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# Accepted Manuscript

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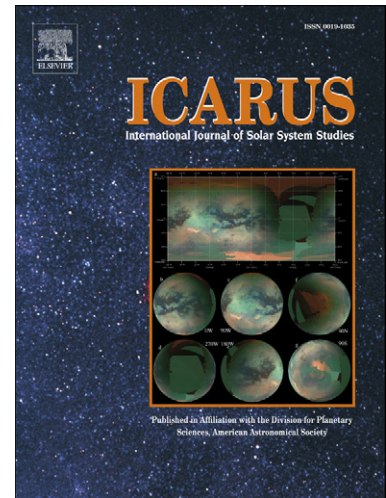
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# MARSIS surface reflectivity of the south residual cap of Mars

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34

35 **(Abstract)**

36 The south residual cap of Mars is commonly described as a thin and bright layer of  
37 CO<sub>2</sub>-ice. The Mars Advanced Radar for Subsurface and Ionospheric Sounding  
38 (MARSIS) is a low-frequency radar on board Mars Express operating at the  
39 wavelength between 55 and 230 m in vacuum. The reflection of the radar wave on a  
40 stratified medium like the residual cap can generate interferences, causing weaker  
41 surface reflections compared to reflections from a pure water ice surface.

42 In order to understand this anomalous low reflectivity, we propose a stratified  
43 medium model, which allows us to estimate both the thickness and the dielectric  
44 constant of the optically thin slab. First, we consider the residual cap as single unit  
45 and show that the decrease in the reflected echo strength is well explained by a mean  
46 thickness of 11 m and a mean dielectric constant of 2.2. This value of dielectric  
47 constant is close to the experimental value 2.12 for pure CO<sub>2</sub>-ice. Second, we study  
48 the spatial variability of the radar surface reflectivity. We observe that the reflectivity  
49 is not homogeneous over the residual cap. This heterogeneity can be modeled either  
50 by variable thickness or variable dielectric constant. The surface reflectivity shows  
51 that two different units comprise the residual cap, one central unit with high  
52 reflectivity and surrounding, less reflective units.

53 **KEYWORD: RADAR OBSERVATIONS, MARS, POLAR CAPS, ICES**

54

## 55 **1. Introduction**

56

### 57 **1.1. South residual cap**

58

59 The south polar plateau of Mars is partially covered by a perennial thin layer of  
60 carbon dioxide (CO<sub>2</sub>) ice, which is easily visible from Earth and spacecraft due to its  
61 high albedo compared to the surrounding regions. Astronomers have observed this  
62 layer over a century [Flammarion 1892], but the composition (CO<sub>2</sub>-ice) was  
63 determined using Viking orbiter thermal data [Kieffer, 1979; Paige *et al.* 1990]. It has  
64 been shown that this CO<sub>2</sub> layer directly lies above water ice (H<sub>2</sub>O-ice), which  
65 comprises the major part of the plateau [Plaut *et al.* 2007] in the form of South Polar  
66 Layered Deposits (SPLD).

67 Thermal data from Thermal Emission Imaging System (THEMIS) revealed the  
68 presence of small exposures of H<sub>2</sub>O-ice adjacent to the CO<sub>2</sub>-ice, based on temperature  
69 signatures [Titus *et al.* 2003]. The Observatoire pour la Minéralogie, l'Eau, les  
70 Glaces, et l'Activité (OMEGA) observed spectral signatures of both CO<sub>2</sub>-ice and trace  
71 amounts of H<sub>2</sub>O-ice within the residual ice cap [Bibring *et al.* 2004, Douté *et al.*  
72 2007]. OMEGA also confirmed the identification of H<sub>2</sub>O-ice-rich surfaces near the  
73 CO<sub>2</sub>-ice cap

74 The perennial CO<sub>2</sub> deposit consists of numerous layers. Using Mars Global Surveyor  
75 Mars Orbiter Camera (MOC) images, Thomas *et al.* [2005] showed that the south  
76 residual cap consists of two distinct layered units, which were deposited at different

77 times, separated by a period of degradation. The older unit, about 10 m thick, has  
 78 layers approximately 2 m thick. The younger unit has variable numbers of layers,  
 79 each about 1 m thick.

80 An estimate of the quantity of CO<sub>2</sub> in the slab, which can be compared to the total  
 81 CO<sub>2</sub> content of the atmosphere, was made by Byrne and Ingersoll [2003]. They  
 82 showed that a CO<sub>2</sub> residual ice cap with 10 m thickness, an area of 87,000 km<sup>2</sup>, and a  
 83 density of 1.6 g.cm<sup>-3</sup>, constitutes only about 5% of the average atmospheric mass.

84

85

## 86 **1.2. Surface Reflectivity measured by MARSIS**

87

88 MARSIS is a decameter-wave sounding radar, which can penetrate kilometers below  
 89 the icy surface. It has provided important results on the Martian subsurface [Picardi *et al.*  
 90 2005; Plaut *et al.* 2007; Watters *et al.* 2007] and ionosphere [Gurnett *et al.* 2005 ;  
 91 Duru *et al.* 2006; Safaeinili *et al.* 2007; Espley *et al.* 2007]. The radar uses four  
 92 frequency bands, which are centered at 1.8, 3, 4 and 5 MHz (166, 100, 75, and 60 m  
 93 wavelength). Each band has a width of 1 MHz.

