considered. In that case, reinfection between individuals was reduced as much as possible (by rearing with individual food and water). That was the case of the first experiment described by Gast (1993) where 40 individuals were considered (Table 4 (a) and (b)) and an another experiment described by Gast et al. (1997) where 36 individuals were considered (Table 4 (c)). In both cases, all of them were inoculated at Day 0. Three bacterial doses, 10^4 cfu, 10^6 cfu and $7.5 \cdot 10^7$ cfu were studied (one per replicate) and infections were regularly investigated on feces samples. As individuals excrete *Salmonella* in feces in I_{D+} and I_S -state, the observed prevalence were compared to the simulated percentages $I_{D+} + I_S$. The percentages of I_S were also considered to investigate the repartition between the two status. A total of 300 simulations were achieved with the same dose and the same number of individuals.

293 Since transmission via the environment was very low if any and can be neglected,
 294 the value of the parameter k in Eq. (2) was set equal to zero.

295 3.1.2. Scenario 2: validation of the *Salmonella* spread from individuals to individuals 296 via the environment

297 We selected for model validation two experiments where experimentally infected
 298 individuals were reared with healthy ones. Gast (1993) studied a total of 72 individ-
 299 uals where he inoculated one-third of them (i.e. every 3rd individual) with a dose of
 300 bacteria at 10^6 cfu. Nakamura et al. (1994) infected 8 individuals out of 16 (i.e. every
 301 2nd individual) with a dose of bacteria at 10^5 cfu. The latter precisely described the
 302 distribution of individuals considering one pair of adjacent rows (i.e. 8 individuals
 303 in one row share drinking water with adjacent individuals) Table 4 (e). First four
 304 individuals was inoculated in one row and last four individuals in the second row at
 305 the beginning of experiment. At the opposite, the former gave no information on
 306 the spatial distribution of individuals but only the route of cross contamination was
 307 known (uninoculated individuals shared drinkers and feeders with inoculated ones).
 308 We therefore assumed that the individuals were housed in one pair of rows as in
 309 Nakamura et al. (1994) (Table 4 (d)). Since in both experiments, *Salmonella* were
 310 searched in feces and our model assumes that excretion occurs in the I_S or $I_{D+} + I_S$
 311 state, results must be compared to the sum of I_{D+} and I_S individuals. However,
 312 since the rate of excretion is five-fold higher in the systemic state, comparison with
 313 number of hens in the Systemic state was also considered. As in scenario 1, observed
 314 and simulated percentages of $I_{D+} + I_S$ and I_S were compared. For simulations, a
 315 total of 300 simulations were achieved.

316 3.1.3. Standard error of simulated and observed data

317 In scenario 1 and 2, we evaluate the root mean squared error ($RMSE$) known as
 318 the standard error of simulated and observed data.

$$RMSE := \sqrt{\frac{\sum_{l=1}^N (obs(t_l) - sim(t_l))^2}{N}} \quad (4)$$

319 where N is the number of observed data, $obs(t_l)$ and $sim(t_l)$ are the observed and
 320 simulated data at time t_l respectively. $RMSE$ has the same units that the simulated
 321 and observed data which are in percentage.

322 3.1.4. Scenario 3: influence of the position of the first infection and the distance 323 between pair of rows in the hen house

324 To investigate the influence of the position of the first infection, initialization of
 325 hen house was achieved as described in the Table 4(f). Two cases were considered

according to this infection occurred either in one corner (i.e. in pair of row 5) or on the middle (i.e. pair of row 3) of the hen house. In both cases, only one individual was infected on Day 0 with a high dose (10^9 cfu).

The effect of the spatial distribution of individuals in hen house was also considered by comparing results with data from scenario in Table 4(f) or (g). In the former case, the distance between pair of row is 2 m versus 1 in the latter.

A total of 300 simulations were achieved and the simulated percentages of I_S or $I_{D+} + I_S$ was represented.

3.2. Results

3.2.1. Scenario 1: validation of kinetics of infection

Results obtained when simulating data and those observed after experimental inoculation are shown on Figure 4a to 4c for doses of 10^4 cfu, 10^6 cfu and $7.5 \cdot 10^7$ cfu respectively. Simulated percentage of $I_{D+} + I_S$ and observed results are very close for the three doses (see Table 5(a), (b) and (c) for $I_{D+} + I_S$) and lay between the 5th and 95th percentiles. Simulated percentages of I_S are also very close to observation made at the first two doses (see Table 5(a) and (b) for I_S). For the highest dose however, the observation obtained one week post inoculation is close but higher than the 95th percentile (see Table 5(c) for I_S).

3.2.2. Scenario 2: validation of the Salmonella spread from individuals to individuals via the environment

Simulated percentages of I_S or $I_{D+} + I_S$ and observed prevalence from experiments are shown in Figure 5a for the experiment of Gast (1993) and Figure 5b for the experiment of Nakamura et al. (1994).

