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Entropy based feature selection for text categorization

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ABSTRACT

In text categorization, feature selection can be essential not only for reducing the index size but also for improving the performance of the classifier. In this article, we propose a feature selection criterion, called Entropy based Category Coverage Difference (ECCD). On the one hand, this criterion is based on the distribution of the documents containing the term in the categories, but on the other hand, it takes into account its entropy. ECCD compares favorably with usual feature selection methods based on document frequency (DF), information gain (IG), mutual information (IM), χ², odd ratio and GSS on a large collection of XML documents from Wikipedia encyclopedia. Moreover, this comparative study confirms the effectiveness of selection feature techniques derived from the χ² statistics.

1. INTRODUCTION

Text categorization (or classification) is a supervised task for which, given a set of categories, a training set of preclassified documents is provided. Given this training set, the task consists in learning the class descriptions in order to be able to classify a new document in one of the categories ([25, 21, 19]).

Irrespective of the categorization method applied, the documents must be represented by a set of features. Several models can be used, such as the boolean model, the probabilistic model or the vector space model which described documents as a bag of words. As each term belonging to at least one document can be considered as a feature, this can lead to an index size (i.e. the feature space dimension) very large, even for a small collection composed of short documents like news articles. Moreover, all these words are not equally useful for the categorization, like for instance stop words, synonymous, etc. Their distribution must also be studied. For example, words that appear in a single document or in all the documents are not relevant for the categorization task. So, we need to extract a more effective set of features from the text, that can be used to efficiently represent the documents for their categorization. This preprocessing step, can be essential on textual data for improving the performance of the categorization algorithm ([26, 7]).

Among the many methods that can be used, two strategies can be distinguished: on the one hand, the dimension reduction which consists in creating new synthetic features that are a combination of the original ones, like for instance the Latent Semantic Analysis (LSA) which uses a Singular Value Decomposition (SVD) to extract concepts from the words [2] and, on the other hand, the feature subset selection that is based on non useful features elimination [9]. In this last case, the selection can be embedded, in other words integrated in the categorization algorithm itself. The feature selection can also be based on a wrapper approach which tries different subsets of features as input and takes the subset that produces the best results. Finally, the selection can be done before the categorization, using a criterion to filter the features.

The common feature selection criteria proposed in the literature ([24, 1, 17, 8]) notably, document frequency (DF), information gain (IG), χ² or mutual information (IM) consider the distribution of the documents containing the term between the categories but they do not take into account the frequency of the term between the categories. However, we can note that a term which is characteristic of a category must appear in a greater number of documents belonging to this category than into the other categories but it should also appear more frequently. For this reason, we propose the Entropy based Category Coverage Difference, denoted (ECCD), which exploits also the entropy of the term.

In this article, this ECCD criterion is also compared to usual feature selection methods mentioned above (IG), χ² and mutual information (IM) on a large collection of XML documents. Indeed, previous works have already shown that removing up to 90% of terms can improve the classification accuracy measured by precision [26]. However, these experiments have been performed on corpora composed of short documents such as the well known Reuters Collection, composed of short news articles ([12, 13, 24, 16, 26, 5, 8, 1]). The second aim of this work is to verify the performance of these feature selection methods on the large INEX XML Mining collection composed of heterogeneous XML documents extracted from the Wikipedia encyclopedia [3].

ECCD proposed in this article is defined in section 2 while
the usual criteria are detailed in section 3. The experiments
and the obtained results are presented respectively in
sections 4 and 5.

2. FEATURE SELECTION BASED ON EN-
TROPY

2.1 Textual document representation

In text categorization, the vector space model (VSM) in-
troduced by Salton et al. [20] is widely used as well for
flat documents as for semi-structured documents written
in markup languages like HTML or XML. In this model,
documents are represented as vectors which contain term
weights. Given a collection \( D \) of documents, an index \( T = \{t_1, t_2, ..., t_p\} \), where \( |T| \) denotes the cardinal of \( T \), gives
the list of terms (or features) encountered in the documents
of \( D \). A document \( d_i \) of \( D \) is represented by a vector \( \bar{d}_i = (w_{i,1}, w_{i,2}, ..., w_{i,|T|}) \) where \( w_{i,j} \) represents the weight of the term
\( t_j \) in the document \( d_i \). In order to calculate this weight,
the TF.IDF formula can be used [20]:

\[
w_{i,j} = \frac{n_{i,j}}{\sum_n n_{i,n}} \times \log \frac{|D|}{|\{d_i : t_j \in d_i\}|}
\]

where \( n_{i,j} \) is the number of occurrences of \( t_j \) in document
\( d_i \), normalized by the number of occurrences of all terms in
document \( d_i \). \(|D|\) is the total number of documents in the

corpus and \(|\{d_i : t_j \in d_i\}|\) is the number of documents in
which the term \( t_j \) occurs at least once time.