94 The data have been corrected for the distortion (phase shift) [Safaeinili *et al.* 2003;  
 95 Mougnot *et al.* 2008a] and absorption [Mougnot *et al.* 2008b] due to the ionosphere.  
 96 The radar frequency is close to the plasma frequency (up to 4 MHz) of the ionosphere  
 97 [Nagy *et al.* 2004; Gurnett *et al.* 2005] and as a result the signal is broadened  
 98 significantly in addition to being delayed. This broadening of the pulses can cause  
 99 smearing of the resulting radargram. Correction for ionospheric effects is performed  
 100 to re-sharpen the pulses and compensate for the absorption effects as described in  
 101 Mougnot *et al.* [2008a].

102

103 We quantify the echo returned by the surface from MARSIS radargrams by localizing  
104 the position in the radargram corresponding to the surface echo and measuring the  
105 amplitude. The position corresponds to the surface elevation given by Mars Orbiter  
106 Laser Altimeter (MOLA).

107 This surface echo amplitude (i.e., surface reflectivity) allows us to build reflectivity  
108 maps in each MARSIS frequency band (map at 4 MHz in Fig. 1a; maps at other  
109 frequencies show the same type of features). The map resolution is 14.7 km per pixel  
110 (about the MARSIS footprint width). For bands centered at 3, 4 and 5 MHz, we used  
111 305, 464 and 539 orbits, respectively, to construct reflectivity maps. For crossing  
112 tracks, we average the data from multiple measurements from MARSIS is a nadir-  
113 looking radar and the Mars Express polar orbit does not allow us to sound the surface  
114 poleward of about  $87^{\circ}\text{N}$  and  $87^{\circ}\text{S}$ ; this lack of data results in a gap centered at the  
115 pole.

116 To first order, the reflectivity is inversely correlated with the surface roughness,  
117 because the power reflected by a surface at nadir decreases with its roughness. Thus  
118 the topographic variations at lateral scales comparable to and/or larger than the  
119 MARSIS wavelength are affecting the signal. This is normal behavior due to the loss  
120 of coherency of the radar signal.

121 A simulator of returned radar echoes from Mars was developed by Nouvel et al.  
122 [2004]. This computationally efficient radar signal simulation is based on the use of  
123 the Facet Method as surface modeling scheme. The slope and the large-scale  
124 roughness effects are simulated using MOLA topography to predict the surface echo  
125 amplitude in each point [Nouvel et al. 2004]. In this simulation, the reflectivity



126 variability is only due to surface slopes, with an assumption of a single fixed surface  
 127 dielectric constant. It allows distinguishing dielectric and topographic effects.  
 128 For each MARSIS radargram, we generate the corresponding radar simulation and  
 129 extract the surface amplitude from simulated radargrams to obtain a simulated  
 130 reflectivity map (Fig. 1b). We use identical procedures to generate both the simulated  
 131 map and the data map (Fig. 1a).  
 132 With such a simulated map, we can correct for any reflectivity variations that are due  
 133 to topographic effects. Indeed, the reflection coefficient (backscattering coefficient)  $R$   
 134 can be written as the product of a dielectric constant function and a roughness  
 135 function [Ulaby et al. 1986], which is independent of the dielectric constant. By  
 136 normalizing the reflectivity map by the simulated one, we obtain a map proportional  
 137 to the dielectric constant (Fig. 1c). This normalization consists of the difference of the  
 138 power logarithms between data and simulated map. This normalized map reveals  
 139 variations of surface reflectivity across our area of interest. Indeed, one can see that  
 140 the region of the residual cap has very low reflectivity values (black box in Fig. 1c)  
 141 compared to the other parts of the SPLD.

142

## 143 **2. Wave propagation in a stratified medium**

144 We built a first order model to describe reflectivity in the south residual cap. This  
 145 model allows us to compute the radar wave propagation in a stratified medium and  
 146 then obtain a corresponding reflectivity.

147 Previous work indicates that the south residual cap consists of a thin perennial slab of  
 148 CO<sub>2</sub>-ice overlapping H<sub>2</sub>O-ice. So we model the south residual cap reflectivity using  
 149 three layers: the atmosphere, the CO<sub>2</sub>-ice and the H<sub>2</sub>O-ice (Fig. 2).