In the former the greatest disagreement between any of the data sets and simulated percentage of infected individuals was found with regards to $I_{D+} + I_S$ see table 5(d). This is especially true for data obtained one week post inoculation (p.i.) while later on both sets of results were very close.

In the latter case, observed results lay between the 5th and 95th percentiles of simulated percentage of $I_{D+} + I_S$ except for the observation obtained three days post inoculation which is close to the 95th percentile. When simulated percentage of I_S is considered, differences are larger. Observed data at 3 and 6 days p.i. were much higher than simulated percentage of I_S : the former ranged from 68.7 to 62.5% while median percentage of I_S varied from 19 to 40%. Comparing results on Table 5(e), $I_{D+} + I_S$ fits observed data better than I_S .

Table 4: Initialisation of individuals in hen house for each scenario.

Description	Scenario 1			Scenario 2		Scenario 3	
	(a)	(b)	(c)	(d)	(e)	(f)	(g)
Inoculum dose in cfu	10^4	10^6	$7.5 \cdot 10^7$	10^6	10^5	10^9	10^9
Number of pair of rows	1	1	1	1	1	8	5
Number of individuals per row	20	20	18	36	8	35	56
Number of individuals	40	40	36	72	16	560	560

Table 5: Standard error in percentage using I_S versus $I_S + I_{D+}$ as simulated data.

Description	Scenario 1			Scenario 2	
	(a)	(b)	(c)	(d)	(e)
Standard error for I_S	0.19	1.67	6.65	8.26	28.38
Standard error for $I_S + I_{D+}$	0.19	4.78	4.51	17.82	14.57

3.2.3. Scenario 3: influence of the position of the first infection and of the distance between pair of rows in the hen house

Influence of the position of the first infection is illustrated on the figures 6 and 7 respectively for a first occurrence in the middle and in the corner of the hen house respectively. The position of the first infection influences both the kinetics of infection and the maximal percentages of infected individuals. As late as 210 days post inoculation, the first pair of rows is still not colonized for an infection starting in the opposite corner (see Figure 7a) while when the infection starts in the middle, all five pair of rows are infected about 210 days post inoculation (see Figure 6a). The infection starting in the middle of the hen house results in a higher maximal of percentage of $I_S + I_{D+}$ than an infection starting at a corner: 25% versus 13% (Figures 6b and 7b, 70 days post inoculation).

Influence of the distance between pair of rows in the hen house (1 m versus 2 m) can be seen by comparing the figures 8 and 7. When the pair of rows are close, the colonization is rapid with a lower maximal of percentage of $I_S + I_{D+}$: for example all eight pair of rows are infected about 110 days post inoculation (see Figure 8a) with maximal percentage of $I_S + I_{D+}$ of 17.5% at 100 days post inoculation (see Figure 8b). At the opposite, the colonization is slow with a close maximal percentage of $I_S + I_{D+}$ but a lower minimal percentage.

4. Discussion

This model extends the previous model derived by Prévost et al. (2006) where individuals infected at the digestive level were only distinguished from those infected at the systemic level. Here, individuals in the I_{D-} status may overcome the bacterial infection as long as the bacterial load remains lower than the $D(x_{a,b})$ threshold. At the opposite, when the individual bacterial dose is higher than $D(x_{a,b})$, individuals change to the I_{D+} status and undergo a longer term infection.

The threshold, $D(x_{a,b})$, which is the maximal bacterial load that the individual may clear without persistent and systemic infection, depends on many factors such as the bacterial strain (as can be seen for example from Bumstead and Barrow, 1988), gut flora (Rantala and Nurmi, 1973), individuals' genetic resistance (see for example Beaumont et al. (2009)). The threshold was thus chosen as random. In practice, the balance between bacterial doses and individuals threshold will be determinant in the propagation of *Salmonella*, since in the field bacterial doses are most often rather small. Introducing this threshold thus allows investigating the effects of both average values and variability of these factors.

In the model immune response was considered only through its impact on the bacterial load, without refining the description of biological processes which are far too complex (see for example Host, 2000) to be modeled at the same time as the whole flock is considered. Moreover, parametrization of the immunity response would have been hardly feasible because of large number of biological steps that may be considered. This would have led to the introduction of a higher uncertainty on the process that would decrease the confidence on the model results. Using the strong allee effect, only three parameters were needed: net growth rate of bacterial within the individual, θ , the individual threshold of bacterial load corresponding to the balance between bacterial multiplication within the host and host response leading to bacterial clearance by immune response, $D(x_{a,b})$ and the carrying capacity M . All three of them have a biological meaning which facilitated their estimation and allowed to base it on experimental data: the threshold $D(x_{a,b})$ and carrying capacity were chosen from numerous results of experimental infections where individuals are infected with inoculum doses ranging between $3 \log_{10}$ and $9.5 \log_{10}$ colony-forming units (cfu) (Humphrey et al., 1991; Gast, 1993; Lever and Williams, 1996; Gast et al., 2004). Large differences in prevalence even in the first days after inoculation were observed when the dose were higher or lower than $5 \log_{10}$ leading us to choose this value as the average value for the threshold.