However, even for limited collections, the dimension of the
index can be exceedingly large. For example, in INEX

collection, 652,876 non-trivial words have been identified.
In a small collection of 21,578 documents extracted from

Reuters news, more than 40,000 non-trivial words could be
identified [19].

Moreover, in the context of categorization, the terms be-
longing to this bag of words are not necessarily discriminant
features of the categories. For this reason, non useful words
must be removed, in order to extract a subset \( T' \) from \( T \)
more suited for the categorization task. For that purpose,
the local approach consists in filtering a specific subset for
each category in such a way that the indices used to rep-
resent documents belonging to different categories are not
the same, while the global approach, adopted in this work,
uses the same subset \( T' \) extracted from \( T \) to represent all
the documents of the collection [21, 10]).

In this article, we introduced the ECCD criterion in order
to select a subset \( T' \) from \( T \), providing a more efficient

description of the documents. ECCD considers not only the
number of documents belonging to the category but also
the number of documents belonging to the other categories.
Moreover, this criterion also takes into account the entropy
of the term. Thus, ECCD exploits two hypotheses to eval-
uate if a term is a characteristic feature for a category. Ac-
cording to the first one, the major part of the documents
containing this term must belong to this category. Ac-
cording to the second one, its number of occurrences must be
important in the documents of the category and, on the
contrary, it must be lower in the other categories.

2.2 Entropy based Category Coverage Differ-
ence criterion (ECCD)

Let \( n_{j,k} \) be the number of occurrences of \( t_j \) in the category
\( c_k \) and, \( tf^k_j \) the frequency of \( t_j \) in this category \( c_k \):

\[
tf^k_j = \frac{n_{j,k}}{\sum_k n_{j,k}}
\]

The Shannon entropy \( E(t_j) \) of the term \( t_j \) is given by [22]:

\[
E(t_j) = - \sum_{k=1}^c (tf^k_j \times (\log_2(tf^k_j)))
\]

The entropy is minimal, equals 0, if the term \( t_j \) appears
only in one category. We consider that this term might have
a good discriminatory power in the categorization task.
Conversely, the entropy is maximal, equals \( E_{max} \), if \( t_j \) is not
a good feature to represent the documents i.e. if \( t_j \) appears
in all the categories with the same frequency. ECCD\((t_j, c_k)\)
is defined by:

\[
ECCD(t_j, c_k) = \frac{(P(t_j|c_k) - P(t_j|\bar{c}_k)) \times E_{max} - E(t_j)}{E_{max}}
\]

with \( P(t_j|c_k) \) (respectively \( P(t_j|\bar{c}_k) \)) the probability of
observing the word \( t_j \) in a document belonging to the category
\( c_k \) (respectively the other categories):

\[
P(t_j|c_k) = \frac{|\{d_i \in c_k : t_j \in d_i\}|}{|c_k|}
\]

\[
P(t_j|\bar{c}_k) = \frac{|\{d_i \notin c_k : t_j \in d_i\}|}{|D| - |c_k|}
\]

where \(|c_k|\) represents the number of documents in the cat-

egory \( c_k \) and \(|D| - |c_k|\) the number of documents in the

rest of the collection.

We can note that the probabilities of observing the word
\( t_j \) in \( c_k \) and \( \bar{c}_k \) could also be compared with a ratio but
this ratio is undefined when the denominator is null. For
this reason, it is better to use a difference as done in the
formula 1. It is obvious that \( P(t_j|c_k) \) increases with the
number of documents in \( c_k \) containing \( t_j \). Consequently,
the higher the number of documents in \( c_k \) containing \( t_j \) and
the lower the number of documents in the other categories
containing \( t_j \), the higher the first part of the formula 1. So,
\( t_j \) is a characteristic feature of the category \( c_k \) if the value
of \( ECCD(t_j, c_k) \) is high, in other words, when the major
part of the documents containing this term belongs to this
category and simultaneously, its number of occurrences is
higher in \( c_k \) than in the other categories.

Given a term \( t_j \) and a category \( c_k \), \( ECCD(t_j, \bar{c}_k) \) can be
computed from a contingency table. Let \( A \) be the number
of documents in the category containing \( t_j \); \( B \), the number
of documents in the other categories containing \( t_j \); \( C \), the
number of documents of \( c_k \) which do not contain \( t_j \) and \( D \),
the number of documents in the other categories which do
not contain \( t_j \) (with \( N = A + B + C + D)\):

<table>
<thead>
<tr>
<th></th>
<th>( c_k )</th>
<th>( \bar{c}_k )</th>
</tr>
</thead>
<tbody>
<tr>
<td>( t_j )</td>
<td>( A )</td>
<td>( B )</td>
</tr>
<tr>
<td>( \bar{t}_j )</td>
<td>( C )</td>
<td>( D )</td>
</tr>
</tbody>
</table>

Using this contingency table, equation 1 can be estimated
3. COMPARATIVE STUDY OF FEATURE SELECTION CRITERIA

In the next section, we compare the criterion defined in the previous section with other usual selection feature methods which have proved good performances in text categorization. These methods are the document frequency (DF), information gain (IG), \( \chi^2 \), mutual information (IM) and odd ratio. In our experiments mutual information (IM) and odd ratio have been less effective. Consequently, only the definitions of the first ones, for which we will detail the results in the next section, are given.

