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APPLICATION OF A HEMODYNAMIC MODEL TO EPILEPTIC SPIKES

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ABSTRACT

Despite the interest in simultaneous EEG-fMRI studies of epileptic spikes, the link between epileptic discharges and their corresponding hemodynamic responses is poorly understood. We applied two biophysical models in order to investigate the mechanisms underlying the neurovascular coupling in epilepsy: a metabolic hemodynamic model, and a neural mass model that simulates epileptic discharges. Analyzing the effect of epileptic neuronal activity on the BOLD response we focussed on the issues of linearity and on the origin of negative BOLD signals. In our BOLD simulation results both sub- and supra-linearity occur one after another. The size of these effects depends on the spike frequency, as well as on the amplitude of the excitatory part of the neural input. For the hemodynamic model used in this study, we found that the sign of the BOLD response is mainly determined by the area under the curve describing the excitatory neural activity. Therefore, a strong deactivation following the initial peak of the excitatory time course of an epileptic spike is necessary to obtain a negative BOLD.

KEY WORDS

hemodynamic model, neural mass model, epileptic spikes, BOLD linearity, negative BOLD

1. Introduction

The present study is a step towards a better understanding of the link between epileptic spikes and their BOLD responses, which is necessary to improve the interpretation of simultaneous EEG-fMRI recordings [1,2,3]. Such measurements combine the high temporal resolution of EEG with the high spatial resolution of fMRI recordings. We apply the metabolic hemodynamic model (MHM) suggested in [4,5] to epileptiform neural activity. One specific feature of neurophysiological recordings in epilepsy is the interictal epileptic spike, i.e. a short period of strongly increased excitatory activity, outside of seizures. The spike shapes show a certain variability, e.g. depending on the recording session, the spatial position of the electrode, or the type of epilepsy [3,6]. Including information about the shape of such interictal discharges can improve the detection of fMRI correlates [7]. In order to specifically analyze the neurovascular coupling in epilepsy we couple a neural mass model (NMM) that simulates realistic epileptiform neural activities [8,9] to the MHM. The two main issues we are focusing on are (1) the question of linearity in BOLD signals, and (2) the source of negative BOLD responses to epileptic spikes. The latter point is of particular interest because interictal epileptic discharges are a marker of neuronal hyper-excitability which is generally related to a BOLD increase. Here, we investigate the influence of the spike shape on the sign of the BOLD response. Originally, the General linear model (GLM) is used in processing and analyzing experimental data from simultaneous EEG-fMRI recordings [10,11], resulting in a linear prediction (LP) of the BOLD response. Such a procedure incorporates only the linear part of the neurovascular coupling. However, there are hints for non-linear correlations between neuronal and hemodynamic responses [12,13,14]. In particular, concerning the localization of epileptic regions, linearity is an important issue [11]: using the GLM if BOLD signals were non-linear would reduce the detection sensitivity.

2. Methods & Results

The general settings, e.g. baselines bl or signal units, used in this study are mostly adopted from [4,5]. It is
bl=0 for the BOLD signal [%], and bl=1 for all neural activities [a.u.], i.e. for the excitatory (exc.) and inhibitory (inh.) parts, as well as for the original output of the NMM.

We initially assumed simple rectangular impulses of \(w=0.5s\) length that represent interictal epileptic discharges. They are stringed together in order to represent burst of spikes. The exc. amplitudes range from \(eA=2\) up to \(eA=10\) while the inh. amplitudes are \(iA=(eA-1)/2\). We also vary the inter-spike-intervals from \(dt=0.5s\) up to \(dt=9s\). As in the GLM, the LP of the BOLD response to a spike train is calculated as follows (see Fig.1): The extraction of the spike times of the spike train leads to the impulse function \(f_{\text{imp}}\). It is \(f_{\text{imp}}(t_i)=1\) for the first point in time of each spike, and \(f_{\text{imp}}(t_i)=0\) otherwise. Then, the BOLD response to a single input impulse is simulated, here called unit BOLD response (uBOLD), and convolved with \(f_{\text{imp}}\): \(\text{LP} = f_{\text{imp}} \ast \text{uBOLD}\). The difference between the signal and its LP characterizes the non-linearity of the BOLD signal simulated with the MHM. To assess these deviations quantitatively for spike trains of 30s duration we calculated the area under the curve of the residual, normalized by the global maximum of the actual BOLD signal:

\[
\sum |\text{BOLD}(t_i) - \text{LP}(t_i)| / \text{BOLD}_{\text{max}}, \text{ for all time steps } t_i < t_b, \text{ and } \\
\sum |\text{BOLD}(t_i) - \text{LP}(t_i)| / f_l, \text{ for } t_i > t_b,
\]

