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Spectroscopy of $\text{YAl}_3(\text{BO}_3)_4\text{:Cr}^{3+}$ crystals following first principles and crystal field calculations

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Abstract:

The CASTEP module of Materials Studio package was used for calculations of the structural, electronic and optical properties of pure and Cr^{3+} -doped YAB. The exchange-correlation effects were treated within the generalized gradient approximation (GGA) with the Perdew-Burke-Ernzerhof functional. The Monkhorst-Pack scheme k -points grid sampling was set at $3 \times 3 \times 4$ for the Brillouin zone (BZ). The plane-wave basis set energy cutoff was set at 340 eV; ultrasoft pseudopotentials were used for all chemical elements. The convergence parameters were as follows: total energy tolerance – 1×10^{-5} eV/atom, maximum force tolerance 0.03 eV/nm, maximal stress component 0.05 GPa and maximal displacement 0.001 Å. Identification of the principal absorption peaks of the studied crystal was done. Influence of the 532 nm cw 300 mW laser beams on the observed absorptions is studied.

Introduction

The rare earth doped $\text{YAl}_3(\text{BO}_3)_4$ (YAB) single crystals are of particular interest due to existence of an interesting physical properties like incommensurate phase [1]; possibility to obtain nanopowder phosphors [2], defect – induced phase transitions [3] existence of up- and down-conversions [4]. Particular interest present the Cr doped YAB crystals. In particularly in the Ref. 5 it was found the piezo-induced second-order nonlinear optical effect in polyvinyl alcohol/YAB:Cr nanocomposites and influence of YAB:Cr³⁺ nanocrystallite sizes [6]. These materials are of special interest for the light emitting diodes [7]. These crystals have a broad fluorescence ranging from the red to near-IR spectral region, and their lifetimes were measured as 170 μs and 87 μs, respectively. The emission cross sections are estimated to be 0.8×10^{-20} and 1.6×10^{-20} cm², respectively. The vibronic levels of their ground state were estimated to be ≈ 1400 cm⁻¹, so they can provide a four-level system [8]. The optical gain of Cr³⁺:YAB crystal was measured in the range from 744 nm to 852.5 nm. The maximum single-pass gain was 1.9 at 830 nm. Second harmonic generation in the UV region (375 nm) was obtained by a Cr³⁺:YAB

crystal with 1.5 times higher conversion efficiency compared with LBO crystal. Consequently $\text{Cr}^{3+}:\text{YAB}$ crystal and $\text{Cr}^{3+}:\text{YGAB}$ crystal have potential as new optically operated materials [9]. To vary the properties of the crystals in the desired direction it is necessary to have the parameters of the band energy structure for the crystals doped by the dopants. This can help to clarify the transfer of the carrier during the interaction with laser beam. In the Ref. 10. it was performed their band structure calculations. However, it would be of great interest to perform the calculation with taking into account of the doping by Cr ions.

In the present work we will do such kind of calculations taking into account of the influence of Chromium ions on the band structure. In the second part are presented the methods of crystal growth and principal features of the crystals. Section 3 describes first methods of principle calculations of the band energy structure. The principal results of the band energy structure calculations and corresponding photoinduced experimental data are given in the Section 4.

2 Crystal growth and crystal features.

$\text{YAl}_3(\text{BO}_3)_4$ single crystals belong to the $R32H$ space group with lattice constants (in Å): $a = 9.293$, $c = 7.236$, $\gamma = 120^\circ$ [11]. The $\text{YAB}:\text{Cr}$ single crystals were synthesized by means of spontaneous crystallization. YAB decomposes at 1280°C into YBO_3 and AlBO_3 due to incongruent melting [12], so crystallization had to be carried out from high-temperature solution. Potassium trimolybdate $\text{K}_2\text{Mo}_3\text{O}_{10}$ with addition of 3wt% of B_2O_3 was used as a solvent [13]. The starting composition of the melt was 20wt% of YAB doped with 1at% of Cr^{3+} ions and 80wt% of the molybdate solvent. The growth was carried out from 200 g of the melt placed in a 100 ml Pt crucible covered with a Pt lid under conditions of low-temperature gradients. The crucible was placed in a resistance furnace isolated thermally to ensure proper temperature gradients. The heating zone of the furnace was controlled with use of Eurotherm 916S programmer. The soaking temperature of the melt was 1100°C , after 24 hours the temperature was lowered at a rate of 10 K/h to 1050°C that is the saturation temperature of the melt. Next the temperature was lowered at a rate of 0.1K/h for 58 days and then the furnace was cooled at a rate of 10 K/h to room temperature. The as-grown $\text{YAB}:\text{Cr}^{3+}$ single crystals (up to $10\times10\times10$ mm) were extracted from the solidified melt by dissolution of the solvent in hot water. According to Ref. [14], the distribution coefficient of Cr^{3+} ions between YAB crystal and the melt is very high and reaches 9.7, what caused non-uniform distribution of the dopant in as-grown crystals. The Cr^{3+} concentration in the central parts of $\text{YAB}:\text{Cr}^{3+}$ crystals was much higher than in the starting composition, and then it decreased towards the faces of the crystals. The photoinduced 532 nm cw laser at wavelength possesses Gaussian-like sequence beam with diameter about 1.5 mm. Its intensity