3.1 Document frequency Thresholding (DF)

This method exploits the hypothesis according to which a term belonging to a few number of documents is not a good feature for the categorization task [24].

So, only the terms, that appear in a number of documents higher to a defined threshold, are selected. This threshold can be determined using a training set.

Given a term \( t_j \), this criterion can be computed globally on the collection \( DFG(t_j) \) or on each category \( c_k \) \( DFL(t_j, c_k) \):

\[
DFG(t_j) = P(t_j) \approx \frac{A + B}{N} \\
DFL(t_j, c_k) = P(t_j|c_k) \approx \frac{A}{A + C}
\]

One usual way to apply this method consists in eliminating all the words which appear in less than \( x \) documents, \( x \) varying between 1 and 3 ([24, 5, 15]). Frequently, this technique is used with another feature selection method.

3.2 Information Gain (IG)

Given a term \( t_j \) and a category \( c_k \), the information gain \( IG(t_j, c_k) \) is defined by [1]:

\[
IG(t_j, c_k) = P(t_j, c_k) \log \left( \frac{P(t_j, c_k)}{P(t_j)P(c_k)} \right) + P(t_j, c_k) \log \left( \frac{P(t_j, c_k)}{P(t_j)P(c_k)} \right)
\]

\[
IG(t_j, c_k) \approx - \frac{A + C}{N} \log \left( \frac{A + C}{N} \right) + \frac{A}{N} \log \left( \frac{A}{A + B} \right) + \frac{C}{N} \log \left( \frac{C}{C + D} \right)
\]

Only the words for which the value of the criterion is the most important are considered as characteristics for \( c_k \).

3.3 The \( \chi^2 \) and its extension GSS

\( \chi^2 \) is used to measure the independence between a term \( t_j \) and a category \( c_k \). It is originally defined by:

\[
\chi^2(t_j, c_k) = \frac{N}{P(t_j).P(c_k)} \cdot \frac{[P(t_j, c_k)P(t_j) - P(t_j)P(c_k)]^2}{P(t_j)P(c_k)}
\]

\[
\chi^2(t_j, c_k) \approx \frac{N(AD - BC)^2}{(A + B)(A + C)(B + D)(C + D)}
\]

This criterion equals 0 when \( t_j \) and \( c_k \) are independent. On the contrary, \( t_j \) is considered as a characteristic feature for \( c_k \) if the value of \( \chi^2(t_j, c_k) \) is high.

Ng et al. [17] have observed that the power of 2 at the numerator must be eliminated because it gives the same importance to the probabilities that indicate a positive correlation between \( t_j \) and \( c_k \) [14] and to those that indicate a negative correlation. Galavotti et al. have also proposed to eliminate on the one hand \( N \), that is constant, and on the other hand, the probabilities at the denominator that emphasize very rare features and very rare categories [8]. By removing these factors, Galavotti has introduced the GSS criterion:

\[
GSS(t_j, c_k) = P(t_j, c_k) \cdot P(\bar{t}_j, \bar{c}_k) - P(\bar{t}_j, c_k).P(t_j, \bar{c}_k)
\]

\[
GSS(t_j, c_k) \approx \frac{AD - BC}{N^2}
\]

Both \( \chi^2 \) and GSS criteria will be presented in the experiments even if the latest is less popular.

4. EXPERIMENTS

In order to evaluate and compare previously defined selection feature criteria, we performed several experiments on the INEX XML Mining collection [3][4]. After describing this collection, we detail the experimental protocol and we present the obtained results.

4.1 Collection description

The different presented selection feature criteria were subject of several studies in the past. The main used collection for these studies is the well known Reuters-21578 collection proposed by Lewis [14]. This collection is composed of 21,578 documents published on the Reuters newswire in 1987 and manually labelled by Carnegie Group, Inc. and Reuters, Ltd. This collection is often used, although it suffers from many problems. The main drawback is its size. Indeed, the number of documents that composed the collection is small with only 21,578 documents. On top of that, these documents are short with on average 137 words per document. This collection is also disputed in reason of the famous "blab blab blab" [14] that composes some documents.

At last, different subsets were used for training and testing in the different studies, that make the comparison tough between obtained results.