150 In a two-layer medium with refractive indices  $n_i$  and  $n_j$ , the reflection coefficient for  
151 normal incidence is given by the equation:

$$152 \quad r_{ij} = \frac{n_j - n_i}{n_j + n_i} \quad (1)$$

153 In a stratified medium (i.e., with three layers in our case), the reflection coefficient  
154 equation may be conveniently expressed in terms of the corresponding coefficients  $r_{12}$   
155 and  $r_{23}$  associated with the reflection coefficients at the first and the second interface,  
156 respectively [Born and Wolf 1959]:

$$157 \quad r = \frac{r_{12} + r_{23}e^{2i\beta}}{1 + r_{12}r_{23}e^{2i\beta}} \quad (2)$$

158 where  $\beta = \frac{2\pi}{\lambda}n_2h$ ,  $h$  is the thickness of the intermediate layer and  $\lambda$  is the  
159 wavelength of the incident wave.  $r_{12}$ ,  $r_{23}$  may be obtained by substituting equation 1  
160 with the corresponding subscripts. This notation implies that  $n_1$ ,  $n_2$  and  $n_3$  are  
161 respectively, the refractive index for the upper (atmosphere), intermediate (CO<sub>2</sub> slab)  
162 and lower (H<sub>2</sub>O-ice) layers (see Fig. 2). This model does not include any losses in the  
163 media, which, we believe, is a good approximation because for CO<sub>2</sub>- and H<sub>2</sub>O-ice  
164 losses are known to be weak. In addition polar MARSIS measurements typically  
165 show low losses [Plaut *et al.*, 2007]. The refractive index  $n_i$  corresponds to the square  
166 root of the real part of dielectric constant:  $n_i = \sqrt{\epsilon_i}$ .

167  
168 As the MARSIS radar signal has a bandwidth of 1 MHz and therefore is not  
169 monochromatic, we cannot limit ourselves to equation 2 to obtain the reflectivity.  
170 Instead, we have to calculate the reflectivity as:

$$171 \quad R = \max \left( \left\| \text{IFFT}(S(f)r(f)S^*(f)) \right\|^2 \right) \quad (3)$$

172 where  $f$  is the frequency,  $r$  is the reflection coefficient defined in equation 2 and  $S$  is  
173 the linearly modulated chirp signal of MARSIS. Equation 3 describes our method to  
174 model the amplitude of the surface echo: we apply to an ideal transmitted signal  
175 (chirp) the reflection coefficient  $r(f)$ . The Inverse Fast Fourier Transform (IFFT) gives  
176 a time dependent signal that corresponds to the output of the matched filter of the  
177 receiver.

178 In our model, we describe the H<sub>2</sub>O-ice as compact pure water ice, which corresponds  
179 to a dielectric constant  $\epsilon_3$  equal to 3.15. This value of pure water ice for the dielectric  
180 constant is probably a good assumption, as previous workers have shown that the  
181 deposits of the south polar-layered deposits are composed of relatively clean water ice  
182 [Plaut *et al.* 2007; Zuber *et al.* 2007]. Moreover laboratory experiments have shown  
183 that the real component varies between 3.14 and 3.19 [Ulaby *et al.* 1986] for various  
184 types of “dirty ices”. In case of porous ice, the dielectric constant decreases. For  
185 example, if the porosity of ice were equal to 10%, then, using Maxwell Garnett  
186 mixing formulas [Sihvola, 1999], the dielectric constant would be 2.87. The dielectric  
187 constant of the atmosphere is set to 1.

188 Fig. 3 presents the model of reflectivity  $R$  as function of the CO<sub>2</sub> thickness,  $h$ , for  
189 different values of CO<sub>2</sub> dielectric constant. The two free parameters in our model are  
190  $h$  and the dielectric constant of the central layer  $\epsilon_2$  (the CO<sub>2</sub>-ice). Both have an  
191 impact on the inferred reflectivity. The CO<sub>2</sub> thickness in the plot is limited to the 0-20  
192 m range because previous studies have shown that the global thickness is around 10  
193 m.

194 First, we see on Fig. 3 that the reflectivity is minimal for a layer whose optical  
195 thickness  $n_2 h$  is close to  $\lambda_0/4$  ( $\lambda_0$  is the central wavelength) and the reflectivity is  
196 maximal when optical thickness is close to  $\lambda_0/2$  (Born and Wolf 1979).

197 Second, the reflectivity is minimum or strictly equal to zero when the dielectric  
 198 constant of the intermediate layer is equal to  $\sqrt{n_1 n_3}$ . In our case, this corresponds with  
 199 a dielectric constant of  $\varepsilon_2 \cong 1.77$ .

### 200 3. Data Analysis

#### 201 1.3. Comparison to H<sub>2</sub>O-ice

202 As the reflectivity measured by MARSIS is not absolutely calibrated, we have to  
 203 compare the reflectivity in the south residual cap to a reference region of known  
 204 composition.

205 We have chosen a reference region in the SPLD around the position 82°S and 150°W  
 206 in a 2° by 2° box. It was chosen because of its flatness, so that we can expect that the  
 207 only parameter that plays a role on the reflectivity is the dielectric constant. We know  
 208 that the radar waves in the region are reflected by pure water ice, overlain by an  
 209 optically thin soil layer [Plaut *et al.* 2007]. In this case, the reflection coefficient of  
 210 the reference region is estimated as  $r_{air/H_2O-ice} = 0.279$  with  $\varepsilon_{H_2O-ice} = 3.15$  (see  
 211 equation 1), which corresponds to a reflectivity  $R = |r_{air/H_2O-ice}|^2 = 0.078$ .

