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Tracking Improvement Based on the Proxy Control Scheme for Bilateral Teleoperation System under Time-Varying Delays

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Abstract
This paper addresses the problem of the position/force tracking in teleoperation system and proposes a haptic proxy control scheme. Compared to previous works, communication delays are assumed to be both time-varying and asymmetric, and the response of the synchronization and the transparency are improved. The control design is performed using Linear Matrix Inequality (LMI) optimization based on Lyapunov-Krasovskii functionals (LKF) and $H_{\infty}$ control theory. With the designed controllers, the simulations of different working conditions, such as abrupt motion and wall contact, are performed and show the effectiveness of the proposed solution.

1. Introduction

A teleoperation system is an extension of human manipulative capabilities to the remote environment. A typical teleoperation system is composed of the human operator, the master haptic-interface robot, the communication medium, the slave robot and the environment. If the position/velocity/force information of the master robot handled by the human operator are only transmitted from the master to the slave, the teleoperation system is called unilateral, and if the corresponding data of the slave is also transmitted back to the master, the teleoperation system is bilateral, we will deal with this second case [1, 12].

In bilateral teleoperation, the master and slave are coupled via the communication medium, which incurs the additional dynamics represented by time-varying delays (especially with the internet) [13, 16, 22]. In order to avoid a severe deterioration of the global performance, these delays must be considered at the control design stage [2]. Many methods have been presented to address the stability problems with time delays, for which the passivity formalism based on the Velocity-Force (VF) scheme is a prevalent one. Since the cornerstone papers of Anderson and Spong [1], Niemeyer and Slotine [15], the conception of the passivity, the scattering and the waving variable has been extensively studied for the controller design in a passive and stable fashion. Besides, another formulation is the passivity-based structure without the transformation of wave variables. A recent approach is the energy/power based time domain passivity control [17, 21]. Overall, the latest passivity-based method can deal with the stabilization and the velocity tracking under time-varying delays, but does not allow for optimizing the system performance, especially, does not guarantee the position/force tracking in general.

For the cases of non-passive approach, various control strategies have been proposed. [8, 11, 18] presented a variety of novel architectures to guarantee the system performance. While these approaches are very inspiring, the time delays are assumed to be constant or symmetric. Recently, some other non-passive based strategies have been proposed, in [4, 7, 12, 14], in order to deal with the time-varying delays, but for these methods, the synchronization or the transparency of the teleoperation system is hard to guarantee.

Apart from the basic stability of teleoperation system under delays, there are primarily two kinds of performance of the bilateral teleoperation system. Firstly, the slave robot should track the position of the master manipulator, and secondly, the environmental force acting on the slave, when it contacts the external environment, should be accurately and real-time transmitted to the master [3]. These two objectives are defined as the position/force tracking, which will be resolved in this paper. With this aim in mind, Lyapunov approaches for time-delay systems are helpful. In the case of time-varying delays, many stability conditions have been proposed in terms of Lyapunov-Krasovskii functionals (LKF), which can be solved by Linear Matrix Inequalities (LMI) [5](see also the included references). For the performance consideration, the $H_{\infty}$ control theory will be used [6, 20, 24]. In short, in this paper, we will propose a novel proxy control scheme for the bilateral teleoperation system under variable and asymmetric delays, which makes use of LKF to ensure the stability, and further, realize the position tracking by $H_{\infty}$ control. Finally, the characteristic of the control scheme can assure the force tracking.

1Jean-Pierre Richard is also with INRIA NON-A.
This paper is organized as follows: Section 2 introduces the theorems to be used later. The problem and the assumptions under consideration are presented in Section 3. In Section 4, the bilateral teleoperation system using the LKF and $H_{\infty}$ control is given. Results of simulation are presented in Section 5. Finally we conclude and discuss the future work in Section 6.