stability did not exceed 1.6 %. The effect shows its non-sensitivity to the photoinducing beam. The light scattering was controlled by the additional sphere spectrophotometer and it was less than 3%. The absorption measurements were done by spectrophotometer Ocean Optics with spectral resolution 0.2 nm.

3. First-principles calculations for pure and Cr³⁺-doped YAl₃(BO₃)₄

The CASTEP module [15] of Materials Studio package was used for calculations of the structural, electronic and optical properties of pure and Cr³⁺-doped YAB. The exchange-correlation effects were treated within the generalized gradient approximation (GGA) with the Perdew-Burke-Ernzerhof functional [16]. The Monkhorst-Pack scheme *k*-points grid sampling was set at 3×3×4 for the Brillouin zone (BZ). The plane-wave basis set energy cutoff was set at 340 eV; ultrasoft pseudopotentials were used for all chemical elements. The convergence parameters were as follows: total energy tolerance – 1×10⁻⁵ eV/atom, maximum force tolerance 0.03 eV/nm, maximal stress component 0.05 GPa and maximal displacement 0.001 Å.

4. Results of calculations.

The calculated lattice constants after optimization of the crystal lattice structure were as follows (in Å): *a* = 9.25562, *c* = 7.22184, *γ* = 120°. The difference between the calculated and experimental lattice parameters is less than 1 %. Fig. 1 shows the calculated band structure (the conduction and valence bands only) for pure YAB. The low dispersion for the upper valence band indicate on the huge effective mass of the holes formed prevalingly by the antibonding 2pO-2pC states. Experimental value of the band gap is 5.7 eV [17], and the calculated value of the band gap was 5.471 eV, which is a little bit underestimated with respect to the experimental value. Such an underestimation of the calculated band gaps is related to well-known DFT limitations, namely not taking into account the discontinuity in the exchange-correlation potential [18], and is a common feature of all DFT calculations. To overcome such a discrepancy, the so called scissor operator [19] can be used. The action of such an operator is to produce a simple rigid shift of the unoccupied conduction band with respect to the valence band, to eliminate effectively the difference between the theoretical and experimental gap values. Usually the values of this operator can be around 1 – 1.5 eV. However, since in this case the difference between the two values of the band gap was only about 0.23 eV, we decided not to apply the scissor operator and thus we remain entirely within the framework of the ab initio calculations.

Fig. 1. Calculated band structure of pure YAB. The coordinates of the special points of the Brillouin zone are (in terms of the unit vectors of reciprocal lattice: $\Gamma(0, 0, 0)$; A $(0, 0, 1/2)$, H $(-1/3, 2/3, 1/2)$; K $(-1/3, 2/3, 0)$; M $(0, 1/2, 0)$; L $(0, 1/2, 1/2)$).

It is necessary to emphasize that the k -dispersion of the valence bands is very flat which corresponds to huge effective mass and low carrier mobility. The higher dispersion is observed in the BZ direction: K – Γ – M. Assignment of the calculated bands can be performed using the partial density of states (PDOS) diagrams, shown in Fig. 2. The conduction band, which is 2.5 eV in wide, is composed mainly of Y 4d states, with some admixture of Al 3p, O and B 2p delocalized states. The upper valence band, whose widths is about 8 eV, is formed by the Al 3s, 3p, O 2p, B 2s, 2p states. The lower valence band from about -22 eV to about -17 eV – has a clearly seen hyperfine structure. The lower narrow sub-band between -22 and -20 eV is due to Y 4p states, whereas the upper sub-band between -17 and -20 eV is a superposition of the O 2s, Al 3s, 3p and B 2s, 2p states. Finally, a very narrow and deep energy band between -40 and -42 eV is formed by the Y 4s states.