with the intersection time \(t_b\) that separates the BOLD response into two parts (vertical line in Fig. 2A) and a factor \(f_l\) that accounts for the different lengths of part I and part II. In part I \((t_i < t_b)\), the simulated BOLD signal behaves linearly or sub-linearly (\(\text{BOLD}<\text{LP}\)), in part II \((t_i > t_b)\) it is linear or supra-linear (\(\text{BOLD}>\text{LP}\)). The size of both effects depends on the spike frequency \(1/dt\), as well as on the amplitude of the exc. activity \(eA\), as shown in Figures 2C and 2D. The phase space plot in Fig. 2B indicates that the border between part I and part II \((t_b)\) also depends on \(dt\) and \(eA\): higher frequencies and larger exc. amplitudes lead to a longer lasting sub-linear behaviour (part I). Within the first 7 to 12s the BOLD response is sub-linear in case of high frequencies and large amplitudes. In part II, the signal turns to supra-linearity, but again only for small \(dt\) and high \(eA\).

Secondly, in order to investigate the neurovascular coupling with respect to more realistic epileptiform neural signals, we coupled a simplified version of the NMM in \([8, 9]\) to the MHM. The original outputs of the NMM are the summed post-synaptic potentials (PSPs) of the exc. population, representing SEEG recordings, here called LFP (local field potential). We plugged one NMM to one MHM, assuming that the neural activity in one cortical region (a voxel of approx. 1mm\(^3\)) causes one isolated hemodynamic response. We convolved the incoming action potential densities at exc. (inh.) synapses with the average shape of the exc. (inh.) post-synaptic potentials (cf. Fig. 1) defined by the input parameters of the NMM. Then each pre-processed NMM output was normalized according to its baseline. In Figures 3A and 3B we present two exemplary spike shapes that result from this procedure. They show different time courses in terms of the LFP output (dotted lines), but the curves of the exc. activities are rather similar. For example, the large undershoot after the peak in the LFP in Fig. 3B is predominately the result of a delayed inhibition, rather than a particularly large undershoot in excitation. The BOLD output of the MHM in \([4,5]\) mainly depends on the exc. activity, therefore the corresponding two BOLD signals in Fig. 3C are very similar. Fig. 3D shows the BOLD response to the epileptic spike train in Fig. 3E. Due to the variations in the frequency of spike occurrences, the BOLD signal constantly changes between supra- and sub-linearity. Note that at \(t=26s\) the LP indicates a slightly negative BOLD whereas the actual BOLD signal is positive. For this spike train we additionally calculated the

\[
\text{Residuals} = \sum |\text{BOLD}(t_i) - \text{LP}(t_i)| / \text{BOLD}_{\text{max}}, \text{ for all time steps } t_i < t_b, \text{ and } \\
\sum |\text{BOLD}(t_i) - \text{LP}(t_i)| / f_l, \text{ for } t_i > t_b,
\]

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neural LP (cf. Fig. 1), i.e., the average spike of a spike train is convolved with its impulse function, and fed into the MHM. If a spike train were based on a non-linear superposition of single spikes, this neural LP would clearly deviate from the actual BOLD signal. However, this is not the case. Thus, this example indicates that the deviations from linearity originate predominately from the neurovascular coupling.

We found that the variability of the exc. time course of the NMM spikes is rather limited (cf. Figures 3A and 3B). In addition, the NMM does not allow for a controlled variation of the features characterizing the shape of an epileptic spike. Therefore, we used another, simplified approach to investigate the influence of the shape of an epileptic spike on the sign of the BOLD response. We simulated artificial spikes (see Fig. 3F) whose exc. time courses are separated into three parts: a first peak p, an undershoot u, and a possible slow wave w. Inhibition is included via delayed peak. Each part is characterized by an amplitude $A$ and a duration $\Delta t$. For a given ratio between exc. and inh. peak amplitudes ($r_i=0.5$ with $eA=2$), we varied the amplitude ratio $eA/\Delta t(p)$ from 1.5 to 100, the duration ratio $\Delta t(p)/\Delta t(u)$ from 0.166 to 100, and the size of the slow wave $(eA/wA, \Delta t(p+u)/\Delta t(w)$ from $(1, 1.5)$ to $(100, 200)$. After feeding these signals into the MHM we determined the extrema of the corresponding BOLD responses. In addition, we calculated the areas under the exc. and inh. curves:

$$\text{area}_{\text{exc}} = \sum T_1 \text{exc}(t_i) - \sum T_2 \text{exc}(t_i) + \sum T_3 \text{exc}(t_i),$$

$T_i = \Delta t(p)$, $T_2 = \Delta t(u)$, $T_3 = \Delta t(w)$, and $\text{area}_{\text{inh}} = \sum \text{inh}(t_i), \text{with } T = T_1 + T_2 + T_3.$

Figure 3G shows the extremal values of the corresponding BOLD responses to these differently shaped spikes in dependence of area$_{\text{exc}}$ (and, for a comparison, also in dependence of area$_{\text{exc}}$-area$_{\text{inh}}$). Most of the artificial spikes lead to a positive simulated BOLD response. Only if the area of the exc. undershoot is larger than the sum the areas of the peak and the slow wave, a negative BOLD signal is possible. Yet, even if there is a negative BOLD response, its minimum is relatively small compared to the maximums of the BOLD increase. The maximums obtained with the MHM of [4,5] exhibit a linear relationship to area$_{\text{exc}}$, while the values of the BOLD minimums immediately saturate for larger negative values of area$_{\text{exc}}$.