2. Preliminaries

This section is devoted to the stability analysis with $H_{\infty}$ performance index. For the simplicity, the teleoperation system will be modeled as a linear time-varying delay system. Firstly, let us consider a bilateral teleoperation system without the time-varying delays, but with the perturbation,

$$\begin{cases}
\dot{x}(t) = Ax(t) + Bw(t) \\
z(t) = Cx(t)
\end{cases} \quad (1)$$

Where, $x(t) \in \mathbb{R}^n$ is the state system, $w(t) \in \mathbb{R}^l$ is defined as the exogenous disturbance signal, and $z(t) \in \mathbb{R}^r$ is seen as the objective control output, $A$, $B$ and $C$ are constant matrices.

For ensuring the stability of system and guaranteeing the improvement of the overall performance, Bounded Real Lemma (BRL) with Lyapunov functional stability condition is used to derive LMI stability conditions [6].

With a prescribed scalar $\gamma$, we define the performance index,

$$J(w) = \int_0^\infty (z(t)^T z(t) - \gamma^2 w(t)^T w(t)) dt \quad (2)$$

Then, according to the theory of $H_{\infty}$ control, we can ensure the stability and optimize the performance of the system by verifying the performance index,

$$J(w) < 0 \quad (3)$$

So, we obtain the following theorem with the consideration of $H_{\infty}$ control [6].

Theorem 1 Suppose there exists $n \times n$ matrices $P > 0$, $P_2$, $P_3$, and a positive scale $\gamma$, such that the condition (4) with the notation (5) is feasible, the system (1) is asymptotically stable and $J(w) < 0$.

$$\Gamma_1 = \begin{bmatrix}
\Gamma_1^{1,1} & P - P_2^T \\
* & -P_3 - P_3^T
\end{bmatrix} < 0 \quad (4)$$

Based on the theorem 1, we consider the bilateral teleoperation system with the time-varying delays and the perturbation, the system is generally modeled as follow,

$$\begin{cases}
\dot{x}(t) = \sum_{i=0}^n A_i x(t - \tau_i(t)) + Bw(t) \\
z(t) = Cx(t) \\
x(t_0 + \theta) = \phi(\theta), \ddot{x}(t_0 + \theta) = \ddot{\phi}(\theta), \theta \in [-h_2, 0]
\end{cases} \quad (6)$$

Where, $\tau_0(\theta) \equiv 0$, $\phi(\theta)$ is the initial condition, and the time-varying delays, $\tau_i(t) \in [h_1, h_2]$, $h_1 \geq 0$, $i = 1, 2, ..., n$. Considering the following Lyapunov-Krasovskii functional [5],

$$V(t, x, \ddot{x}(t)) = x(t)^T P x(t) + \int_{t-h_2}^t x(s)^T S x(s) ds + \int_{h_1}^t x(s)^T S x(s) ds + \int_{h_1}^{t+h} \dot{x}(s)^T R \dot{x}(s) ds d\theta + \sum_{i=1}^n (h_2 - h_1) \int_{-h_2}^{h_2} \dot{x}(s)^T R \dot{x}(s) ds d\theta \quad (7)$$

Theorem 2 [23] Suppose there exists $n \times n$ matrices $P > 0$, $R > 0$, $S > 0$, $S_a > 0$, $R_a > 0$, $P_2$, $P_3$, $Y_1$, $Y_2$, $i = 1, 2, ..., n$, and a positive scale $\gamma$, such that the condition (8) with the notation (9) is feasible, the system (6) is asymptotically stable and $J(w) < 0$ for time-varying delays $\tau_i(t) \in [h_1, h_2]$, $i = 1, 2, ..., n$.