212 In our modeling effort, we consider the south residual cap according to the geological  
 213 unit defined by Skinner *et al.* [2006] in the Mars geologic maps. MARSIS  
 214 measurements cover about 60% of the 87,000 km<sup>2</sup> the south residual cap (to 87°S).  
 215 We select all MARSIS reflectivity measurements that are either within the south  
 216 residual cap or in the reference region. We obtain a distribution (see Fig. 4) of the  
 217 reflectivity for both regions and for each of the three MARSIS frequency bands. The  
 218 band 1 centered at 1.8 MHz is not used because of the low amount of data.

In order to find the most probable reflectivity values that characterize each region, we fit this distribution by a Gaussian function. Best-fit parameters are summarized in Table 1. Results show that for all frequencies, the reflectivity is much lower in the south residual cap than in the reference region.

In order to find the best values for model parameters ( $\epsilon$ , thickness) that reproduce the observations, we use the model described previously. We fix a range for these parameters, which are from 0 to 20 m for the thickness and from 1.0 to 3.15 for the dielectric constant. The limits for the dielectric constant are the dielectric constant of the upper and lower media (i.e. respectively the atmosphere and the water ice). The procedure consists of a minimization between the model of reflectivity in a stratified medium and the MARSIS measurements for all frequency bands simultaneously.

Application of this procedure gives the best value in our model of a mean thickness of 11 m and a mean dielectric constant of 2.3. This CO<sub>2</sub> dielectric constant is close to the value measured by Pettineli *et al.* [2003] of 2.12. It confirms that the thin bright slab in the south residual cap is primarily CO<sub>2</sub>-ice. The formal 1-sigma errors on each parameter, computed from the covariance matrix in the minimization, are 1 m for the thickness and 0.2 for the dielectric constant.

#### **1.4. Local Study**

In this section, we are not considering the south residual cap as a single unit, but we try to evaluate, locally, (with a resolution of about 14.7 km) the properties of the CO<sub>2</sub> slab. One can see in Fig. 1c that there is a large variability of reflectivity in the residual cap.

242 Within our model representation, these variations can be explained as a change in  
243 thickness or change in the dielectric constant. In the previous section, we use all the  
244 data in the residual cap and so the statistics are robust. This allows us to easily extract  
245 the mean behavior. However, in the local study, the statistics for each bin are poor and  
246 it is difficult to invert the two parameters at the same time because they play a similar  
247 role in reducing the reflectivity of the surface. Alternatively, we can fix one parameter  
248 and solve for the other one. Thus for each pixel, we try to describe the reflectivity  
249 variation as a change in dielectric constant only, or as a change in CO<sub>2</sub>-ice thickness  
250 only.

### 251 **1.1.1. Spatial Variability of the dielectric constant?**

252 First, we fix the thickness at 10 meters and look at the changes in the dielectric  
253 constant due to variation of the reflectivity. The resulting dielectric map is shown in  
254 Fig. 5a. One can see that the low reflectivity regions (Fig. 1c) correspond to areas  
255 where the dielectric constant is close to the value of pure CO<sub>2</sub>-ice (2.12) [Pettineli *et*  
256 *al.* 2003]. The central part of the residual cap corresponds to higher values of the  
257 dielectric constant, between the CO<sub>2</sub>-ice (2.12) and H<sub>2</sub>O-ice (3.15) reflectivity values,  
258 which means in this case a mixture between H<sub>2</sub>O-ice and CO<sub>2</sub>-ice. This mixture could  
259 be intimate (at the grain size level) or, because MARSIS has a large footprint, CO<sub>2</sub>  
260 residual cap and water outcrop reflectivity can be mixed in the returned signal. Using  
261 the Maxwell Garnett mixing formula [Sihvola, 1999] and supposing that the effective  
262 dielectric constant is only due a mixing between H<sub>2</sub>O- and CO<sub>2</sub>-ice, we obtain the  
263 percentage of CO<sub>2</sub>-ice compared to H<sub>2</sub>O-ice. Fig. 5a shows that the ice content in the  
264 central part could be up to 50% of H<sub>2</sub>O, whereas surrounding terrains would contain  
265 less than 20%.

### 1.1.2. Spatial Variability of the thickness?

Next, we fix the CO<sub>2</sub> dielectric constant at 2.12 and estimate the thickness with our model. This CO<sub>2</sub> dielectric constant is close to the previously found value and corresponds to the value measured by Pettineli *et al.* 2003.

Fig. 5b shows the CO<sub>2</sub> thickness computed by our reflectivity model. In this hypothesis, we observe on the Fig. 4b two types of terrains: terrains with relatively low thickness in the central part (less than 6-7m thick) and higher thickness in the surrounding terrains (about 12 m thick). As it is difficult to measure a 1 dB decrease, thicknesses under 4 m cannot be extracted from our analysis.

## 4. Discussion

### 1.5. Errors

In this section, we discuss possible errors in our method.

In the first part of the analysis, where we study the general reflectivity of the residual cap, we make an assumption of the constant dielectric of the reference region. For example, if there is a porosity in the shallow subsurface of the ice sheet, the dielectric constant of the reference would decrease and so the reflectivity. For 10% porosity,  $\epsilon_{H_2O-ice}$  would be 2.87 and the corresponding reflectivity would be  $R = 0.066$ . A porosity of 10% in water ice would thus reduce the reflectivity less than 1 dB.