3. Discussion & Conclusion

We investigated the BOLD response of the MHM proposed in [4,5] with respect to epileptic spikes. The spikes can occur isolated or in short bursts. Concerning such bursts we found a non-linear behavior that increases for large exc. amplitudes (typical for epilepsy), and for high spike frequencies. The sub-linearity of the first part of the BOLD signal and its stimulus dependence is a well-known feature [11,12,13].

Fig. 3, left: (A,B) Two exemplary spike shapes generated with the NMM and their corresponding BOLD signals (C) generated with the MHM. (E) BOLD response, its (neural) LP to the spike train in (E) from which the average spike shape $S_3$ was calculated. Right: (F) Schematic representation of the time curves of exc. and inh. activity constituting an epileptic spike. (G) Maximum and minimum of the BOLD response to differently shaped spikes in dependence of the area under the time curves of exc. and inh. neural activities.

area$_{\text{exc}}$ = $\sum T_1 \text{exc}(t_i) - \sum T_2 \text{exc}(t_i) + \sum T_3 \text{exc}(t_i),$
Most studies agree on a linear relationship for stimulus durations or inter-spike-intervals longer than approximately 4 to 6s, and a sub-linear behavior for shorter periods. The supra-linearity in the second part is surprising with no direct experimental evidence. Yet, such a changeover is not necessarily detectable by a mere comparison of BOLD signals to different activation durations, i.e., without calculating the LP [12,14]. Moreover, there are some findings that indirectly support our findings. Our results indicate that the supra-linearity is induced by the negative part of the uBOLD response (cf. Fig. 2). Similarly, Birn et al. [15] found that the BOLD decrease on stimulus cessation was smaller that linearly expected, opposite to what has been reported for its increase, and Deneux & Faugeras [12] mention nonlinear effects in the post-stimulus undershoot. With respect to epileptiform activity, Bagshaw et al. [11] reported the absence of the linearly predicted plateau for particularly long lasting events (in addition to the sub-linear effect). For the interpretation of combined EEG-fMRI data, such an additional supra-linearity may significantly impact the detection of epileptic regions, and, in the worst case, lead to a false negative BOLD detection (Fig. 3D).

We had difficulties in simulating differently shaped spikes with the NMM. This topic was not the original focus of the model adapted from [7,8] who aimed at reproducing the transformation between interictal and ictal activity, in particular in terms of the frequency domain. Our simulations indicate similar BOLD responses for very different LFP spikes, because of very similar exc. signals and the domination of excitation in the MHM [4,5]. As a consequence, the most important feature is not the actual shape of the spike but rather the time-course of excitatory activity. Indeed, a negative BOLD response occurs only for epileptic spikes including a large undershoot in excitation but how realistic is such an assumption? High firing rates of exc. neurons may induce strong inh. feedback that, in combination with a pronounced exc. refractory period, may lead to such a strong decrease in excitation. The absence of a BOLD decrease for spike shapes that include a third slow wave is, however, in disagreement with [3] who suggest that negative BOLD occurs predominantly for SEEG signals that contain a high amount of low frequencies (i.e. slow waves). Yet, it is not possible to specify whether these low frequencies are based on positive or negative slow waves.

In addition, it is important to note that any kind of electrophysiological recording (EEG, LFP etc.) is only an indirect representation of the neural activities inducing a BOLD signal. A spike recorded by an EEG electrode is presumed based on the activities of many interconnected NMMs (larger spatial scale). Let us, for example, consider two spatially separated NMMs (only one of them, NMM1, exhibits epileptiform activity) that are coupled by an inhibitory link. Then each epileptic spike of NMM1 inhibits the ongoing background activity of NMM2. Based on the the low spatial resolution of EEG compared to fMRI recordings we assume just one combined EEG signal for both NMMs but two separate fMRI signals. Thus, one would obtain one positive (due to NMM1) and one negative BOLD response (related to NMM2). The investigation of the neurovascular coupling would presumably benefit from simulations including a more detailed neuronal network model that includes a spatial component [16]. In particular we suggest to avoid a direct coupling between EEG and BOLD signals, but to calculate them separately from the underlying neural activities.

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**References**