Fig. 2. Calculated partial and total density of states (DOS) for pure YAB.

Fig. 3. Calculated band structure of the YAB:Cr³⁺ crystal. The special points of the Brillouin zone are: $\Gamma(0, 0, 0)$; A $(0, 0, 1/2)$, H $(-1/3, 2/3, 1/2)$; K $(-1/3, 2/3, 0)$; M $(0, 1/2, 0)$; L $(0, 1/2, 1/2)$. The highest occupied state is taken as zero of energy.

Situation becomes different when doping with Cr³⁺ ions (which generally should substitute for Al³⁺ ions) is considered. First of all, the calculated lattice parameters become now (in Å): $a = 9.2932$, $b = 9.2774$, $c = 7.2575$, $\alpha = 89.95^\circ$, $\beta = 90.0^\circ$, $\gamma = 120.08^\circ$. It is crucial that doping with Cr³⁺ leads to minor changes in the lattice constants. The Fig. 3 shows the calculated band structure for the YAB:Cr³⁺ crystal. The most striking difference from the previous case shown in Fig. 1 is that the Cr³⁺ states appear within the forbidden energy band gap. They possess some dispersion which is maximal Moreover, it is possible to distinguish between the t_{2g} and e_g states, which arise from the crystal field splitting of the Cr³⁺ 3d states and which are separated by about 2 eV (Fig. 3). The maximal dispersion of these levels is observed for F – Q – Z direction. The localized Cr impurities are sensitive to the crystalline anisotropy. Such a separation is denoted by $10Dq$ and its value can be determined from the absorption spectra by the position of the first strong spin-allowed transition, which corresponds to the 4T_2 state. Fig. 4 shows the PDOS diagrams. The composition of the calculated electronic bands is the same as for pure YAB, but two very narrow deep bands appear at about -44 eV and -72 eV; they are due to the chromium 3p and 3s states, respectively.

Fig. 4. Calculated partial and total density of states for YAB:Cr³⁺.

For an analysis of the absorption spectra of the Cr³⁺-doped YAB, crystal field theory (namely, exchange charge model, ECM [20]) has been used.

Since detailed description of this model can be found in the literature [21], we shall not give here description of the model and its main equations, but restrict ourselves to mentioning the details of calculations and obtained results. To calculate the crystal field parameters, a large cluster of 31793 ions located at the distances up to 73 Å from the central ion was considered. The overlap integrals between the Cr³⁺ and O²⁻ ions were calculated previously [27]. The calculated values of the crystal field parameters (in Stevens normalization, all in cm⁻¹) are as follows:

Values of the crystal field and $B_4^{-4}=1422.0$; $B_4^{-3}=-3.5$; $B_4^{-2}=994.0$; $B_4^{-1}=1564.0$; $B_4^0=-3259$; $B_4^1=902.8$; $B_4^2=-573.9$; $B_4^3=-77950.4$; $B_4^4=822.0$; $B_2^{-2}=294.9$; $B_2^{-1}=-334.5$; $B_2^0=3098.0$; $B_2^1=-194.3$; $B_2^2=-170.8$. The crystal field Hamiltonian with these parameters was diagonalized in the space

spanned by all LS wave functions of the LS terms of the $3d^3$ electron configuration of Cr^{3+} ion. The Racah parameters B and C were chosen to be 700 and 3163 cm^{-1} , respectively. The calculated energy levels are given below (all in cm^{-1}). The spin-quartet energy levels: ${}^4\text{A}_2 - 0$; ${}^4\text{T}_2 - 16439, 16451, 17254$; ${}^4\text{T}_1 ({}^4\text{F}) - 22672, 24155, 24171$; ${}^4\text{T}_1 ({}^4\text{P}) - 35855, 35947, 39538$. The spin-doublet energy levels: ${}^2\text{E} - 14471, 14489$; ${}^2\text{T}_1 - 15112, 15129, 15677$; ${}^2\text{T}_2 - 20994, 22383, 22498$; ${}^2\text{A}_1 - 28958$; then very dense group of energy levels arising from the orbital triplets and doublets: 30884, 30927, 31052, 31464, 31673, 31818, 33612, 33724 cm^{-1} .