Our model assumes no porosity for water ice (i.e.  $\epsilon_{H_2O-ice} = 3.15$ ) and we think that the assumption does not have a significant effect on our results. Our model is not particularly sensitive to this parameter. For the 10%-porosity case, the output values of the model would be still 11 m for the thickness and 2.2 for the dielectric constant of

289 the CO<sub>2</sub>. This change is inside the uncertainties given by the 1-sigma errors on each  
290 parameter.

291 In the second part, where we study the spatial variability in the south residual cap, we  
292 cannot exclude that the effect of roughness at about tens of meters scale could explain  
293 the reflectivity variability. However we think that the geologic features in the residual  
294 cap (depressions of few meters) are small compared to the MARSIS wavelength and  
295 are not responsible for the decrease in reflectivity.

296

297

## 298 **1.6. Conclusions**

299

300 The multi-layered reflection model proposed in this paper allows us to estimate a CO<sub>2</sub>  
301 slab thickness for a portion of the south residual cap of Mars. The mean CO<sub>2</sub>  
302 thickness measured by MARSIS seems to be in agreement with the thickness  
303 estimated by Thomas *et al.* 2005.

304 It is interesting to note that the reflectivity detected by MARSIS is not homogenous  
305 across the residual cap. Indeed we observe that the central part of the residual cap has  
306 higher reflectivity than surrounding areas.

307 We have proposed an interpretation of this heterogeneity in terms of dielectric  
308 constant and thickness of the CO<sub>2</sub>-ice slab.

309 Firstly, supposing that the thickness is constant across the residual cap and solving for  
310 dielectric variations, we would conclude that the central part is a mixture of CO<sub>2</sub> and  
311 H<sub>2</sub>O ices, and the surrounding terrains are mainly pure CO<sub>2</sub>-ice.

312

313 Alternatively, supposing that the residual cap composition is homogeneously pure



314 CO<sub>2</sub>-ice and solving for thickness variations, it appears that the central terrains are  
315 thinner than the surrounding terrains. In this case, the volume of CO<sub>2</sub>-ice contained in  
316 the mapped part of the residual cap is about  $4.1 \times 10^{11} \text{ m}^3$ . As MARSIS measurements  
317 cover 60% of the residual cap, we can estimate that the total volume  $6.85 \times 10^{11} \text{ m}^3$ ,  
318 which corresponds to about 5% (0.27 mbar) of atmospheric surface pressure (5.6  
319 mbar) if we assume that the CO<sub>2</sub>-ice density is about  $1.6 \text{ g.cm}^3$ . This estimation is  
320 consistent with previous works that predict that the amount of CO<sub>2</sub> in the residual cap  
321 is small compared to the mass of the atmosphere [Prettyman *et al.* 2004; Byrne and  
322 Ingersoll, 2003].

323 In both cases, our model shows that the central part of the mapped portion of the  
324 residual cap, which shows lower surface reflectivity, contains less CO<sub>2</sub>-ice than the  
325 surrounding parts of the residual cap.

326 A similar analysis could be conducted with the SHallow subsurface RADar  
327 (SHARAD), which operates at 20 MHz (i.e., a wavelength of 15 m in vacuum). The  
328 SHARAD horizontal resolution is 300 m, which would allow description of the  
329 surface features at a better resolution. SHARAD may also be sensitive to the seasonal  
330 CO<sub>2</sub> deposits when the thickness is 1-2 m as described by Nunes and Phillips 2006.,  
331 although this study is probably more difficult because SHARAD is more sensitive to  
332 meter-scale roughness.

333

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335

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340

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## Tables

Center of the Gaussian	3 MHz	4 MHz	5 MHz
South residual cap	-13.1	-14.1	-15.5
Surface reference [H <sub>2</sub> O-ice]	-7.5	-8.5	-8.3
Reflectivity decrease	5.6	5.5	7.2

## Table Captions

Table 1: The table summarizes the result of the Gaussian fit made on the distribution presented in Fig. 4. The two first lines show the reflectivity (in dB) of the central position of the Gaussian (for the residual cap and for the reference region, respectively). The last line corresponds to the difference (in dB) between reference and residual cap.

443

## 444 **Figure Captions**

445

446 Fig. 1: (a) Surface reflectivity map from MARSIS using the radar frequency centered  
447 at 4 MHz. The projection is polar stereographic. The reflectivity is represented in  
448 decibel scale. (b) Simulated reflectivity map using MOLA topography. The  
449 simulation is performed with a constant  $\epsilon_{surface}$ . (c) Surface reflectivity map at 4 MHz  
450 normalized by the simulated reflectivity map. (d) Mars Orbiter Camera (MOC) wide-  
451 angle mosaic map of the south polar region of Mars. The map resolution is about 14.7  
452 km per pixel.

453

454 Fig. 2: Schematic view of a vertical ground section of the south residual cap, as  
455 described in our model.

456

457 Fig. 3: Reflectivity  $R$  of the layered surface (see Fig. 2) as a function of the thickness  
458  $h$  for different values of the dielectric constant  $\epsilon_{CO_2}$ . The dielectric constants of the  
459 upper and lower medium are 1 and 3.15, respectively.

