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A Comparison of Symmetrical and Asymmetrical Three-Phase H-Bridge Multilevel Inverter for DTC Induction Motor Drives

Farid Khoucha, Mouna Soumia Lagoun, Abdelaziz Kheloui, and Mohamed El Hachemi Benbouzid, Senior Member, IEEE

Abstract—Earlier studies have pointed out the limitations of conventional inverters, especially in high-voltage and high-power applications. In recent years, multilevel inverters are becoming increasingly popular for high-power applications due to their improved harmonic profile and increased power ratings. Several studies have been reported in the literature on multilevel inverters topologies, control techniques, and applications. However, there are few studies that actually discuss or evaluate the performance of induction motor drives associated with three-phase multilevel inverter. This paper presents then a comparison study for a cascaded H-bridge multilevel direct torque control (DTC) induction motor drive. In this case, symmetrical and asymmetrical arrangements of five- and seven-level H-bridge inverters are compared in order to find an optimum arrangement with lower switching losses and optimized output voltage quality. The carried out experiments show that an asymmetrical configuration provides nearly sinusoidal voltages with very low distortion, using less switching devices. Moreover, torque ripples are greatly reduced.

Index Terms—Direct torque control (DTC), induction motor, multilevel inverters.

I. INTRODUCTION

MULTILEVEL voltage-source inverters are intensively studied for high-power applications [1], [2], and standard drives for medium-voltage industrial applications have become available [3], [4]. Solutions with a higher number of output voltage levels have the capability to synthesize waveforms with a better harmonic spectrum and to limit the motor winding insulation stress. However, their increasing number of devices tends to reduce the power converter overall reliability and efficiency. On the other hand, solutions with a low number of levels either need a rather large and expensive LC output filter to limit the motor winding insulation stress, or can only be used with motors that do withstand such stress. The various voltage stages have been chosen after considering the real-power contribution of the highest voltage stage. The maximum power supplied by highest voltage stage is maintained below the load power.

Many studies have been conducted toward improving multilevel inverter. Some studies dealt with innovative topologies, such as cascaded multilevel inverter, to optimize the components utilization and the asymmetrical multilevel inverter to improve the output voltage resolution [5]. Other studies focused on developing advanced control strategies or upgrading the voltage-source inverter strategies for implementation in multilevel inverter [6], [7].

In symmetrical multilevel inverter, all H-bridge cells are fed by equal voltages, and hence all the arm cells produce similar output voltage steps. However, if all the cells are not fed by equal voltages, the inverter becomes an asymmetrical one. In this inverter, the arm cells have different effect on the output voltage. Other topologies are possible, such as the neutral point clamped fed by unequal capacitors.

Asymmetrical multilevel inverter has been recently investigated [8], [9]. In all these studies, H-bridge topology has been considered and a variety of selection of cascaded cell numbers and dc-sources ratios have been adopted [8]. The suggested pulsewidth-modulation strategy that maintains the high-voltage stage to operate at low frequency limits the source-voltage selection.

One of the methods that have been used by a major multilevel inverter manufacturer is direct torque control (DTC), which is recognized today as a high-performance control strategy for ac drives [10]–[13]. Several authors have addressed the problem of improving the behavior of DTC ac motors, especially by reducing the torque ripple. Different approaches have been proposed [14]. Although these approaches are well suitable for the classical two-levels inverter, their extension to a greater number of levels is not easy. Throughout this paper, a theoretical background is used to design a strategy compatible with hybrid cascaded H-bridge multilevel inverter; symmetrical and asymmetrical configuration are implemented and compared [15]. Experimental results obtained for an asymmetrical inverter-fed induction motor confirm the high dynamic performance of the used method, presenting good performances and very low torque ripples.
II. CASCaded H-Bridges STRUCTURE AND OPERATION

The cascaded H-bridge inverter consists of power conversion cells, each supplied by an isolated dc source on the dc side, which can be obtained from batteries, fuel cells, or ultracapacitors [15]–[17], and series-connected on the ac side. The advantage of this topology is that the modulation, control, and protection requirements of each bridge are modular. It should be pointed out that, unlike the diode-clamped and flying-capacitor topologies, isolated dc sources are required for each cell in each phase. Fig. 1 shows a three-phase topology of a cascade inverter with isolated dc-voltage sources. An output phase-voltage waveform is obtained by summing the bridges output voltages

$$v_o(t) = v_{o,1}(t) + v_{o,2}(t) + \cdots + v_{o,N}(t)$$  \hspace{1cm} (1)

where $N$ is the number of cascaded bridges.