Proof. The proof can be found in the theorem 2 of [23]. To ensure $J(w) < 0$, the term $z(t)^T z(t) - \gamma^2 w(t)^T w(t)$ can be added into $\dot{V}(t, x(t), \ddot{x}(t))$. Considering the system of (6), we get,

$$\dot{V}(t, x(t), \ddot{x}(t)) + z(t)^T z(t) - \gamma^2 w(t)^T w(t) = x(t)^T (S + S_a) x(t) + \dot{x}(t)^T P x(t) + x(t)^T P \dot{x}(t) - x(t-h_1)^T S x(t-h_1) - x(t-h_2)^T S_a x(t-h_2) + \dot{x}(t)^T [h_2^T R + (h_2 - h_1)^2 \sum_{i=1}^n R_a] \dot{x}(t) \quad (10)$$

Then, substituting for $z(t)$, applying the Jensen’s inequality [9], then obtain,
\[
\Gamma^2 = \begin{pmatrix}
\Gamma_{11}^2 & \Gamma_{12}^2 & R + \sum_{i=1}^n P_i^T A_i - nY_i^T & nY_i^T & -P_i^T A_i + Y_i^T & \ldots & -P_i^T A_i + Y_i^T & Y_i^T & \ldots & Y_i^T & P_i^T B \\
* & * & * & -S - R & 0 & 0 & 0 & 0 & 0 & 0 & 0 \\
* & * & * & * & -S_n & 0 & 0 & 0 & 0 & 0 & 0 \\
* & * & * & * & * & -R_{a1} & 0 & 0 & 0 & 0 & 0 \\
* & * & * & * & * & * & \ldots & 0 & 0 & 0 & 0 & 0 \\
* & * & * & * & * & * & * & -R_{an} & 0 & 0 & 0 \\
* & * & * & * & * & * & * & * & * & -R_{an} & 0 \\
* & * & * & * & * & * & * & * & * & * & -\gamma^2 I \\
\end{pmatrix} < 0
\]

\(\Gamma_{11}^2 = S + S_n - R + A_0^T P_2 + P_2^T A_0 + C^T C, \quad \Gamma_{12}^2 = P - P_2^T + A_0^T P_3, \quad \Gamma_{22}^2 = -P_3 - P_3^T + h_1^2 R + (h_2 - h_1)^2 \sum_{i=1}^n R_{ai}\)
• $F_m(t)$ and $F_s(t)$ are the actuated inputs of the master and the slave.

• $F_h(t)$ and $F_c(t)$ are the effects of the human operator and environment on the system, $F_h(t)$ and $F_c(t)$ are the estimations of these two forces, which can be obtained by adding the perturbation observers in reality (due to the space limitation, the perturbation observer will not be introduced in the paper).

• $\tau_1(t)$ (from the master to the slave) and $\tau_2(t)$ (from the slave to the master) are the time-varying delays, which are modeled in [13].

• $\theta_m(t)\theta_m(t)$, $\theta_p(t)\theta_p(t)$ and $\hat{\theta}_s(t)\hat{\theta}_s(t)$ are the velocities/positions of the master, the proxy of master and the slave.

The controller $C$ and the proxy of master will be designed in sequential steps in next section. In particular, the proxy of master is like a remote observer of the master, which is used in the slave side to reduce the impact of the time-varying delays.

According to the novel scheme, the following assumptions are made,

1. The master and the slave are linear dynamical systems.

2. The communication delays are bounded, $\tau_1(t)$, $\tau_2(t)\in [h_1, h_2]$.

3. The data packet exchanged between the master, the proxy of master and the slave are time-stamped, so the master, the proxy of master and the slave clock are synchronized [13].

4. The master, the proxy and the slave systems have a local controller ensuring the marginal stability (only the speed stability), $K_{mp}^0$ and $K_{s}^0$.

The objective of the paper is to design the proxy of master and the controller $C$ in Figure 1 to ensure the stability of the whole system and the position tracking between the master and the slave under time-varying delays. Besides, because of the characteristic of the control scheme, the force tracking, $F_m(t) = \hat{F}_c(t) - \tau_2(t)$, is realized, if the stability of the whole system is verified. The master is given by following model,

\[
\begin{align*}
\Sigma_m : \quad & \dot{x}_m(t) = (A_m - B_m K_{mp}^0) x_m(t) + B_m (F_m(t) + F_h(t)) \\
& + B_m (\hat{F}_c(t) + \hat{F}_h(t) - \hat{\tau}_1(t))
\end{align*}
\]

(16)

Where, $x_m(t) = \hat{\theta}_m(t)$ is the state of the master, $K_{mp}^0$ is the local partial state feedback, it is supposed to be known as the assumption 4 above.