460

461 Fig. 4: The distribution of surface reflectivity in the reference region (dark grey) and  
462 the south residual cap (light grey). The black dashed lines are the Gaussian fit made  
463 on the distribution. The results of the fit are summarized in Table 1.

464

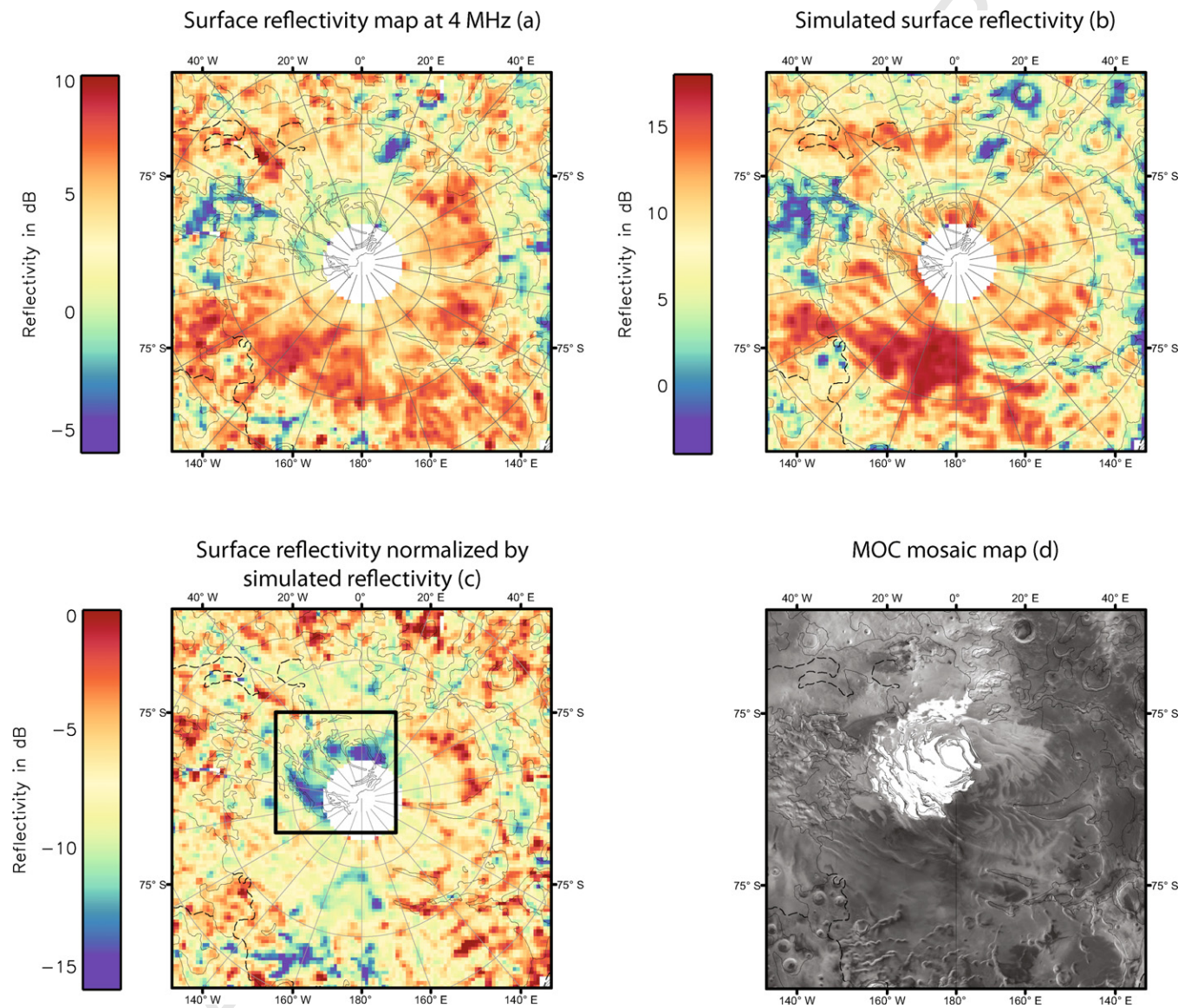
465 Fig. 5: Maps of the south residual cap region. (a) Map of the dielectric constant found  
466 by our reflectivity model with the thickness fixed at 10 meters. Using the Maxwell  
467 Garnett mixing formula [Sihvola, 1999] and assuming that the effective dielectric



468 constant is only due to mixing between H<sub>2</sub>O- and CO<sub>2</sub>-ice, we give the percentage of  
469 CO<sub>2</sub>-ice and H<sub>2</sub>O-ice. (b) Map of the CO<sub>2</sub> thickness found by our model with  
470 dielectric constant fixed at 2.12.