In this article, we aim to verify that feature selection, frequently evaluated on small collections of short documents, is also efficient on a bigger collection composed of heterogeneous XML documents. The collection, used in the experiments, is the INEX XML Mining collection from the competition INEX 2008 [4]2. This INEX XML Mining collection is composed of 114,366 documents extracted from the well known Wikipedia encyclopedia [3]. The number of words per document is 423 on average, which is three times more than for the documents of Reuters-21578. Moreover, the index size is greater for the INEX XML Mining collection with 160,000 words compared to 40,000 words for the Reuter-21578 collection.

Documents of the INEX XML Mining collection are categorized into 15 categories that correspond to specific topics, such as sociology, sport, fiction, europe, tourism, united states, etc.. Each document belongs to exactly one category.

2INEX competition: http://www.inex.otago.ac.nz
The training set, given by the competition INEX, is created using 10% of the whole collection.

4.2 Preprocessing, feature selection and categorization

Before performing the categorization task, the index of words that is used to represent documents is preprocessed. In order to perform the indexing, the LEMUR software has been used. Without preprocessing, the original index size is 652,876. In order to reduce this index, we perform a common stemming step using the Porter algorithm that aims to reduce each word to its root form. Thanks to this stemming, the index is reduced to 560,209 distinct words. A lot of words that are not discriminant for the categories are useless. Thus, we remove numbers and words that contain figures (7277, -2311, 0b254c, etc.). The obtained index \( T^* \) after removing all useless words is composed of 161,609 words over the whole collection and 77,706 words in the training set.

However, as explained in the previous section, the terms of \( T^* \) are not necessarily appropriated for the categorization task inasmuch they are not discriminatory for the categories. Thus, thanks to the feature selection criteria, we create a subset \( T' \) from \( T \) that is more representative than \( T \).

All criteria have been used in the same way: firstly, a number \( n \) of words that will be selected for each category, is set. Secondly, given a category, terms are ranked by decreasing order in function of the selection feature criteria values and, the first \( n \) words are selected. Finally, the index \( T'' \) is composed of the union of the first \( n \) selected words for each category. Experiments have been done with values of \( n \) varying between 10 to 5,000.

In our experiments, the categorization task is performed using SVM algorithm available in the Liblinear library. SVM has been introduced by Vapnik for solving two class pattern recognition problems using Structural Risk Minimization principal. Many studies showed the efficiency of SVM in text categorization. The results provided by this approach on the INEX XML Mining collection are presented in the next section.

5. RESULTS

In our experiments mutual information (IM) and odd ratio have been less effective. Consequently, only the results obtained with ECCD, DF, IG, \( \chi^2 \) and GSS are given.

Two different measures are used to evaluate the performance of the categorization. The first one is the classification rate which corresponds to the number of correct labelled documents divided by the total number of documents. The second measure is the reduction rate obtained using the index \( T'' \) relatively to the original index \( T \) (77,706 words) and it is computed by

\[
\frac{|T| - |T''|}{|T|}
\]

If we consider the original index \( T \) composed of 77,706 words and if we perform the categorization, we obtain a classification rate of 78.79%. Figure 1 represents the obtained classification rate in function of the size of the index \( T'' \) that depends on the number \( n \) of words selected by category with the different selection feature criteria. As shown by this figure, reducing significantly the index size leads to still quite good results. Except for the DFG and the \( \chi^2 \), for an index \( T'' \) of 3,000 words the classification rate is around 75% which corresponds to a loss of around 5% on the classification rate with an important reduction rate of about 96%. By decreasing order of performance, ECCD criterion obtains the best results, followed by GSS, IG, CC, DFL, DGL and \( \chi^2 \). Globally, these results confirm the different comparative studies performed on smaller collections. We can notice that the \( \chi^2 \) criterion leads to unsatisfactory results when, according to [21], those results should have been similar to those obtained with IG. The ECCD criterion leads to the best results and this improvement is more significant for a small index size. For an index size of 5,495 words, which corresponds to a reduction rate of 92.93%, the classification rate is 77.86%, which corresponds to a loss of only 1.18%.

6. CONCLUSION

This study, realized on the INEX XML Mining 2008 collection, confirms the importance in the use of selection feature for the categorization of XML documents and emphasizes the efficiency of criteria derived from the \( \chi^2 \) such as GSS. It also shows the interest of using the words frequency with the entropy. Indeed, we observed that taking into account the occurrence of terms within the different classes using the entropy of the terms lets us improve significantly classification rate. We can also note that the term occurrence could be integrated into the other criteria. To this extend, we could calculate these criteria with the number of term per class instead of the number of document that contain the term.

7. REFERENCES


\[\text{Lemur Project: } \text{http://www.lemurproject.org}\]

\[\text{Liblinear: } \text{http://www.csie.ntu.edu.tw/~cjlin/liblinear/ - L2 loss support vector machine primal}\]