Figure 2 shows the scheme of the proxy of master, the block diagram 'Proxy' represents the proxy model, which is exactly same with the master. $L$ is the gain that will be designed, $\hat{\tau}_1(t)$ is the estimated network delay between the master and proxy. As the assumption 3 above, the delay can be measured at the proxy and slave side, $\hat{\tau}_1(t) = \tau_1(t)$. The model of the proxy is as follow,

(17)

\[
\begin{align*}
\Sigma_p : \quad & \dot{x}_p(t) = (A_m - B_m K_{mp}^0) x_p(t) - B_m F_p(t - \tau_1(t)) \\
& + B_m (\hat{F}_c(t) + \hat{F}_h(t) - \hat{\tau}_1(t))
\end{align*}
\]

As the master, $x_p(t) = \hat{\theta}_p(t)$, and the gain $L$ is used to synchronize the position between the master and the proxy of master,

\[
\begin{align*}
F_p(t - \tau_1(t)) = L \begin{pmatrix}
\hat{\theta}_p(t - \hat{\tau}_1(t)) \\
\hat{\theta}_m(t - \tau_1(t))
\end{pmatrix}
\end{align*}
\]

(18)

\[
L = \begin{pmatrix}
L_1 & L_2 & L_3
\end{pmatrix}
\]

Next, $K$ is the gain of the controller $C$,

\[
F_s(t) = K \begin{pmatrix}
\hat{\theta}_s(t) \\
\hat{\theta}_p(t) - \hat{\theta}_p(t)
\end{pmatrix}
\]

(19)

\[
K = \begin{pmatrix}
K_1 & K_2 & K_3
\end{pmatrix}
\]

Finally, the model of the slave is given,

\[
\begin{align*}
\Sigma_s : \quad & \dot{x}_s(t) = (A_s - B_s K_{s}^0) x_s(t) - B_s F_s(t) \\
& + B_s F_c(t)
\end{align*}
\]

(20)

Where, $x_s(t) = \hat{\theta}_s(t)$.

4. Main Results

The objective of this section is to provide a control design for the proxy of master and the controller $C$, to achieve the stability of the whole system with guaranteed performance, the position/force tracking.

4.1. The design of proxy of master

Firstly, we will design the proxy of master by Lyapunov-Krasovskii functional, $H_\infty$ control and LMI. Taking into the master and the proxy, we describe the two systems as the stabilization of the following linear system,

\[
\begin{align*}
\Sigma_{mp} : \quad & \begin{pmatrix}
\dot{x}_{mp}(t) \\
\dot{z}_{mp}(t)
\end{pmatrix} = \begin{pmatrix}
A_{mp} x_{mp}(t) + A_{mp}^2 x_{mp}(t - \tau_1(t)) \\
B_{mp} u_{mp}(t) \\
C_{mp} x_{mp}(t)
\end{pmatrix}
\end{align*}
\]

(21)
Where,
\[
x_{mp}(t) = \begin{pmatrix} \dot{\theta}_p(t) \\ \dot{\theta}_m(t) \\ \theta_p(t) - \theta_m(t) \end{pmatrix}
\]
\[
w_{mp}(t) = F_r(t) + F_h(t - \tau_1(t))
\]
\[
z_{mp}(t) = \begin{pmatrix} \theta_p(t) - \theta_m(t) \end{pmatrix}
\]
\[(22)\]