471

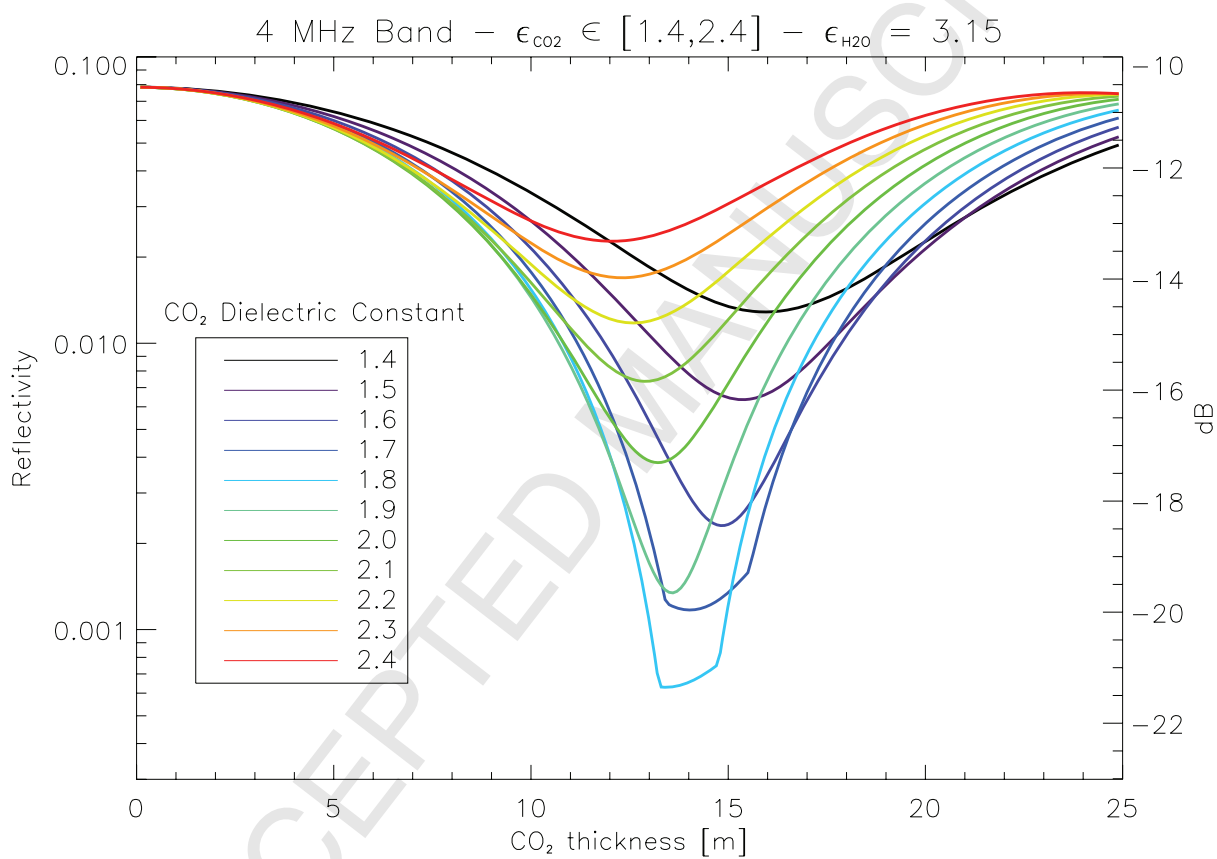
472

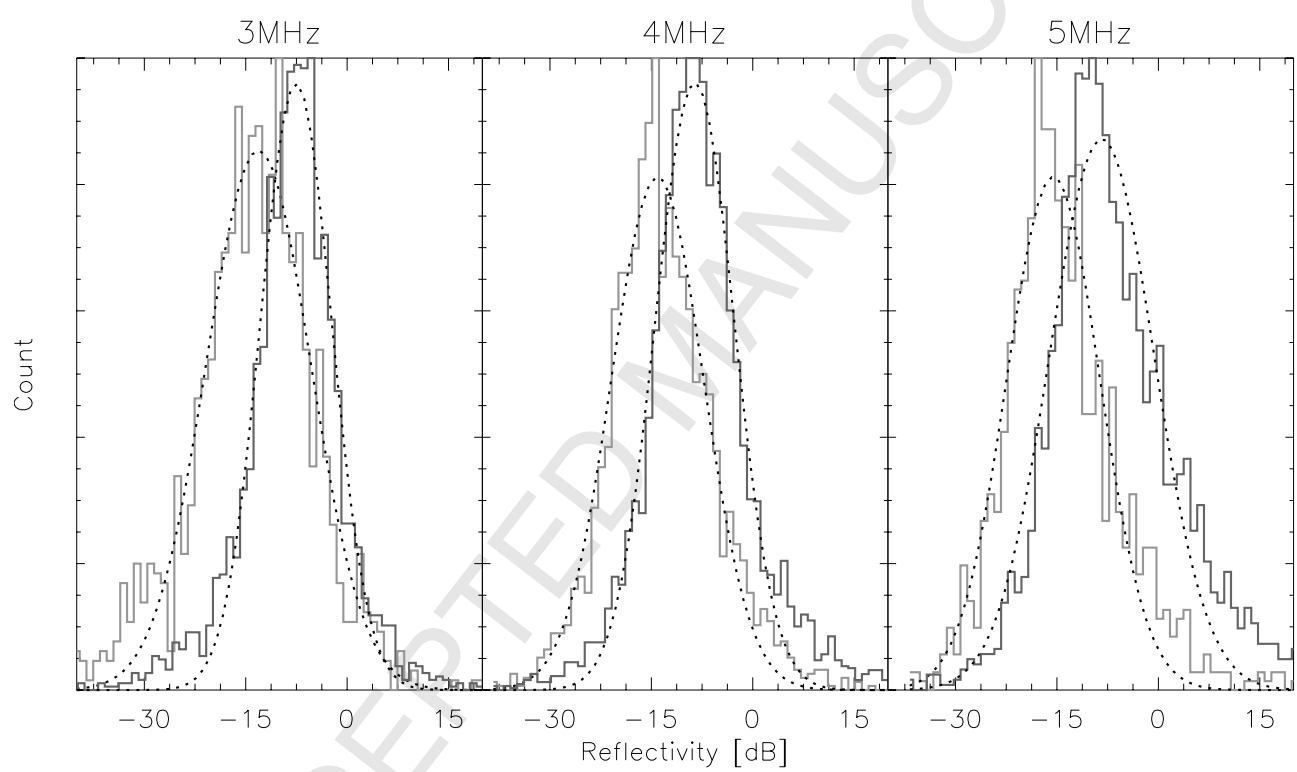


$\epsilon_{1r}=1$  Atmosphere