The inverter output voltage $v_o(t)$ may be determined from the individual cells switching states

$$v_o(t) = \sum_{j=1}^{N} (\mu_j - 1) V_{dc,j}, \hspace{1cm} \mu_j = 0, 1, \ldots$$  \hspace{1cm} (2)

If all dc-voltage sources in Fig. 1 are equal to $V_{dc}$, the inverter is then known as a symmetric multilevel one. The effective number of output voltage levels $n$ in symmetric multilevel inverter is related to the cells number by

$$n = 1 + 2N$$  \hspace{1cm} (3)

For example, Fig. 2 illustrated typical waveforms of Fig. 1 multilevel inverter with two dc sources (five-levels output). The maximum output voltage $V_{o,\text{Max}}$ is then

$$V_{o,\text{Max}} = NV_{dc}$$  \hspace{1cm} (4)

To provide a large number of output levels without increasing the number of inverters, asymmetric multilevel inverters can be used.

In [18] and [19], it is proposed to choose the dc-voltage sources according to a geometric progression with a factor of 2 or 3. For $N$ of such cascade inverters, one can achieve the following distinct voltage levels

$$\begin{align*}
    n &= 2^{N+1} - 1, \hspace{1cm} \text{if } V_{dc,j} = 2^{j-1}V_{dc}, \hspace{1cm} j = 1, 2, \ldots, N \\
    n &= 3^N, \hspace{1cm} \text{if } V_{dc,j} = 3^{j-1}V_{dc}, \hspace{1cm} j = 1, 2, \ldots, N.
\end{align*}$$  \hspace{1cm} (5)

For example, Figs. 3 and 4 illustrated typical waveforms of Fig. 1 multilevel inverter with, respectively, two dc sources ($V_{dc}$ and $2V_{dc}$) (seven-levels output) and two dc sources ($V_{dc}$ and $3V_{dc}$) (nine-levels output).
TABLE I

<table>
<thead>
<tr>
<th></th>
<th>Symmetrical inverter</th>
<th>Asymmetrical inverter</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>Binary</td>
<td>Ternary</td>
</tr>
<tr>
<td>$N$</td>
<td>$2N+1$</td>
<td>$2^{N+1}-1$</td>
</tr>
<tr>
<td>DC sources number</td>
<td>$N$</td>
<td>$N$</td>
</tr>
<tr>
<td>Switches number</td>
<td>$4N$</td>
<td>$4N$</td>
</tr>
<tr>
<td>$V_{o,MAX}$ [pu]</td>
<td>$N$</td>
<td>$2^N-1$</td>
</tr>
</tbody>
</table>

The maximum output voltage of these $N$ cascaded multilevel inverters is

$$V_{o,MAX} = \sum_{j=1}^{N} V_{dc,j}. \quad (6)$$

Equation (6) can be rewritten as

$$V_{o,MAX} = \begin{cases} \left(2^N - 1\right) V_{dc}, & \text{if } V_{dc,j} = 2^{j-1} V_{dc}, \quad j = 1, 2, \ldots, N \\
\left(3^N - 1\right) V_{dc}, & \text{if } V_{dc,j} = 3^{j-1} V_{dc}, \quad j = 1, 2, \ldots, N. 
\end{cases} \quad (7)$$

Comparing (3) to (7), it can be seen that asymmetrical multilevel inverters can generate more voltage levels and higher maximum output voltage with the same number of bridges.

Table I summarizes the number of levels, switches, dc sources, and maximum available output voltages for classical cascaded multilevel inverters.

Increasing the number of levels provides more steps; hence, the output voltage will be of higher resolution and the reference sinusoidal output voltage can be better achieved. Among the $n^3$ switching states of $n$-level inverter, there is $n$ zero states, where zero output voltages are produced. Among the $(n^3-n)$ nonzero remaining states, there are unique states and mutual states. The unique states provide voltage vectors that cannot be obtained by any other states. The mutual state on the other hand, provides a set of output voltages that can be provided by some other mutual state or states. The equivalent mutual states share the same voltage vectors. The $n$-level inverter has $[(n-1)^3-(n-1)]$ nonzero mutual states. The voltage vectors of the five-level inverter are shown in Fig. 5. The number of distinct voltage vectors obtained from $n$-level inverter is $\left[n^3-(n-1)^3\right]$. The existence of equivalent mutual states has usually been used to minimize the switching losses. Nevertheless, the equivalent mutual states can be replaced by any one of these states and the other states can be considered redundant. There are $(n-1)^3$ redundant states in the $n$-level symmetrical H-bridge multilevel inverter.

III. INDUCTION MOTOR DIRECT TORQUE CONTROL

DTC is an alternative method to flux-oriented control [12]. However, in the standard version, important torque ripple is obtained even at high sampling frequencies. Moreover, the inverter switching frequency is inherently variable and very dependent on torque and shaft speed. This produces torque harmonics with variable frequencies and an acoustic noise with disturbance intensities very dependent on these mechanical variables and particularly grating at low speed. The additional degrees of freedom (space vectors, phase configurations, etc.) provided by the multilevel inverter should, therefore, be exploited by the control strategy in order to reduce these drawbacks [6], [15].