So,
\[
A_{mp} = \begin{pmatrix} A_m - B_mK_m^0 & 0 & 0 \\ -B_mL_1 & A_m - B_mK_m^0 & 0 \\ 0 & 0 & 0 \end{pmatrix}
\]
\[
A_{mp}^1 = \begin{pmatrix} B_m & 0 \\ 0 & B_m \end{pmatrix} = \begin{pmatrix} B_{mp}^1 & B_{mp}^2 \end{pmatrix}
\]
\[
B_{mp} = \begin{pmatrix} 0 & 0 \end{pmatrix}
\]
\[
C_{mp} = \begin{pmatrix} 0 & 0 & 0 \end{pmatrix}
\]

For applying LMI to the system above, we have made the transformation of the system term \(A_{mp}^1x_{mp}(t - \tau_1(t))\) as follow,
\[
A_{mp}^1x_{mp}(t - \tau_1(t)) = -B_{mp}^1Lx_{mp}(t - \tau_1(t))
\]
\[(24)\]

Then, the following stability theorem is obtained.

**Theorem 3** Suppose there exists matrices \(P > 0, R > 0, S > 0, S_a > 0, R_{a1} > 0, P_2, Y_1, Y_2, M, \) and positive scales \(\gamma \) and \(\xi\), such that the condition (26) with the notation (27) is feasible, the system (21) is asymptotically stable and \(J(\omega) < 0\) for time-varying delays \(\tau_1(t) \in [h_1, h_2]\). The control gain of the proxy is given by,
\[
L = MP_2^{-1}
\]
\[(25)\]

**Proof.** We substitute the system (21) into the theorem 2, and the proof can be found in [6].

**Remark 1** The \(H_{\infty}\) control design objective is to minimize the norm of the closed-loop mapping \(w_{mp}(t) \rightarrow z_{mp}(t)\). More precisely, we look for a minimum characterization of levels \(\gamma\), which is defined as \(\gamma_{\text{min}}^L\), therefore, the bound \(\sup_{w_{mp}}(\|z_{mp}(t)\|_2, \|w_{mp}(t)\|_2) < \gamma_{\text{min}}^L\) is achievable in the closed-loop system. Therefore, by theorem 3, we can minimize the deviation of position \(z_{mp}(t)\), in the condition of exogenous disturbance input \(w_{mp}(t)\), further achieve some minimal level of synchronization, as the position tracking. Besides, the performance of synchronization is proportional to the magnitude of \(\gamma_{\text{min}}^L\), the smaller \(\gamma_{\text{min}}^L\) produces the better performance of system [19].

### 4.2. The design of the controller \(C\)

The position tracking between the master and the proxy of master has been achieved. In this subsection, the position tracking between the proxy of master and the slave is proved by designing the controller \(C\). The model of the system containing the proxy of master, the controller \(C\) and the slave, is given as follow,
\[
(\Sigma_{ps}) \begin{cases}
\dot{x}_{ps}(t) = A_{ps}x_{ps}(t) + B_{ps}w_{ps}(t) \\
x_{ps}(t) = C_{ps}x_{ps}(t)
\end{cases}
\]
\[(28)\]

Similarly,
\[
x_{ps}(t) = \begin{pmatrix} \hat{\theta}_s(t) \\ \hat{\theta}_p(t) \\ \theta_s(t) - \theta_p(t) \end{pmatrix}, \quad z_{ps}(t) = (\theta_s(t) - \theta_p(t))
\]
\[(29)\]

Particularly, the input of the proxy, \(F_p(t - \tau_1(t))\), is considered as the exogenous disturbance signal,
\[
w_{ps}(t) = \begin{pmatrix} \hat{F}_s(t) \\ \hat{F}_h(t - \tau_1(t)) - F_p(t - \tau_1(t)) \end{pmatrix}
\]
\[(30)\]