$\epsilon_{2r}$  Bulk CO<sub>2</sub> ice  $h$

$\epsilon_{3r}=3.15$  Water ice





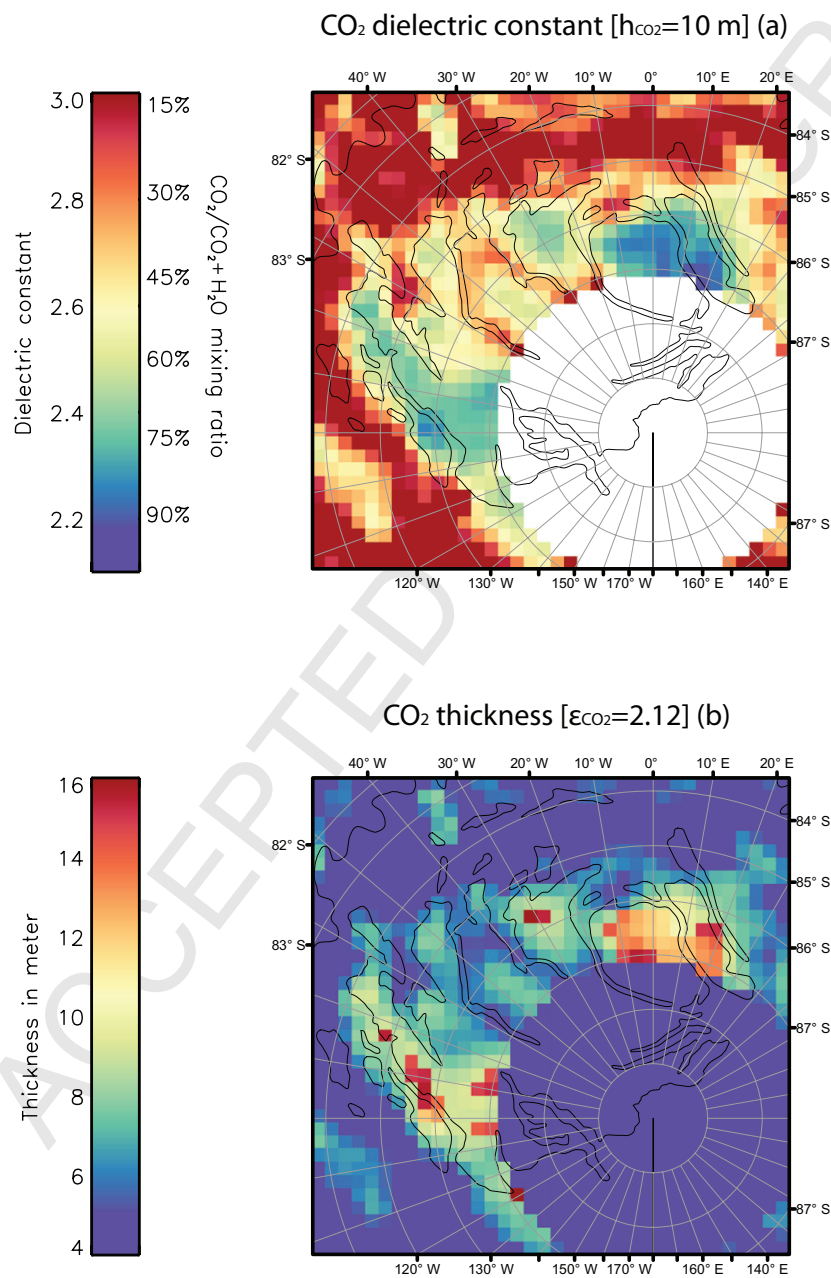


Figure 5 - Mougnot (2008)