A. Nomenclature

$V_s$ Stator voltage vector.

$\phi_s(\phi_r)$ Stator (rotor) flux vector.

$T_e$ Electromagnetic torque.

$R_s$ Stator resistance.

$L_s$ ($L_r$) Stator (rotor) inductance.

$L_m$ Magnetizing inductance.

$\sigma$ Total leakage coefficient, $\sigma = 1 - L_m^2/L_s L_r$.

$\theta_{sr}$ Angle between stator and rotor flux vectors.

$p$ Pole pair number.

B. Torque and Flux Estimation

The stator flux vector an induction motor is related to the stator voltage and current vectors by

$$\frac{d\phi_s(t)}{dt} = v_s(t) - R_s i_s(t) \quad (8)$$

Maintaining $v_s$ constant over a sample time interval and neglecting the stator resistance, the integration of (10) yields

$$\Delta\phi_s(t) = \phi_s(t) - \phi_s(t - \Delta t) = \int_{t-\Delta t}^{t} v_s(t) \Delta t. \quad (9)$$

Equation (9) reveals that the stator flux vector is directly affected by variations on the stator voltage vector. On the contrary, the influence of $v_s$ over the rotor flux is filtered by the rotor and stator leakage inductance [20], and is, therefore, not relevant over a short-time horizon. Since the stator flux can be changed quickly while the rotor flux rotates slower, the angle between both vectors $\theta_{sr}$ can be controlled directly by $v_s$. A graphical representation of the stator and rotor flux dynamic behavior is
illustrated in Fig. 6. The exact relationship between stator and rotor flux shows that keeping the amplitude of $\phi_s$ constant will produce a constant flux $\phi_r$ [21].

Since the electromagnetic torque developed by an induction motor can be expressed by [22]

$$T_e = \frac{3}{2} \frac{L_m}{\sigma L_s L_r} \phi_s \phi_r \sin \theta_{sr}$$  

(10)

it follows that change in $\theta_{sr}$ due to the action of $v_s$ allows for direct and fast change in the developed torque. DTC uses this principle to achieve the induction motor desired torque response, by applying the appropriate stator voltage vector to correct the flux trajectory.

C. Voltage Vector Selection [6], [15]

Fig. 7 illustrates one of the 127 voltage vectors generated by the inverter at instant $t = k$, denoted by $v_s^k$ (central dot). The next voltage vector, to be applied to the load $v_s^{k+1}$, can be expressed by

$$v_s^{k+1} = v_s^k + \Delta v_s^k$$  

(11)

where $\Delta v_s^k = \{v_i | i = 1, \ldots, 6\}$. Each vector $v_i$ corresponds to one corner of the elemental hexagon illustrated in gray and by the dashed line in Fig. 7.

The task is to determine which $v_s^{k+1}$ will correct the torque and flux responses, knowing the actual voltage vector $v_s^k$, the torque and flux errors $e_T^k$ and $e_\phi^k$, and the stator flux vector position (sector determined by angle $\theta_s$). Note that the next voltage vector $v_s^{k+1}$ applied to the load will always be one of the six closest vectors to the previous $v_s^k$; this will soften the actuation effort and reduce high dynamics in torque response due to possible large changes in the reference. Table II summarizes vector selections for the different sectors and comparators output (desired $\phi_s$ and $T_e$ corrections).

To implement the DTC of the induction motor fed by a hybrid H-bridge multilevel inverter, one should determine at each sampling period, the inverter switch logic states as a function of the torque and flux instantaneous values for the selection of the space vector in the $\alpha$–$\beta$ frame [23], [24]. The proposed control algorithm was divided into two major tasks, which are independent and executed in cascade.

1) First task: It aims at the control of the electromagnetic state of the induction motor. The torque and flux instantaneous values, and their variations will be taken into account for the space vector selection in the $\alpha$–$\beta$. Once the space is chosen, the phase levels sequence can be selected. To ensure this task, one should detect the space vector position in the $\alpha$–$\beta$ frame ($Q^k$ at sampling time $k$). The algorithm must then select the next position $Q^{k+1}$ to be achieved before next sampling instant $k + 1$ (see Fig. 8) in order to reduce voltage steps magnitude. Only one step displacement...
Fig. 10. Five-levels cascaded H-bridge inverter estimated torque waveform.

Fig. 11. Five-levels cascaded H-bridge inverter stator flux waveform.

Fig. 12. Five-levels cascaded H-bridge inverter output current waveform.