So,
\[
A_{ps} = \begin{pmatrix} A_s - B_sK_s^0 & -B_sK_s^1 & -B_sK_s^2 & -B_sK_s^3 \\ 0 & A_m - B_mK_m^0 & 0 \\ 1 & -1 & 0 \\ 0 & 0 & 0 & 0 \end{pmatrix}
\]
\[
B_{ps} = \begin{pmatrix} B_s & 0 \\ 0 & B_m \end{pmatrix} = \begin{pmatrix} B_{ps}^1 & B_{ps}^2 \end{pmatrix}, \quad C_{ps} = \begin{pmatrix} 0 & 0 & 1 \end{pmatrix}
\]
\[(31)\]

The controller gain \(K\) should be calculated by LMI, but with the term \(A_{ps}\), this is difficult to apply LMI, so the transformation is made,
\[
A_{ps}x_{ps}(t) = A_{ps}^0x_{ps}(t) + A_{ps}^1x_{ps}(t)
\]
\[
= \begin{pmatrix} A_s - B_sK_s^0 & 0 & 0 \\ 0 & A_m - B_mK_m^0 & 0 \\ 0 & 1 & -1 \end{pmatrix}x_{ps}(t)
\]
\[
+ \begin{pmatrix} 0 & 0 & 0 \\ -B_sK_s^1 & -B_sK_s^2 & -B_sK_s^3 \\ 0 & 0 & 0 \end{pmatrix}x_{ps}(t)
\]
\[
= A_{ps}^0x_{ps}(t) - B_{ps}^1Kx_{ps}(t)
\]
\[(32)\]

Then, we obtain the following theorem.

**Theorem 4** Suppose there exists matrices \(P > 0, P_2, W, \) and positive scales \(\gamma \) and \(\xi\), such that the condition (34) with the notation (35) is feasible, the system (28) is asymptotically stable and \(J(\omega) < 0\). The control gain of the controller \(C\) is given by,
\[
K = WP_2^{-1}
\]
\[(33)\]
4.3. The global stability of the system

With the results of the subsections above, the position tracking, finally, the objective is to ensure the global stability of the system. In this context, the force tracking from the slave to the master can be realized on the basis of the characteristic of the control scheme.

The whole system is described,

\[ \begin{align*}
\dot{x}(t) &= A_0 x(t) + A_1 x(t - \tau_1(t)) + B w(t) \\
\dot{z}(t) &= C x(t)
\end{align*} \]  

(36)

Where,

\[ x(t) = \begin{bmatrix} \dot{\theta}_s(t) \\ \dot{\theta}_p(t) \\ \dot{\theta}_m(t) \end{bmatrix}, \quad w(t) = \begin{bmatrix} F_c(t) \\ \bar{F}_c(t) + \bar{F}_h(t - \tau_1(t)) \\ F_m(t) + \bar{F}_h(t) \end{bmatrix}, \quad z(t) = \begin{bmatrix} \dot{\theta}_s(t) - \theta_p(t) \\ \dot{\theta}_p(t) - \theta_m(t) \end{bmatrix} \]  

(37)

So, we can get,

\[ A_0 = \begin{bmatrix} A_0(1,1) & -B_s K_2 & -B_s K_3 \\ 0 & A_0(2,2) & 0 \\ 1 & -1 & 0 \end{bmatrix}, \quad A_0(1,1) = A_s - B_s K_0^a - B_s K_1 \]

\[ \begin{aligned}
A_0(2,2) &= A_m - B_m K_m^a \\
A_0(3,3) &= A_m - B_m K_m^a \\
A_1 &= \begin{bmatrix} 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix} \\
B &= \begin{bmatrix} B_s \\ 0 \\ 0 \end{bmatrix}, \quad C = \begin{bmatrix} 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}
\end{aligned} \]  

(38)

By the theorem 2, we can verify the global stability of the system. That is to say, with the force tracking, \( F_m(t) = \bar{F}_c(t - \tau_1(t)) \), the system is globally stable under the \( H_\infty \) constraint.