The character of splitting of the orbital triplets and doublets suggests a low symmetry of the Cr^{3+} position (C_1). However, splitting of the orbital doublets is very small, and in all triplet states it is possible to find a group of two very closely located energy levels and a single level, lying far apart from this group. Such a splitting pattern suggests that the local symmetry of the Cr^{3+} position can be approximately described as a trigonal, when a triplet state is split into the doublet and singlet. Such a conclusion can be also verified by the values of the crystal field parameters: the main contribution comes from the B_2^0, B_4^0, B_4^3 parameters, which are characteristic for a trigonal crystal field. Moreover several contribution here should give the broadening caused by electron-phonon interactions and occurrence of non-homogeneities.

Fig. 5 below shows the experimental absorption spectrum of YAB:Cr^{3+} , in comparison with the above-given calculated energy levels. Following the performed X-ray microanalysis these spectra correspond to the 0.85 % of Cr^{3+} ions. However, there exists some non-uniformity through the sample's surface (from 0.65 % up to 1.05 %). So we present the averaged spectrum of the absorption.

Following this figure, agreement between the positions of the calculated energy levels and main features of the absorption spectrum is good. In particular, narrow peaks at about $14800 - 15100 \text{ cm}^{-1}$ nicely agree with the calculated positions of the spin doublets ${}^2\text{E}$ and ${}^2\text{T}_1$. Calculated splitting of the ${}^4\text{T}_2$ state (between 16400 and 17250 cm^{-1}) agrees with the width of the first spin-allowed absorption band. Moreover, the ECM calculated position of the ${}^4\text{T}_2$ state is in a very good agreement with the estimation of the $10Dq$ parameter obtained from the band structure calculations for YAB:Cr^{3+} (Fig. 3). Two wide intensive peaks at about 33000 and 37000 cm^{-1} are due to the superposition of transitions from the ${}^4\text{A}_2$ ground state to the ${}^4\text{T}_1 ({}^4\text{F})$ state and a very dense group of the spin doublet states, which are mixed up with the ${}^4\text{T}_1 ({}^4\text{F})$ state by spin-orbit interaction.

Fig. 5. Experimental absorption spectrum of YAB:Cr³⁺ (solid line) and calculated energy levels (vertical lines). Assignment of the dense group of the spin doublet states in the region above 30000 cm⁻¹ is ambiguous.

Following the absorption spectra we have verified their sensitivity to the illumination by 300 mW SHG of the Nd:YAG laser with wavelength 532 nm. Following the Fig. 6 one can say that the changes are very small. So these crystal may be promising for the high intensive nonlinear optical interactions. The obtained parameters show that the Cr ions change not only the energy positions of the bands, however cause an influence on the band dispersion. Additional monitoring of the photocrystallization does not show any signs of crystallization.

Fig. 6. Changes of the absorption caused by illumination of 532 nm cw laser with power 300 mW in the points corresponding to two different Cr contents.

CONCLUSIONS

Following the experimental measurements and theoretical simulations for the YAB:Cr crystals we have established a good agreement between the positions of the calculated energy levels and main features of the absorption spectrum is good. In particular, narrow peaks at about $14800 - 15100 \text{ cm}^{-1}$ nicely agree with the calculated positions of the spin doublets 2E and 2T_1 . Calculated splitting of the 4T_2 state (between 16400 and 17250 cm^{-1}) agrees with the width of the first spin-allowed absorption band. Moreover, the ECM calculated position of the 4T_2 state is in a very good agreement with the estimation of the $10Dq$ parameter obtained from the band structure calculations for YAB:Cr³⁺ (Fig. 3). The localized Cr³⁺ impurities are sensitive to the crystalline anisotropy. Two wide intensive peaks at about 33000 and 37000 cm^{-1} are due to the superposition of transitions from the 4A_2 ground state to the 4T_1 (4F) state and a very dense group of the spin doublet states, which are mixed up with the 4T_1 (4F) state by spin-orbit interaction. Additional treatment by the 300 mW cw 532 nm wavelengths does not caused any significant changes of the absorption.