Variations in durations of bacterial clearance were also considered, taking advantage of experimental data obtained in Humphrey et al. (1991); Gast et al. (2005). Indeed, this duration was shown by Prévost et al. (2008) to be partly under a genetic

control. Preliminary investigations showed that this duration had a large impact on kinetics of colonization, especially at longer intervals post inoculation.

This model allows reproducing experimental results. Indeed, the simulated percentages and observed data are very coherent when experimental inoculations are considered. They are also consistent with observations resulting from infection between individuals via environment, although simulations overestimated the outcome compared to the second experiment by Gast (1993) where the spatial distribution of individuals in the hen house was unknown. As the spatial distribution of individuals such as the distance between pair of rows influences both the kinetics of infection and the maximal percentages of infected individuals (see scenario 3), it might explain the disagreement between experimental and simulated data. Moreover, no experimental data were available for the first six days post-inoculation for model validation as in Nakamura et al. (1994).

Distinguishing individuals I_S and I_{D+} allows to understand what happens during the first days post inoculation. At the opposite, the sum $I_{D+} + I_S$ gives the real prevalence of infection since fecal samples may found be negative even in the case of caecal infection. The differences between both sets of data disappear at longer post inoculation intervals. Then only systemically infected individuals may be observed so that both simulations and observations refer to the same category of individuals.

Moreover, this model makes it possible to study the spatial diffusion of the bacteria and disease, while until now, to our knowledge at least, no data or model were available to study spatial diffusion of *Salmonella* or any other pathogenic agents in a hens' flock.

Most studies showed that flock size has an effect on the prevalence of *Salmonella* within a laying flock (EFSA, 2009; Huneau-Salaun et al., 2009; Carrique-Mas et al., 2009) but the influence of the position of the first infection or the distance between pair of rows in hen house may have an important effect in the prevalence (see scenario 3). Our results show that these assumptions are exact and that the speed of colonization may depend on the position of the first infection.

However, the model considers all hens in a cage as an epidemiological unit. Indeed, most often all of them will be infected at the same time (by contaminated feed, water, rodent...) and/or cross infected through aerosols contamination via excreted bacteria of the environment (among which food and drinkers).

This model will make it possible to investigate new strategies of reduction of *Salmonella* prevalence. That will be the case for the spatial effect of introducing more resistant individuals. (Prévost et al., 2008) showed that introducing a proportion of more resistant fowls, assuming a homogenous mixing of the two subpopulations of resistant and of susceptible individuals resulted in a reduction of the overall propor-

tion of infected fowls. With our model, we will be able to study possible effects of the relative spatial positions of susceptible and resistant individuals on the spatial spread of the *Salmonella* in hen house. Considering individual variations in bacterial threshold and duration of clearance will also make it possible to study possible effects of differences in excretion rates which may have a major impact on environmental contamination.

5. Conclusion

In this article, we formulated an individual-based model to describe the spread of *Salmonella* within a laying flock. This is the first stochastic model describing *Salmonella* spatio-temporal spread within a poultry flock. It is able to reproduce experimental data; the conceptual understanding of environmental mediated *Salmonella* spread appears complete. It will thus allow studying the interest of various prophylactic means against this disease as well as the effect of changes or variability of various factors. The model could also be adapted to study the propagation of other pathogens within laying hens.

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Appendix A. Continuous formulation of sub-model 2.7.3

Let $C(t, x)$ be the density of bacteria in the environment at time t and position $x = (x_1, x_2) \in \Omega$, $t \geq 0$. $C(t, x)$ depends on the initial contamination, $C(0, x) \geq 0$, bacterial diffusion rate, α^2 , and mortality rate, λ , as well as on excretion rate, $\beta_{I_{D+}}$, and, β_{I_S} , by individuals at I_{D+} and I_S -state respectively. The density dynamics satisfies the following equation:

$$\frac{\partial C(t, x)}{\partial t} = \alpha^2 \Delta_x C(t, x) - \lambda C(t, x) + \beta_{I_S}(x) + \beta_{I_{D+}}(x) \quad (\text{A.1})$$

where $\Delta_x = \partial^2 / \partial x_1^2 + \partial^2 / \partial x_2^2$, with no flux boundary condition $\partial C(t, x) / \partial \nu = 0$ on $\partial \Omega$, ν is the outward normal. $\beta_{I_S}(x) = 0$ if at position x there is no individual at I_{D+} -state; $\beta_{I_{D+}}(x) = 0$ if at position x there is no individual at I_S -state. We assume that $\beta_{I_{D+}}$ and β_{I_S} are constant. Therefore their values are uniformly distributed in the area covered by the individual during excretion.

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