Remark 3 The global design of \( L \) and \( K \) with the terms \( A_0 \) and \( A_1 \) is impossible, because the \( L \) and \( K \) in (38) cannot be calculated in the form of LMI, which normally requires the transformation as (24), (32).

5. Simulation

To evaluate the performance of the proposed approach, different working conditions have been simulated. The maximum amplitude and sampling time of time-varying delays are 0.2s (greater amplitude of delays can also be handled) and 0.001s, which satisfy most network-based applications of teleoperation system, as internet-based teleoperation system. Notice that, the time-varying delays in two channels are asymmetric.

In order to simplify the system simulation, the master, the proxy of master and the slave models can be described as \( m_m/s \), \( m_m/s \) and \( m_s/s \). And for verifying the posi-
tion tracking, the effective endpoint mass is chosen differently, $m_m = 1$ and $m_s = 2 \text{kg}$. Besides, the poles of the master, the proxy and the slave are given as $[-100.0]$, then, $K_m^0 = 100, K_s^0 = 50$.

The subsystems mentioned above ($A_{mp}^0, B_{mp}, A_{ps}^0$ and $B_{ps}$) can be obtained. Then, according to the theorems above, the gains of the proxy of master and the controller $C, L$ and $K$, are obtained by YALMIP/MATLAB,

$$L = \begin{pmatrix} -1.6296 & 0.3669 & 283.5530 \end{pmatrix}, \quad \gamma^L_{min} = 0.0083$$
$$K = \begin{pmatrix} -29.9635 & -3.6393 & 618.5365 \end{pmatrix}, \quad \gamma^K_{min} = 0.0075$$

And, the global stability of the system ($A_0, A_1$ and $B$) is verified with $\gamma^g_{min} = 0.0054$.

Figure 3. Position response in abrupt changing motion.

5.1. Tracking in abrupt changing motion

Because the free motion simulation can be represented by the abrupt changing motion, it is omitted here. For simulation purpose of the abrupt change, the human operator ($F_h(t)$) is modeled as the pulse generator. Figure 3 shows the position tracking between the master and the slave. At the mutation point, good convergence between the master and the slave can be seen.

In this context, $F_e(t) = 0$, so the actuated inputs of the master $F_m(t) = 0$ in steady state.

5.2. Tracking in wall contact motion

We also performed simulation in wall contact motion, where the slave is driven to the hard wall with a stiffness of $K_e = 30kN/m$ located at the position $x = 1.0m$.

The upper part of Figure 4 shows the position tracking in [21], in which, the deviation of the position between the master and the slave is obvious. In the lower part of Figure 4, the system shows a satisfactory position tracking with the method proposed in the paper under the same conditions.

Figure 4. Position response in wall contact motion (upper: from [21]; lower: this paper)

Figure 5 shows the force tracking between the master and the slave, $F_m(t)$ and $F_e(t)$. We added a simple perturbation observer in the scheme to obtain unmeasured $F_e(t)$.

As the results of the simulation, the proposed method in the paper can greatly improve the performance of the system, the position tracking, and achieve the force tracking by the perturbation estimation and force feedback in steady state.

6. Conclusions and Future Works

In this paper, a new architecture and design for bilateral teleoperation has been proposed to obtain good position tracking, and then, comparable force tracking ability. It is based on the global stability analysis. The new configuration addresses asymmetric and time-varying delays, and builds upon the design of the proxy of master and the position error controller $C$. We use the theory of Lyapunov/Lyapunov-Krasovskii functional with $H_\infty$ control, which is given in the form of LMI. Moreover, the novel LMI-based architecture is a comprehensive summary of the Position-Position scheme and Position-Force scheme, and presents a more flexible tool for the control design of the bilateral teleoperation system.

Numerical simulations, achieved by YALMIP and SIMULINK, have confirmed the accuracy of analysis, and
proved that the teleoperation system, designed by our theory, can run in different workshop conditions.

The better estimation of the exogenous perturbation force will be entailed in the future work. Besides, the real implementations are being planned on an experimental testbench.

References