Fig. 13. Five-levels cascaded H-bridge inverter phase current fast Fourier transform (FFT) analysis.

Fig. 14. Five-levels cascaded H-bridge inverter voltage waveforms. (a) Phase voltage. (b) Line voltage.

Fig. 15. Five-levels cascaded H-bridge inverter phase voltage FFT analysis.

Fig. 16. Seven-levels cascaded H-bridge inverter estimated torque waveform.
in the $\alpha-\beta$ frame is authorized per sampling period $T_s$. Hence, in the absence of inverter saturation, $Q^{k+1}$ must coincide with one of the six corners of the elementary hexagon centered at $Q^k$. The same procedure will be carried out at the next period in order to determine the next trajectory direction, yielding $Q^{k+2}$, which in turn will coincide with one of the six corners of the new elementary hexagon centered at $Q^{k+1}$. In case of inverter saturation (if $Q^k$ gives an unreachable point for $Q^{k+1}$), a trajectory correction is necessary (see Fig. 8). In cases (2) and (3), the closest displacement direction is selected. Case (1) illustrates a particular situation in which no switching should be performed, since the nearest reachable trajectory goes roughly toward the opposite sense of the favored one given by the lookup table (see Table II).

2) Second task: It exploits the degree of freedom related to the multilevel topology to choose the phase levels sequence that synthesizes the voltage vector selected previously. There are several phase levels sequences that are able to generate the same vector illustrated in Fig. 9; this degree of freedom can, therefore, be exploited to reduce voltage steps magnitude according to one of the following criteria:

- a) minimize the commutation number per period;
- b) distribute commutations for the three-phases per period;
- c) choose a vector which minimizes the homopolar voltage.

This task allows losses and torque ripple minimization.
Finally, the configuration of each phase will be selected and must be able to generate the phase levels.

IV. SIMULATION AND EXPERIMENTAL RESULTS

For the validation of the earlier discussed control approach, simulations and experiments have been carried out.

Figs. 10–15 and Figs. 16–21 show simulation results for five-levels cascaded and seven-levels H-bridge inverter, respectively. For further verification, a three-phase DSP (TMS320LF2407 A) controlled five- and seven-levels cascaded H-bridge multilevel DTC induction motor drive system prototype was built and tested (see Fig. 22). The induction motor ratings are given in the Appendix. The switch ratings are (600 V/27 A) for the insulated gate bipolar transistors. The prototype is versatile; it consists of a multiwinding transformer and an inverter with a
burst structure that contains six H-bridges. The H-bridges and transformer terminals are connected through a single-phase rectifier with standard laboratory wires and connectors to get the tested, or any other desired, topology. The multilevel inverter control algorithms and the DTC are running in the same DSP. The control cycle is 120 μs.

It should be noted, as illustrated in Fig. 22(a), that the experimental setup was built to slightly emulate an automotive application (electric vehicle).

Figs. 23–26 and Figs. 27–30 illustrate experimental results for five-levels cascaded and seven-levels H-bridge inverter, respectively.

The output voltages form with seven-levels stepped multilevel waveform can be clearly appreciated; the motor currents complete the overview of the performance of the drive. They appear completely sinusoidal, since the low-pass nature of the load has filtered the high-frequency content of the applied voltage. The stator flux with constant amplitude imposed by the flux controller confirms the good dynamic performance of the drive. The most important results are that torque ripple has been almost eliminated in comparison to five-levels classic DTC.

V. Conclusion

This paper dealt with a comparison study for a cascaded H-bridge multilevel DTC induction motor drive. Indeed, symmetrical and asymmetrical arrangements of five- and seven-levels H-bridge inverters have been compared in order to find an optimum arrangement with lower switching losses and optimized output voltage quality.

The carried out experiments show that an asymmetrical configuration provides nearly sinusoidal voltages with very low distortion, using less switching devices. In addition, torque ripples are greatly reduced: asymmetrical multilevel inverter enables a DTC solution for high-power induction motor drives, not only due to the higher voltage capability provided by multilevel inverters, but mainly due to the reduced switching losses and the improved output voltage quality, which provides sinusoidal current without output filter.

APPENDIX

RATED DATA OF THE SIMULATED AND TESTED INDUCTION MOTOR

<table>
<thead>
<tr>
<th>1 kW, 50 Hz, 400/230 V, 3.4/5.9 A, 1420 rpm</th>
</tr>
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<tbody>
<tr>
<td>$R_s = 4.67 \Omega$, $R = 8 \Omega$, $L_s = L = 0.347 , H$, $M = 0.366 , H$</td>
</tr>
</tbody>
</table>

$J = 0.06 \, kg \cdot m^2$, $\beta = 0.042 \, Nm \cdot sec$

REFERENCES


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