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References:

1. T. Bodnar, V. V. Filippov, N. V. Kuleshov, N. I. Leonyuk, V. V. Mal'tsev and O. V. Pilipenko. *Inorganic Materials*, 44, (2008), 863.
2. A. Szysia, L. Lipińska, W. Ryba-Romanowski, P. Solarz, R. Didusko and A. Pajczkowska. *Materials Res. Bulletin*, 44, (2009), 2228.
3. A. Majchrowski & I.V. Kityk. *Ferroelectrics Letters*. V.29, (2002), pp. 31-37.
4. G. Dominiak-Dzik, W. Ryba-Romanowski, R. Lisiecki, I. Földvári, E. Beregi. *Optical Materials*, 31, (2009), 989.
5. A. Majchrowski, J. Ebothe, B.Sahraoui, I.V. Kityk. *Nanotechnology*, V.15, (2004), pp.118-1121.

6. A.Majchrowski, I.V.Kityk, J.Ebothe. *Phys.Status Solidi*, V. **B241**, (2004), pp.3047-3055
7. Elmar C. Fuchs and Karl Gatterer. *Central European Journal of Chemistry*, 6, (2008), 497
8. Iwai, Makoto; Mori, Yusuke; Sasaki, Takatomo; Nakai, Sadao; Sarukura, Nobuhiko; Liu, Zhenlin; Segawa, Yusaburo. *Japanese Journal of Applied Physics*, 34, (1995) pp. 2338 (1995).
9. Rajeev Bhatt, S. Kar, K. S. Bartwal, V. K. Wadhawan. *Solid State Communications*, **127**, (2003), 457.
10. A.H.Reshak, S.Auluck, A.Majchrowski, I.V.Kityk. *Solid State Sciences*, V.**10**, (2008), pp.1445-1448.
11. G. Meszaros, E. Svab, E. Beregi, A. Watterich, M. Toth, *Physica B* 276 (2000) 310
12. S.F. Akhmetov, G.L. Akhmetova, V.S. Kovalenko, N.I. Leonyuk, A.V. Pashkova, *Soviet-Phys. Dokl.*, **23** (1978) 107
13. G. Wang, H.G. Gallagher, T.P.J. Han, B. Henderson, J. Cryst. Growth, **153** (1995) 169
14. N.I. Leonyuk, E.V. Korpulina, J.Y. Wang, X.B. Hu, and A.V. Mokhov, *J. Cryst. Growth*, **252** (2003) 174
15. M.D. Segall, P.J.D. Lindan, M.J. Probert, C.J. Pickard, P.J. Hasnip, S.J. Clark, M.C. Payne, *J. Phys.: Condens. Matter* 14 (2002) 2717
16. J.P. Perdew, K. Burke, M. Ernzerhof, *Phys. Rev. Lett.* 77 (1996) 3865
17. A.H. Reshak, S. Auluck, A. Majchrowski, I.V. Kityk, *PMC Physics B* 1 (2008) 8
18. J.P. Perdew, M. Levy, *Phys. Rev. Lett.* 51 (1983) 1884
19. Z.H. Levine, D.C. Allane, *Phys. Rev. B* 43 (1991) 4187
20. B.Z. Malkin, in: A.A. Kaplyanskii, B.M. Macfarlane (Eds.), *Spectroscopy of solids containing rare-earth ions*, North-Holland, Amsterdam, (1987), 33–50
21. B.Z. Malkin, in: A.A. Kaplyanskii, B.M. Macfarlane (Eds.), *Spectroscopy of solids containing rare-earth ions*, North-Holland, Amsterdam, (1987), 33–50;
22. C. Jousseume, D. Vivien, A. Kahn-Harari, B.Z. Malkin, *Opt. Mater.* 24 (2003) 143;
23. M.N. Popova, S.A. Klimin, E.P. Chukalina, R.Z. Levitin, B.V. Mill, B.Z. Malkin, E. Antic-Fidancev, J. Alloys Compds. 380 (2004) 84;
24. M.N. Popova, E.P. Chukalina, B.Z. Malkin, A.I. Iskhakova, E. Antic-Fidancev, P. Porcher, J.P. Chaminade, *Phys. Rev. B* 63 (2001) 075103;
25. M.N. Popova, S.A. Klimin, E.P. Chukalina, E.A. Romanov, B.Z. Malkin, E. Antic-Fidancev, B.V. Mill, G. Dhalenne, *Phys. Rev. B* 71 (2005) 024414;
26. A.V. Savinkov, D.S. Irisov, B.Z. Malkin, K.R. Safiullin, H. Suzuki, M.S. Tagirov, D.A. Tayurskii, *J. Phys.: Condens. Matter* 18 (2006) 6337
27. E. Cavalli, A. Belletti, M.G. Brik, *J. Phys. Chem. Solids* 69 (2008) 29.